

YEAR 12
IARTV TEST — OCTOBER 1994
MATHEMATICAL METHODS Units 3 and 4
CAT 2 — Facts and Skills Task
SECTION A — ANSWERS & SOLUTIONS

Question 1 E

Question 2 D

Question 3 A

Question 4 D

Question 5 B

Question 6 C

Question 7 C

Question 8 A

Question 9 B

Question 10 C

Question 11 E

Question 12 A

Question 13 E

Question 14 D

Question 15 B

Question 16 A

Question 17 E

Question 18 B

Question 19 A

Question 20 C

Question 21 A

Question 22 B

Question 23 C

Question 24 B

Question 25 C

Question 26 D

Question 27 D

Question 28 D

Question 29 D

Question 30 E

Question 31 C

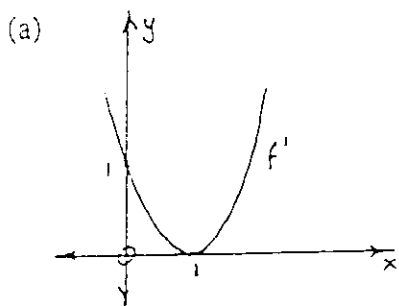
Question 32 C

Question 33 B

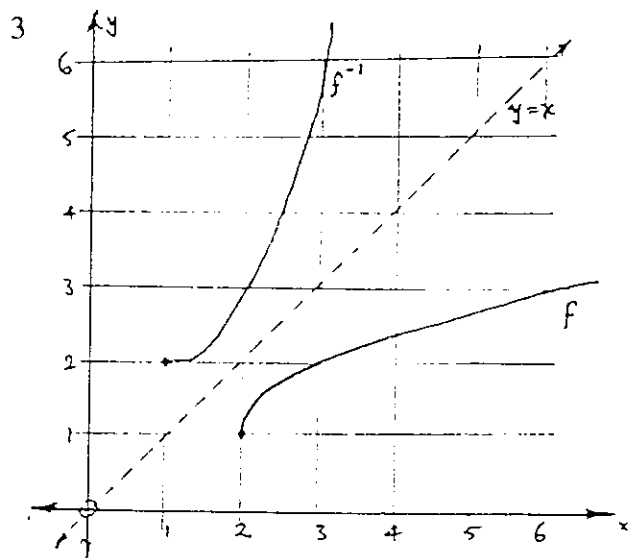
1 (a) $2x^3 + x^2 - 8x - 4$
 $= x^2(2x + 1) - 4(2x + 1)$
 $= (2x + 1)(x^2 - 4)$
 $= (2x + 1)(x - 2)(x + 2)$

(b) $6x^4 + 5x^3 - 6x^2$
 $= x^2(6x^2 + 5x - 6)$
 $= x^2(3x - 2)(2x + 3)$
 $= x^2(3x - 2)(2x + 3)$

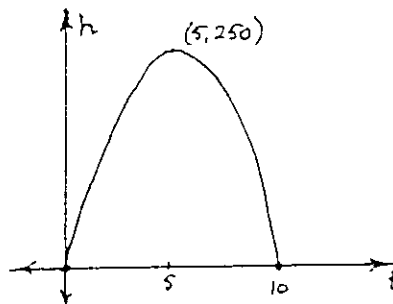
2 $f(x) = \frac{1}{3}x^3 - x^2 + x$
Hence $f'(x) = x^2 - 2x + 1$
 $= (x - 1)^2$



- (b) (i) Local minimum point and x-intercept [$f'(1) = 0$]
(ii) Stationary point of inflexion



4 $h = 100t - 10t^2 = -10t(t - 10)$



(a) Average velocity over first 5 sec. = $(250 - 0)/(5 - 0)$ m/s
 $= 50$ m/s

(b) $\frac{dh}{dt} = 100 - 20t$

When $t = 0$, $\frac{dh}{dt} = 100$

Hence initial velocity = 100 m/s

5 For first quartile Q_1 , $\Pr(Z < z) = 0.25$
Hence $\Pr(Z > z) = 0.75$
Hence (from table), $z = -0.6745$
Hence $Q_1 = 175 - 0.6745 \times 12$ cm
 $= 166.906$ cm

For third quartile Q_3 , $\Pr(Z < z) = 0.75$
Hence (from table), $z = 0.6745$
Hence $Q_3 = 175 + 0.6745 \times 12$ cm
 $= 183.094$ cm

Hence inter-quartile range
 $= 183.094 - 166.906$ cm
 ≈ 16 cm (to nearest cm)