**Year 2018**

**VCE**

**Mathematical Methods**

**Trial Examination 1**

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Victorian Certificate of Education

 **2018**

###### STUDENT NUMBER

 Letter

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| FiguresWords |  |  |  |  |  |  |  |  |  |  |  |
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**MATHEMATICAL METHODS**

**Trial Written Examination 1**

Reading time: 15 minutes

Total writing time: 1 hour

**QUESTION AND ANSWER BOOK**

**Structure of book**

|  |
| --- |
|  *Number of Number of questions Number of* *questions to be answered marks* |
|  9 9 40 |

* Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers.
* Students are NOT permitted to bring into the examination room: any technology (calculators or software) notes of any kind, blank sheets of paper, and/or correction fluid/tape.

**Materials supplied**

* Question and answer book of 17 pages.
* Detachable sheet of miscellaneous formulas at the end of this booklet.
* Working space is provided throughout the booklet.

**Instructions**

* Detach the formula sheet from the end of this book during reading time.
* Write your **student number** in the space provided above on this page.
* Unless otherwise indicated, the diagrams in this booklet are **not** drawn to scale.
* All written responses must be in English.

**Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.**

**Instructions**

Answer **all** questions in the spaces provided.

In all questions where a numerical answer is required an exact value must be given unless otherwise specified.

In questions where more than one mark is available, appropriate working **must** be shown.

Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

##### Question 1 (4 marks)

**a.** Let  , find .

 2 marks

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**b.** Let  . Evaluate .

 2 marks

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**Question 2** (3 marks)

A binomial distribution of the random variable *X*, with four independent trials, is such that

. If *p* is the probability of a success on any trial, find the value of *p*.

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**Question 3** (6 marks)

**a.** The tangent to the curve  at the point where  makes an angle

 of  measured with the positive direction of the *x*-axis. Find the value of *p*.

 3 mark

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**b.** A rectangle has two vertices on the graph of , one at the point 

 where  and two on the *x*-axis as shown in the diagram below.

 



**i.** Let *A* be the area of the rectangle, show that 

 1 mark

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**ii.** Hence find the value of *a*, for which the area of the rectangle is a maximum.

 2 marks

##### \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Question 4** (4 marks)

**a.** Solve the equation  for *x*.

 2 marks

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**b.** Solve the equation  for *x*.

 2 marks

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**Question 5** (4 marks)

Packets of smarties contain red smarties and other smarties of other colours.

**a.** A small packet of ten smarties contains three red smarties.

 Let  represent the sample proportion of red smarties in a packet.

**i.** What values can take.

 1 mark

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**ii.** Find 

 1 mark

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**b.** A large jar of smarties contains over 600 smarties. One in four of these are red smarties. A random sample of 300 smarties is selected.

 Find an approximate 95% confidence interval for , the sample proportion of red smarties. Use an integer multiple of the standard deviation in your calculations.

 2 marks

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**Question 6** (5 marks)

Consider the functions with the rules  and ,

defined on their maximal domains.

**i.** Show that  does not exist. 2 marks

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**ii.** If , find the largest subset *D* of *R*, such that

  is defined and determine the function .

 3 marks

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**Question 7** (3 marks)

A discrete random variable *X* has a probability distribution given by

|  |  |  |
| --- | --- | --- |
| *X* | 1 | 2 |
|  |  |  |

**a.** Find the possible values of *k*, given .

2 marks

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**b.** Find .

 1 mark

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**Question 8** (5 marks)



The probability density function of a continuous random variable *X* is given by



The graph of  is shown.





**i.** Explain why 

 1 mark

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**ii.** Find the values of *a* and *k*.

 4 marks

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**Question 9** (6 marks)

**a.** Differentiate  with respect to *x*.

 1 mark

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**b.** Part of the graph of the function  is shown below.



**i.** Find the coordinates of the minimum turning point on the graph of *f*.

 2 marks

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**ii.** Find area of the shaded region.

 Give your answer in the form , where 

 3 marks

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**END OF QUESTION AND ANSWER BOOKLET**

**END OF EXAMINATION**

**EXTRA WORKING PAGE**

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**MATHEMATICAL METHODS**

**Written examination 1**

FORMULA SHEET

Directions to students

Detach this formula sheet during reading time.

 This formula sheet is provided for your reference.

## Mathematical Methods formulas

##  Mensuration

|  |  |  |  |
| --- | --- | --- | --- |
| area of a trapezium |  | volume of a pyramid  |  |
| curved surface area of a cylinder |  | volume of a sphere  |  |
| volume of a cylinder |  | area of triangle  |  |
| volume of a cone |  |  |  |

##  Calculus

|  |  |
| --- | --- |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
| product rule |  | quotient rule  |  |
| chain rule |  |  |

##  Probability

|  |  |
| --- | --- |
|  |  |
|  |  |
| mean |    | variance |  |

|  |  |  |
| --- | --- | --- |
| **Probability distribution** | **Mean** | **Variance** |
| discrete |  |  |  |
| continuous |  |  |  |

##

##  Sample proportions

|  |  |  |
| --- | --- | --- |
|  | mean |    |
| standard deviation |    | approximateconfidenceinterval |  |

**END OF FORMULA SHEET**

##