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NAME:	:	

VCE® General Mathematics

Unit 3 & 4 Examination 1

Reading time: 10 minutes Writing time: 90 minutes

QUESTION AND ANSWER BOOK

Section	Number of questions	Number of questions Number of questions	
		to be answered	
A	16	16	16
В	8	8	8
C	8	8	8
D	8	8	8
		Total	40

This exam will be marked out of 40.

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, and rulers.
- Students are permitted to bring into the examination room: Bound reference notebook, 1 CAS calculator, 1 Scientific calculator.

Materials supplied

- Question and Answer Book of 22 pages.
- Answer sheet for Multiple-Choice Questions.

Instructions

- Write your **student name** in the space provided above on this page.
- Check that your **student name** is printed on your answer sheet for multiple-choice.
- All written responses must be in English.

At the end of the examination

• Place the answer sheet for multiple-choice questions inside the front cover of this book.

Your teacher will advise you of the contribution of this exam to your School-Assessed Coursework.

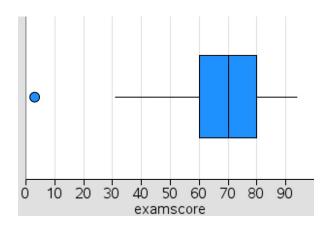
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Section A – Data Analysis

Suggested time: 36 minutes

The following information is to be used for Questions 1, 2 & 3

The box plot below contains the results of 32 students doing a General Maths Examination



Question 1

What is the approximate range of the plot?

- **A.** 62
- **B.** 20
- **C.** 10
- **D.** 91
- **E.** 100

Question 2

The upper and lower fences of the plot respectfully are

- **A.** 60 & 80
- **B.** 3 & 94
- **C.** 30 & 110
- **D.** 58.5 & 81.5
- **E.** 31 & 94

The number of students that achieved results below 60 on the exam is

- **A.** 25
- **B.** 50
- **C.** 75
- **D.** 16
- **E.** 8

The following information is to be used for Questions 4, 5, 6 & 7

Stem	Leaf			
4	567788			
5	24688			
6	589			
7	4 5			
8	7			
9	9			

Question 4

The Shape of the Stem and Leaf plot is

- A. Symmetric
- **B.** Positive
- C. Negative
- D. Square
- E. Random

Question 5

The Median of the Stem and Leaf plot is

- **A.** 57
- **B.** 58
- **C.** 68
- **D.** 69

E. 47

95% of the data in the Stem and Leaf plot is approximately between

- **A.** 14.87 & 106.91
- **B.** 30.21 & 76.23
- **C.** 45.55 & 91.57
- **D.** 30.21 & 91.57
- **E.** 45.55 & 76.23

Question 7

A Z-Score of 2.36 would result in a value of approximately

- **A.** 24.7
- **B.** 97
- **C.** 96
- **D.** -3.84
- **E.** 92

Cooling Water

100
80
60
40
20
0
10
20
30
40

Time

The following information is to be used for Questions 8, 9, 10 and 11.

Question 8

The direction and form of the scatter plot is

- **A.** Positive Linear
- **B.** Positive Non-Linear
- C. Negative Linear
- **D.** Negative Non-Linear
- E. Strong Negative

Question 9

Which transformation would be best used to linearise the data?

- **A.** Log(Temperature)
- **B.** Time²
- C. Temp²
- **D.** Time³
- E. Log(Time²)

If the linearised data results in the following values, the gradient and intercept would be

r	S _y	S_x	$\overline{\mathbf{x}}$	y
-0.995	0.18	11.83	21	1.6

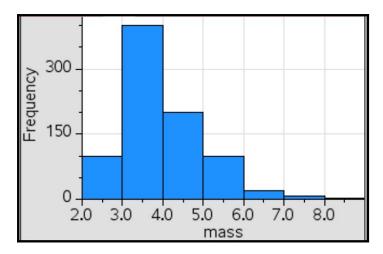
- **A.** 1.6 & 21
- **B.** -0.015 & 1.92
- **C.** -0.995 & 0.18
- **D.** 11.83 & -0.015
- **E.** 1.92 & -0.995

Question 11

The transformation provides a predicted value of 20.61 for a time of 40 minutes. The resultant residual value is

- **A.** -19.39
- **B.** -0.61
- **C.** 0.61
- **D.** 19.39
- E. Not enough information

The graph below shows the log(mass) of animals against the frequency of them.

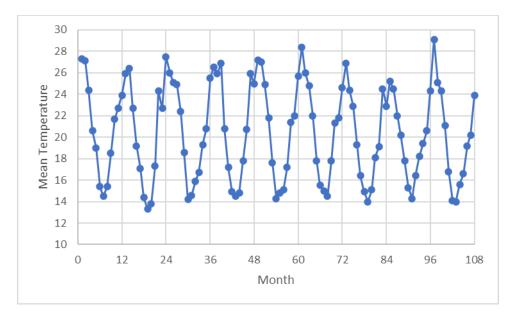


How many animals had a mass between 100000 and 1000000 grams?

- **A.** 100
- **B.** 400
- **C.** 200
- **D.** 20
- **E.** 8

Question 13

The following plot shows the Mean temperature in Melbourne over 9 years:



The plot can be best described as

- A. Cyclic
- B. Increasing trend
- C. Decreasing trend
- D. Seasonal
- E. Random

Question 14

In the table below, what is the missing Seasonal Index value?

	Winter	Spring	Summer	Autumn
Seasonal Index	1.28	1.02		0.96

- **A.** 0.98
- **B.** 1.04
- **C.** 0.80
- **D.** 1.42
- **E.** 0.74

To correct for seasonality, the 5 point smoothed value for week 7 is

Week	1	2	3	4	5	6	7	8	9
Rainfall (mm)	32	18	15	17	48	9	12	23	22

- **A.** 22.8
- **B.** 21.8
- **C.** 20.2
- **D.** 21.4
- **E.** 26

Question 16

The seasonal index of ice cream sales in December is 1.8. To correct for seasonality, the actual value in December needs to be

- **A.** Increased by 55.6%
- **B.** Increased by 80%
- **C.** Stay the same
- **D.** Decreased by 55.6%
- E. Decreased by 80%

Section B - Recursion and Financial Modelling Suggested time: 18 minutes

Question 17

For the following sequence of terms, the relevant Recurrence relation is

450, 900, 1350, 1800, 2250, 2700...

A.
$$V_0 = 450$$
, $V_{n+1} = V_n - 450$

B.
$$V_0 = 450, V_{n+1} = V_n + 450$$

$$\mathbf{C.} \ V_0 = 450, \ V_{n+1} = V_0 - 450$$

D.
$$V_0 = 450$$
, $V_{n+1} = V_0 + 450$

$$V_{n+1} = V_0 + 450$$

Ouestion 18

A car is purchased for \$74 999. After it has driven for 5 years it now has a value of \$42 599. On average the car is driven for 24000 km a year.

The unit rate that the car depreciates per km is

- **A.** \$0.27
- **B.** \$2.70
- **C.** \$27
- **D.** \$32400
- **E.** \$0.35

Question 19

Dana has invested their life savings into a bank account that pays 6.4% p/a simple interest. They deposited \$12400. After 3 years the value of their account is

- **A.** \$793.60
- **B.** \$79360
- **C.** \$2380.80
- **D.** \$14780.80
- **E.** \$13987.20

If the investment from question 19 was instead a compound investment, the difference in account balance after 3 years, compounding 6 monthly, would be

- **A.** \$14979.59
- **B.** \$2579.59
- **C.** \$198.79
- **D.** \$3210.87
- **E.** \$14936.40

The following information is for Questions 21 and 22

Payment Number	Payment	Interest	Principal reduction	Balance
0	0	0	0	35000
1	4825	1295	3530	31470
2	4825	1164.39	3660.61	27809.39
3	4825		3796.05	24013.34

Question 21

The missing value in the reducing balance amortisation table is

- **A.** \$4825
- **B.** \$35000
- **C.** \$1028.95
- **D.** \$3.7
- **E.** \$3796.05

The value of the final payment would be

- **A.** \$2793.60
- **B.** \$2819.40
- **C.** \$4825
- **D.** \$2923.72
- E. \$1901.28

Question 23

A company wishes to start a yearly prize. They intend to invest \$325000 into an account and each year have \$12000 to award. What is the annual interest rate the account would need to be invested at, to one decimal place?

- **A.** 3.7%
- **B.** 3.6%
- **C.** 96.3%
- **D.** 96.4%
- **E.** 1.03%

Question 24

Using the recurrence relation below, the value of the account after 5 years is closest to

$$V_0 = 37000, \ V_{n+1} = 1.0034V_n + 600$$

- **A.** \$37632.92
- **B.** \$37932.92
- **C.** \$38233.29
- **D.** \$40633.33
- **E.** \$40653.76

Section C – Matrices

Suggested time: 18 minutes

The following information is to be used for Questions 25 and 26

$$A = \begin{bmatrix} 12 & 13 & 19 & 22 \\ 7 & 12 & 31 & 44 \\ 54 & 23 & 3 & 46 \\ 16 & 12 & 4 & 27 \end{bmatrix}$$

Question 25

The element in position A₃₁, if matrix A is transposed, is

- **A.** 12
- **B.** 13
- **C.** 19
- **D.** 22
- **E.** 54.

Question 26

To the nearest value, what is the determinant of matrix A?

- **A.** 116719
- **B.** 116720
- **C.** 911
- **D.** 1418
- **E.** 18188

If a matrix follows the rule 3i - 2j what is the missing value in the matrix below?

$$\begin{bmatrix} 1 & -1 & -3 \\ 4 & 2 & 0 \\ 7 & 5 \end{bmatrix}$$

- **A.** 1
- **B.** 2
- **C.** 3
- **D.** 4
- E. 5

Question 28

Why does a Leslie matrix only use the females of a sample?

- **A.** You only need to use 50% of data.
- **B.** Male animals have a shorter life expectancy.
- C. Only female animals give birth.
- **D.** Female animals have a longer life expectancy.
- E. You don't have to use only Females.

The matrix product $\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix}$ is equal to

L

[E]N L \boldsymbol{A} R G

GLER

E N L \boldsymbol{A} G

R

D. $\lfloor E \rfloor$

EGR \boldsymbol{A} LN

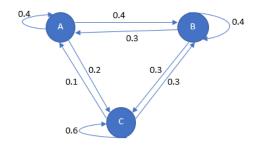
The steady state of the matrix equation below is found after how many iterations?

$$T = \begin{bmatrix} 0.7 & 0.3 & 0.1 \\ 0.1 & 0.3 & 0.4 \\ 0.2 & 0.4 & 0.5 \end{bmatrix} and S_0 = \begin{bmatrix} 2400 \\ 1200 \\ 9000 \end{bmatrix}$$

- **A.** 50
- **B.** 12
- **C.** 13
- **D.** 20
- **E.** 99

Question 31

The graph below results in which transition matrix?



- $\begin{array}{c}
 A \\
 B \\
 C
 \end{array}
 \begin{bmatrix}
 0.4 & 0.4 & 0.2 \\
 0.4 & 0.3 & 0.1 \\
 0.2 & 0.3 & 0.6
 \end{array}$
 - $A \begin{bmatrix} 0.4 & 0.3 & 0.1 \end{bmatrix}$
 - $B \mid 0.4 \ 0.4 \ 0.3 \mid$
- **B.** $C \begin{bmatrix} 0.2 & 0.3 & 0.6 \end{bmatrix}$
 - $A \begin{bmatrix} 0.4 & 0.4 & 0.1 \end{bmatrix}$
 - $B \mid 0.4 \mid 0.3 \mid 0.3 \mid$
- C. $C \begin{bmatrix} 0.2 & 0.3 & 0.6 \end{bmatrix}$
 - $A [0.4 \ 0.4 \ 0.2]$
 - $B \mid 0.3 \ 0.4 \ 0.3 \mid$
- **D.** $C \begin{bmatrix} 0.1 & 0.3 & 0.6 \end{bmatrix}$

 - $\begin{array}{c|cccc}
 A & 0.6 & 0.3 & 0.2 \\
 B & 0.3 & 0.4 & 0.4
 \end{array}$
- $C \begin{bmatrix} 0.1 & 0.3 & 0.4 \end{bmatrix}$

To find the value of S_{n+1} the rule $S_{n+1} = TS_n + D$ is used, where the values of T, S_0 and D are:

$$T = \begin{bmatrix} .6 & .5 \\ .4 & .5 \end{bmatrix}, S_0 = \begin{bmatrix} 320 \\ 580 \end{bmatrix} \text{ and } D = \begin{bmatrix} -12 \\ 27 \end{bmatrix}$$

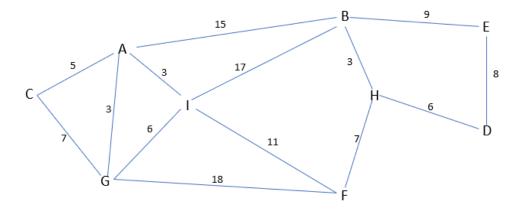
The value of S₄ to 2 decimal places is

- **A.** $\begin{bmatrix} 470 \\ 445 \end{bmatrix}$
- B. \[\begin{pmatrix} 492.5 \\ 437.5 \end{pmatrix}
- C. $\begin{bmatrix} 510.73 \\ 449.28 \end{bmatrix}$
- **D.** $\begin{bmatrix} 487.98 \\ 427.02 \end{bmatrix}$
- E. $\begin{bmatrix} 502 \\ 442 \end{bmatrix}$

Section D - Networks

Suggested time: 18 minutes

The following graph is to be used for Questions 33, 34 and 35



Question 33

The number of faces in the graph is

- **A.** 7
- **B.** 6
- **C.** 5
- **D.** 9
- **E.** 8

Question 34

A Eulerian Trail of the graph is

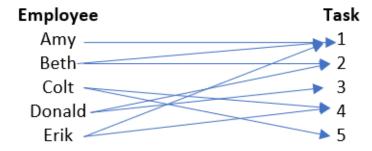
- **A.** H-D-E-B-F-G-C-A-G-I-A-B-I-F
- **B.** H-D-E-B-H-F-G-C-A-G-I-A-B-I-F
- C. H-F-G-C-A-G-I-A-B-I-F
- D. H-D-E-B-H-F-G-C-A-G-I-A-B
- E. H-D-E-B-H-F-G-C- A-B-I-F

The length of the minimum spanning tree of the graph is

- **A.** 26
- **B.** 36
- **C.** 46
- **D.** 56
- **E.** 66

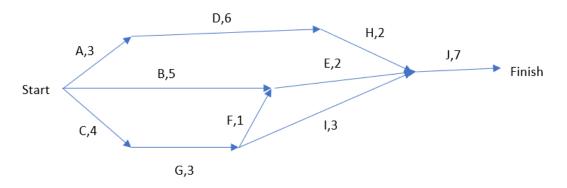
Question 36

By using the bipartite graph below, who will be doing task 4?



- A. Amy
- B. Beth
- C. Colt
- **D.** Donald
- E. Erik

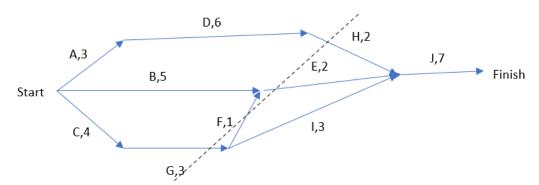
In the graph below, the LST of activity C is



- **A.** 0
- **B.** 1
- **C.** 2
- **D.** 3
- **E.** 4

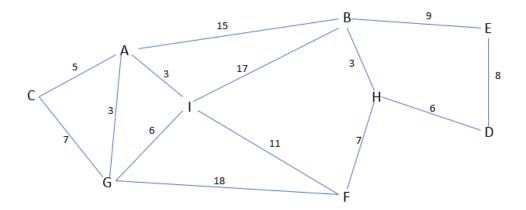
Question 38

The size of the cut in the graph below is



- **A.** 6
- **B.** 7
- **C.** 8
- **D.** 9
- **E.** 10

What is the shortest path from A to H in the graph below?



- **A.** 15
- **B.** 16
- **C.** 17
- **D.** 18
- **E.** 20

Question 40

What is the critical path for the activity table below?

Activity	Predecessor	Duration
A	-	3
В	A	4
С	A	2
D	В	5
Е	С	1
F	С	2
G	D, E	4
Н	F, G	3

- A. A-B-C-D-E-F-G-E
- **B.** A-B-D-G-H
- **C.** A-B-C-G-H
- **D.** A-B-D-F-H
- **E.** A-C-E-G-H

Multiple-Choice Answer Sheet

INSTRUCTIONS FOR MULTIPLE-CHOICE ANSWER SHEET

Use a **PENCIL** for **ALL** entries. For each question, shade the box which indicates your answer.

Marks will **NOT** be deducted for incorrect answers.

NO mark will be given if more than **one** answer is completed for any question.

If you make a mistake, ERASE the incorrect answer - DO NOT cross it out.

1	A	В	C	D	E
2	A	В	C	D	E
3	A	В	C	D	E
4	A	В	C	D	E
5	A	В	C	D	E
6	A	В	C	D	E
7	A	В	C	D	E
8	A	В	C	D	E
9	A	В	C	D	E
10	A	В	C	D	E
11	A	В	C	D	E
12	A	В	C	D	E
13	A	В	C	D	E
14	A	В	C	D	E
15	A	В	C	D	E
16	A	В	C	D	E
17	A	В	C	D	E
18	A	В	C	D	E
19	A	В	C	D	E
20	A	В	C	D	E

					1
21	A	В	C	D	E
22	A	В	C	D	E
23	A	В	С	D	E
24	A	В	С	D	E
25	A	В	С	D	E
26	A	В	C	D	E
27	A	В	C	D	E
28	A	В	С	D	E
29	A	В	C	D	E
30	A	В	C	D	E
31	A	В	С	D	E
32	A	В	C	D	E
33	A	В	C	D	E
34	A	В	С	D	E
35	A	В	C	D	E
36	A	В	С	D	E
37	A	В	С	D	E
38	A	В	С	D	E
39	A	В	С	D	E
40	A	В	C	D	E



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VCE® General Mathematics Unit 3 & 4 Examination 1

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Solution Pathway

Below are sample answers. Please consider the merit of alternative responses.

1	A	В	C	D	E
2	A	В	С	D	E
3	A	В	C	D	E
4	A	В	С	D	E
5	A	В	C	D	E
6	A	В	С	D	E
7	A	В	C	D	E
8	A	В	C	D	E
9	A	В	C	D	E
10	A	В	C	D	E
11	A	В	C	D	E
12	A	В	C	D	E
13	A	В	C	D	E
14	A	В	C	D	E
15	A	В	C	D	E
16	A	В	C	D	E
17	A	В	C	D	E
18	A	В	C	D	E
19	A	В	C	D	E
20	A	В	C	D	E

21	A	В	C	D	E
22	A	В	C	D	E
23	A	В	С	D	E
24	A	В	С	D	E
25	A	В	C	D	E
26	A	В	C	D	E
27	A	В	C	D	E
28	A	В	C	D	E
29	A	В	C	D	E
30	A	В	C	D	E
31	A	В	С	D	E
32	A	В	С	D	E
32					
	A	В	C	D	E
33	A	B B	C C	D D	E E
33	A A A	B B	C C	D D D	E E E
33 34 35	A A A	B B B	C C C	D D D	E E E
33 34 35 36	A A A A	B B B	C C C	D D D D	E E E E
33 34 35 36 37	A A A A A	B B B B	C C C C	D D D D D	E E E E
33 34 35 36 37 38	A A A A A A A	B B B B B	C C C C	D D D D D D D	E E E E E

Question 1: D

Top whisker is approximately 94, lower outlier is at approximately 3.

Question 2: C

Q1 is 60 and Q3 is 80.

 $upper\,f\,ence \colon 80 + 1.5 \times 20 = 110$

lower f ence: $60 - 1.5 \times 20 = 30$.

Question 3: E

60 is the Q1, below this is 25% of the data. 25% of 32 is 8.

Question 4: B

The data is bunched more towards the start of the graph.

Question 5: A

Median is between 56 and 58.

Question 6: D

95% of the data is 2 standard deviations, the mean is 60.89.

Question 7: B

Using the z-score formula
$$2.36 = \frac{x - 60.89}{15.34}$$
.

Question 8: D

The data is decreasing and clearly shows a curve.

Question 9: A

The possible transformations are Log and reciprocal.

Question 10: B

gradient =
$$r \frac{s_y}{s_x} = -0.995 \frac{.18}{11.83} = -0.015$$

$$Intercept = 1.6 - -0.015 \times 21 = 1.92$$

Question 11: B

Reading the graph shows 40min is 20.20-20.61 = -0.61.

Question 12: A

Log(100000) is 5, log(1000000) is 6, from the graph between 5 and 6 is 100.

Question 13: D

The graph repeats with every 7th value of the year being a minimum.

Question 14: E

The index values need to total 4.

Question 15: A

$$\frac{48+9+12+23+22}{5} = 22.8$$

Question 16: D

$$\frac{1}{1.8} = 0.556$$
This is a reduction of 55.6%

Question 17: B

The first value is 450 and increases by 450 each time.

Question 18: A

The change in value is \$32400. This divided by 5 years of 24000km is 0.27.

Question 19: D

The interest over the 3 years amounts to \$2380.80. Adding this to the initial amount results in a balance of \$14780.80.

Question 20: C

The value after 3 years is \$14979.60. This results in a difference of \$198.79.

Question 21: C

By using the values in payment 1 or 2, it can be determined that the interest is 3.7%. 3.7% of \$27809.39 is \$1028.95.

Question 22: D

After 8 full payments there is still \$2819.40. 3.7% on top of this results in a payment of \$2923.72.

Question 23: A

This is a perpetuity, to maintain the balance an interest level of 3.69223% is needed, thus 3.7%.

Question 24: E

By completing the formula 5 times, the value \$40653.76 is found.

Question 25: C

When the matrix is transposed the third row starts with 19.

Question 26: B

The determinant is 116720.

Question 27: C

Using the formula shows that 3(3) - 2(3) = 3.

Question 28: C

Leslie matrices only take into consideration the females as they are the ones that give birth, given Leslie matrices are looking at birth and survival rates.

Question 29: B

The permutation is asking for the 2nd letter, then the 3rd, last, 6th, 5th, 1st and finally 4th.

Question 30: C

The 13th state rounds to the result that is equal to the steady state.

Question 31: D

Only D has all the correct values.

Question 32: C

By completing the relation 4 times results in option C.

Question 33: A

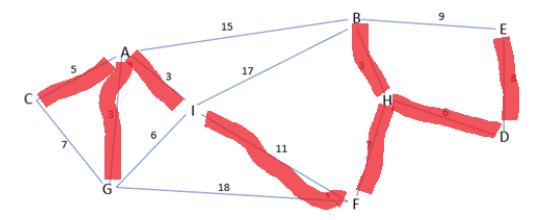
There are 7 faces in the graph.

Question 34: B

Only option B shows a complete Eulerian Trail.

Question 35: C

The minimum spanning tree is as below and is 46 long.



Question 36: E

Only Erik and Colt can do task 4, Colt is the only person who can do task 5, thus Erik has to do 4.

Question 37: B

The critical path is 18 long. The longest path including C is 17, thus its latest start time is 1.

Question 38: B

The cut goes over 4 lines, however the path F is going into the back of the cut and not counted.

Question 39: D

The shortest path is A-B-H which is 18 long.

Question 40: B

The critical path is A-B-D-G-H.