2022 VCE Further Mathematics Trial Examination 1 Suggested Solutions



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Section A Core – Data Analysis

Question 1 C

Fruit name is nominal. Age group is ordinal (makes sense to order it; younger, older etc.)

Question 2 C

66/110 i.e. 60% of under 12 prefer grapes 72/160 i.e. 45% of 12 and over prefer grapes

Option C shows this.

Question 3 E

Under 6 attempts means 5 attempts or less. This adds to 15 occasions. $15/21 = 0.7142... \sim 71\%$

Question 4 B

Range = 8 - 1 = 7IQR = 6 - 3 = 3

Question 5 B

Number of attempts is numerical data. There are only **two** categories of *amount of sleep* so this information can be shown on a back-to back stem plot.

Question 6 A

Adding frequencies gives us 20 insects. The median mass is somewhere between 10^{-1} and 10^{0} , that is between 0.1 gram and 1gram. 0.78 is the only option that satisfies this.

Question 7 C

46 is 2 standard deviations below the mean. 2.5% of the sample is expected to be 2 standard deviations below the mean. 2.5% = 1.6

2.5% of 640 = 16

Question 8 B

48 and 54 are 1 standard deviation below the mean and 2 standard deviations above the mean respectively.

Expected % of boxes to be within these limits is 68 + 13.5 = 81.5%

Section A Core – Data Analysis

Question 9 A

The gradient of the least squares line will give the expected change in *height* for every one unit change in *weight*.

gradient of least squares line =
$$r \frac{S_y}{S_x}$$

 $= 0.7062 \times \frac{7.426}{8.241} = 0.63635 \dots$

Question 10 D

$$r = \pm \sqrt{0.87329} \sim \pm 0.934$$

The gradient of the least squares line is **negative**, so *r* will be **negative**.

r = -0.934

Question 11 E

Predicted success rate = $84.2 - 0.327 \times 150 = 35.15$ Residual = actual – predicted

Question 12 B

Choose two points that the line passes through, or **very** near to. For example, (35,70) and (25, 59) Gradient = $\frac{70-59}{35-25} = 1.1$ Substitute (35,70) into y = mx + c $70 = 1.1 \times 35 + c$ c = 31.5

Question 13 D

Need the median of 35, 36, 45, 38, 40 When arranged in ascending order, 38 is the middle value.

Question 14 D

Use technology to find the equation of the least squares regression line.

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Br	nags	С		D	E	
•					=LinRegB;	
1	34			Title	Linear Re	
2	32		(RegEqn	a+b*x	
3	35			а	31.3030	
4.	36		$\overline{\ }$	b	1.28671	
5	45			r²	0.42994	
DI	="Title	н			•	

Question 15 C

Long term yearly average =

$$\frac{27.2 + 19.9 + 12.6 + 21.5}{4} = 20.3$$

SI _{autumn} $=\frac{12.6}{20.3} = 0.62$

Question 16 A

Deseasonalised value = $\frac{actual}{SI}$

actual = deseasonalised value
$$\times$$
 SI = 22.2 \times 0.98
= 21.756 \sim 21.8

Section A Core – Recursion and financial modelling

Question 17 D

Number of copies per year = $\frac{960}{0.03}$ = 32000

Question 18 B

Flat rate =

 $\frac{960}{24000} \times 100 = 4\%$

Question 19 B

The sequence is: 5, 15, 35, 75, 155, ... where $T_0=5$ $T_4-T_3=155-75=80$

Question 20 E

Jim's number of followers is 97% of the last month's number (a loss of 3%) with 200 added on each time.

Question 21 A

Amount of principal reduction = payment – interest.

Payment = principal reduction + interest = 1115.45 + 2184.55 = 3300

Question 22 C

Using figures from the table, interest rate per month $=\frac{2187.50}{750000} \times 100 \sim 0.219667$ Annual interest rate $= 0.219667 \times 12 = 3.5\%$

Section A Core – Recursion and financial modelling (continued)

Question 23 D

1.1 1.2 1.3	*2022 exam ngs 🗢 🛛 🚺
eff(4.2,4)	4.26661426551
eff(4.2,12)	4.28180071986
eff(4.25,52)	4.33979445696
eff(4.3,12)	4.38576628342
eff(4.3,4)	4.36983575422
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Use technology to convert the nominal rates to effective rates. 4.3% p.a. compounding monthly gives the highest effective rate of about 4.39%

Question 24 C

Calculate how much is owing after the first year

Finance Solver				
N:	12			
l(%):	8.5	Þ		
PV:	32000			
Pmt:	-658			
FV:	-26617.513777644	•		
PpY:	12	÷		
Finance Solver info stored into				
tvm.n, tvm.i, tvm.pv, tvm.pmt,				

This amount now becomes the present value. Calculate how much is owing after the second year.



Principal reduction = 32000 - 20235.16 = \$11764.84

Total payments = $12 \times 658 + 12 \times 700 = 16296 Total interest paid = 16296 - 11764.84 = \$4531.16

End of solutions Section A Core

Module 1 – Matrices

Question 1 C

The matrix is symmetric about its leading diagonal, so it is an example of a symmetric matrix.

Question 2 A

$$A = \begin{bmatrix} 9 & 7 \\ 1 & 1 \end{bmatrix} - \begin{bmatrix} 6 & 9 \\ 0 & -3 \end{bmatrix} = \begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix}$$

Question 3 D

Inspecting the position of the '1' in each row of the permutation matrix:

5th letter becomes 1st 3rd letter becomes 2nd 2nd letter becomes 3rd 1st letter becomes 4th 4th letter becomes 5th

AGENT becomes TEGAN

Question 4 D

Can do by inspection, or by squaring the one-step dominance matrix. One-step dominant matrix is

0	1	1	[0
1	0	0	1
0	1	0	1
1	0	0	0

Squaring it results as follows.

1.2 1.3	3 1.4 🕨 *2022	2 exam …ngs マ	
$\begin{bmatrix} 0 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}^2$	0 1 1 0 1 0 0 1	0 2 0 0 0 1 1 0
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Question 5 E

Columns must add to 1.0, so eliminate options C and D. Now, 68% of Warburn viewers don't change, and 83% of Yarragrove viewers don't change. This is indicated in option E.

Question 6 B

Option B does not follow the rule. n_{21} must be 5, not 1 as is shown. $3 \times 2 - 1 = 5$

Module 1 – Matrices (continued)

Question 7 B

Solving $T \times F_2 - B = \begin{bmatrix} 77 \\ 110 \\ 59 \end{bmatrix}$ Gives $X = 108.571 \sim 109$
🖣 1.1 1.2 1.3 🕨 *2022 exam ngs 🗢 🛛 🚺 🗙
solve $\begin{bmatrix} 0.3 & 0.2 & 0.3 & x & y \\ 0.6 & 0.4 & 0.3 & y & 2 & 110 & x \\ 0.1 & 0.4 & 0.2 & z & 7 & 59 \end{bmatrix}$
x=77.1428571429 and y=108.571428571 an▶
solve $\begin{pmatrix} 0.3 & 0.2 & 0.5 \\ 0.6 & 0.4 & 0.3 \\ 0.1 & 0.4 & 0.2 \end{pmatrix} \begin{pmatrix} w \\ x \\ y \end{pmatrix} = \begin{bmatrix} 5 \\ 2 \\ 5 \\ 110 \\ y \end{bmatrix} \begin{pmatrix} 77 \\ 10 \\ 59 \end{bmatrix}$
w=77.1428571429 and x=108.571428571 ar
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Question 8 C

The numbers in the rooms remain constant, so if 27 participants change from room A to room B for session 2, 27 must change from room B to room A.

36% of x = 27	
250/cfu = 27	$x = \frac{27}{0.36} = 75$
2370 of y - 27	$y = \frac{27}{0.25} = 108$
Total number of participants = 183	

End of Module 1 Solutions

Module 2 – Networks and decision mathematics

Question 1 E

Only the middle vertex has an even degree. (remember that a loop counts as 2)

Question 2 D

e = v + f - 2= 9 + 4 - 2 = 11

Question 3 B

Option B involves an edge (connecting C and G) being used twice.

A<mark>GC</mark>DEF<mark>CG</mark>ABCFH

Question 4 D

C and D both have A and B as immediate predecessors, so a dummy must run from either A or B to start of both C and D.

E has both C and D as immediate predecessors, so a dummy must run from end of either C or D to the start of E.

This is satisfied in option D.

Question 5 A



Following the arrows, we see that B D, E and G are all reachable from C. A and F are unreachable.

Question 6 B



The spanning tree includes x and y. The smallest edge coming from the end of y weighs 3. Smallest edge coming from end of x weighs 2, so spanning tree length = 1 + 2 + 3 + 5 + x + y = 19. x + y = 8, so eliminate options A, D and E.

Now if y = 7, this edge would **not** be in the minimal spanning tree (as its greater than 6), so eliminate option C.

A quick check will show that if x = 3 and y = 5, the minimal spanning tree will have a length of 19.

Module 2 – Networks and decision mathematics (continued)

Question 7 C

Forward and backward scanning show that the earliest completion time is 24 hours and that the critical path is BEG. Activity E has two immediate predecessors, A and B. Float time for activity D = 21 - 7 - 5 = 9 hours. Latest start time for activity F is 12 hours, **not** 11.



Question 8 B



Minimum cut gives maximum flow. The minimum cut, as shown, has capacity of 6+3+13+8=30