

VCE General Mathematics Units 1&2

AT2.1 – OUTCOMES 1 and 2

| Thursday Feb 9, 2023 - Pe | eriod 1 | | | | |
|---|--|--|---------------------------|------------------------------|----------|
| You have 75 minutes to co | omplete this test | | | | |
| Calculators and notes are | permitted. | | | | |
| | Uni | variate Data 1 | ſest | | |
| | Name: | | | | |
| Circle teacher's name: | Ms Jabeen | Mr Rossignolo | Ms Le | Ms Yang | |
| Note: The grade or score for Coursework score may | this task is only pa y change as a result | rt of the internal assessi of statistical moderatic | ment for this Unit on. | t. Your total School- | assessed |
| Section A/ | 15 Sect | tion B | /30 To | otal | / 45 |
| Satisfactory Comple | tion? S/N: _ | | | | |
| | | | | | |

Assessment Criteria

Students should be able to:

- Define and explain key concepts and apply a range of related mathematical routines and procedures.
- Apply mathematical processes in non-routine contexts, including situations requiring problemsolving, modelling or investigative techniques or approaches, with a view to analyse and discuss these applications of mathematics.
- Use numerical, graphical and symbolic functionalities of technology to develop mathematical ideas, produce results and carry out analysis in situations requiring problem-solving, modelling or investigative techniques or approaches.

Instructions

A single bound reference and a CAS and scientific calculator permitted.

Answer all questions in the spaces provided.

Round values to 2 decimal places where not specified.

In questions where more than one mark is available, appropriate working must be shown.

Multiple choice questions are worth one mark each.

| Section | А |
|---------|---|
| | |

Multiple Choice Questions

15 marks

Circle the letter corresponding to the correct response.

The following information relates to Questions 1, 2, 3 and 4.

The number of lollies in a selection of packets are recorded below:

 $16 \ \ 21 \ \ 18 \ \ 15 \ \ 19 \ \ 17 \ \ 24 \ \ 15 \ \ 32 \ \ 13$

1. The mean of the data set is:

- **A.** 17
- **B.** 17.5
- **C.** 18
- **D.** 18.5
- **E.** 19

2. The median of the data set is:

- **A.** 17
- **B.** 17.5
- **C.** 18
- **D.** 18.5
- **E.** 19

3. The standard deviation of the data set is:

- **A.** 5.58
- **B.** 5.29
- **C.** 19
- **D.** 190
- E. 3890

4. The percentage frequency of packs containing 15 lollies is:

- **A.** 2%
- **B.** 6.7%
- **C.** 10%
- **D.** 15%
- **E.** 20%

5. Examine the following boxplot



For the distribution shown in the boxplot it is true to say that:

- A. The range is 35
- **B.** The interquartile range is 15
- **C.** The mean is 20
- **D.** The interquartile range is 24
- **E.** The median = interquartile range

The following information relates to Questions 6, 7 and 8.

The marks gained by two classes X and Y on a test are given below:

| | (| Cla | SS | Х | | Class Y |
|---|---|-----|----|---|---|-----------|
| | | | 8 | 2 | 5 | 89 |
| | 5 | 3 | 2 | 1 | 6 | 0 3 4 6 |
| 8 | 5 | 3 | 1 | 0 | 7 | 0 2 6 6 7 |
| | | 2 | 1 | 0 | 8 | 1 4 8 |
| | | | 8 | 0 | 9 | 2 8 |
| | | | | | | |

Key:
$$5|8 = 58$$

6. The interquartile range for Class X is:

A. 16

- **B.** 17
- **C.** 18
- **D.** 19
- **E.** 20

7. The distribution of the grades for Class Y can best be described as:

- A. Symmetric
- B. Positively skewed
- C. Negatively skewed
- D. Bimodal
- E. Clustered

The following information relates to Questions 8 and 9.

Consider the following graph. It displays the number of children in various households.



- 8. Based on the graph, it can be said that:
- A. 50 families were surveyed and the data is negatively skewed.
- **B.** 50 families were surveyed and the data is positively skewed.
- C. 55 families were surveyed and the data is negatively skewed.
- **D.** 55 families were surveyed and the data is positively skewed.
- E. 55 families were surveyed and the data is symmetrical.
- **9.** Which of the following statements is NOT true regarding the distribution of children in households.
- A. Less than 50% of households had fewer than one child
- **B.** More than 10% of households had one child.
- C. 10% of families had 2 children.
- **D.** 15 families had one child.
- **E.** 15 families had more than one child.

10. The level of *water usage* of 250 houses was rated in a survey as **low**, **medium** and **high**, and the *corresponding size of the houses* as **small**, **standard** or **large**.

The variables, level of water usage and size of house, as recorded in this survey are:

- A. Both nominal variables
- **B.** Both ordinal variables
- C. Categorical and numerical variables respectively
- D. Numerical and categorical variables respectively
- E. Neither categorical nor numerical variables.

The following information relates to Questions 11 and 12.

The following parallel box and whisker plot below, showing the Algebra Scores for Classes 1 and 2.



Algebra Scores

11. On the Algebra test, the students in the top half of Class 1 scored at least:

- **A.** 50%
- **B.** 72%
- **C.** 80%
- **D.** 85%
- E. 90%

12. When comparing Class 1 to Class 2, which of the following statements is true.

- A. The median mark of Class 2 is greater than the median mark for Class 1.
- **B.** The interquartile range of Class 1 is greater than the interquartile range of Class 2.
- C. The range of both classes was the same.
- **D.** The middle 50% of students in Class 2 did better than the top 75% of Class 1.
- E. The top 25% of students in Class 2 did better than the top students in Class 1.

13. The stem plot below shows the *height*, in centimetres, of 20 players in a junior football team.

| key: | 14 2 | = 142 | 2 cm | | <i>n</i> = | 20 | | |
|------|------|-------|------|---|------------|----|---|---|
| 14 | 2 | 2 | 4 | 7 | 8 | 8 | 9 | |
| 15 | 0 | 0 | 1 | 2 | 5 | 5 | 6 | 8 |
| 16 | 0 | 1 | 1 | 2 | | | | |
| 17 | 9 | | | | | | | |

A player with a height of 179 cm is considered an outlier because 179 cm is greater than:

- **A.** 162 cm
- **B.** 169 cm
- **C.** 172.5 cm
- **D.** 173 cm
- **E.** 175.5 cm

The following information relates to Questions 14 and 15.

800 participants auditioned for a stage musical. Each participant was required to complete a series of ability tests for which they received an overall score.

The overall scores were approximately normally distributed with a mean score of 69.5 points and a standard deviation of 6.5 points.

14. The percentage of participants who scored between 56.5 and 82.5 points is:

- **A.** 50%
- **B.** 68%
- **C.** 95%
- **D.** 99.7%
- **E.** 100%
- **15.** Only the participants who scored at least 76.0 points in the audition were considered successful. Using the 68-95-99.7% rule, how many of the participants were considered unsuccessful?
- **A.** 127
- **B.** 128
- **C.** 272
- **D.** 672
- **E.** 673

Include working throughout.

Question 1 (7 marks)

A group of Year 11 students were surveyed for shoe size. Their results are listed below:

| 7 | 9 | 10 | 8 | 7 | 8 | 9 | 6 | 6 | 7 |
|---|---|----|---|---|----|---|---|---|---|
| 9 | 9 | 8 | 8 | 8 | 10 | 9 | 9 | 8 | 7 |

(a) Complete the following frequency table. Correct your answer to one decimal place.

| Shoe Size | Frequency | Percentage Frequency |
|-----------|-----------|----------------------|
| 6 | | |
| 7 | | |
| 8 | | |
| 9 | | |
| 10 | | |
| Total | | |

3 marks

(b) Draw a bar chart for the data on the grid below:



3 marks

(c) What percentage of students had a shoe size greater than 7? Round your answer to the nearest whole number.

1 mark

Question 2 (10 marks)

The VCE student population at St Leonard's college were surveyed for the number of hours spent on homework (rounded to the nearest whole hour) for the week beginning 1 February 2023. The mean of the data is 13.2 and the mode is 13. The number of hours spent on completing the homework is summarised in the boxplot below:



(a) Write down the five-number summary for the data.

| X_{min} | |
|----------------|--|
| \mathbf{Q}_1 | |
| Q 2 | |
| Q3 | |
| Xmax | |
| | |

5 marks

(b) Find the value of the interquartile range (IQR)

1 mark

(c) Write down the percentage of students who spent more than 12 hours on homework in that week.

1 mark

(d) Given that 166 students spent between 12 and 15 hours on homework, how many students were surveyed?

1 mark

(e) Determine the upper fence and the lower fence for this boxplot.

Question 3 (13 marks)

(b)

(c)

The age of the patients (in years) admitted to a small hospital during one week, and their gender were recorded:

Females: 9, 10, 15, 27, 31, 37, 40, 43, 50, 79

Males: 13, 16, 21, 24, 25, 26, 27, 34, 40, 47

(a) Construct a back-to-back stem and leaf plot of these data sets by using the key given.

| | Females | | Males | |
|----------|--------------------|--------|--------|---------|
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | Ke | y: 2 1 | =21 | |
| | | | | 4 marks |
| Determin | ne the median for: | | | |
| Fema | ales: | | Males: | |
| | | | | 2 marks |
| Determir | ne the IQR for: | | | |
| Fema | ales: | | Males: | |
| | | | | 2 marks |

| (d) Calculate the percentage of patients who were admitted to | o the hospital age | d over 40, for both genders. |
|---|--------------------|------------------------------|
|---|--------------------|------------------------------|

2 marks

(e) Do the back-to-back plots support the contention that the age of the patients is associated with their gender? Write a brief explanation that compares the distributions in terms of centre and spread.

3 marks

END OF TEST