



Trial Examination 2023

# HSC Year 12 Mathematics Standard 2

Solutions and Marking Guidelines

**SECTION I**

<b>Answer and explanation</b>	<b>Syllabus content, outcomes and targeted performance bands</b>
<p><b>Question 1      B</b></p> <p>1 microsecond = <math>1 \times 10^{-6}</math> s</p> <p><math>\therefore</math> 6 microseconds = <math>6 \times 10^{-6}</math> s</p>	<p>MS–M1 Applications of Measurement MS11–4                                      Bands 2–3</p>
<p><b>Question 2      C</b></p> <p>A path is a walk with no repeated vertices. Therefore, <i>ACBEC</i> is not a path.</p>	<p>MS–N2 Network Concepts MS2–12–8                                      Bands 2–3</p>
<p><b>Question 3      D</b></p> <p><b>D</b> is correct. Given that there are six values in each data set, the median is found by calculating the mean of the middle two values (45 and 55 in option <b>D</b>).</p> $\begin{aligned} \text{median} &= \frac{45 + 55}{2} \\ &= 50 \end{aligned}$ <p>Finding the mean gives:</p> $\begin{aligned} \text{mean} &= \frac{40 + 45 + 45 + 55 + 85 + 90}{6} \\ &= \frac{360}{6} \\ &= 60 \end{aligned}$ <p><b>A</b> is incorrect. This dataset has a median of 55 and a mean of 60.</p> <p><b>B</b> is incorrect. This dataset has a median of 50 and a mean of 53.33.</p> <p><b>C</b> is incorrect. This dataset has a median of 50 and a mean of 56.67.</p>	<p>MS–S1 Data Analysis MS11–7                                      Bands 2–3</p>
<p><b>Question 4      B</b></p> <p>Substituting <math>V_0 = 17\,500</math>, <math>r = 0.11</math> and <math>n = 5</math> into the declining-balance formula gives:</p> $\begin{aligned} S &= V_0(1 - r)^n \\ &= 17\,500 \times (1 - 0.11)^5 \\ &= \$9772.10 \end{aligned}$	<p>MS–F4 Investments and Loans MS2–12–5                                      Bands 3–4</p>

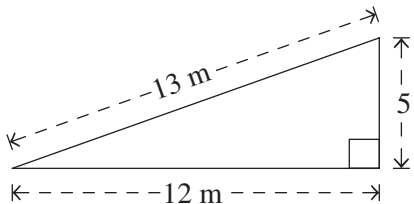
Answer and explanation	Syllabus content, outcomes and targeted performance bands
<p><b>Question 5</b>      <b>C</b></p> <p>Finding the price per gram for each packet of chips gives:</p> $1 \text{ g of Nofrills chips} = \frac{1.25}{60}$ $= 0.0208$ $= 2.08 \text{ cents}$ $1 \text{ g of Smithy chips} = \frac{2.40}{135}$ $= 0.0178$ $= 1.78 \text{ cents}$ $1 \text{ g of Top chips} = \frac{4.10}{240}$ $= 0.0171$ $= 1.71 \text{ cents}$ $1 \text{ g of Cheap chips} = \frac{5.20}{300}$ $= 0.0173$ $= 1.73 \text{ cents}$ <p>As the packet of Top chips has the lowest cost per gram, it has the best value.</p>	<p>MS–M7 Rates and Ratios MS2–12–10                      Bands 4–5</p>
<p><b>Question 6</b>      <b>B</b></p> $W = \sqrt[3]{\frac{2\pi}{6Y}}$ $= \sqrt[3]{\frac{2\pi}{6 \times 6.83}}$ $= 0.535$	<p>MS–A1 Formulae and Equations MS11–1                      Bands 2–3</p>
<p><b>Question 7</b>      <b>A</b></p> <p><b>A</b> is not a true statement and is therefore the required response. Positively skewed data would be bunched on the right-hand side of the dot plot.</p> <p><b>B</b> is a true statement and is therefore not the required response. As the data is bunched on the left-hand side of the dot plot, it is negatively skewed.</p> <p><b>C</b> is a true statement and is therefore not the required response. The data has one outlier near 50.</p> <p><b>D</b> is a true statement and is therefore not the required response. The standard deviation cannot be found because the horizontal scale does not include specific scores.</p>	<p>MS–S1 Data Analysis MS11–1                      Bands 2–3</p>





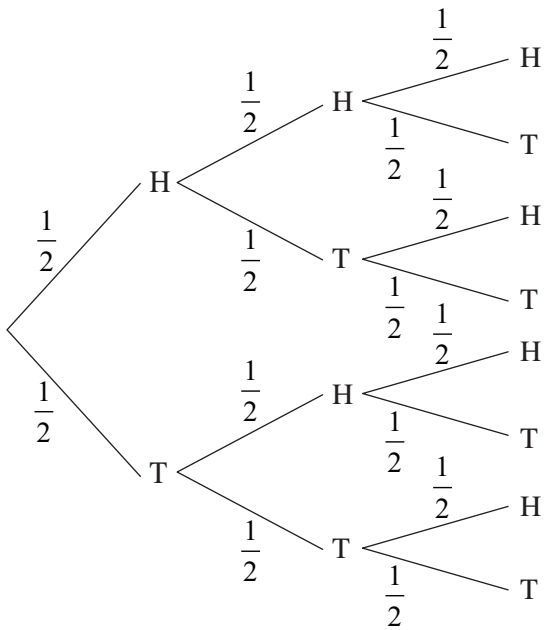
Answer and explanation	Syllabus content, outcomes and targeted performance bands
<p><b>Question 13</b>      C</p> <p>Finding the area of triangle <math>ABC</math> gives:</p> $\begin{aligned} \text{area of } \triangle ABC &= \frac{1}{2} \times 3 \times 4 \times \sin A \\ &= \frac{1}{2} \times 12 \times \sin A \end{aligned}$ <p>Finding the area of triangle <math>ADE</math> gives:</p> $\begin{aligned} \text{area of } \triangle ADE &= \frac{1}{2} \times 7 \times 10 \times \sin A \\ &= \frac{1}{2} \times 70 \times \sin A \end{aligned}$ <p>Finding the ratio gives:</p> $\begin{aligned} \frac{1}{2} \times 12 \times \sin A &: \frac{1}{2} \times 70 \times \sin A \\ 12 : 70 \\ 6 : 35 \end{aligned}$	<p>MS–M7 Rates and Ratios MS2–12–3                      Bands 4–5</p>
<p><b>Question 14</b>      C</p> <p>Finding the height of the cylinder gives:</p> $\begin{aligned} h &= 3 \times 2r \\ &= 6r \end{aligned}$ <p>Therefore:</p> $\begin{aligned} \text{volume of cylinder} &= \pi r^2 h \\ &= \pi r^2 \times 6r \\ &= 6\pi r^3 \end{aligned}$ $\begin{aligned} \text{volume of tennis balls} &= 3 \times \frac{4}{3} \pi r^3 \\ &= 4\pi r^3 \end{aligned}$ <p>Thus, finding the fraction of the volume of the cylinder that is occupied by the tennis balls gives:</p> $\begin{aligned} \frac{\text{volume of tennis balls}}{\text{volume of cylinder}} &= \frac{4\pi r^3}{6\pi r^3} \\ &= \frac{4}{6} \\ &= \frac{2}{3} \end{aligned}$	<p>MS–M1 Applications of Measurement MS11–4                      Bands 5–6</p>
<p><b>Question 15</b>      C</p> <p>The mode gives the most frequent value in a dataset; thus, it will be most useful to the owner as it will indicate which size is sold most often.</p>	<p>MS–S1 Data Analysis MS11–2                      Bands 3–4</p>

**SECTION II**


Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 16</b></p> <p>(a) Using Pythagoras' theorem to find the third side length of the triangle gives:</p> $a^2 + b^2 = c^2$ $a^2 = c^2 - b^2$ $a^2 = 13^2 - 12^2$ $a^2 = 25$ $a = 5 \text{ m}$  <p>Therefore:</p> $h = 11 + 5$ $= 16 \text{ m}$	<p>MS–M1 Applications of Measurement MS11–3 Bands 2–3</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 1</li> </ul>
<p>(b) area of triangle = <math>\frac{1}{2} \times 12 \times 5</math></p> $= 30 \text{ m}^2$ <p>area of rectangle = <math>11 \times 12</math></p> $= 132 \text{ m}^2$ <p>Therefore:</p> <p>total area = <math>132 + 30</math></p> $= 162 \text{ m}^2$	<p>MS–M1 Applications of Measurement MS11–3 Bands 2–3</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the area of the triangle OR rectangle. . . . . 1</li> </ul>
<p><b>Question 17</b></p> <p>The mean of class A is less than the mean of class B.</p> <p>The standard deviation of class A is less than the standard deviation of class B.</p>	<p>MS–S1 Data Analysis MS11–7 Bands 3–4</p> <ul style="list-style-type: none"> <li>Compares the means AND standard deviations. . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Compares the means OR standard deviations . . . . . 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<b>Question 18</b>	
<p>Finding the distance that each car travelled gives:</p> $\text{speed} = \frac{\text{distance}}{\text{time}}$ $\text{distance} = \text{speed} \times \text{time}$ $= 90 \times 5$ $= 450 \text{ km}$ <p>Finding the time it took car B to complete the journey gives:</p> $\text{time} = \frac{\text{distance}}{\text{speed}}$ $= \frac{450}{80}$ $= 5.625 \text{ hours}$ $= 5 \text{ hours } 38 \text{ minutes}$	<p>MS–M7 Rates and Ratios MS2–12–3 Bands 2–3</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the distance travelled during the journey . . . . . 1</li> </ul>
<b>Question 19</b>	
<p>Given that <math>S = 180</math>, <math>D = 220</math> and <math>n = 4</math>:</p> $S = V_0 - Dn$ $180 = V_0 - 220 \times 4$ $V_0 = 180 + 880$ $= \$1060$	<p>MS–F1 Money Matters MS11–5 Bands 2–3</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Finds the total amount of depreciation . . . . . 1</li> </ul>
<b>Question 20</b>	
<p>longitude difference = <math>75 + 150</math></p> $= 225^\circ$ <p>Given that <math>15^\circ = 1 \text{ hour}</math>:</p> $\text{time difference} = \frac{225}{15}$ $= 15 \text{ hours}$ <p>Therefore, New York is 15 hours behind Sydney, so the event was broadcast at 11:00 pm on Tuesday.</p>	<p>MS–M2 Working with Time MS11–3 Bands 2–4</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the longitude difference AND time difference . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the longitude difference . . . . . 1</li> </ul>

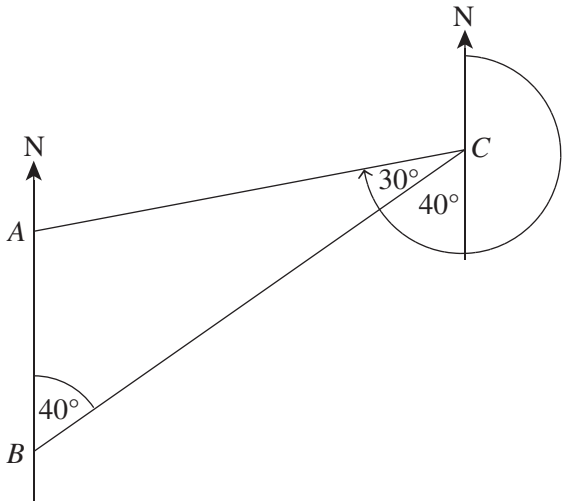


Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 21</b></p> <p>(a) <i>First toss</i>      <i>Second toss</i>      <i>Third toss</i></p>  <p><i>Note: Accept diagrams that show the probabilities as decimals.</i></p>	<p>MS–S2 Relative Frequency and Probability MS11–2      Bands 3–5</p> <ul style="list-style-type: none"> <li>• Draws a tree diagram that shows all the possible outcomes AND probabilities ..... 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Draws a tree diagram that shows all the possible outcomes with no probabilities OR some correct probabilities ..... 1</li> </ul>
<p>(b) <math>P(\text{exactly one tail})</math>  <math>= P(\text{THH or HTH or HHT})</math>  <math>= \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}</math>  <math>= \frac{1}{8} + \frac{1}{8} + \frac{1}{8}</math>  <math>= \frac{3}{8}</math></p> <p><b>OR</b></p> <p>Reading from the tree diagram:  <math>P(\text{exactly one tail}) = P(\text{THH, HTH or HHT})</math> from          (HHH, HHT, HTH, HTT, THH, THT, TTH, TTT)</p> $= \frac{3}{8}$	<p>MS–S2 Relative Frequency and Probability MS11–8      Bands 3–5</p> <ul style="list-style-type: none"> <li>• Provides the correct solution ..... 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Calculates at least ONE of the three probabilities ..... 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p>(c) <math>P(\text{all heads}) = P(\text{HHH})</math></p> $= \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$ $= \frac{1}{8}$ <p><b>OR</b></p> <p>Reading from the tree diagram:</p> <p><math>P(\text{all heads}) = (\text{HHH})</math> from (HHH, HHT, HTH, HTT, THH, THT, TTH, TTT)</p> $= \frac{1}{8}$	<p>MS–S2 Relative Frequency and Probability MS11–8 Bands 3–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 1</li> </ul>
<b>Question 22</b>	
<p>(a) taxable income = <math>108\,000 - 342 - 674</math> = \$106 984</p> <p>Medicare levy = <math>0.02 \times 106\,984</math> = \$2140</p>	<p>MS–F1 Money Matters MS11–10 Bands 4–5</p> <ul style="list-style-type: none"> <li>Calculates the taxable income AND Medicare levy. . . . . 2</li> <li>Calculates the taxable income . . . . . 1</li> </ul>
<p>(b) income tax payable = <math>5902 + 0.325 \times (106\,984 - 45\,000)</math> = <math>5902 + 0.325 \times 61\,984</math> = <math>5902 + 20\,144.80</math> = \$26 046.80</p> <p>tax payable = income tax payable + Medicare levy = <math>26\,046.80 + 2140</math> = \$28 187</p> <p><i>Note: Consequential on answer to Question 22(a).</i></p>	<p>MS–F1 Money Matters MS11–10 Bands 4–5</p> <ul style="list-style-type: none"> <li>Calculates the tax payable . . . . . 2</li> <li>Calculates the income tax payable. . . . . 1</li> </ul>
<p>(c) Cameron will owe money to the Australian Taxation Office because his tax payable of \$28 187 is greater than his PAYG tax of \$26 200.</p>	<p>MS–F1 Money Matters MS11–5 Bands 3–4</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 1</li> </ul>

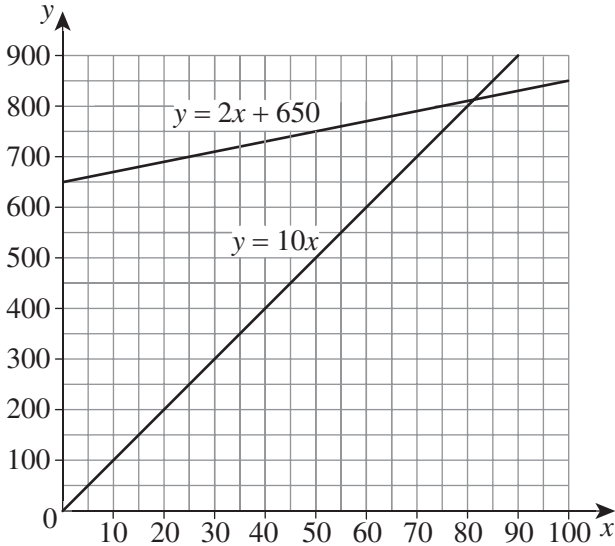
Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<b>Question 23</b>	
<p>(a) City <math>D</math> is most frequently used. It is the vertex with the highest degree (5), so it has the largest number of direct connections to other cities.</p>	<p>MS–N2 Network Concepts MS2–12–8 Bands 2–3</p> <ul style="list-style-type: none"> <li>States the correct city.</li> </ul> <p>AND</p> <ul style="list-style-type: none"> <li>Justifies the answer by identifying that city <math>D</math> has the highest degree . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>States the correct city. . . . . 1</li> </ul>
<p>(b) </p> <p>total travel time = <math>2 + 9 + 1</math> = 12 hours</p> <p><i>Note: Students do not need to include flight times in their paths to obtain full marks.</i></p>	<p>MS–N2 Network Concepts MS2–12–8 Bands 2–3</p> <ul style="list-style-type: none"> <li>Draws the path AND determines the total travel time . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Draws the path OR determines the total travel time . . . . . 1</li> </ul>
<b>Question 24</b>	
<p>(a) The third second is the interval between <math>t = 2</math> and <math>t = 3</math> seconds.</p> <p>Substituting <math>t = 2</math> into the equation gives:</p> $h = 20 \times 2 - 2^2$ $= 40 - 4$ $= 36 \text{ m}$ <p>Substituting <math>t = 3</math> into the equation gives:</p> $h = 20 \times 3 - 3^2$ $= 60 - 9$ $= 51 \text{ m}$ <p>Therefore, the ball travels a vertical distance of <math>51 - 36 = 15 \text{ m}</math> in the third second.</p>	<p>MS–A4 Types of Relationships MS2–12–1 Bands 4–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the vertical distance at <math>t = 3</math> . . . . . 1</li> </ul>
<p>(b) average speed = <math>\frac{\text{distance travelled from } t = 2 \text{ to } t = 3}{\text{time between } t = 2 \text{ and } t = 3}</math></p> $= \frac{15}{1}$ $= 15 \text{ m/s}$ <p><i>Note: Consequential on answer to Question 24(a).</i></p>	<p>MS–A4 Types of Relationships MS2–12–1 Bands 4–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides some relevant working . . . 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 25</b></p> <p>The absolute error of a measurement is half of the amount it is rounded by. Therefore, the absolute error of the loaf of bread is 5 g.</p> <p>Finding the percentage error gives:</p> $\text{percentage error} = \frac{\text{absolute error}}{\text{measurement}} \times 100$ $= \frac{5}{700} \times 100$ $= 0.714\%$	<p>MS–M1 Applications of Measurement MS11–3 Bands 2–3</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Provides some relevant working . . . 1</li> </ul>
<p><b>Question 26</b></p> <p>(a) Finding the total value of Charlotte’s investment after six years gives:</p> $FV = PV(1+r)^n$ $= 7000 \times (1 + 0.045)^6$ $= \$9115.82$ <p>Thus, the compound interest earned is:</p> $9115.82 - 7000 = \$2115.82$	<p>MS–F4 Investments and Loans MS2–12–5 Bands 3–4</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Finds the total value of the investment . . . . . 1</li> </ul>
<p>(b) Substituting the compound interest found in part (a) into the simple interest formula gives:</p> $I = Pm$ $2115.82 = 7000 \times r \times 6$ $r = \frac{2115.82}{42\,000}$ $= 0.050376$ $= 5.04\%$ <p><i>Note: Consequential on answer to Question 26(a).</i></p>	<p>MS–F4 Investments and Loans MS2–12–5 Bands 4–5</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Uses the simple interest formula with ONE error . . . . . 1</li> </ul>

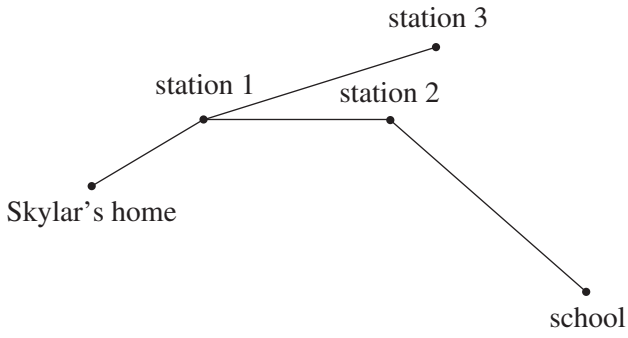
Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<b>Question 27</b>	
<p>(a) Using interior angles gives:</p>  <p>Therefore, the bearing of point A from point C is:  <math>180 + 70 = 250^\circ</math></p>	<p>MS–M6 Non-right-angled Trigonometry                      MS2–12–4 Bands 3–4</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Uses interior angles to find the angle of <math>70^\circ</math> . . . . . 1</li> </ul>
<p>(b) Using the sine rule gives:</p> $\frac{12}{\sin(40)} = \frac{AB}{\sin(30)}$ $AB = \frac{12 \sin(30)}{\sin(40)}$ $= \frac{12 \times \frac{1}{2}}{\sin(40)}$ $= \frac{6}{\sin(40)}$ $= 9.3343 \text{ km}$ $\approx 9 \text{ km}$	<p>MS–M6 Non-right-angled Trigonometry                      MS2–12–4 Bands 4–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Uses the sine rule with ONE error. . . 1</li> </ul>
<b>Question 28</b>	
<p>(a) Using a calculator to find Pearson’s correlation coefficient gives:  <math>r = 0.8047</math></p>	<p>MS–S4 Bivariate Data Analysis                      MS2–12–7 Bands 2–3</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 1</li> </ul>
<p>(b) It is a strong positive correlation, since <math>0.75 &lt; r &lt; 1</math>.  <i>Note: Consequential on answer to Question 28(a).</i></p>	<p>MS–S4 Bivariate Data Analysis                      MS2–12–7 Bands 2–3</p> <ul style="list-style-type: none"> <li>Describes the correlation with reference to the Pearson’s correlation coefficient . . . . . 1</li> </ul>
<p>(c) As engine size increases, fuel economy becomes worse/fuel economy becomes poorer.</p>	<p>MS–S4 Bivariate Data Analysis                      MS2–12–7 Bands 2–3</p> <ul style="list-style-type: none"> <li>States the relationship between engine size and fuel economy . . . . . 1</li> </ul>

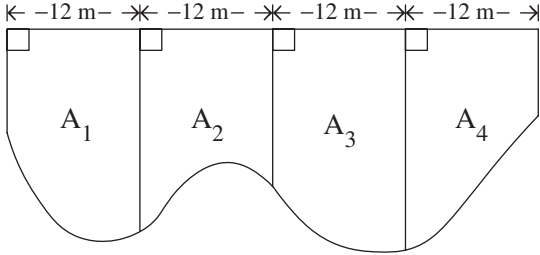
Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 29</b></p> $\frac{3x}{2} - \frac{x}{4} = 5 + x$ $4 \times \frac{3x}{2} - \frac{x}{4} = 4 \times (5 + x)$ $6x - x = 20 + 4x$ $5x = 20 + 4x$ $5x - 4x = 20$ $x = 20$	<p>MS–A1 Formulae and Equations MS11–1 Bands 3–4</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Calculates the value of <math>x</math> with ONE error . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Provides some relevant working . . . 1</li> </ul>
<p><b>Question 30</b></p> $\text{dividend yield} = \frac{\text{dividend per share}}{\text{market price per share}} \times 100$ $= \frac{0.76}{8.50} \times 100$ $= \$8.94$	<p>MS–F4 Investments and Loans MS2–12–5 Bands 3–4</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Calculates the dividend yield with ONE error OR incorrect rounding . . . . . 1</li> </ul>
<p><b>Question 31</b></p> $12\% \text{ per annum} = \frac{12}{12}$ $= 0.01$ $= 1\% \text{ per month}$ <p>Therefore, <math>r = 0.0100</math>.</p> $N = 12 \times 5$ $= 60$ <p>Using the table to find Natalia’s monthly repayment, <math>a</math>, gives:</p> $10\,000 = a \times 30.9766$ $a = \frac{10\,000}{30.9766}$ $= \$322.82$	<p>MS–F4 Investments and Loans MS2–12–5 Bands 4–5</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Calculates the monthly repayment with ONE error . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Provides some relevant working . . . 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<b>Question 32</b>	
(a) positive correlation	MS–S4 Bivariate Data Analysis MS2–12–2 Bands 2–3 • Identifies the correct correlation . . . 1
<p>(b) Using two points on the line of best fit – (16, 22) and (15, 21) – to find the gradient gives:</p> $m = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{22 - 21}{16 - 15}$ $= \frac{1}{1}$ $= 1$ <p>Substituting <math>m = 1</math> into the general equation of a line gives:</p> $y = 1 \times x + c$ $y = x + c$ <p>Substituting the point (16, 22) into <math>y = x + c</math> gives:</p> $22 = 16 + c$ $c = 22 - 16$ $= 6$ <p>Therefore, the equation of the line of best fit is <math>y = x + 6</math>.</p>	<p>MS–S4 Bivariate Data Analysis MS2–12–2 Bands 4–5</p> <p>• Finds the gradient AND the equation of the line of best fit . . . . . 2</p> <hr/> <p>• Finds the gradient . . . . . 1</p>
<p>(c) Substituting <math>x = 10</math> gives:</p> $y = 10 + 6$ $= 16 \text{ cm}$ <p><i>Note: Consequential on answer to <b>Question 32(b)</b>.</i></p>	<p>MS–S4 Bivariate Data Analysis MS2–12–2 Bands 3–4</p> <p>• Provides the correct solution . . . . . 1</p>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 33</b></p>	
<p>(a) <math>y = 2x + 650</math></p>	<p>MS–A4 Types of Relationships MS2–12–6 Bands 3–4</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides the correct gradient OR y-intercept . . . . . 1</li> </ul>
<p>(b)</p>  <p><i>Note: Consequential on answer to Question 33(a).</i></p>	<p>MS–A4 Types of Relationships MS2–12–6 Bands 3–4</p> <ul style="list-style-type: none"> <li>Sketches the graphs of <math>y = 10x</math> AND <math>y = 2x + 650</math>. . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Sketches the graph of <math>y = 10x</math> OR <math>y = 2x + 650</math> . . . . . 1</li> </ul>
<p>(c) Equating the two equations to find the <math>x</math> value of the point of intersection gives:</p> $10x = 2x + 650$ $8x = 650$ $x = 81.25$ <p>Therefore, the manufacturer must produce 82 pairs of shorts to generate a profit.</p> <p><i>Note: Consequential on answer to Question 33(a) and Question 33(b).</i></p>	<p>MS–A4 Types of Relationships MS2–12–6 Bands 4–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides some relevant working . . . 1</li> </ul>



Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<b>Question 34</b>	
<p>energy used in 2.5 hours = <math>800 \times 2.5</math>  <math>= 2000 \text{ Wh}</math></p> <p>Converting the energy used each day into kWh gives:</p> $\frac{2000 \text{ Wh}}{1000 \text{ kWh}} = 2 \text{ kWh}$ <p>Finding the cost of using the drill for one year gives:</p> $\begin{aligned} \text{cost} &= 2 \times 365 \times 0.2866 \\ &= 730 \times 0.2866 \\ &= \$209.22 \end{aligned}$	<p>MS–A4 Types of Relationships                      MS2–12–6 Bands 4–5</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Calculates the cost for one year with ONE error . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Provides some relevant working . . . 1</li> </ul>
<b>Question 35</b>	
<p>(a) The shortest path is:</p> <ul style="list-style-type: none"> <li>• home to station 1 = 8 minutes</li> <li>• station 1 to station 2 = 7 minutes</li> <li>• station 2 to school = 14 minutes</li> </ul> <p>Therefore, the time it takes for Skylar to travel to school is <math>8 + 7 + 14 = 29</math> minutes.</p>	<p>MS–N3 Critical Path Analysis                      MS2–12–8 Bands 4–5</p> <ul style="list-style-type: none"> <li>• Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>• Finds the time of the shortest path with ONE error . . . . . 1</li> </ul>
<p>(b)</p> 	<p>MS–N3 Critical Path Analysis                      MS2–12–8 Bands 3–4</p> <ul style="list-style-type: none"> <li>• Draws the minimum spanning tree . . . . . 1</li> </ul>
<p>(c) It would be faster for Skylar to wait for the train to station 2 and then walk to school from station 2 (5-minute wait + 7-minute train ride + 14-minute walk = 26 minutes).</p>	<p>MS–N3 Critical Path Analysis                      MS2–12–8 Bands 3–4</p> <ul style="list-style-type: none"> <li>• States the faster path . . . . . 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 36</b></p> <p>(a) Dividing the wall into the four sections gives:</p>  $A = \frac{h}{2}(d_f + d_l)$ $A_1 = \frac{12}{2} \times (15 + 25)$ $= 6 \times 40$ $= 240 \text{ m}^2$ $A_2 = \frac{12}{2} \times (25 + 20)$ $= 6 \times 45$ $= 270 \text{ m}^2$ $A_3 = \frac{12}{2} \times (20 + 26)$ $= 6 \times 46$ $= 276 \text{ m}^2$ $A_4 = \frac{12}{2} \times (26 + 14)$ $= 6 \times 40$ $= 240 \text{ m}^2$ $\text{total area} = 240 + 270 + 276 + 240$ $= 1026 \text{ m}^2$	<p>MS–M7 Rates and Ratios MS2–12–4 Bands 4–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the area of the wall with ONE error . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides some relevant working . . . 1</li> </ul>
<p>(b) <math>V = \text{area} \times \text{width of dam}</math></p> $= 1026 \times 28$ $= 28\,728 \text{ m}^3$ <p><i>Note: Consequential on answer to Question 36(a).</i></p>	<p>MS–M1 Applications of Measurement MS11–4 Bands 2–3</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides some relevant working . . . 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<p><b>Question 37</b></p> <p>Calculating the <math>z</math>-score for Kenna's first exam gives:</p> $z = \frac{73 - 78}{4}$ $= -1.25$ <p>Calculating the <math>z</math>-score for Kenna's second exam gives:</p> $z = \frac{70 - 84}{8}$ $= -1.75$ <p>As the first exam has a better <math>z</math>-score, Kenna achieved a better result in the first exam.</p>	<p>MS–S5 The Normal Distribution MS2–12–7 Bands 5–6</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Finds the <math>z</math>-scores with ONE error . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides some relevant working . . . 1</li> </ul>
<p><b>Question 38</b></p> <p><math>N</math> = number of standard drinks = <math>5 \times 1.1</math> = 5.5 standard drinks</p> <p><math>H</math> = hours spent drinking = 4.5 hours</p> <p><math>M</math> = mass of the person = 110 kg</p> $\text{BAC}_{\text{male}} = \frac{10N - 7.5H}{6.8M}$ $= \frac{10 \times 5.5 - 7.5 \times 4.5}{6.8 \times 110}$ $= 0.0284$	<p>MS–A1 Formulae and Equations MS11–1 Bands 3–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the BAC with ONE error . . . . . 1</li> </ul>
<p><b>Question 39</b></p> <p>dosage in mg = <math>100 \times 18</math> = 1800 mg</p> $\text{dosage in mL} = \frac{1800}{40}$ $= 45 \text{ mL}$	<p>MS–A1 Formulae and Equations MS11–1 Bands 3–5</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 3</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the dosage with ONE error . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Provides some relevant working . . . 1</li> </ul>

Sample answer	Syllabus content, outcomes, targeted performance bands and marking guide
<b>Question 40</b>	
<p>(a) As the account compounds biannually for five years, the period is 10.</p> <p>The interest rate is <math>\frac{12}{2} = 6\%</math> for each period of six months.</p> <p>Therefore, in five years Jamari will have saved <math>13.1808 \times 2000 = \\$26\,361.60</math></p>	<p>MS–S5 The Normal Distribution MS2–12–7 Bands 5–6</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the amount with ONE error . . . . . 1</li> </ul>
<p>(b) Finding the time it would take Cara to save \$26 361.60 gives:</p> $26\,361.60 = 1600 \times x$ $x = \frac{26\,361.60}{1600}$ $= 16.476$ <p>Referring to the table, <math>x = 16.476</math> corresponds most closely to the future value of 16.8699, which results from an interest rate of 6% over 12 periods.</p> <p>Therefore, Cara will be able to contribute more to the deposit after <math>\frac{12}{2} = 6</math> years.</p> <p><i>Note: Consequential on answer to Question 40(a).</i></p>	<p>MS–S5 The Normal Distribution MS2–12–7 Bands 5–6</p> <ul style="list-style-type: none"> <li>Provides the correct solution . . . . . 2</li> </ul> <hr/> <ul style="list-style-type: none"> <li>Calculates the number of years with ONE error . . . . . 1</li> </ul>