

## 2005 VCAA Specialist Mathematics Exam 1 Part I

### Multiple-choice question 26

A particle initially at the origin starts from rest at  $t = 0$ . The particle moves in a **straight line** in such a way that its acceleration at time  $t$  is given by  $e^{-0.1t} \mathbf{i} + (6t)\mathbf{j}$ .

The velocity of the particle at time  $t$  is given by

- A.  $-(0.1e^{-0.1t})\mathbf{i} + 6\mathbf{j}$
- B.  $-(10e^{-0.1t})\mathbf{i} + (3t^2)\mathbf{j}$
- C.  $10(1 - e^{-0.1t})\mathbf{i} + (3t^2)\mathbf{j}$
- D.  $0.1(1 - e^{-0.1t})\mathbf{i} + (3t^2)\mathbf{j}$
- E.  $10(10 - t - 10e^{-0.1t})\mathbf{i} + (t^3)\mathbf{j}$

None of the above choices for the velocity of the particle provides a straight line path. In fact a particle with the given acceleration will not move in a straight line.

VCAA suggested **C** is the correct answer, i.e.  $\mathbf{v} = 10(1 - e^{-0.1t})\mathbf{i} + (3t^2)\mathbf{j}$ .

From there,  $\mathbf{r} = 10(t + 10e^{-0.1t} - 10)\mathbf{i} + (t^3)\mathbf{j}$ .

$\therefore x = 10(t + 10e^{-0.1t} - 10)$  and  $y = t^3$ .

$\therefore$  the cartesian equation for the path is  $x = 10(\sqrt[3]{y} + 10e^{-0.1\sqrt[3]{y}} - 10)$ .

The path is shown below. It is obviously not a straight line.

