

NAME:

**VSV Student ID:** 

# **ALGORITHMICS UNIT 3**

# SAC 2: Algorithms (Weeks 1 to 5)

# Outcome 2

# Date of Completion: 13-17 May 2024

Reading Time: 5 minutes Writing time: 55 minutes TOTAL (60 minutes)

#### **QUESTION AND ANSWER BOOK**

Туре	Number of questions	Number of questions to be answered	Number of marks
Short/ Extended Response	10	10	38
		Total	38

#### Materials supplied

• Question and answer book of 8 pages

#### Materials permitted

• Pens/Stationary and one Scientific Calculator permitted.

# No Reference material permitted.

#### Instructions

- Write your **name** in the space provided above on this page.
- All written responses must be in English, point form is preferred.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the test room.

1. Consider the graph below:



(a) Carry out a depth first search traversal, stating the order in which vertices are added, adding items to the stack/queue in alphabetical order where multiple options exist.

ABDGIHEC if not added in alphabetical order

(2 marks)

(b) Carry out a breadth first search traversal, stating the order in which vertices are added, adding items to the stack/queue in alphabetical order where multiple options exist.

(2 marks)

2. Maureen is responsible for providing free Wifi to a large city. The city is made up of a number of suburbs, and each suburb has a Wifi access point. These are connected to a central computer by underground cables. The access points are represented as nodes on a graph. The computer needs to be stored at the same place as one of the access points.

To work out the distance from the central computer to each Wifi access point, the following functions are available:

```
Dijkstra(start, end) – uses Dijkstra to return the distance between start and end.
BellmanFord(start) – uses Bellman-Ford to return an array containing the distances between the start node and every other node.
```

Maureen wants to find out where to place the central computer to minimise the average distance between the central computer and each Wifi access point. In addition, where there are multiple solutions with a similar average distance, she would like the central computer to be as close to the suburb "Porttown" as possible.

Describe an algorithmic approach that Maureen can take to achieve these goals. Explain your choice of Dijkstra/BellmanFord at each stage, and why this gives you the most efficient solution.

(4 marks)

3. Consider the following recursive algorithm. It uses the binary operator % such that a % b returns the remainder when a is divided by b. For example, 10 % 3 = 1.

```
Algorithm Surprise(a,b):
    rem = a % b.
    if rem = 0:
        return b
    else:
        return Surprise(b, rem)
```

Showing your working, find what Surprise(56, 12) returns.

(2 marks)

4. Write a recursive function in pseudocode to check that a given string is a palindrome. (i.e. it reads the same forwards and backwards. TACOCAT is a palindrome.)

(4 marks)

(1 mark)

(b) If this algorithm is run on the following graph, add edges to show the resulting output graph.



(2 marks)

#### 6.

Use Prim's algorithm to find a MST for the graph below, starting at node A.



(3 marks)

7. Charles wants to compress a range of strings To compress a string means to make its length smaller whilst preserving the original information, using some clever tricks.

He is using the following pre-existing functions:

compress (X): takes a string X, compresses it and returns a string Y.

length(X): takes a string X and returns its length in bytes.

It is possible to run 'compress' more than once to make a file even smaller. Because of the way the function works, Charles cannot predict how much smaller the compressed file will be in relation to its original file. Sometimes the function cannot make a file any smaller.

His aim is to reduce any given string to 100 bytes or less.

Using the functions compress(X) and length(X), write pseudocode which:

- takes a string input
- compresses it
- checks to see if it is smaller than or equal to 100 bytes
- if it is, then return the compressed string along with the integer '1' to indicate it was compressed once
- if not, compress it again
- keep compressing it until the file size does not change, i.e. maximum compression has been achieved
- returns the compressed string, along with an integer showing the number of times it was compressed

(4 marks)

8. Gita is constructing a social network called Snapgram. A snapgram user can follow another user, and can view the users that any given user follows. A user's popularity increases with the number of followers they have, and with the popularity of those followers.

(a) Explain how three features of this scenario can map onto the PageRank algorithm.

(3 marks)

(b) A small subset of the network is shown here:



*d* = 0.8

Find Pr(C) after the second iteration to three decimal places. (Initialisation does not count as an iteration).



(c) An even smaller subset of the network is shown here:

$$D \longrightarrow E$$

Deduce the value of *d* such that Pr(D) = Pr(E) for all iterations.

(1 mark)

9. Consider the following graph:



Explain whether or not each of the following algorithms can be run on this graph, specifying the range of possible values for the weight of edge *AD* if appropriate.

(i) Bellman Ford

(ii) Dijkstra's

(3 marks)

10. The coin change problem asks what the minimum number of coins is required to make a certain amount of money.

Suppose we take the following approach: at each stage, use the largest coin available which does not exceed the remaining amount.

(a) State the name of this algorithm design pattern.

For example, given the coins [50c, 30c, 5c, 1c], we want to make 60c change.

(b) What solution does the above approach provide?

(1 mark)

(1 mark)

(c) Explain whether or not this approach is guaranteed to be optimal.

END OF TEST

(1 mark)