Supervision Instructions

Mathematics Methods (Unit 1-2)
Task #6
5th of October 2023 – Period 4

Task consists of two papers: **Paper 1** and **Paper 2**. Students will have access to only one paper at a time.

Paper 1:

- 15 minutes
- Calculator is not allowed

After 15 minutes **Paper 1** is to be collected and **Paper 2** will be given.

Paper 2:

- 25 minutes
- Calculator is allowed

After 25 minutes **Paper 2** is to be collected.

Check that students put their names.

2023 Mathematical Methods (Unit 1-2)
Task 6
Paper 1 – Calculator not allowed

Number of marks: 10
Writing time: 15 minutes

Name: Marks:

Instructions

Answer **all** questions in the spaces provided.
In all questions where a numerical answer is required, an exact value must be given unless otherwise specified.
In questions where more than one mark is available, appropriate working **must** be shown.
Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

Question 1

Solve the following for x.

a. $3^{2x} - 3^{x+2} + 18 = 0$ 2 marks

b. $\log_e(2x) + \log_e(x+2) = \log_e(6)$ 2 marks

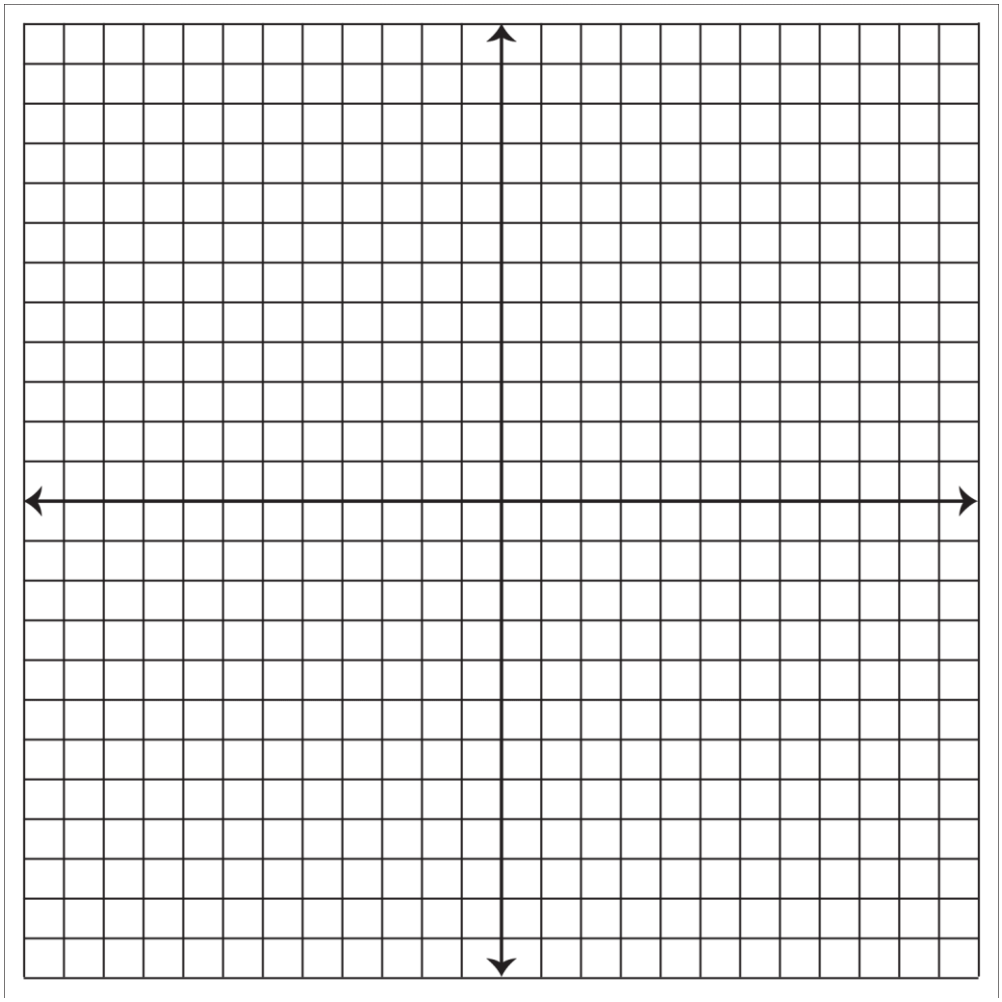
Question 2

Express $\dfrac{9^{1-2m} \times 3^{m-1}}{27^{-m+2}}$ as a power of 3. 2 marks

Question 3

2+1 marks

a. Sketch the graph of $y = 2 - 2\log_{10}(x-1)$ showing any asymptote(s) and axis intercept(s).



b. State the domain of $y = 2 - 2\log_{10}(x-1)$.

2023 Mathematical Methods (Unit 1-2)
Task 6
Paper 2 – Calculator allowed

Number of marks: 15
Writing time: 25 minutes

Name: Marks – Section 1: Section 2:

SECTION 1

Instructions for Section 1

Answer **all** questions in pencil on the answer sheet provided for multiple-choice questions.
Choose the response that is **correct** for the question.
A correct answer scores 1, an incorrect answer scores 0.
Marks will **not** be deducted for incorrect answers.
No marks will be given if more than one answer is completed for any question.

Question 1

The function has a rule $h(x) = r\log_e(x-m)+k$ where *m* and *k* are positive constants and *r* is a negative constant. What is the maximal domain for *h(x)*?

A R^+

B $R\setminus\{m\}$

C $R\setminus\{n\}$

D (m,n)

E (m,∞)

Question 2

When the function $f(x) = \log_{10}(x-1)$ is translated 2 units up, 1 unit right and then reflected in the x axis, the function becomes;

A $y = -\log_{10}(x-2)+2$

B $y = \log_{10}(x-2)+2$

C $y = -\log_{10}(x-2)-2$

D $y = \log_{10}(x-1)+2$

E $y = -\log_{10}(x-1)+2$

Question 3

If $7e^{ax} = 3$ then x equals

A $\dfrac{3}{7}\log_e a$

B $a\log_e\left(\dfrac{3}{7}\right)$

C $\dfrac{\log_e\left(\dfrac{3}{7}\right)}{a}$

D $\dfrac{\log_e(3)}{a\log_e(7)}$

E $\dfrac{a\log_e(3)}{\log_e(7)}$

Question 4

What is the inverse function of $f(x) = 4e^{2x-6} + 2$?

A $\log_e \dfrac{x-2}{4} + 6$

B $\log_e \dfrac{\sqrt{x-2}}{2} + 6$

C $\log_e \dfrac{\sqrt{x-2}}{2} + 3$

D $\dfrac{1}{2}\log_e \dfrac{\sqrt{x+2}}{2} - 3$

E $2\log_e \dfrac{x+2}{4} + 6$

Question 5

What is $e^{(3\log_e x - \log_e(3x))}$ equal to?

A $3\log_e\left(\frac{1}{3}\right)$

B 0

C 1

D $x^3 - 3x$

E $\frac{x^2}{3}$

SECTION 2

Instructions for Section 2

Answer **all** questions in the spaces provided.

In all questions where a numerical answer is required, an exact value must be given unless otherwise specified.

In questions where more than one mark is available, appropriate working **must** be shown.

Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.

Question 1

In her chemistry class, Sarah is preparing a special solution for an experiment that she has to complete. The concentration of the solution can be modelled by the rule.

$$C = A\log_e(kt)$$

Where C is the concentration in moles per litre (M) and t represents the time of the mixing in seconds. The concentration of the solution after 30 seconds as of mixing is 4 M, and the concentration of the solution after 2 seconds of mixing was 0.1 M.

a. Find the values of A and k, correct to 3 decimal places. 2 marks

b. Find the concentration of the solution after 15 seconds of mixing, correct to the nearest whole number. 1 mark

c. How long does it take for the concentration of the solution to reach 10 M, correct to five significant figures? 1 mark

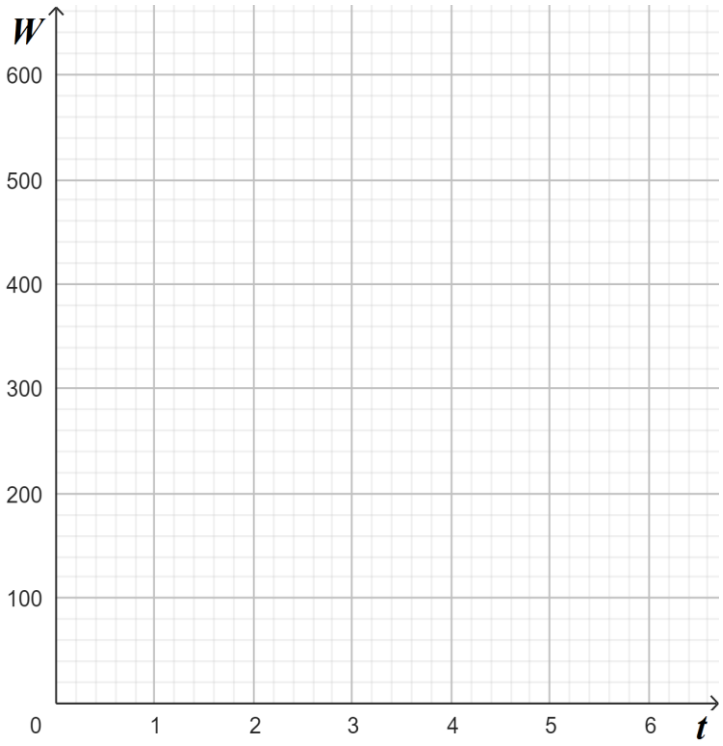
Question 2

The population of the species of wallaby found on a reserve is increasing according to the equation $W = 150 \times 1.08^t$, W is the number of wallabies t years after records were first kept.

a. **i.** Find the initial size of the population. 1+1 marks

ii. Find the population, to the nearest whole number, 1 year and 5 years after records were first kept.

b. Plot a graph of W versus t, showing the coordinates found in part (a). 2 marks



c. Find how long, correct to the nearest whole number, would it take for the population to double. 2 marks