TEST 1

Functions and graphs Technology-free end-of-year examination Total marks: 25 Suggested writing time: 40 minutes

Specific instructions to students

- Answer all of the questions in the spaces provided.
- Show all workings in questions where more than one mark is available.
- An exact value must be provided in questions where a numerical answer is required, unless otherwise specified.

QUESTION 1

a State the maximal domain for the function $y = 2\sqrt{x-2}$.

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x \in [2, \infty)
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1 mark

b Hence sketch the graph of $y = 2\sqrt{x-2}$, labelling any axial intercepts with their coordinates.



2 marks (Total: 3 marks)

QUESTION 2

a Sketch the graph of f(x) = 1 - 6x, labelling all axial intercepts.



2 marks

b On the same set of axes, sketch the graph of the inverse function f^{-1} , labelling all axial intercepts clearly.



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2 marks (Total: 4 marks)

QUESTION 3

a Sketch the graph of
$$y = \begin{cases} x^3, & x \ge 1\\ 2, & x < 1 \end{cases}$$



2 marks

b State the value of f(2).

f(2) = 8

1 mark (Total: 3 marks)

QUESTION 4

a State the domain and range of the function $y = -\frac{2}{(x+1)^2} + 3.$

Domain: $x \in \mathbb{R} \setminus \{-1\}$

Range: $y \in (-\infty, 3)$

2 marks

b Hence sketch the graph of function $y = -\frac{2}{(x+1)^2} + 3$, labelling equations of asymptotes and any

y- intercepts with their coordinates.



2 marks (Total: 4 marks) **QUESTION 5**

A cubic function is shown below.



Sketch the inverse relation on the same set of axes.



QUESTION 6

Sketch the graph of $y = -e^{x-1} - 3$, labelling intercepts with the axes and giving the equations of any asymptotes.



2 marks

QUESTION 7

Sketch the graph of $y = 2 \log_e (2x + 2)$, labelling intercepts with the axes and giving the equations of any asymptotes.



2 marks

QUESTION 8

Sketch $y = \cos(x)$ and $y = \cos(2x)$ on the same set of axes for $0 \le x \le 2\pi$. Hence, using addition of ordinates, sketch the graph of $y = \cos(x) + \cos(2x)$.



3 marks

QUESTION 9

The coordinates of *A* and *B* are (-3, 1) and (2, -3) respectively. Find the equation of the line that passes through the points *A* and *B*.



2 marks