

HSC Trial Examination 2020

Mathematics Standard 2

Solutions and marking guidelines

Section I

| Answer and explanation | Syllabus content, outcomes and targeted performance bands |
|--|---|
| Question 1 D The travel route is a walk (a connected sequence of edges showing a route between vertices and edges). The travel route is not a cycle nor a path since the vertices are repeated, so A and B are incorrect. It is not a trail since the edges are repeated, so C is incorrect. | MS-N2 Network Concepts MS2-12-8 Bands 1-2 |
| Question 2 A fuel used = 7 L for 100 km $= \frac{7}{100} \text{ for } 1 \text{ km}$ $= \frac{7}{100} \times 382$ $= 26.74 \text{ L}$ | MS-M7 Rates and Ratios MS2-12-3 Bands 1-2 |
| Question 3 C $z = \frac{x - \bar{x}}{s} \qquad z = \frac{x - \bar{x}}{s}$ $= \frac{66 - 72}{6} \qquad = \frac{78 - 72}{6}$ $= -1 \qquad = 1$ 68% of scores have a z-score between -1 and 1. | MS-S5 The Normal Distribution MS2-12-7 Bands 2-3 |
| Question 4 B There are 30 scores. The median is the average of the 15th (33) and 16th (34) score. Therefore, the median is 33.5. | MS-S1 Data Analysis MS-11-4 Bands 2-3 |
| Question 5 D $ \frac{CE}{\sin 127^{\circ}} = \frac{25.8}{\sin 18^{\circ}} $ $ CE = \frac{25.8 \times \sin 127^{\circ}}{\sin 18^{\circ}} $ $ = 66.6785 \dots $ $ \approx 67 $ | MS-M6 Non-right-angled Trigonometry MS2-12-3 Bands 2-3 |
| Question 6 C earnings = $2 \times 8 \times 19.20 + 6 \times 1.5 \times 19.20$ = \$480 Evelyn earned \$480 in total for working Thursday, Friday and Saturday. | MS-F1 Money Matters MS-11-5 Bands 3-4 |

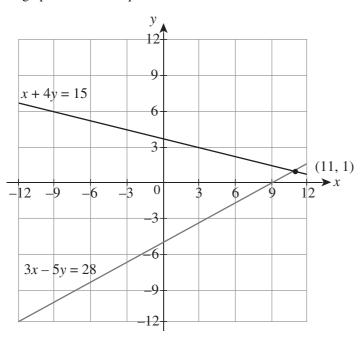
| A | Answer and e | xplanation | | Syllabus content, outcomes an performance bands | |
|---|------------------------|-----------------|----------|---|-----------|
| Question 7 B $FV = PV(1+r)^{n}$ $= 1600 \times \left(1 + \frac{0.08}{4}\right)$ | | | | MS–F4 Investments and Loans MS2–12–5 | Bands 3–4 |
| $\approx 2029.19 $I = FV - PV$ $= $2029.19 - 1600 $= 429.19 | | | | | |
| Liam will receive \$429 | 9.19 compound | d interest. | | | |
| Question 8 B The relationship is a strong scatter and a line wi | rong positive | correlation (sm | l amount | MS–S4 Bivariate Data Analysis MS2–12–7 | Bands 2–3 |
| Question 9 A $y = 2^{-x}$ is an exponention each graph. | | heck (0, 1) and | -1, 2) | MS-A4 Types of Relationships MS2-12-6 | Bands 3- |
| -6 -4 -2 -2 -4 -4 -6 | 4 6 | | | | |
| Question 10 B $ \frac{170}{p} = \frac{10}{32} $ $ 10p = 5440 $ $ p = 544 $ | | | | MS-M7 Rates and Ratios MS2-12-3 | Bands 4- |
| The estimate of the par Question 11 C | | ı is approximat | y 544. | MS-S1 Data Analysis | |
| | | E | | MS-11-4 | Bands 3–4 |
| Hours per week 0 | Class centre 2 | Frequency 5 | | | |
| 5–9 | 7 | 10 | | | |
| 10–14 | 12 | 3 | | | |
| 15–19 | 17 | 2 | | | |
| $mean = \frac{\sum fx}{n}$ | . 12 2 :5 | | | | |
| $= \frac{2 \times 5 + 7 \times 10}{2 \times 5 \times 5}$ $= 7.5 \text{ hours}$ | $+12 \times 3 + 17$ 20 | <u>× 2</u> | | | |

3

Syllabus content, outcomes and targeted Answer and explanation performance bands **Question 12** MS-F5 Annuities MS2-12-5 $r = \frac{2\%}{2} = 1\%$ $n = 2 \times 2 = 4$ The intersection value is 4.0604. $FV = 4.0604 \times 80000$ = \$324 832 **Question 13** D MS-M6 Non-right-angled Trigonometry MS2-12-3 S43°W

Question 14 A

The graphs of the two equations are as follows.



Alternatively, substitute each answer into the equations. So A (11, 1):

$$x + 4y = 15$$

$$11 + 4 \times 1 = 15$$

$$3x - 5y = 28$$

$$3 \times 11 - 5 \times 1 = 28$$

MS-A4 Types or Relationships MS2-12-6

Bands 4-5

Bands 3-4

Bands 4-5

Syllabus content, outcomes and targeted Answer and explanation performance bands **Question 15** D MS-N3 Critical Path Analysis MS2-12-8Bands 5-6 The critical path is $A \to C \to F \to I$. C, 14 *I*, 10 A, 9G, 6 D, 15 finish start 0 J, 7B, 4E, 24 H, 14

The minimum completion time is 52.

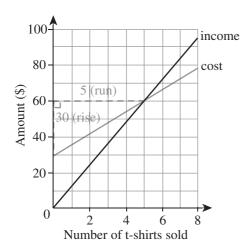
Section II

Syllabus content, outcomes, targeted Sample answer performance bands and marking guide **Question 16** MS-M6 Non-right-angled Trigonometry MS2-12-3 49° Shows some understanding 7.3 m $\tan 49^\circ = \frac{h}{7.3}$ $h = 7.3 \times \tan 49^{\circ}$ = 8.3976 ... ≈ 8.4 m The difference in height is 8.4 metres. **Question 17** MS-M7 Rates and Ratios V = AhMS2-12-3 Bands 1-2 $= 26 \times 15 \times 0.015$ Gives the correct answer. 2 $= 5.85 \text{ m}^3$ Finds the volume of water V in litres = 5.58×1000 = 5850 LThe volume of water collected by the water tank is 5850 litres. **Question 18** (a) MS-A4 Types of Relationships MS2-12-6 Bands 2-3 100 income 80 cost Amount (\$) 60 40 60 (rise) 20 5 (run) 0 6 Number of t-shirts sold $m = \frac{\text{rise}}{\text{run}} = \frac{60}{5} = 12$ The y-intercept of the income received line is \$0. y = mx + cI = 12n

Sample answer

Syllabus content, outcomes, targeted performance bands and marking guide

(b)



$$m = \frac{\text{rise}}{\text{run}} = \frac{30}{5} = 6$$

The y-intercept of the cost line is \$30.

$$y = mx + c$$

$$C = 6n + 30$$

(c) $profit = (12 \times 7) - (6 \times 7 + 30)$ = \$12

(d) n = 5 t-shirts (the point of intersection on the graph) MS-A4 Types of Relationships

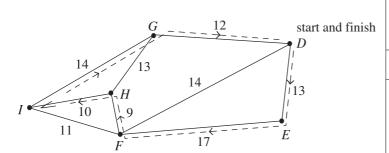
MS2-12-6 Bands 2-3

MS-A4 Types of Relationships MS2-12-6

Bands 2-3 Gives the correct answer 1

MS-A4 Types of Relationships MS2-12-6 Bands 1-2 Gives the correct answer 1

Question 19



The shortest path is $D \to E \to F \to H \to I \to G \to D$.

length =
$$13 + 17 + 9 + 10 + 14 + 12$$

=75 min

The shortest average completion time is 75 minutes.

MS-N2 Network Concepts

MS2-12-8 Bands 4-5 Gives the correct answer 3

- Makes significant progress 2
- Shows understanding of the

| Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide |
|---|--|
| Question 20 | |
| $S = V_0(1+r)$ = 19 990 (1 - 0.18) ⁴ | MS-F4 Investments and Loans MS2-12-5 Bands 1-2 Gives the correct answer |
| = 9037.9139 ≈ \$9038 The salvage value after four years is \$9038. Question 21 | Substitutes TWO correct values into the declining-balance formula 1 |
| (a) Leaking at 0.25 litres per minute, $m = -0.25$. Initially, at $t = 0$, $V = 10$ L. $y = mx + c$ $V = mt + c$ $= -0.25t + 10$ | MS-A4 Types of Relationships MS2-12-6 Bands 2-3 Gives the correct answer |
| (b) $t = 90 \text{ s or } 1.5 \text{ min}$ V = -0.25t + 10 $= -0.25 \times 1.5 + 10$ = 9.625 L There are 9.625 litres of water remaining. | MS-A4 Types of Relationships MS2-12-6 Bands 2-3 Gives the correct answer |
| (c) All the water leaks out when $V = 0$. $V = -0.25t + 10$ $0 = -0.25t + 10$ $0.25t = 10$ $t = 40 \text{ min}$ It would take 40 minutes for all the water to leak out. | MS-A4 Types of Relationships MS2-12-6 Bands 3-4 Gives the correct answer |
| Question 22 $BAC_{\text{Female}} = \frac{10N - 7.5H}{5.5M}$ $= \frac{10 \times (2 \times 0.8 + 3 \times 1.5) - 7.5 \times 5}{5.5 \times 66}$ $= 0.0647$ ≈ 0.065 Alexis' blood alcohol content (BAC) at midnight is 0.065. | MS-A1 Formulae and Equations MS-11-6 Bands 2-3 Gives the correct answer |
| Question 23 (a) $t = \frac{k}{n}$ $t = \frac{21}{n}$ $7 = \frac{k}{3}$ $= \frac{21}{4}$ $k = 21$ $= 5.25$ days It would take 5.25 days for four workers to lay the timber floor. | MS-A4 Types of Relationships MS2-12-6 Bands 3-4 Gives the correct answer |

| | Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide |
|------|---|---|
| (b) | $t = \frac{21}{n}$ | MS-A4 Types of Relationships MS2-12-6 Bands 3-4 |
| | $1 = \frac{21}{n}$ | • Gives the correct answer 1 |
| | n = 21 workers | |
| | Twenty-one workers would be required to lay the timber floor in one day. | |
| Ques | stion 24 | |
| (a) | The precision or limit of reading is 100 kg. | MS-M1 Applications of Measurement MS-11-7 Bands 1-2 • Gives the correct answer |
| (b) | absolute error = $\frac{1}{2}$ × precision = $\frac{1}{2}$ × 100 | MS-M1.1 Practicalities of measurement MS-11-7 Bands 2-3 • Gives the correct answer |
| | = 50 kg | |
| (c) | upper bound = measurement + absolute error = 1800 + 50 = 1850 kg | MS-M1.1 Practicalities of measurement MS-11-7 Bands 2-3 • Gives the correct answer |
| | lower bound = measurement – absolute error | |
| | = 1800 - 50 | |
| | = 1750 kg | |
| (d) | percentage error = $\pm \frac{50}{1800} \times 100$ = ± 2.777 $\approx \pm 2.8\%$ | MS-M1.1 Practicalities of measurement MS-11-7 Bands 3-4 • Gives the correct answer |
| Ques | stion 25 | |
| (a) | AB is parallel to porth direction. Therefore, $\langle CAB = 40^{\circ} \rangle$ | MS-M6 Non-right-angled Trigonometry MS2-12-3 Bands 1-2 Gives the correct answer |
| | AB is parallel to north direction. Therefore, $\angle CAB = 49^{\circ}$. (Alternate angles are equal when two lines are parallel.) | |

| | Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide |
|----------------------|---|--|
| (b) | $a^{2} = b^{2} + c^{2} - 2b\cos A$ $BC^{2} = 27^{2} + 12^{2} - 2 \times 27 \times 12 \times \cos 49^{\circ}$ | MS-M6 Non-right-angled Trigonometry MS2-12-3 Bands 3-4 • Gives the correct answer |
| | BC = 21.1630 $\approx 21.2 \text{ km}$ The distance from B to C is 21.2 km. | Uses the cosine rule with at least ONE correct value |
| (c) | Use the sine rule to find $\angle ACB$. $\frac{\sin \angle ACB}{12} = \frac{\sin 49^{\circ}}{21.1630}$ $\sin \angle ACB = \frac{12 \sin 49^{\circ}}{21.1630}$ $\angle ACB = 25.3369$ $\approx 25^{\circ}$ The true begging of <i>B</i> from <i>C</i> is 074°T (49° ± 25°) | MS-M6 Non-right-angled Trigonometry MS2-12-3 Bands 4-5 • Gives the correct answer |
| Quest | The true bearing of <i>B</i> from <i>C</i> is 074° T ($49^{\circ} + 25^{\circ}$). | |
| = 10 = 40 ≈ 40 | $000(2.1^t)$ 000×2.1^5 0.841.01 0.841 five years, the population of the town is 40.841. | MS-4 Types of relationships MS2-12-6 Bands 1-2 Gives the correct answer |
| | ion 27 | |
| (a) | inflow for vertex $E = 23 + 78 = 101$ L possible outflow for vertex $E = 118$ L The inflow is less than the possible outflow. Therefore, the outflow for vertex E is 101 L. | MS-N3 Critical Path Analysis MS2-12-8 Bands 3-4 Gives the correct answer |
| (b) | 048 | MS-N3 Critical Path Analysis MS2-12-8 Bands 4-5 • Gives the correct answer |
| (c) | Maximum flow equals the minimum cut. maximum flow = $63 + 78 + 8$ = $149 L$ The maximum flow of the network is 149 litres . | MS-N3 Critical Path Analysis MS2-12-8 Bands 3-4 Gives the correct answer |

| Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide | |
|--|---|--|
| Question 28 | | |
| maximum heart rate (MHR) = 220 – age (years) = 220 – 18.25 = 201.75 heart rate when Maya begins exercising = 0.58×201.75 = 117.015 ≈ 117 bpm Maya's heart rate is estimated to be 117 bpm when she begins exercising. | MS-M7 Rates and Ratios MS-11-8 Bands 2-3 • Gives the correct answer | |
| Question 29 | | |
| daily interest rate = $\frac{15.7}{365}$ = 0.043013 $\approx 0.0430\%$ interest = $1240 \times 0.0403 \times 12$ = 6.4004 $\approx 6.40 | MS-F4 Investments and Loans MS2-12-5 Bands 3-4 Gives the correct answer | |
| total paid = 1240 + 6.40 = \$1246.40 The total amount paid is \$1246.40. Question 30 | | |
| expected frequency = np = 0.6×200 = 120 seeds | MS-S2 Relative Frequency and Probability MS-11-8 Bands 2-3 Gives the correct answer | |
| Question 31 | | |
| (a) The intersection value is 3.7908 (10% and 5 years). $PV = 3.7908 \times 15000$ = \$56 862 | MS-F5 Annuities MS2-12-5 Bands 1-2 Gives the correct answer | |
| (b) The intersection value is 3.9020 (1% and 4 years). $PV = 3.9020 \times 10~000$ = \$39 020 | MS-F5 Annuities MS2-12-5 Bands 3-4 Gives the correct answer | |
| (c) The intersection value is 2.5771 (8% and 3 years). $52\ 217 = x \times 2.5771$ $x = \frac{52\ 217}{2.5771}$ $= 20\ 261.9223$ $\approx $20\ 262$ The value of the annuity is \$20\ 262 per year. | MS-F5 Annuities MS2-12-5 Bands 4-5 Gives the correct answer | |

| Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide | |
|--|--|--|
| Question 32 | | |
| time = $\frac{4000 \text{ L}}{5 \text{ min}}$ = 800 min = $\frac{800}{60} \text{ h}$ = 13,3333h | MS-M7 Rates and Ratios MS2-12-3 Bands 2-3 Gives the correct answer | |
| = 13 h 20 min | | |
| The tank will be emptied in 13 hours 20 minutes. | | |
| Question 33 | | |
| Tens Units 3 | MS-S2 Relative Frequency and Probability MS-11-8 Bands 3-4 Gives the correct answer | |
| 5 5 5 5 4 The sample space is {34, 35, 43, 45, 53, 54}. | diagram correctly OR lists the sample space | |
| (b) $P(55) = 0$ (Numbers are not repeated.) | MS-S2 Relative Frequency and Probability MS-11-8 Bands 1-2 Gives the correct answer | |
| (c) $P(35) = \frac{n(35)}{n(S)} = \frac{1}{6}$ | MS-S2 Relative Frequency and Probability MS-11-8 Bands 2-3 Gives the correct answer | |
| (d) The sample space is {33, 34, 35, 43, 44, 45, 53, 54, 55}. $P(35) = \frac{1}{9}$ | MS-S2 Relative Frequency and Probability MS-11-8 Bands 3-4 • Gives the correct answer | |
| Question 34 | | |
| $c = \overline{y} - m\overline{x}$ $= 85 - 0.4 \times 60$ $= 61$ | MS-S4 Bivariate Data Analysis MS2-12-7 Bands 3-4 Gives the correct answer | |
| The <i>y</i> -intercept is 61. | | |
| Question 35 | | |
| (a) The standard deviation is 10 kg. | MS-S5 The Normal Distribution MS2-12-7 Bands 2-3 Gives the correct answer | |
| (b) Sixty-eight percent of scores have a z-score between -1 and 1 (or from 60 kg to 80 kg). region A = $\frac{68\%}{2}$ = 34% | MS-S5 The Normal Distribution MS2-12-7 Bands 3-4 Gives the correct answer | |

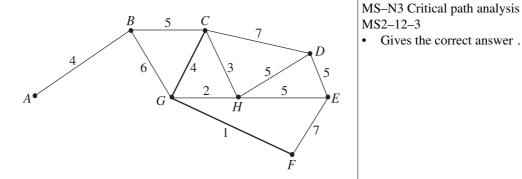
Syllabus content, outcomes, targeted Sample answer performance bands and marking guide (c) A student with a z-score of -2 is two standard deviations MS-S5 The Normal Distribution below the mean $70 - (2 \times 10) = 50$. MS2-12-7 Bands 3-4 Gives the correct answer 1 The weight of the student would be 50 kg. MS-S5 The Normal Distribution $z = \frac{x - \bar{x}}{s} = \frac{100 - 70}{10} = 3$ (d) MS2-12-7 Bands 5-6 Gives the correct answer 2 The percentage of scores less than a *z*-score of 3 is 99.85%. number of students = $99.85\% \times 500$ Finds the z-score OR shows some understanding of the problem 1 =499.25= 499 There are 499 students with a mass less than 100 kg. **Question 36** (a) MS-S4 Bivariate Data Analysis MS2-12-7 Bands 2-3 Population's mortality rate due to cancer (%) 20 40 60 80 100 People with a healthy diet (%) $m = \frac{\text{rise}}{\text{run}}$ =-0.4The gradient is -0.4 (b) The y-intercept is 85. MS-S4 Bivariate Data Analysis MS2-12-7 Bands 3-4 y = mx + cGives the correct answer 1 c = -0.4d + 85The correlation coefficient is approximately -0.8 (small MS-S4 Bivariate Data Analysis amount of scatter and a line with a negative gradient). MS2-12-7 Bands 1-2 Gives the correct answer 1 *Note:* Any value between -0.9 and -0.7 is acceptable.

| | Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide | |
|---|--|---|--|
| Ques | tion 37 | | |
| $z = \frac{x}{2}$ $= \frac{7}{2}$ $= -\frac{1}{2}$ We consider the second of the se | $=\frac{66-76}{10}$ | MS-S5 The Normal Distribution MS2-12-7 Bands 4-5 Gives the correct answer | |
| | tion 38 | | |
| (a) | total amount repaid = monthly repayment \times number of repayments $= 3318 \times 20 \times 12$ $= \$796\ 320$ The total amount to be repaid if the loan were taken over | MS-F4 Investments and Loans MS2-12-5 Bands 2-3 Gives the correct answer | |
| (b) | 20 years is \$796 320. total amount repaid = monthly repayment \times number of repayments $= 3034 \times 25 \times 12$ $= \$910\ 200$ extra amount to be repaid = $\$910\ 200 - \$796\ 320$ $= \$113\ 880$ The extra amount to be repaid would be $\$113\ 880$. | MS-F4 Investments and Loans MS2-12-5 Bands 3-4 Gives the correct answer | |
| Oues | tion 39 | | |
| (a) | The intersection value is 3.3744 (12% per year for 3 years). $FV = 3.3744 \times \$17\ 200$ = \$58 039.68 $\approx \$58\ 040$ | MS-F5 Annuities MS2-12-5 Bands 1-2 Gives the correct answer | |
| (b) | The intersection value is 5.1010 (1% per month for 5 months). $FV = 5.1010 \times 900$ $= 4590.90 $\approx 4591 | MS-F5 Annuities MS2-12-5 Bands 3-4 Gives the correct answer | |
| Ques | tion 40 | | |
| (a) | distance = $4 + 5 + 7 + 5$ = 21 km The distance to travel <i>ABCDE</i> is 21 km. | MS-N2 Network Concepts MS2-12-3 Bands 3-4 Gives the correct answer | |
| (b) | The vertices with an even degree are C , F , G and H . | MS-N2 Network Concepts MS2-12-3 Bands 1-2 Gives the correct answer | |

Sample answer

Syllabus content, outcomes, targeted performance bands and marking guide

(c)



MS2-12-3 Bands 4-5 Gives the correct answer 1

shortest distance = 4 + 1

= 5 km

The shortest distance to travel from C to F is 5 km.

MS-N3 Critical path analysis

MS2-12-3

Bands 5-6

- Gives the correct answer 3
- Finds the minimum spanning tree 2
- Calculates the correct length from an incorrect spanning tree 1

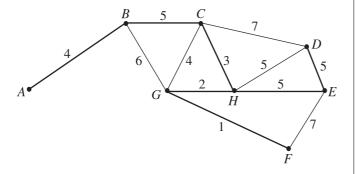
(d)

length =
$$4 + 5 + 3 + 2 + 1 + 5 + 5$$

= 25 km

The length of the spanning tree is 25 km.

Note: The following is an alternative solution.

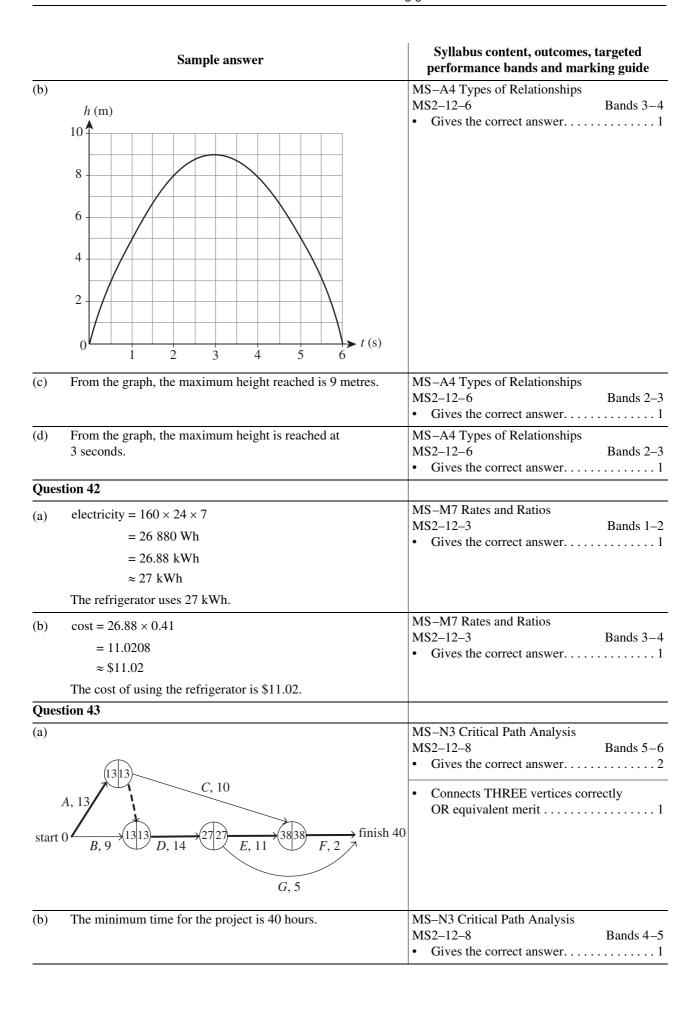


Question 41

(a) 0 1 2 3 5 6 0 5 9 5 h 8 8 0

MS-A4 Types of Relationships MS2-12-6 Bands 3-4

Gives the correct answer 1



| | Sample answer | Syllabus content, outcomes, targeted performance bands and marking guide |
|-----|---|--|
| (c) | float time = LST – EST | MS-N3 Critical Path Analysis |
| | = 35 – 27 | MS2–12–8 Bands 4–5 • Gives the correct answer |
| | = 8 h | |
| | The float time for activity G is 8 hours. | |