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# Victorian Certificate of Education 2003

# MATHEMATICAL METHODS (CAS) PILOT STUDY Written examination 1 (Facts, skills and applications)

### Friday 7 November 2003

Reading time: 9.00 am to 9.15 am (15 minutes) Writing time: 9.15 am to 10.45 am (1 hour 30 minutes)

# PART I MULTIPLE-CHOICE QUESTION BOOK

This examination has two parts: Part I (multiple-choice questions) and Part II (short-answer questions). Part I consists of this question book and must be answered on the answer sheet provided for multiple-choice questions.

Part II consists of a separate question and answer book.

You must complete **both** parts in the time allotted. When you have completed one part continue immediately to the other part.

	Structure of book	
Number of questions	Number of questions to be answered	Number of marks
27	27	27

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers, a protractor, set-squares, aids for curve sketching, up to four pages (two A4 sheets) of pre-written notes (typed or handwritten) and one approved CAS calculator (memory may be retained) and/or one scientific calculator. For the TI-92, Voyage 200 or approved computer based CAS, their full functionality and/or one scientific calculator may be used, but other programs or files are not permitted.
- Students are NOT permitted to bring into the examination room: blank sheets of paper and/or white out liquid/tape.

#### Materials supplied

- Question book of 14 pages, with a detachable sheet of miscellaneous formulas in the centrefold.
- Answer sheet for multiple-choice questions.

#### Instructions

- Detach the formula sheet from the centre of this book during reading time.
- Check that your **name** and **student number** as printed on your answer sheet for multiple-choice questions are correct, **and** sign your name in the space provided to verify this.
- Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

#### At the end of the examination

- Place the answer sheet for multiple-choice questions (Part I) inside the front cover of the question and answer book (Part II).
- You may retain this question book.

Students are NOT permitted to bring mobile phones and/or any other electronic communication devices into the examination room.

## Working space

#### **Instructions for Part I**

Answer all questions in pencil on the answer sheet provided for multiple-choice questions.

Choose the response that is **correct** for the question.

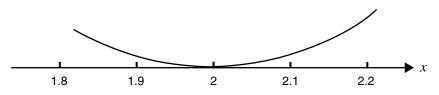
A correct answer scores 1, an incorrect answer scores 0.

Marks will not be deducted for incorrect answers.

No marks will be given if more than one answer is completed for any question.

#### **Question 1**

A polynomial function p has degree three. A portion of its graph near the point on the graph with coordinates (2,0) is shown below.

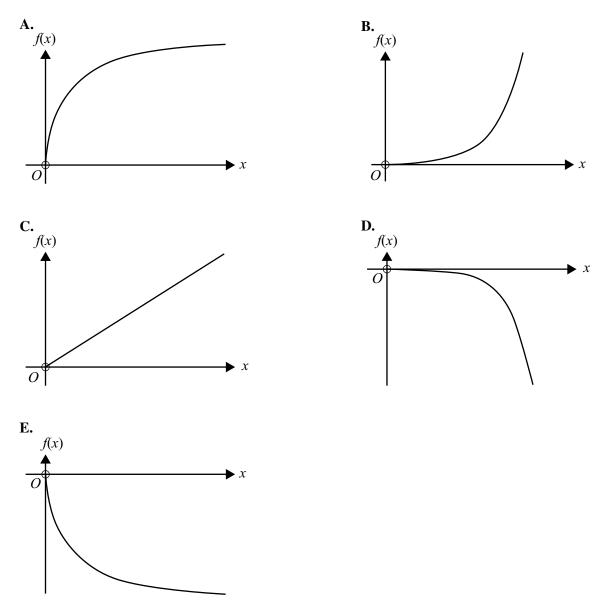


Which one of the following could be the rule for the third degree polynomial *p*?

- **A.**  $p(x) = x(x+2)^2$
- **B.**  $p(x) = (x 2)^3$
- C.  $p(x) = x^2(x-2)$
- **D.**  $p(x) = (x-1)(x-2)^2$
- **E.**  $p(x) = -x(x-2)^2$

#### CONTINUED OVER PAGE

The graph of the function  $f: \mathbb{R}^+ \to \mathbb{R}$  with rule  $f(x) = x^{\frac{1}{3}}$  is most likely to be



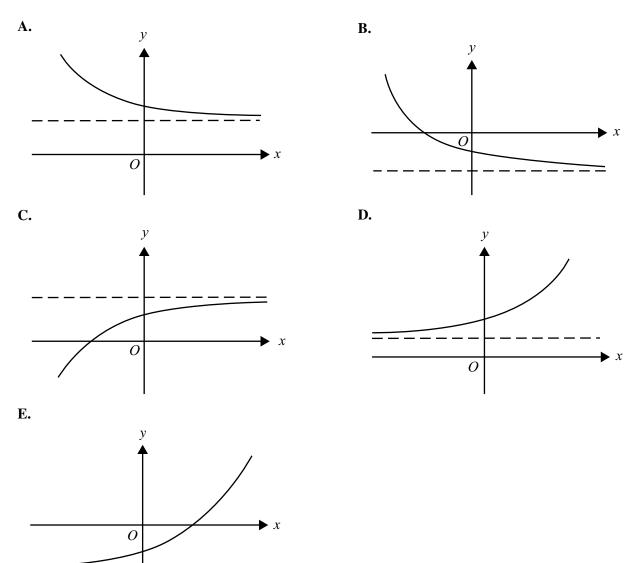
#### **Question 3**

Dylan drew the graph of the function  $f: R \to R$ ,  $f(x) = \frac{x^3 + 1}{x}$  by adding the ordinates of the graphs of two functions g and h.

The rules for g and h that Dylan could have used are

- **A.**  $g(x) = x^3$  and  $h(x) = \frac{1}{x}$ **B.**  $g(x) = x^2$  and  $h(x) = \frac{1}{x}$
- **C.**  $g(x) = x^3 + 1$  and h(x) = x
- **D.**  $g(x) = x^3 + 1$  and  $h(x) = \frac{1}{x}$
- **E.**  $g(x) = x^2$  and h(x) = 1

If *k* and *P* are positive real numbers, which one of the following graphs is most likely to be the graph of the function with equation  $y = e^{kx} + P$ ?



PART I – continued TURN OVER

The graph of the function f is obtained from the graph with equation  $y = \sqrt{x}$  by a reflection in the y-axis followed by a dilation of 2 units from the x-axis.

The rule for f is

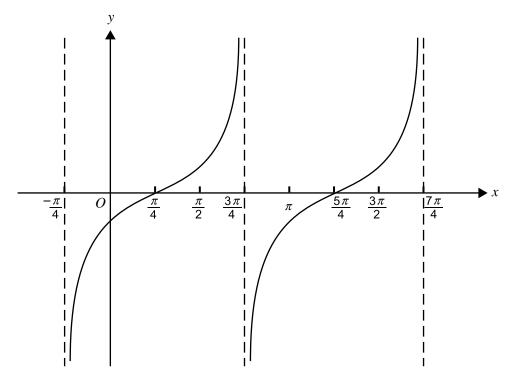
- A.  $f(x) = -2\sqrt{x}$
- **B.**  $f(x) = \sqrt{-2x}$
- $\mathbf{C.} \quad f(x) = \sqrt{-0.5x}$
- **D.**  $f(x) = -0.5\sqrt{x}$
- $\mathbf{E.} \quad f(x) = 2\sqrt{-x}$

#### **Question 6**

The number of solutions of the equation  $0.5 \cos(2x) = 1$ , for  $x \in [-\pi, \pi]$  is

- **A.** 0
- **B.** 1
- **C.** 2
- **D.** 3
- **E.** 4

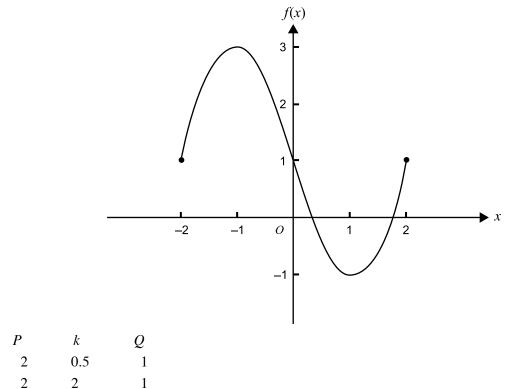
The diagram shows two cycles of the graph of a circular function.



The period of the circular function is

- **A.**  $\frac{\pi}{2}$  **B.**  $\frac{3\pi}{4}$ **C.**  $\pi$
- **D.**  $\frac{7\pi}{4}$
- **Ε.** 2*π*

The graph of the function  $f:[-2, 2] \rightarrow R$ ,  $f(x) = P \sin(k\pi x) + Q$  is shown below. The values of *P*, *k*, and *Q* respectively are



B.	2	2	1
C.	-2	2	-1
D.	-2	0.5	1
E.	-2	0.5	-1

### **Question 9**

A.

If  $y = \cos^2(2x)$ , then  $\frac{dy}{dx}$  is equal to A.  $4\sin(2x)\cos(2x)$ B.  $-4\sin(2x)\cos(2x)$ C.  $4x\sin(2x^2)$ D.  $-4x\sin(2x^2)$ 

**E.**  $-4\sin(x)\cos(2x)$ 

#### **Question 10**

If  $y = x \log_e(x)$ , then the rate of change of y with respect to x when x = 2 is equal to

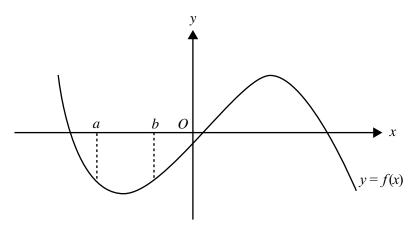
- **A.**  $\log_{e}(2)$
- **B.** 1
- **C.**  $1 + \log_e(2)$
- **D.** 2
- **E.**  $1 + \log_2(e)$

Let  $f: R \to R$  be a function such that f'(-1) = 0and f'(x) > 0 when x < -1and f'(x) > 0 when x > -1. At x = -1, the graph of f has a **A.** local minimum. **B.** local maximum.

- C. stationary point of inflection.
- **D.** point of discontinuity.
- **E.** gradient of -1.

#### **Question 12**

Part of the graph of the function f is shown below.



Let g be a function such that g'(x) = f(x).

On the interval (a, b), the graph of g will have

- A. negative gradient.
- **B.** positive gradient.
- **C.** a local minimum value.
- **D.** a local maximum value.
- E. zero gradient.

#### **Question 13**

- If  $f'(x) = 4e^{2x}$ , then f(x) could be equal to
- **A.**  $2 e^{2x} + 3$
- **B.**  $4 e^{2x} + 5$
- C. 8  $e^{2x} + 2$
- **D.**  $4 \log_e(2x) 4$
- **E.**  $\log_e(8x) + 5$

If 
$$\int_{1}^{4} f(x)dx = 2$$
, then  $\int_{1}^{4} (2f(x)+3)dx$  is equal to  
**A.** 2  
**B.** 4  
**C.** 7  
**D.** 10  
**E.** 13

#### **Question 15**

Let g be a continuous function on the interval [0, 5], and f a function such that f'(x) = g(x) for all  $x \in [0, 5]$ .

Then  $\int_{0}^{5} g(x)dx$  is equal to **A.** g'(5) - g'(0) **B.** f(5) **C.** f'(5) - f'(0) **D.** g(5) - g(0)**E.** f(5) - f(0)

#### **Question 16**

The total area of the regions enclosed by the graph of  $y = \sin(2x)$  and the *x*-axis, between x = 0 and  $x = 2\pi$ , is equal to

- **A.** 1
- **B.** 2
- **C.** 4
- **D.** 8
- **E.** 16

#### **Question 17**

The interval [0, 4] is divided into *n* equal subintervals by the points  $x_0$ ,  $x_1$ , ...,  $x_{n-1}$ ,  $x_n$  where  $0 = x_0 < x_1 < ... < x_{n-1} < x_n = 4$ . Let  $\delta x = x_i - x_{i-1}$  for i = 1, 2, ..., n.

Then 
$$\lim_{\delta x \to 0} \sum_{i=1}^{n} (x_i \, \delta x)$$
 is equal to  
**A.**  $\int_{4}^{0} x \, dx$   
**B.**  $\int_{0}^{4} \frac{x^2}{2} dx$   
**C.** 0  
**D.** 4  
**E.** 8

Let  $f(x) = e^x$ .

For all positive real numbers x and y, f(x + y) is equal to

**A.** f(x) + f(y)

- **B.** f(x)f(y)
- C. f(xy)
- **D.**  $(f(x))^y$
- **E.**  $f(x^y)$

#### **Question 19**

The line with equation y = x + k, where k is a real number, intersects the parabola with equation  $y = x^2 + x - 2$  in two distinct points if

- **A.** k < -2
- **B.** k > -2
- **C.** k = -2
- **D.** *k* < 2
- **E.**  $k \neq 2$

#### Question 20

Let  $p(x) = (x^2 + a)(x + b)(x - c)$  where a, b and c are three distinct positive real numbers.

The number of real solutions to the equation p(x) = 0 is exactly

- **A.** 0
- **B.** 1
- **C.** 2
- **D.** 3
- **E.** 4

#### **Question 21**

Let  $f(x) = \frac{2}{x-3} + 1$ .

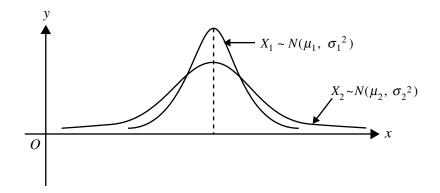
The equations of the asymptotes of the graph of the inverse function  $f^{-1}$  are

A. x = 1 and y = 3B. x = 1 and y = -3C. x = 3 and y = 1D. x = -3 and y = -1E. x = -1 and y = -3 If  $2\log_e(x) - \log_e(x+2) = 1 + \log_e(y)$ , then y is equal to

**A.**  $\frac{x^2}{10(x+2)}$  **B.**  $\frac{2x}{x+2} - 1$  **C.**  $\frac{x^2}{x+2}$  **D.**  $\frac{2x}{x+2}$ **E.**  $\frac{x^2}{e(x+2)}$ 

#### **Question 23**

The diagram below shows the graphs of two normal distribution curves with means  $\mu_1$  and  $\mu_2$  and standard deviations  $\sigma_1$  and  $\sigma_2$  respectively.



Which one of the following statements is true?

- **A.**  $\mu_1 > \mu_2$  and  $\sigma_1 = \sigma_2$
- **B.**  $\mu_1 > \mu_2$  and  $\sigma_1 > \sigma_2$
- **C.**  $\mu_1 = \mu_2$  and  $\sigma_1 > \sigma_2$
- **D.**  $\mu_1 = \mu_2$  and  $\sigma_1 < \sigma_2$
- **E.**  $\mu_1 < \mu_2$  and  $\sigma_1 = \sigma_2$

Which of the following tables could represent the probability distribution of a discrete random variable?

Ι	v	2	3	4	5					
	$\Pr(V = v)$	0.1	0.2	0.4	0.5					
II	W	-2	-1	0	1					
	$\Pr(W = w)$	0.2	0.3	0.3	0.2					
III	x	10	20	30	40					
	$\Pr(X = x)$	0.4	0.3	0.2	0.1					
IV	у	0	1	2	3					
	$\Pr(Y = y)$	-0.1	0.4	0.5	0.2					
V	Z.	1	2	3	4					
	$\Pr(Z=z)$	1	$\frac{1}{8}$	1	1					
		8	$\overline{8}$	$\overline{4}$	$\frac{1}{2}$					

- A. I and III
- **B.** I and IV
- C. II and IV
- **D.** II, III and V
- **E.** I, II and V

#### **Question 25**

The lifetime, in hours, of a light globe, can be modelled by a continuous random variable with probability density function

$$g(t) = \begin{cases} 0.001e^{-0.001t} & \text{if } t > 0 \\ 0 & \text{if } t \le 0 \end{cases}$$

The probability, correct to three decimal places, that a randomly selected light globe has a lifetime less than 1000 hours is

- **A.** 0.095
- **B.** 0.368
- **C.** 0.500
- **D.** 0.632
- **E.** 0.905

60 per cent of all tickets sold at a racecourse are Adult tickets and the remaining 40 per cent are Concession tickets. A random sample of 20 tickets is taken.

The probability that this sample contains exactly twelve Adult tickets is equal to

$$\mathbf{A.} \quad \frac{{}^{60}C_{12} \times {}^{40}C_8}{{}^{100}C_{20}}$$

**B.**  ${}^{20}C_{12} (0.4)^8 \times (0.6)^{12}$ 

C. 
$${}^{20}C_{12} (0.4)^{12} \times (0.6)^8$$

**D.** 
$$(0.4)^8 \times (0.6)^{12}$$

**E.**  $(0.4)^{12} \times (0.6)^8$ 

#### **Question 27**

A bag contains 12 bread rolls, of which 8 are white and the remainder multigrain. Tony takes 2 bread rolls at random from the bag to eat.

The probability that at least one is a multigrain roll is

**A.** 
$$1 - \frac{2^{12}}{3^{12}}$$
  
**B.**  $1 - \frac{{}^{8}C_{2}}{{}^{12}C_{2}}$ 

$$\mathbf{C.} \quad 1 - \frac{2^{12}}{3^{12}} - 12 \times \frac{1}{3} \times \frac{2^{11}}{3^{11}}$$

**D.** 
$$1 - \frac{{}^{8}C_{2}}{{}^{12}C_{2}} - \frac{{}^{8}C_{1} \times {}^{4}C_{1}}{{}^{12}C_{2}}$$

**E.** 
$$\frac{{}^{8}C_{1} \times {}^{4}C_{1}}{{}^{12}C_{2}}$$



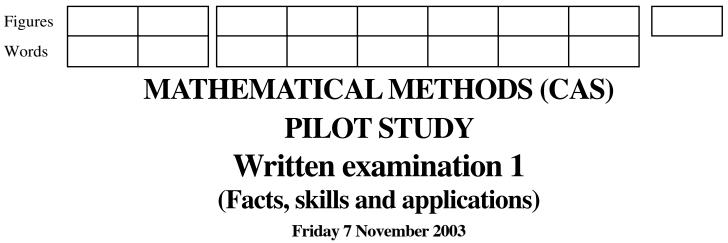


SUPERVISOR TO ATTACH PROCESSING LABEL HERE

Letter

Victorian Certificate of Education 2003

#### STUDENT NUMBER



Reading time: 9.00 am to 9.15 am (15 minutes) Writing time: 9.15 am to 10.45 am (1 hour 30 minutes)

# PART II QUESTION AND ANSWER BOOK

This examination has two parts: Part I (multiple-choice questions) and Part II (short-answer questions). Part I consists of a separate question book and must be answered on the answer sheet provided for multiple-choice questions.

Part II consists of this question and answer book.

You must complete **both** parts in the time allotted. When you have completed one part continue immediately to the other part.

	Structure of book							
Number of questions	Number of questions to be answered	Number of marks						
6	6	23						

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers, a protractor, set-squares, aids for curve sketching, up to four pages (two A4 sheets) of pre-written notes (typed or handwritten) and one approved CAS calculator (memory may be retained) and/or one scientific calculator. For the TI-92, Voyage 200 or approved computer based CAS, their full functionality and/or one scientific calculator may be used, but other programs or files are not permitted.
- Students are NOT permitted to bring into the examination room: blank sheets of paper and/or white out liquid/ tape.

#### Materials supplied

• Question and answer book of 8 pages.

Instructions

- Detach the formula sheet from the centre of the Part I book during reading time.
- Write your **student number** in the space provided above on this page.
- All written responses must be in English.

#### At the end of the examination

• Place the answer sheet for multiple-choice questions (Part I) inside the front cover of this question and answer book.

Students are NOT permitted to bring mobile phones and/or any other electronic communication devices into the examination room.

PART II - continued

Working space

#### **Instructions for Part II**

- Answer all questions in the spaces provided.
- A decimal approximation will not be accepted if an exact answer is required to a question.
- In questions where more than 1 mark is available, appropriate working must be shown.
- Unless otherwise indicated, the diagrams in this book are not drawn to scale.

#### **Question 1**

Let  $f: R \to R$ ,  $f(x) = ax^2 + bx + c$ , where a, b and c are real numbers and  $a \neq 0$ .

Suppose that f(1) = 6 and f'(1) = 4.

**a.** Find the values of *a* and *b* in terms of *c*.

Suppose  $\int_{0}^{\infty} f(x) dx = 6$ . Find the value of c. b.

2 + 2 = 4 marks

Find the **exact** solutions of the equation  $\sin(2\pi x) = -\sqrt{3}\cos(2\pi x), 0 \le x \le 1$ .

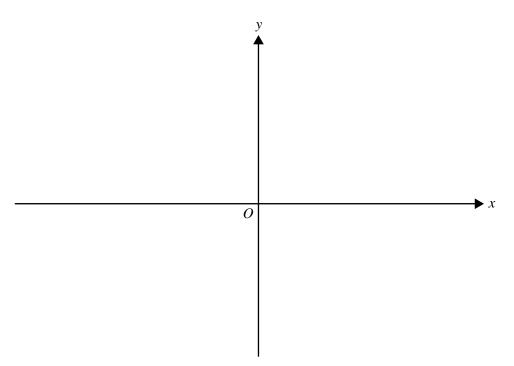
2 marks

#### **Question 3**

Let  $f: D \to R$ ,  $f(x) = 2 \log_e(|x+3|) + 1$ , where *D* is the maximal domain of *f*. **a.** State *D*.

**b.** Find the exact coordinates of the points where the graph of y = f(x) intersects the *x*- and *y*-axes.

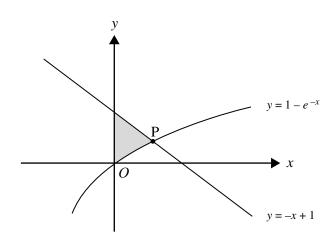
c. Sketch the graph of y = f(x) on the axes below. Indicate any asymptote with its equation.



1 + 3 + 2 = 6 marks

The graphs with equations y = -x + 1 and  $y = 1 - e^{-x}$  are shown below. The graphs intersect at the point P which has *x*-coordinate *k*.

6



**a.** Find the value of *k*, correct to three decimal places.

**b.** Write down a definite integral, the value of which is the area of the shaded region.

c. Hence find the area of the shaded region, correct to two decimal places.

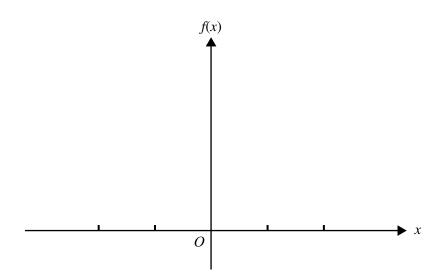
1 + 1 + 1 = 3 marks

PART II - continued

The probability density function of the continuous random variable X is given by

f(x) = a(2 - |x|), for -2 < x < 2 and 0 elsewhere (where *a* is a real constant).

**a.** On the axes provided sketch the graph of this probability density function.



#### **b.** Find the value of *a*.



2 + 2 = 4 marks

Kim goes to the sports centre each evening and either works out in the gym or has a swim. She never has a swim two evenings in a row. If she has a work-out in the gym one evening, then the next evening she is twice as likely to have a swim as she is to have a work-out in the gym. On a particular Monday evening, she works out in the gym.

- **a.** What is the probability that she works out in the gym on both the Tuesday and Wednesday evenings of that week?
- **b.** What is the probability that she has a swim on the Friday of that week?

1 + 3 = 4 marks

# MATHEMATICAL METHODS (CAS) PILOT STUDY

Written examinations 1 and 2

FORMULA SHEET

**Directions to students** 

Detach this formula sheet during reading time.

This formula sheet is provided for your reference.

# **Mathematical Methods CAS Formulas**

## Mensuration

area of a trapezium:	$\frac{1}{2}(a+b)h$	volume of a pyramid:	5
curved surface area of a cylinder:	$2\pi rh$	volume of a sphere:	$\frac{4}{3}\pi r^3$
volume of a cylinder:	$\pi r^2 h$	area of a triangle:	$\frac{1}{2}bc\sin A$
volume of a cone:	$\frac{1}{3}\pi r^2h$		

## Calculus

$$\frac{d}{dx}(x^{n}) = nx^{n-1}$$

$$\frac{d}{dx}(e^{ax}) = ae^{ax}$$

$$\frac{d}{dx}(\log_{e}(x)) = \frac{1}{x}$$

$$\frac{d}{dx}(\sin(ax)) = a\cos(ax)$$

$$\frac{d}{dx}(\cos(ax)) = -a\sin(ax)$$

$$\frac{d}{dx}(\tan(ax)) = \frac{a}{\cos^{2}(ax)} = a\sec^{2}(ax)$$

approximation:  $f(x + h) \approx f(x) + hf'(x)$ 

average value:  $\frac{1}{b-a}\int_{a}^{b} f(x)dx$ 

volume of a pyramid: 
$$\frac{3}{3}Ah$$
  
volume of a sphere:  $\frac{4}{3}\pi r^3$   
area of a triangle:  $\frac{1}{2}bc \sin A$ 

$$\int x^n dx = \frac{1}{n+1} x^{n+1} + c, n \neq -1$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + c$$

$$\int \frac{1}{x} dx = \log_e |x| + c$$

$$\int \sin(ax) dx = -\frac{1}{a} \cos(ax) + c$$

$$\int \cos(ax) dx = \frac{1}{a} \sin(ax) + c$$
product rule:  $\frac{d}{dx} (uv) = u \frac{dv}{dx} + v \frac{du}{dx}$ 
chain rule:  $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$ 
quotient rule:  $\frac{d}{dx} \left(\frac{u}{v}\right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$ 

### **Statistics**

$$Pr(A) = 1 - Pr(A') \qquad Pr(A \cup B) = Pr(A) + Pr(B) - Pr(A \cap B)$$

$$Pr(A|B) = \frac{Pr(A \cap B)}{Pr(B)} \qquad \text{transition matrices:} \quad S_n = T^n \times S_0$$

$$\text{mean:} \quad \mu = E(X) \qquad \text{variance:} \quad var(X) = \sigma^2 = E((X - \mu)^2) = E(X^2) - \mu^2$$

Discrete dis	tribut	ions						
		$\Pr(X = x)$	mean	variance				
general		p(x)	$\mu = \Sigma x p(x)$	$\sigma^2 = \Sigma (x - \mu)^2 p(x)$				
			$= \Sigma x^2 p(x) - \mu^2$					
binomial		${}^{n}C_{x}p^{x}(1-p)^{n-x}$	np	np(1-p)				
hypergeometric		$\frac{{}^{D}C_{x}{}^{N-D}C_{n-x}}{{}^{N}C_{n}}$	$n \frac{D}{N}$	$n\frac{D}{N}\left(1-\frac{D}{N}\right)\left(\frac{N-n}{N-1}\right)$				
Continuous	distri	butions						
		$\Pr(a < X < b)$	mean	variance				
general	$\int_{a}^{b} f(x) dx$		$\mu = \int_{-\infty}^{\infty} x \ f(x) dx$	$\sigma^2 = \int_{-\infty}^{\infty} (x-u)^2 f(x) dx$				
				$=\int_{-\infty}^{\infty}x^2f(x)dx-\mu^2$				
normal	If X i	s distributed N( $\mu$ , $\sigma^2$ ) and Z =	$\frac{X-\mu}{\sigma}$ , then Z is distrib	uted N(0, 1), $f(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}$				

Table 1 Normal distribution – cdf

	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359	4	8	12	16	20	24	28	32	36
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753	4	8	12	16	20	24	28	32	35
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141	4	8	12	15	19	23	27	31	35
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517	4	8	11	15	19	23	26	30	34
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879	4	7	11	14	18	22	25	29	32
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224	3	7	10	14	17	21	24	27	31
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549	3	6	10	13	16	19	23	26	29
0.7	.7580	.7611	.7642	.7673	.7703	.7734	.7764	.7793	.7823	.7852	3	6	9	12	15	18	21	24	27
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133	3	6	8	11	14	17	19	22	25
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389	3	5	8	10	13	15	18	20	23
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621	2	5	7	9	12	14	16	18	21
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830	2	4	6	8	10	12	14	16	19
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015	2	4	6	7	9	11	13	15	16
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177	2	3	5	6	8	10	11	13	14
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319	1	3	4	6	7	8	10	11	13
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441	1	2	4	5	6	7	8	10	11
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545	1	2	3	4	5	6	7	8	9
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633	1	2	3	3	4	5	6	7	8
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706	1	1	2	3	4	4	5	6	6
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767	1	1	2	2	3	4	4	5	5
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817	0	1	1	2	2	3	3	4	4
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857	0	1	1	2	2	2	3	3	4
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890	0	1	1	1	2	2	2	3	3
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916	0	1	1	1	1	2	2	2	2
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936	0	0	1	1	1	1	1	2	2
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952	0	0	0	1	1	1	1	1	1
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964	0	0	0	0	1	1	1	1	1
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974	0	0	0	0	0	1	1	1	1
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981	0	0	0	0	0	0	0	1	1
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986	0	0	0	0	0	0	0	0	0
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990	0	0	0	0	0	0	0	0	0
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993	0	0	0	0	0	0	0	0	0
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995	0	0	0	0	0	0	0	0	0
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997	0	0	0	0	0	0	0	0	0
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998	0	0	0		0		0	0	
3.5	.9998	.9998	.9998	.9998	.9998	.9998	.9998	.9998	.9998	.9998	0	0	0	0	0	0	0	0	0
3.6	.9998	.9998	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	0	0	0	0	0	0	0	0	0
3.7	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	0	0	0	0	0	0	0	0	0
3.8	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	0	0	0	0	0	0	0	0	0
3.9		1.0000			1.0000				1.0000		0	0	0		0			0	0

#### **END OF FORMULA SHEET**