# Neap

**Trial Examination 2020** 

# **VCE Specialist Mathematics Units 1&2**

Written Examination 1

**Suggested Solutions** 

Neap Education (Neap) Trial Exams are licensed to be photocopied or placed on the school intranet and used only within the confines of the school purchasing them, for the purpose of examining that school's students only. They may not be otherwise reproduced or distributed. The copyright of Neap Trial Exams remains with Neap. No Neap Trial Exam or any part thereof is to be issued or passed on by any person to any party inclusive of other schools, non-practising teachers, coaching colleges, tutors, parents, students, publishing agencies or websites without the express written consent of Neap.

Question 1 (7 marks)				
a.	$t_2 = -$	$4 \times 3 - 2$	M1	
	=	10		
	$t_3 = 4$	$4 \times 10 - 2$		
	= .	38	A1	
b.	i.	$\frac{x}{x-2} = \frac{x+3}{x}$	M1	
		$x^2 = (x - 2)(x + 3)$		
		$x^2 = x^2 + x - 6$		
		0 = x - 6		
		x = 6	A1	
	ii.	sequence:		
		x - 2, x, x + 3		
		$x = 6 \rightarrow 4,  6,  9$		

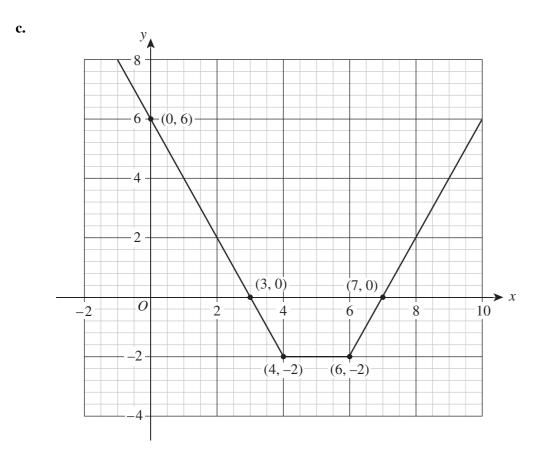
$$r = \frac{6}{4} = \frac{9}{6}$$
$$= \frac{3}{2}$$
A1

iii. 
$$S_{n} = \frac{a(r^{n} - 1)}{r - 1}$$
$$= \frac{4\left(\left(\frac{3}{2}\right)^{n} - 1\right)}{\frac{3}{2} - 1}$$
$$= \frac{4\left(\frac{3}{2}\right)^{n} - 4}{\frac{1}{2}}$$
$$= 8\left(\frac{3}{2}\right)^{n} - 8$$
$$= 2^{3} \cdot \frac{3^{n}}{2^{n}} - 8$$
$$= \frac{3^{n}}{2^{n-3}} - 8$$

M1

A1

Question 2 (7 marks)			
a.	f(0) =  0 - 4  +  0 - 6  - 4 $= 6$		A1
b.	x-4  +  x-6  - 4 = 0		
	Case 1: $x \ge 6$		
	(x-4) + (x-6) - 4 = 0		
	2x = 14		
	<i>x</i> = 7		
	Case 2: 4 < <i>x</i> < 6		
	(x-4) + -(x-6) - 4 = 0		
	-4 + 6 - 4 = 0		
	-2 = 0		
	$\therefore$ no solution		
	Case 3: $x \le 4$	I	<b>M</b> 1
	-(x-4) + -(x-6) - 4 = 0		
	-2x + 6 = 0		
	<i>x</i> = 3		
	Solutions:		
	<i>x</i> = 3		A1
	x = 7		A1



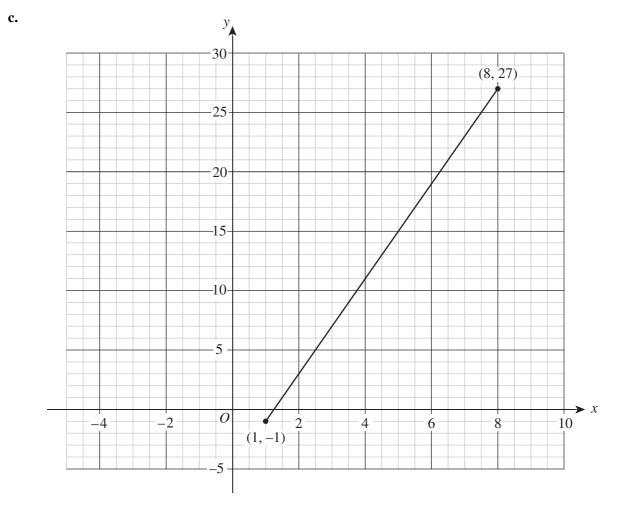
#### 3 marks

*intercept points, correct position and coordinate* A1 *cusp points, correct position and coordinate* A1

correct shape A1

# Question 3 (6 marks)

a.	$t = 0 \rightarrow x = 1, y = -1$	
	$t = 3 \rightarrow x = 8, y = 28$	
	domain:	
	$x \in [1, 8)$	A1
	range:	
	$y \in [-1, 27)$	A1
b.	$x = 2^t$ and $y = 2^{t+2} - 5$	
	$y = 2^2 \times 2^t - 5$	
	$=4 \times 2^t - 5$	M1
	=4x-5	A1



2 marks correct endpoints A1 correct shape A1

## **Question 4** (5 marks)

Assume the contradictory position that  $\sqrt{x} \le 2x$ , for x > 0. a.

$x \le 4x^2$	
$1 \le 4x$	M1
$x \ge \frac{1}{4}$	
The original assumption is incorrect and therefore $0 < x < \frac{1}{4}$ .	A1

The original assumption is incorrect and therefore  $0 < x < \frac{1}{4}$ .

**b.** Assume  $2^{3n} - 1 = 7k$  where  $n, k \in Z^+$ . M1 For  $n = 1 \to LHS = 2^{3 \times 1} - 1 = 7 \to k = 1$   $\therefore$  true for n = 1For  $n + 1 \to LHS = 2^{3(n+1)} - 1$  M1  $LHS = 2^{3n+3} - 1$   $= 8 \times 2^{3n} - 1$   $= 8(2^{3n} - 1) + 7$  = 8(7k) + 7 = 7(8k + 1)As 8k + 1 is an integer, 7(8k + 1) is divisible by 7. A1

As the rule is true for n = 1 and consecutive cases, the rule is true for all n for  $n \in \mathbb{Z}^+$ .

### Question 5 (3 marks)

$$m_{AB} = \frac{6-2}{2-1}$$

$$= 4$$

$$\rightarrow m_{AP} = 0.5 \times 4$$

$$= 2$$
Let the point  $P(x, y)$ .
$$\rightarrow m_{AP} = \frac{y-2}{x-1}$$
M1
$$\frac{y-2}{x-1} = 2$$

$$y-2 = 2(x-1)$$

$$y = 2x$$
 A1

### Question 6 (7 marks)

**a. i.** 
$$\overrightarrow{OC} = \underline{i} + 2\underline{j}$$
 A1

$$OD = 5\underline{i} + \underline{j}$$
 A1

ii. 
$$\overrightarrow{CD} = \overrightarrow{OD} - \overrightarrow{OC}$$
  
=  $5\underline{i} + \underline{j} - (\underline{i} + 2\underline{j})$  M1

$$\left|\overline{CD}\right| = \sqrt{4^2 + (-1)^2}$$
$$= \sqrt{17}$$
A1

b.	$\overrightarrow{EF} = \overrightarrow{OF} - \overrightarrow{OE}$	
	$= p \overrightarrow{OB} - p \overrightarrow{OA}$	
	= p(25i + 5j - 10i - 20j)	
	= p(15i - 15j)	M1
	$\left \overrightarrow{EF}\right  = \sqrt{p^2 (15)^2 + (-15)^2}$	M1
	$=p\sqrt{450}$	
	$= p \sqrt{9 \times 5 \times 5 \times 2}$	
	$=15p\sqrt{2}$	
	unit vector $\left  \overrightarrow{EF} \right  = 1$	
	$15p\sqrt{2} = 1$	
	$p = \frac{\sqrt{2}}{30}$	A1
Question 7 (5 marks)		
a.	Using the alternate segment theorem:	
	$\angle BCX = 50^{\circ}$	A1
b.	Using alternate angles on parallel lines:	
	$\angle CBD = 50^{\circ}$	A1
c.	As $\angle ABC$ is twice the bisected angle,	
	$\angle ABC = 2 \times 50^{\circ} = 100^{\circ}.$	A1
d.	Let $ED = x \rightarrow DB = 2x$	M1
	$ED \times DB = AD \times DC$	
	$x \times 2x = 6 \times 4$	
	$2x^2 = 24$	
	$x = \sqrt{12}$	A1

$$= 2\sqrt{3}$$
 cm

Copyright © 2020 Neap Education Pty Ltd

7