ESSENTIAL MATHEMATICS CORE FOR THE VICTORIAN CURRICULUM

David Greenwood Bryn Humberstone Justin Robinson Jenny Goodman Jennifer Vaughan Stuart Palmer

CAMBRIDGE UNIVERSITY PRESS

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About the Authors

David Greenwood is the Head of Mathematics at Trinity Grammar School in Melbourne and has 25+ years' experience teaching mathematics from Years 7 to 12. He has run numerous workshops within Australia and overseas regarding the implementation of the Australian Curriculum and the use of technology for the teaching of mathematics. He has written more than 30 mathematics titles and has a particular interest in the sequencing of curriculum content and working with the Australian Curriculum proficiency strands.

Bryn Humberstone graduated from the University of Melbourne with an Honours degree in Pure Mathematics, and has taught secondary school mathematics for over 15 years. He has been a Head of Mathematics since 2014 at two independent schools in Victoria. Bryn is particularly passionate about designing engaging mathematical activities and effective assessment tasks for students with a variety of backgrounds and ability levels.

Justin Robinson is the inaugural Director of the Institute of Positive Education based at Geelong Grammar School where he leads a team of staff dedicated to promoting the theory and practice of Positive Education. Prior to this, he spent 20 years teaching mathematics covering all levels of secondary education and with significant experience teaching VCE, IB and A-Levels. Justin is passionate about challenging students within a safe learning environment. Justin is an Honorary Fellow of the University of Melbourne's Graduate School of Education, and was listed in *The Educator's* 2017 'Top 50' Hot List.

Jenny Goodman has taught in schools for over 25 years and is currently teaching at a selective high school in Sydney. Jenny has an interest in the importance of literacy in mathematics education, and in teaching students of differing ability levels. She was awarded the Jones Medal for Education at Sydney University and the Bourke Prize for Mathematics. She has written for *CambridgeMATHS NSW* and was involved in the *Spectrum and Spectrum Gold* series.

Jennifer Vaughan has taught secondary mathematics for over 30 years in New South Wales, Western Australia, Queensland and New Zealand, and has tutored and lectured in mathematics at Queensland University of Technology. She is passionate about providing students of all ability levels with opportunities to understand and to have success in using mathematics. She has had extensive experience in developing resources that make mathematical concepts more accessible; hence, facilitating student confidence, achievement and an enjoyment of maths.

Stuart Palmer has been a head of department in two schools and is now an educational consultant who conducts professional development workshops for teachers all over New South Wales and beyond. He is a Project Officer with the Mathematical Association of New South Wales, and also works with pre-service teachers at The University of Sydney and Western Sydney University.













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Essential Mathematics CORE for the Victorian Curriculum is the successor to the prior *GOLD* series. The new name better reflects the nature of the series: a set of books that focuses on covering the basics of the curriculum in an accessible, straightforward manner. It has been tailored to the Victorian Curriculum and is best suited for students aiming to undertake General/Further Mathematics, a VET course or Foundation Mathematics in Years 11 and 12.

Compared to previous editions, the *CORE* series features some substantial new features in the print and digital versions of the textbook, as well as in the Online Teaching Suite. The main ones are listed below.

Learning intentions and chapter checklist

At the beginning of every lesson is a set of learning intentions that describe what the student can expect to learn in the lesson. At the end of the chapter, these appear again in the form of a chapter checklist of "I can..." statements; students can use this to check their progress through the chapter. Every criterion is listed with an example question to remind students of what the mathematics looks like. These checklists can also be downloaded and printed off so that students can physically check them off as they accomplish their goals.

Now you try

Every worked example now contains additional questions, without solutions, called 'Now you try'. We anticipate many uses of these questions, first and foremost to give students immediate practice at what they've just seen demonstrated in a worked example, rather than expecting students to simply absorb the example by reading through it. We also anticipate these questions will be useful for the teacher to do in front of the class, given that students will not have seen the solution or answer before.

Workspaces and self-assessment

In the Interactive Textbook, students can complete almost any question from the textbook inside the platform via workspaces. Questions can be answered with full worked solutions using three input tools: 'handwriting' using a stylus, inputting text via a keyboard and in-built symbol palette, or uploading an image of work completed elsewhere. Then students can critically engage with their own work using the self-assessment tools, which allow them to rate their confidence with their work and also red-flag to the teacher any questions they have not understood. All work is saved, and teachers will be able to see both students' working-out and how they've assessed their own work via the Online Teaching Suite.

Note that the workspaces and self-assessment feature is intended to be used as much or as little as the teacher wishes, including not at all (the feature can be turned off). However, the ease with which useful data can be collected will make this feature a powerful teaching and learning tool when used creatively and strategically.

Algorithmic Thinking

Х

Previously included as an appendix chapter, Algorithmic Thinking now becomes the last chapter of each book in the series. Instead of exercises and worked examples, this chapter contains a range of activities that show how algorithms and programming can be used as powerful tools for solving mathematical problems across all three Victorian Curriculum content strands (Number and Algebra, Measurement and Geometry, Statistics and Probability). The activities utilise a range of readily-available technologies, can be completed at any time during the year, and assume no prior knowledge of algorithms or coding.

Guide to the working programs

Essential Mathematics CORE for the Victorian Curriculum contains working programs that are subtly embedded in the exercises. The suggested working programs provide two pathways through the book to allow differentiation for Building and Progressing students.

Each exercise is structured in subsections that match the Victorian Curriculum proficiency strands (with Problem-solving and Reasoning combined into one section to reduce exercise length), as well as 'Gold star' (*). The questions* suggested for each pathway are listed in two columns at the top of each subsection.

- The left column (lightest shade) shows the questions in the Building working program.
- The right column (darkest shade) shows the questions in the Progressing working program.

Gradients within exercises and proficiency strands

The working programs make use of two gradients that have been carefully integrated into the exercises. A gradient runs through the overall structure of each exercise – where there's an increasing level of sophistication required as a student progresses through the proficiency strands and then on to the 'Gold Star' question(s) – but also within each proficiency strand; the first few questions in Fluency are easier than the last few, for example, and the first few Problem-solving and reasoning questions are easier than the last few.



The right mix of questions

Questions in the working programs have been selected to give the most appropriate mix of types of questions for each learning pathway. Students going through the Building pathway are given extra practice at the Understanding and basic Fluency questions and only the easiest Problem-solving and reasoning questions. The Progressing pathway, while not challenging, spends a little less time on basic Understanding questions and a little more on Fluency and Problem-solving and reasoning questions. The Progressing pathway also includes the 'Gold star' question(s).

Choosing a pathway

There are a variety of ways of determining the appropriate pathway for students through the course. Schools and individual teachers should follow the method that works best for them. If required, the Warm-up quiz at the start of each chapter can be used as a diagnostic tool. The following are recommended guidelines:

- A student who gets 40% or lower should heavily revise core concepts before doing the Building questions, and may require further assistance.
- A student who gets between 40% and 75% should do the Building questions.
- A student who gets 75% and higher should do the Progressing questions.

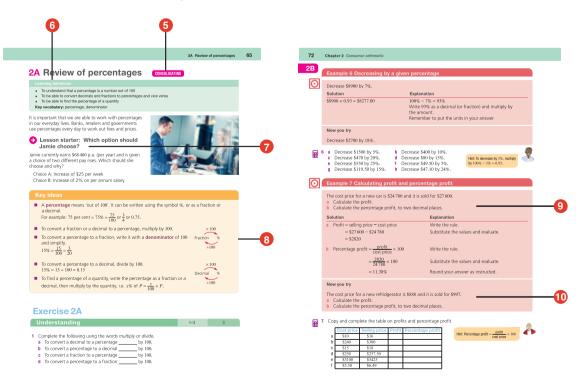
For schools that have classes grouped according to ability, teachers may wish to set either the Building or Progressing pathways as the default pathway for an entire class and then make individual alterations depending on student need. For schools that have mixed-ability classes, teachers may wish to set a number of pathways within the one class, depending on previous performance and other factors.

* The nomenclature used to list questions is as follows:

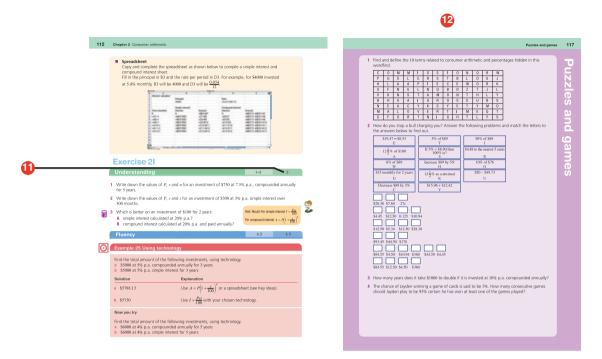
- 3, 4: complete all parts of questions 3 and 4
- 10(1/2): complete half of the parts from question 10 (a, c, e, or b, d, f,)
- 4(1/2), 5: complete half of the parts of question 4 and all parts of question 5
- 1–4: complete all parts of questions 1, 2, 3 and 4
- $2-4(\frac{1}{2})$: complete half of the parts of questions 2, 3 and 4
- – : complete none of the questions in this section.

PRINT TEXTBOOK FEATURES

- 1 **Victorian Curriculum:** content strands, sub-strands and content descriptions are listed at the beginning of the chapter (see the teaching program for more detailed curriculum documents)
- 2 In this chapter: an overview of the chapter contents
- **3 Chapter introduction:** sets context for students about how the topic connects with the real world and the history of mathematics
- 4 Warm-up quiz: a quiz for students on the prior knowledge and essential skills required before beginning each chapter
- **5** Sections labelled to aid planning: All non-core sections are labelled as 'Consolidating' (indicating a revision section) or with a gold star (indicating a topic that could be considered challenging) to help teachers decide on the most suitable way of approaching the course for their class or for individual students.
- 6 **NEW** Learning intentions: sets out what a student will be expected to learn in the lesson
- 7 Lesson starter: an activity, which can often be done in groups, to start the lesson
- 8 Key ideas: summarises the knowledge and skills for the section
- **9** Worked examples: solutions and explanations of each line of working, along with a description that clearly describes the mathematics covered by the example. Worked examples are placed within the exercise so they can be referenced quickly, with each example followed by the questions that directly relate to it.
- 10 **NEW** Now you try: try-it-yourself questions provided after every worked example in exactly the same style as the worked example to give students immediate practice



- 11 Working programs: differentiated question sets for two ability levels in exercises
- **12 Puzzles and games:** in each chapter provide problem-solving practice in the context of puzzles and games connected with the topic

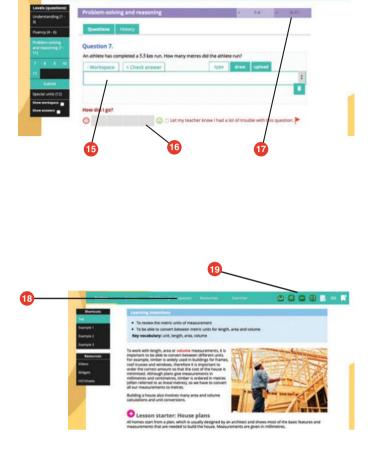


- 13 **NEW Chapter checklist:** a checklist of the learning intentions for the chapter, with example questions
- 14 **Chapter reviews:** with short-answer, multiple-choice and extended-response questions; questions that are 'Gold Star' (extension) are clearly signposted

	B	•
470	Chapter 7 Geometry	240 Chapter 4 Probability
Chapter checklist	 Account the declet the type or an orise of a second complete case to deverticeded from your threads the results. a constraints of the type of type of type of the type of type	<page-header><page-header></page-header></page-header>

INTERACTIVE TEXTBOOK FEATURES

- **15 NEW Workspaces:** almost every textbook question – including all working-out – can be completed inside the Interactive Textbook by using either a stylus, a keyboard and symbol palette, or uploading an image of the work
- **16 NEW Self-assessment:** students can then self-assess their own work and send alerts to the teacher. See the Introduction on page x for more information
- **17 Interactive question tabs** can be clicked on so that only questions included in that working program are shown on the screen
- 18 HOTmaths resources: a huge catered library of widgets, HOTsheets and walkthroughs seamlessly blended with the digital textbook
- **19 Desmos graphing calculator**, scientific calculator and geometry tool are always available to open within every lesson
- 20 Scorcher: the popular competitive game
- 21 Worked example videos: every worked example is linked to a high-quality video demonstration, supporting both in-class learning and the flipped classroom



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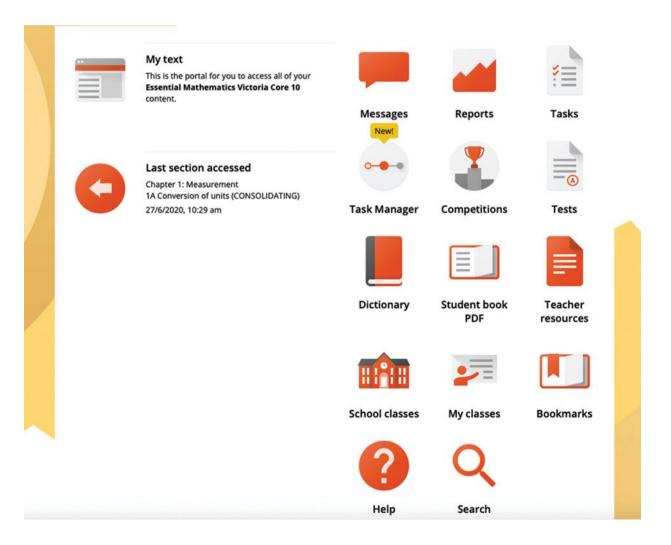
- 22 A revised set of differentiated auto-marked practice quizzes per lesson with saved scores
- 23 Auto-marked maths literacy activities test students on their ability to understand and use the key mathematical language used in the chapter
- 24 Auto-marked prior knowledge pre-test (the 'Warm-up quiz' of the print book) for testing the knowledge that students will need before starting the chapter
- 25 **NEW** Auto-marked diagnostic pre-test for setting a baseline of knowledge of chapter content
- **26** Auto-marked progress quizzes and chapter review multiple-choice questions in the chapter reviews can now be completed online

DOWNLOADABLE PDF TEXTBOOK

27 In addition to the Interactive Textbook, a **PDF version of the textbook** has been retained for times when users cannot go online. PDF search and commenting tools are enabled.

ONLINE TEACHING SUITE

- **28 Learning Management System** with class and student analytics, including reports and communication tools
- 29 **NEW Teacher view of students' work and self-assessment** allows the teacher to see their class's workout, how students in the class assessed their own work, and any 'red flags' that the class has submitted to the teacher
- 30 Powerful test generator with a huge bank of levelled questions as well as ready-made tests
- 31 **NEW Revamped task manager** allows teachers to incorporate many of the activities and tools listed above into teacher-controlled learning pathways that can be built for individual students, groups of students and whole classes
- **32** Worksheets, skillsheets, maths literacy worksheets, and two differentiated chapter tests in every chapter, provided in editable Word documents
- **33 NEW More printable resources:** all Pre-tests and Progress quizzes are provided in printable worksheet versions



Chapter **Whole numbers**

Essential mathematics: why working with whole numbers is important

It is essential for skilled workers in the industrial, construction and service trades to perform accurate arithmetic calculations and to make accurate estimates.

- A carpenter uses addition and subtraction to calculate the length of wood that will remain if 4 table legs are cut from it.
- A nurse multiplies the number of heart beats in 15 seconds by 4 to estimate a patient's heart rate in beats per minute.
- A house painter divides the area to be painted by the paint's coverage rate in m²/litre, to find the volume of paint required.
- Plumbers and electricians apply the order of operations when calculating the price of a job that equals a callout fee plus an hourly rate times the number of hours.



- 1A Place value (Consolidating)
- 1B Adding and subtracting whole numbers
- 1C Algorithms for addition and subtraction
- 1D Multiplying small whole numbers
- 1E Multiplying large whole numbers
- **1F** Dividing whole numbers
- 1G Estimating and rounding whole numbers (Consolidating)
- 1H Order of operations with whole numbers

Victorian Curriculum

NUMBER AND ALGEBRA Number and place value

Apply the associative, commutative and distributive laws to aid mental and written computation and make estimates for these computations (VCMNA240)

© Victorian Curriculum and Assessment Authority (VCAA)

Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

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- 1 Write down the larger number from each pair of numbers.
 - **a** 9,11
 - **c** 99,104

- **b** 137, 129
- d 10102,9870

2 For each of the following, match the symbol (A, B, C or D) to the given word (a, b, c, and d).

- a add Δ **b** subtract B÷ **C** + c multiply $D \times$
- d divide
- **3** Write each of the following as numbers.
 - a fifty-seven
 - **b** one hundred and sixteen
 - c two thousand and forty-four
 - d eleven thousand and two
- 4 Which number is:
 - a 2 more than 11?
 - **b** 5 less than 42?
 - **c** 1 less than 100?
 - **d** 3 more than 7997?
 - e double 13?
 - f half of 56?

5 Complete these patterns, showing the next four numbers.

- **a** 7, 14, 21, 28, 35, ___, ___, ___, ___.
- **b** 9, 18, 27, 36, 45, ___, ___, ___, ___.
- **c** 11, 22, 33, 44, 55, ___, ___, ___,
- 6 How many equal groups can 48 be divided into if the size of each group is:

a 24? b 48? c 16? d 4?	а	24?		b 48?	c 16?	d 4	1?
--	---	-----	--	--------------	--------------	------------	----

7 Give the result for each of these sums and differences.

а	3 + 11	b	14 + 9	C	99 + 20	d	138 + 12
е	199 + 11	f	1010 + 100	g	396 + 104	h	837 + 71
- i -	20 - 11	j j	41 - 9	k	96 - 17	1	101 - 22
m	136 – 24	n	421 – 23	0	783 - 84	р	1200 - 299

8 Give the result for each of these multiplications and divisions.

а	5×6	b	9×7	C	12×12	d	8×11
е	7×8	f	10×13	g	100×11	h	2000×4
- i -	10 ÷ 2	j –	30 ÷ 15	k	66 ÷ 6	Ι.	132 ÷ 12
m	110 ÷ 11	n	63 ÷ 7	0	27 ÷ 9	р	108 ÷ 12

9 Arrange these numbers from smallest to largest.

- **a** 37, 73, 58, 59, 62, 159
- **b** 301, 103, 31, 310, 130
- **c** 29 143, 24 913, 13 429, 24 319, 24 931

10 What is the remainder when these numbers are divided by 3? **a** 12 **b** 10 **c** 37

d 62

1A Place value

CONSOLIDATING

Learning intentions

- To understand how place value works in the decimal (Hindu-Arabic) system.
- To be able to identify the place value of digits in different numbers.
- To be able to compare two whole numbers by considering the digits in each position.

Key vocabulary: place value, digit, decimal system, Hindu-Arabic system

The decimal system is the number system used most often today. It is also called the Hindu-Arabic system. It uses the digits 0, 1, 2, 3, 4, 5, 6, 7, 8 and 9. The decimal system originated in ancient India about 3000 BCE and spread across Europe through Arabic texts over the next 4000 years.

	1	Ancien	s G	arac	tères	. Ir	ithm	ictiqu	ues.	
A otes .				÷				-		
2. Plumde.	{1	μ	μ	24	S	4	v	А	9	10
Sauteres .	{'			2						
4 Sacro Borros.	{'			۶						
S. Reger Bacen.	1			8						
6. Der ladiens Modernes.	19			Ŷ						
7. Mindernes.				4						
8 Monthere) a Misephadi.										

Lesson starter: Write the largest number

Write the largest possible number using these digits.

- 7, 1, 3, 6
- 1, 0, 5, 2, 6
- 9, 1, 2, 8, 4
- 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

Explain why your number is the largest possible.

Key ideas

- The symbols 0, 1, 2, 3, 4, 5, 6, 7, 8 and 9 are called **digits**.
- The value of each digit depends on its place in the number.
 The place value of the digit 2 in the number 3254, for example, is 200.

3254 = 3000 + 200 + 50 + 4

	thousands	hundreds	tens	ones
digit	3	2	5	4
value	3000	200	50	4

Symbols used to compare nu = (equal to)	1 + 3 = 4	de the or	following. 10 - 7 = 3
≠ (not equal to)	$1 + 3 \neq 5$	or	$11+38 \neq 50$
> (greater than)	5 > 4	or	100 > 37
\geq (greater than or equal to)	$5 \ge 4$	or	$4 \ge 4$
< (less than)	4 < 5	or	13 < 26
\leq (less than or equal to)	$4 \le 5$	or	$4 \le 4$
\approx (approximately equal to)	$4.02 \approx 4$	or	$8997\approx9000$

Exercise 1A

Understanding	1–3	3
 1 For the number 5207, write down which digit is in the: a tens place b thousands place c hundreds place d ones place 		
 2 Write down these numbers using digits. a forty-six b two hundred and sixty-three c seven thousand, four hundred and twenty-one d thirty-six thousand and fifteen 		
3 Which symbol (A, B, C, D, E or F) matches the given words (a, b, c, d, ea not equal toA =b less thanB \neq c greater than or equal toC >d equal toD \geq	and f)?	

Ε <

F ≤

1A

Essential Mathematics for the Victorian Curriculum	
CORE Year 7	

f less than or equal to

e greater than

	Fluency				4–5(½), 7	4-5(1/2), 6, 7(1/2)
E	xample 1 Findin	ng place valu	e			
а	Vrite down the plac 437 olution	e value of the d	igit 4 in these numbers. b 1043 Explanati	on		
a	4 100 400		The 4 has The 3 has	value 4×100 value 3×10 value 7×1)	
b	$4 \times 10 = 40$		The 0 has The 4 has	value 1×100 value 0×100 value 4×10 value 3×1		
W	l ow you try Vrite down the plac 162	e value of the d	igit 6 in these numbers. b 4628			
4	Write down the pl a 37 e 1712	lace value of the b 7 1 f 7 001	e digit 7 in these numbers. c 3 7 9 g 45 7 20	d 7 04 h 1 7 0966		Hint: Write your answe as 7, 70, 700, 7000 or 70 000.
5	Write down the pl a 43 e 2931	lace value of the b 37 f 3846	e digit 3 in these numbers. c 238 g 99 213	d 1 3 20 h 2 3 0040		
6	Write down the pl a 126 b 2143 c 91214 d 1268804	lace value of the	e digit 2 in these numbers.			
7	State whether eac a $5 > 4$ b $6 = 10$ c $9 \neq 99$ d $1 < 12$ e $22 \le 11$ f $126 \le 126$ g $19 \ge 20$ h $138 > 137$ i $3 \le 3$ j $7 \ne 7$ k $0 \ge 1$ l $2013 < 2031$	h of these state:	ments is true or false. Hint: < less than ≤ less than or equal to > greater than ≥ greater than or equal to = equal to ≠ not equal to			

Essential Mathematics for the Victorian Curriculum CORE Year 7

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Problem-solving and reas	soning		8, 9	8(1⁄2), 9, 10				
Example 2 Arranging number	S							
Arrange these numbers from smalles 29, 36, 18, 132, 1001, 99, 592, 123, 952	2							
Solution	Expla	nation						
18, 29, 36, 99, 123, 132, 592, 952, 1001	numb Then o and so	nallest two-digit er in the tens co choose the next o on, before mov igit numbers.	llumn. smallest two	-digit,				
Arrange these numbers from smalles	Now you try Arrange these numbers from smallest to largest. 37, 102, 117, 9001, 324, 9, 312, 8413, 799							
 8 Arrange these numbers from small a 55, 45, 54, 44 c 23, 951, 136, 4 e 12 345, 54 321, 34 512, 31 254 	b 72 d 43	29, 29, 92, 927, 2 35, 453, 534, 345 010, 1001, 10 001	, 543, 354)				
 9 In the following questions, digits cannot be used more than once, and all the given digits must be used. Do not use a decimal point. a Write the largest possible number using the digits 2, 7 and 8. b Write the smallest possible number using the digits 9, 1, 3, 6 and 4. 								
10 How many numbers can be made once and all the given digits musta 2, 8 and 9		-	allowed to b 2, 5, 6 and 7	e used more thar				

Large numbers

- 11 The names of large numbers depend on the number of digits grouped into threes. For example, 1000 is 1 thousand, 1 000 000 is 1 million and 1 000 000 000 is 1 billion.
 - a Write these numbers using digits.
 - ii 46 thousand i 7 thousand
 - iii 712 thousand iv 5 million
 - **v** 44 million **vi** 6 billion
 - vii 437 billion viii 15 trillion
 - **b** Research the number 1 googol and write a sentence explaining what it is.



11

1B Adding and subtracting whole numbers

- To understand that numbers can be added in any order, but that for subtraction order does matter.
- To be able to use the mental strategies partitioning, compensating and doubling/halving to calculate a sum or difference of whole numbers mentally.

Key vocabulary: partitioning, compensating, mental strategy

The process of finding the total value of two or more numbers is called addition. The words 'plus', 'add' and 'sum' are also used to describe addition.

The process for finding the difference between two numbers is called subtraction. The words 'minus', 'subtract' and 'take away' are also used to describe subtraction.

Lesson starter: Your mental strategy

Many problems that involve addition and subtraction can be solved mentally without the use of a calculator or written working.

Explain your mental strategy for working out the answer to these problems.

132 + 245• 99 + 35 73 - 41

Key ideas

The symbol + is used to show addition or find a sum. For example: 4 + 3 = 7

$$+3$$

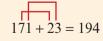
3 4 5 6 7 8

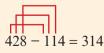
- Note that the order does *not* matter with addition. For example: 5 + 2 = 2 + 5 and 21 + 12 = 12 + 21
- The symbol is used to show subtraction or find a difference. For example: 7 - 2 = 5

 Note that the order does matter with subtraction. For example: $5 - 2 \neq 2 - 5$ and $21 - 12 \neq 12 - 21$

Mental addition and subtraction can be done using different strategies.

Partitioning (Grouping digits in the same position)





Compensating (Making a 10, 100 etc. and then adjusting or compensating by adding or subtracting) 46

$$5 + 9 = 46 + 10 - 1$$

= 55
 $138 - 99 = 138 - 100 + 399 = 138 - 100 + 399 = 39$



Exercise 1B

Understanding		1–4 4				
 a List three words that tell you v b List three words that tell you v 2 Write the number which is: 		Hint: Choose from these words: <i>minus</i> , add, sum, subtract, plus, take away	y			
a 2 more than 5 d 5 less than 9	b 3 more than 7 c e 7 less than 19 f	58 more than 11 137 less than 157				
b Subtract (take away) to find th	pairs of numbers. and 8 iii 62 and 70 the difference between these pairs of and 13 iii 101 and 93	⁻ numbers.				
 4 Give the result for each of these p a 7 plus 11 b 22 m d 128 add 12 e 36 tag 	the sum of 11	and 21 between 13 and 4				
Fluency		5-8(1/2) 5-8(1/2)				
Example 3 Mental addition a						
Use the suggested strategy to ment a 132 + 156 (partitioning) c 25 + 19 (compensating)	ally work out the answer. b 429 – 203 (partition d 56 – 18 (compension)					
Solution	Explanation					
a 132 + 156 = 288	100 + 30 + 2Group the he $100 + 50 + 6$ tens and one $200 + 80 + 8$ $100 + 100$					
b 429 - 203 = 226	400 - 200 = 200 20 - 0 = 20 9 - 3 = 6					
c 25 + 19 = 44	25 + 19 = 25 + 20 - 1 To add 19, a = $45 - 1$ then take as = 44					
d 56 - 18 = 38	56 - 18 = 56 - 20 + 2 To take away 2 = $36 + 2$ take away 2 = 38 then add 2.	20				
Now you tryUse the suggested strategy to mentally work out the answer.a 423 + 236 (partitioning)b 758 - 321 (partitioning)c 46 + 29 (compensating)d 134 - 28 (compensating)						

and so on.

Hint: Work out the answer by

Hint: Round one of the number

to the nearest ten, then

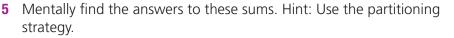
9–12

compensate by adding or

subtracting the difference.

adding the ones, then the tens

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- **a** 11 + 23 **b** 14 + 32**c** 43 + 16**d** 23 + 41**e** 71 + 26 f 138 + 441 **q** 246 + 502**h** 937 + 111304 + 4293
- 6 Mentally find the answers to these differences. Hint: Use the partitioning strategy.
 - **a** 29 18 **b** 57 - 21 **c** 94 - 43**d** 249 - 137 **e** 357 - 124 f 836 - 704 **g** 1045 - 1041 h 4396 - 1285 i . $10\,101 - 100$
- 7 Mentally find the answers to these sums. Hint: Use the compensating strategy. **a** 15+9 **c** 19 + 76**b** 64 + 11
 - **d** 18 + 115**e** 31 + 136f 245 + 52
- 8 Mentally find the answers to these differences. Hint: Use the compensating strategy.
 - **a** 35 11 **b** 45 - 19 **c** 156 - 48 d 244 - 22**e** 376 – 59 f 5216 - 199

Problem-solvin	d and	reasoning
	g ana	i casoning

9 Mary has \$101 in her piggy bank. She takes out \$22 to buy a jumper. How much money remains in her piggy bank?

- 10 Gary worked 7 hours on Monday, 5 hours on Tuesday, 13 hours on Wednesday, 11 hours on Thursday and 2 hours on Friday. What is the total number of hours that Gary worked during the week?
- 11 In a batting innings, Phil hit 126 runs and Mario hit 19 runs. How many more runs did Phil hit compared to Mario?







1B

Mentally find the answers to these mixed problems. 12

a 11 + 18 - 17	b $37 - 19 + 9$	c $101 - 15 + 21$
d 136 + 12 - 15	e $28 - 10 - 9 + 5$	f $39 + 71 - 10 - 10$
g 1010 - 11 + 21 - 1	h $5 - 7 + 2$	i $10 - 25 + 18$

13 Matt has 36 cards and Andy has 35 more cards than Matt.

- a How many cards does Andy have?
- **b** If they combine their cards, how many do they have in total?

14 Are these statements true or false?

a 4+3 > 6**b** $11 + 19 \ge 30$ **c** 13 - 9 < 8**d** $26 - 15 \le 10$ **e** $1+7-4 \ge 4$ f 50 - 21 + 6 < 35

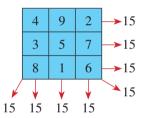
15 Complete these number sentences. (The letters *a*, *b* and *c* represent numbers.)

- **a** 2+3=5 so 5- ____ = 2 **b** 9 + 6 = 15 so $15 - _ = 9$ **d** a + c = b so b - a =
- **c** a + b = c so c = a

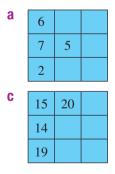
Magic squares

16 A magic square has every row, column and main diagonal adding to the same number, called the magic sum. For example, this magic square has a magic sum of 15.

16



Find the magic sums for these squares, then fill in the missing numbers.



b	10			
	10	11	13	
			12	
d	1	15		4
		6		9
			11	
	13		2	16

1C Algorithms for addition and subtraction

Learning intentions

- To be able to apply the addition algorithm to find the sum of whole numbers.
- To be able to apply the subtraction algorithm to find the difference of whole numbers.

Key vocabulary: borrow, carry, algorithm, place value

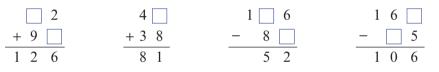
To add or subtract larger numbers we can use a step-by-step process called an algorithm.

Adding can involve carrying a 'one' to the next column, while subtracting can involve borrowing a 'one' from the next column.



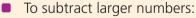
Lesson starter: The missing digits

Discuss what digits should go in the empty boxes. Give reasons for your answers.



Key ideas

- To add larger numbers:
 - Arrange the numbers vertically (above each other) so that the digits with similar **place value** are in the same column.
 - Add digits in the same column, starting on the right.
 - If the digits add to more than 9, **carry** the 1 to the next column.



- Arrange the numbers vertically so that the digits with similar place value are in the same column.
- Subtract digits in the same column top-down, starting on the right.
- If the digits subtract to less than 0, **borrow** a 1 from the next column to form an extra 10.

Borrow 1 $1^{1}2^{1}5 9$ -1 8 2 77 1-1=0 9-2=715-8=7

Carry the 1

¹234

+192

4 2 6

Exercise 1C

	Understanding				1–3	3
1	Mentally find the rest a 7+6 e 998+7	ults to these simp b 11 + 9 f 19 + 124		8 + 9 102 + 99	d 138 + h 52 + 3	
2	Mentally find the rest a 13 - 6 e 37 - 22	ults to these simp b 16 - 11 f 104 - 12	C	13 - 5 46 - 17	d 75 – h 1001	
3	J	digit in these prob b 3 6 +1 5 5 f 6 7 -4 8 9	blems? c 1 2 3 + 9 1 2 4 g 1 6 2 - 1 8 1	+[1 h 1	$ \begin{array}{c} 4 & 6 \\ $	
	Fluency				4-6(1/2)	4-7(1/2)

Example 4 Adding larger numbers	
Give the result for each of these sums. a 26 +66	b 439 $+172$
Solution	Explanation
a ${}^{1}26$ $+ \frac{66}{92}$	Add the digits vertically. 6 + 6 = 12, so carry the 1 to the tens column.
b ${}^{1}4^{1}3 9$ + 1 7 2 $\overline{6 1 1}$	9+2=11, so carry a 1 to the tens column. 1+3+7=11, so carry a 1 to the hundreds column.
Now you try Give the result for each of these sums. a 48 ± 27	b 718 + 184
4 Give the result for each of these sums. a 36 b 74 c 17 c ± 51 ± 25 ± 24 e 54 f 36 g 64 f ± 27 ± 15 ± 28	+ 39 Hint: For parts c to h, don't forget to carry the 'one'.

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5	Gi	ve the resu	It for each	n of these s	sums.					
	а	138	b	257	C	449	d	871	*	
		<u>+84</u>		+65		<u>+72</u>		<u>+49</u>	Hint: You will need to carry	
	e	129 +97	f	458 + 287	g	1041 +982	h	3092 +1988	the 'one' twice in these questions.	
		<u> </u>		<u> </u>		<u> </u>				

Example 5 Subtracting larger numbers

Give the result for each of these differences.	
a 74	b 526
<u>-15</u>	<u>-138</u>
Solution	Explanation
a ${}^{6}7^{1}4$	Borrow 1 from 7 to make $14 - 5 = 9$.
- 1 5	Then subtract 1 from 6 (not 7).
59	
b ${}^{4}{5}^{11}{2}^{-1}{6}$	Borrow 1 from 2 to make $16 - 8 = 8$.
-138	Borrow 1 from 5 to make $11 - 3 = 8$.
3 8 8	4 - 1 = 3.

Now you try

Give the result for each of these differences.

а	52	b	341
	<u>-24</u>		<u>-156</u>

6	Fir	nd the answ	wers to	these dif	ferences				
	а	54	b	85	C	46	d	94	
		-23		<u>-65</u>		-27		<u>-36</u>	Hint: For parts c to h , you
	е	85	f	43	g	82	h	66	will need to borrow a 'one' from the tens column.
		-27		-14		-56		<u>-27</u>	
7	Fir	nd the answ	wer to 1	these diffe	erences.				
	а	235	b	352	С	714	d	932	
		- 86		- 79		- 58		44	Hint: You will need to
	е	125	f	241	g	358	h	531	borrow a 'one' twice in each question.
		- 89		- 189		-279		-469	each question.

Problem-solving and reasoning

8 Farmer Green owns 287 sheep, Farmer Brown owns 526 sheep and Farmer Grey owns 1041 sheep. How many sheep are there in total?



9–12



8–10

- 1<u>C</u>
- **9** A car's odometer shows 12138 kilometres at the start of a journey and 12714 kilometres at the end of the journey. How far was the journey?



10 Give the result for each of these sums.

a 17	b 126	c 152	d 2197
26	47	247	1204
+34	+ 19	+ 19	+ 807

11 Find the missing digits in these sums and differences.

а	3	b 1 4	c 6	d 2 5
	+ 5 3	+ 7	- 2 8	- 8
	1	9 1	4	8 1

b

12 a What are the missing digits in this sum?

- $\begin{array}{c|c}
 2 & 3 \\
 + & & \\
 \hline
 4 & 2 & 1
 \end{array}$
- **b** Explain why there is more than one possible set of missing digits in the sum above. Give some examples.

More magic squares

13 Complete these magic squares. Remember that in a magic square, each row, column and diagonal has the same sum.

а	62	67	60	
			65	

101		114	
	106		109
	110		
113	103	102	116

13

1D Multiplying small whole numbers

Learning intentions

- To understand the commutative and associative laws for multiplication.
- To be able to use mental strategies to find products.
- To be able to apply the multiplication algorithm to find the product of a single-digit number by a whole number.

Key vocabulary: product, commutative law, associative law, distributive law, algorithm

The multiplication of two numbers represents a repeated addition. For example, 4×2 could be thought of as 4 groups of 2 or 2+2+2+2, or 4×2 could be thought of as 2 groups of 4 or 2×4 or 4+4.



Lesson starter: Museum tickets

Your teacher purchases 21 tickets at \$9 each for a class excursion to the museum. You need to work out the total cost.

Look at the following strategies. Do any of them give the correct answer?

- 21×9 is the same as 20×10 , so the answer is \$200
- 21×9 is the same as $21 \times 10 1$, so the answer is 210 1 = \$209
- 21×9 is the same as $20 \times 9 + 1$, so the answer is 180 + 1 = \$181
- 21×9 is the same as $21 \times 10 21$, so the answer is 210 21 = \$189
- 21×9 is the same as $20 \times 9 + 9$, so the answer is 180 + 9 = \$189

Key ideas

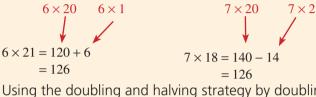
- Finding the **product** of two numbers involves multiplication. We say 'the product of 2 and 3 is 6'.
- $a \times b = b \times a$ For example: $2 \times 3 = 3 \times 2$
 - The order does *not* matter when you multiply numbers. This is the **commutative law**. For example:
 - $2 \times 3 = 3 \times 2$
 - $5 \times 11 = 11 \times 5$
 - The result of adding or multiplying three or more numbers does not depend on how they are grouped. This is the associative law. For example:
 (2 × 3) × 4 = 2 × (3 × 4)
- To multiply by a single digit:
 - Multiply the single digit by each digit in the other number, starting from the right.
 - Carry and add any digits with a higher place value to the total in the next column.
 ¹23

```
\times 4 4 × 3 = 12
92 4 × 2 + 1 = 9
```

- Mental strategies for multiplication include:
 - Knowing your multiplication tables off by heart. For example:
 - $9 \times 7 = 63$
 - $12 \times 3 = 36$

1D

- Changing the order. For example: $15 \times 3 = 3 \times 15$ (3 groups of 15) = 45 $5 \times 13 \times 2 = 5 \times 2 \times 13$ $= 10 \times 13$ = 130
- Using the **distributive law** by making a 10,100 etc. and then adjusting by adding or subtracting. The distributive law means that adding numbers and then multiplying the total gives the same answer as multiplying each number first and then adding the products. For example:



Using the doubling and halving strategy by doubling one number and halving the other.
 Double the 5 Halve the 4

$$5 \times 7 \times 4 = 10 \times 7 \times 2$$
$$= 70 \times 2$$
$$= 140$$

Exercise 1D

	Unde	erstandi	ng	9						1, 2, 3(½)	3(1/2)
1	a Th c 2 e 5	ver true or fa he product of $\times 3 = 3 \times 2$ $\times 8 = 10 \times 1$ $\times 31 = 4 \times 3$	of 4 6	and 7 is 21			d f	The product $10 \times 5 \times 2$ $20 \times 3 \times 2$ $6 \times 19 = 6$	$2 = 2 \times 2 = 10$	$\times 6 \times 2$	
2		the missing $\times 5 = 5 \times _$ $\times 2 \times 6 = 6 \times 1$			b e	$2 \times 7 = 7 \times _$ $12 \times 2 \times 4 =$	$\overline{2\times}$	12 ×	C f	$15 \times 11 = _$ 7 × 3 × 9 = 9 ×	× 15 × 3 ×
3	a 11 f 12 k 3 p 8	1×2 2×5 $\times 7$ $\times 5$	b g l q	3×9 4×11 6×9 7×7	c h m r	ation tables t 8×4 11×7 6×5 9×7 4×6	d i n s	7×8 12×9 10×11 11×12	e j o t	9×8 12 × 12 12 × 6	
	Flue	ncy								4–7(½)	4-7(1/2)
	Examp	ple 6 Usin	g I	mental str	ate	gies for m	ulti	plication			
	Jsean 3×1	nental strate 13	gу		b 4	× 19			c 5	× 24	

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Solution		Explanation		
a $3 \times 13 = 30 + 9$ = 39)	$3 \times 13 = 3 \times 10$ The distributive	$+ 3 \times 3$ law is being used.	
b $4 \times 19 = 80 - 4$ = 76	4	$4 \times 19 = 4 \times 20^{-1}$ The distributive	-4×1 law is being used.	
c $5 \times 24 = 10 \times 10^{-10}$ = 120	12	The doubling ar	nd halving strategy is	being used.
Now you try				
Use a mental strat	tegy to find:			
a 5 × 41	b	7 × 19	c 5 × 16	
 4 Find the results calculator. a 5 × 21 e 5 × 23 	to these products m b 4×31 f 7×31	nentally. Check your c 3×31 g 9×22	answers with your d 6×22 h 6×42	Hint: For part a , work out 5×20 and then add 5×1 .
5 Find the answe	rs to these products	mentally		
a 3×19	b 2×19	c 2×29	d 4×29	Hint: For part a, work out
e 5 × 18	f 7 × 18	g 3 × 39	h 4×49	3×20 and then subtract 3×1 .
6 Find the answe	rs to these products	mentally.		
a 5 × 14	b 5 × 18	c 22 × 5	d 36×5	Hint: Double one number
e 4 × 24	f 3 × 18	g 6×16	h 24×3	and halve the other. So $5 \times 14 = 10 \times 7 = 70$

Example 7 Multiplication showing working

Give the result for each of these products.

Give the result for each of these products.	
a 31 × 4	b 197 × 7
Solution	Explanation
31	
a × 4	$4 \times 1 = 4$
124	$4 \times 3 = 12$
b ⁶ 1 ⁴ 97	$7 \times 7 = 49$ (carry the 4)
× 7	$7 \times 9 + 4 = 67$ (carry the 6)
1379	$7 \times 1 + 6 = 13$
Now you try	
Give the result of each of these products.	
a 52 × 3	b 286 × 4

1D

7	Give the result of each of these products	, showing working.
---	---	--------------------

а	$\frac{33}{\times 2}$	b	43×3	C	$\frac{72}{\times 6}$	d	$\frac{55}{\times 3}$
е	37×4	f	51×9	g	$\frac{48}{\times 7}$	h	$\frac{59}{\times 8}$
i	$\frac{129}{\times 2}$	j	$\frac{407}{\times 7}$	k	526×5	L	$\frac{3509}{\times 9}$

Problem-solving and reasoning

8 What is the missing digit in these products?

а	2 1	b 36	c 76	d 4 0 2
	× 3	× 5	\times 2	× 3
	6	18	1 2	1 0 6

9 Eight tickets costing \$33 each are purchased for a concert. What is the total cost of the tickets?



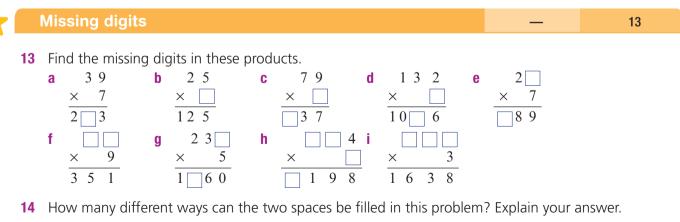
8–10

8, 10–12

- 10 A circular race track is 240 metres long and Rory runs seven laps. How far does Rory run in total?
- **11** Reggie and Angelo combine their packs of cards. Reggie has five sets of 13 cards and Angelo has three sets of 17 cards. How many cards are there in total?

12 Classify these statements as true or fa	alse.
--	-------

a $4 \times 3 = 3 \times 4$	b $2 \times 5 \times 6 = 6 \times 5 \times 2$	c $11 \times 5 = 10 \times 6$
$\mathbf{d} 3 \times 32 = 3 \times 30 + 3 \times 2$	e $5 \times 18 = 10 \times 9$	$f 21 \times 4 = 2 \times 42$
g $19 \times 7 = 20 \times 7 - 19$	$h 39 \times 4 = 40 \times 4 - 1 \times 4$	$64 \times 4 = 128 \times 8$



1E Multiplying large whole numbers

Learning intentions

- To be able to multiply by a power of ten.
- To be able to apply the multiplication algorithm to find the product of any two whole numbers.

Key vocabulary: product, algorithm, place value

There are many situations that require the multiplication of large numbers. For example, finding the total amount made from selling 40 000 tickets at \$23 each. Another example is finding the area of a rectangular park with length and width dimensions of 65 metres by 122 metres. Doing such calculations by hand requires a number of steps.



Lesson starter: Spot the errors

There are three types of errors in the working shown for this problem. Find the errors and describe them.

82			
\times	16		
482			
82			
464			

Key ideas

When multiplying by 10, 100, 1000, 10000 etc. each digit moves to the left by the number of zeros.

 $2 \times 100 = 200$ $41 \times 10 = 410$ $279 \times 1000 = 279\,000$

• A strategy for multiplying by multiples of 10, 100 etc. is to first multiply by the number without the zeros then add the zeros to the answer later.

For example: $21 \times 3000 = 21 \times 3 \times 1000 = 63 \times 1000 = 63\ 000$

• To multiply large numbers, divide the problem into smaller products and then add the totals.

37			14	3		
$\times 12$			\times 1	4		
74	-	37×2	57	2	-	143×4
370	←	37×10	143	0	←	143×10
444	-	370 + 74	200	2	-	1430 + 572

Exercise 1E

Understanding			1–3	3
1 Write the missing num a $35 \times _ = 350$		c $49 \times __ = 49000$	0 d 213 >	<= = 2130
 2 Answer true or false. a 6 × 200 = 6 × 2 × 10 c 9 × 3000 = 9 × 3 × 10 		b $65 \times 40 = 65 \times 4$ d $24 \times 500 = 24 \times$		
3 Which of the following A 23 $\times 11$ 23 23 46	g is the correct set-up for $ \begin{array}{c} \mathbf{B} & 23 \\ $	23 × 11? C	$ \begin{array}{r} 23 \\ \times 11 \\ \hline 23 \\ \hline 230 \\ \hline 253 \end{array} $	
Fluency			4-6(1/2)	4–6(½)

-		L
(•)	L

Example 8 Multiplying large numbers

Give the result for each o a 37×100	f these products. b 21×50	c 87 × 13
Solution	. 217.00	Explanation
a $37 \times 100 = 3700$		Move the 3 and the 7 two places to the left and add two zeros.
b $21 \times 50 = 21 \times 5 \times 10$ = 105×10 = 1050		First multiply by 5, then multiply by 10. 21 $\times \frac{5}{105}$ Final weight 0.5
$ \begin{array}{c} \mathbf{c} & 87 \\ \times & 13 \\ \hline & 261 \\ & 870 \\ \hline & 1131 \end{array} $		First multiply 87×3 . Then multiply 87×10 . Add the results to give the answer.
Now you try Give the result for each o a 53×100	f these products. b 32×40	c 74 × 17
	$\begin{array}{ccc} 29 \times 10 & & \mathbf{c} & 18 \\ 192 \times 10 & & \mathbf{g} & 30 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$

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5	Fir a d g j	nd these pro- 12×20 21×30 92×70 92×5000		b e h	18×30 17×20 45×500 317×20		C f i	36 13	5 × 20 5 × 40 38 × 300 043 × 9000	0			non-zero dig	ultiply by the single it, then write the $20 = 12 \times 2 \times 10$	Q
6	Fir a	nd these pro 21 ×12	odu b	cts. 26 ×11	C	31 ×14		d	43 ×15	е	37 ×11	f	72 ×19		
	g	$\frac{\times 12}{88} \times 14$	h	$\frac{\times 11}{57}$ $\times 22$	i	$\frac{\times 11}{92}$ $\times 23$		j	$\frac{\times 15}{84}$ $\times 27$	k	$\frac{46}{\times 31}$	I	$\frac{1}{72} \times 65$		
	Problem-solving and reasoning									7,8	8, 9(½), 10	8, 9(½), 11, 12			

- 7 Mandy buys 28 tickets at \$15 each. What is the total cost of the tickets?
- 8 A pool area includes 68 square metres of paving at \$32 per square metre. What is the total cost of paving?



9 These products involve a number with three digits. Find each answer, showing your working.

a 123	b 138	c 126	d 428
<u>× 11</u>	× 22	\times 15	× 22
e 396 × 46	f 416 × 98	g 380 × 49	$\begin{array}{c} h 1026 \\ \times 33 \end{array}$
<u>× 40</u>	× 96	<u>× 49</u>	× 33

- 10 Waldo buys 215 metres of pipe at \$28 per metre. What is the total cost of piping?
- 11 How many seconds are there in one day?
 Hint: There are 60 seconds in a minute.
- 12 If both numbers in a multiplication problem have at least three digits, then more steps need to be shown. Find these products.

a 294 ×136	b 1013 \times 916	c 3947 ×1204	d 47126 × 3107
Missing digit pu	zzle		— 13
13 Find the missing d a $2 \square$ $\times 1 7$	igits in these products. b 1 \square 3 \times 1 \square	c	d 2 × 2
1 🗌 1		3 4 3	1 2 6
2 0	1 3		5 2
	5		6

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1F Dividing whole numbers

Learning intentions

- To know that a division of two numbers can result in a quotient and a remainder, and the result can be written as a mixed number if there is a remainder.
- To be able to use mental strategies to find quotients.
- To be able to apply the short division algorithm to divide whole numbers.

Key vocabulary: quotient, dividend, divisor, remainder

Division is used to find the number of equal groups from a given total. Dividing 20 apples among five people or dividing \$10,000 between three bank accounts are examples of when division can be used.

Lesson starter: Arranging counters

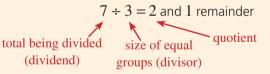
A total of 24 counters sit on a table. Using whole numbers, in how many ways can the counters be divided into equal-sized groups with no counters left over?

- Is it also possible to divide the counters into equal-sized groups but with two counters left over?
- If five counters are to remain, how many equal-sized groups can be formed and why?



Key ideas

- The number of equal-sized groups made by dividing is called the **quotient**.
- The total being divided is called the **dividend**. The size of the equal groups is called the **divisor**.
- Any amount remaining after division into equal-sized groups is called the **remainder**.



The order *does* matter when you divide numbers. You cannot swap numbers in a division to make the calculation easier. For example:

 $6 \div 3 \neq 3 \div 6$ $(10 \div 5) \div 2 \neq 10 \div (5 \div 2)$

- Use short division to work with larger numbers.
 - Start by dividing the divisor into the first (left) digit, then carry any remainder. This example shows that $413 \div 3 = 137$ and 2 remainder.

 $4 \div 3 = 1$ and 1 rem. $11 \div 3 = 3$ and 2 rem. $23 \div 3 = 7$ and 2 rem. $3 4^{1}1^{2}3$ So $413 \div 3 = 137$ and 2 remainder

$$= 137\frac{2}{3}$$

Exercise 1F

	Understanding				1–3	3
1	Find the remainder when 24 is divided a 1 b 2 d 5 e 6 Write the number that is missing in the a $8 \div 2 = 4$ is the same as $4 \times ? = 8$. b $36 \div 12 = 3$ is the same as $? \times 12 =$ c $42 \div ? = 6$ is the same as $6 \times 7 = 42$ d $72 \div 6 = ?$ is the same as $12 \times 6 = 7$	2 6 ese statements. 36. 2.	C f	3 7	Hint: The rem	ainder can be zero.
3	Consider the division 83 ÷ 7 = 11 and 6 a the remainder c the divisor	6 left over. Which number is: b the quotient d the dividend				
	Fluency				4–9(1⁄2)	4–9(½)
a	Solution $56 \div 8 = 7$ $93 \div 3 = 31$ $57 \div 3 = 19$	c $57 \div 3$ d $128 \div$ Explanation $8 \times ? = 56$ (Use your knowledge from $90 \div 3 = 30 \text{ so } 93 \div 3 = 31$ $60 \div 3 = 20 \text{ so } 57 \div 3 = 19$	mu	ltipli	cation tabl	es.)
d	$128 \div 8 = 16$	$128 \div 8 = 64 \div 4 = 32 \div 2 =$ (Halve both numbers repeation)		y.)		
ι	low you try Use a mental strategy to find the answer $42 \div 7$ b $82 \div 2$	r. c 95 ÷ 5 d 112 ÷	- 7			

1F

6

- Find the answers to these using a mental strategy.
- **a** 87 ÷ 3
- **c** 96 ÷ 4
- **e** 117 ÷ 3
- **g** 116 ÷ 4
- 7 Find the answers to these using a mental strategy.
 - **a** 88 ÷ 4
 - **b** 124 ÷ 4
 - **c** 136 ÷ 8
 - **d** 112 ÷ 16
- 8 Write the answers to these divisions, which involve 0s and 1s.
 - **a** 26 ÷ 1
 - **b** 1094 ÷ 1
 - **c** 0 ÷ 7
 - **d** 0 ÷ 458
- Example 10 Using short division

Use short division to find the quotient and remainder. Then write the result using a fraction.

b $7)195$
Explanation
$3 \div 3 = 1$ with no remainder.
$7 \div 3 = 2$ with 1 remainder.
12 rem. $1 = 12\frac{1}{3}$
7 does not divide into 1. $19 \div 7 = 2$ with 5 remainder. $55 \div 7 = 7$ with 6 remainder.
27 rem. $6 = 27 \frac{6}{7}$

b 76 ÷ 4

d 63 ÷ 7

f

56 ÷ 4

h $180 \div 20$

Now you try

Use short division to find the quotient and remainder. Then write the result using a fraction.

a 4)89 **b** 6)237

9 Use the short division algorithm to find the quotient and remainder. Then write the result using a fraction.

a 3)71	b 7)92	C 5)139
d $6)247$	e $5)217$	f 4)506
g 3)794	h 9)814	(4) 2173
j $3\overline{)61001}$	k $5\overline{)4093}$	9)90009

Hint: Halve both numbers, since they are both even. So, part a,

Hint: For part a, remember that

 $90 \div 3 = 30.$

 $88 \div 4 = 44 \div 2$.



Problem-solving and reasoning 10-12 12-15 **10** Write the missing digit in each of these divisions. **b** $7 \frac{2}{84}$ **c** 5)125d 9)135а 3)51

- If 117 food packs are divided equally among nine families, how many packs does each family receive? 11
- 12 Spring Fresh Company sells mineral water in packs of six bottles. How many packs are there in a truck containing 744 bottles?
- **13** A straight fence has two end posts. It also has other posts that are divided evenly along the fence 4 metres apart. If the fence is to be 264 metres long, how many posts are needed, including the end posts?
- 14 Friendly Taxis can take up to four passengers each. How many taxis are required to transport 59 people?
- **15** Pies are purchased wholesale at three for \$4. How much will it cost to purchase 153 pies?

	Long, short division		—	16, 17
16	Short division can also be used e.g. $215 \div 12 = 17$ and 11 remain	to divide by numbers with more than nder.	n one digit.	$\frac{1}{12} \frac{7}{2195}$ rem. 11
	Use the short division algorithm	to find the quotient and remainder.		
	a 371 ÷ 11	b 926 ÷ 17	c 404 ÷ 13	

d 1621 ÷ 15 **e** 2109 ÷ 23

In this square, every row, column and diagonal has a product of 6720. Find the missing numbers.

56

10

2 3

1 6

40

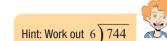
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CORE Year 7

f 6914 ÷ 56







')15.	,
es	each	f

	а	356	value of the digit 5 i b 5103	C	857 412
1A	mo a		an be made using th Il digits must be use		n digits? Digits are not allowed to be used
18	a b c	entally find the answ 146 + 332 754 - 531 85 - 19 21 + 49 - 28	vers to these probler	ns.	
18	а	e these statements t 23 - 17 < 8 60 - 18 + 11 > 50	rue (T) or false (F)?		
10	5 Giv		n of these sums and	differe	
	а	37 + 58		b	4584 + 897
	C	63 - 48		d	413 - 296
10	а	d the answers to th 6×18 32×5	ese products mental	lly.	
10	7 Giv a	we the result for each $82 \\ \times 7 \\ \hline $	n of these products.	b	534×3
1E			n of these products.		
	a c	71 × 1000 23		d d	37 × 200 59
	U	×12		u	×23
1E	9 Jac	k purchases 15 bask	etball tickets at \$21	each.	What is the total cost of the tickets?
1F	a b c	nd the answer to the 63 ÷ 3 495 ÷ 5 160 ÷ 20 240 ÷ 16	ese using a mental s	strategy	ļ.
1F		se the short division $5\overline{)227}$	algorithm to find th		tient and remainder. 8)4237

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1G Estimating and rounding whole numbers CONSOLIDATING

Learning intentions

- To understand that in some practical situations, an estimate or approximation is acceptable.
- To be able to round numbers to a degree of accuracy (e.g. to the nearest 100).
- To be able to estimate numerical answers to arithmetic questions by rounding each number in the question.

Key vocabulary: estimate, approximation, rounding

Often, a good estimate is enough to answer a question and it is not necessary to find an exact answer. In such cases we use rounding to help. For example, the approximate total cost of 18 truckloads of soil at \$54 per load could be estimated as $20 \times 50 = 1000$, so the cost is about \$1000.

Lesson starter: Counting crowds

Here is a photo of a crowd at a sporting event. Describe how you might estimate the number of people in the photo. What is your answer? How different is your answer from those of others in your class?



Key ideas

- An estimate is an informed guess, an approximation is a value close to the real value, and rounding involves approximating a number to a specified place value.
- Estimates or approximations can be found by rounding numbers to the nearest 10, 100, 1000 etc.
 - If the next digit is 0, 1, 2, 3 or 4, then round down.
 - If the next digit is 5, 6, 7, 8 or 9, then round up.
- Leading digit approximation involves rounding to the first digit. For example: For 932, round to 900
 For 968, round to 1000
- The symbol \approx means 'approximately equal to'.

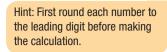
Exercise 1G

	Jnderstanding						1, 2–3(½)		2-3(1/2)
1	Have these numbers been rounder a $59 \approx 60$ d $255 \approx 260$	b	up or down? 14 ≈ 10 924 ≈ 900			C f	$137 \approx 140$ $1413 \approx 1000$		
2	The following numbers are to be a 19 b 37 g 45 h 95		unded to the r 21 132				ey be roundec 72 288	l up f I	o or down? 33 304
3	The following numbers are to be down. a 103 b 201 g 427 h 552		unded to the 195 956	nea d j	rest 100. Decid 186 349	de e k	if they would 172 198	be f I	rounded up o 131 359

Fluency		4–6(½)	4–6(½)							
Example 11 Rounding										
Round these numbers as in a 86 (to the nearest 10)	dicated. b 4142 (to the neare	st 100)								
Solution	Explanation									
a 86 ≈ 90	The digit after the 8 is greater round up.	than or equal to	o 5, so							
b 4142 ≈ 4100	The digit after the 1 is less that down. Keep the 1 and make the follo	·								
Now you try Round these numbers as in a 93 (to the nearest 10)	dicated. b 5851 (to the neare	st 100)								
 4 Round these numbers as a 59 (nearest 10) c 124 (nearest 10) e 231 (nearest 100) g 96 (nearest 10) j 1492 (nearest 1000) 	b 32 (nearest 10)									
 5 Round these numbers us a 21 e 241 i 5600 		Hint: Round to the first the left, so $284 \approx 300$ d 857 h 962 l 14								
Example 12 Using lead	Example 12 Using leading digit approximation									
Estimate the answers to the a 42×7 Solution	 b 95 × 326 c 3 Explanation 	to the leading di $02 \div 29$	git.							
a $42 \times 7 \approx 40 \times 7$	The leading digit in 42 is the 4	in the 'tens' col	umn.							
= 280 b $95 \times 326 \approx 100 \times 300$ = 30 000	The nearest 'ten' to 95 is 100, is in the 'hundreds' column.									
c $302 \div 29 \approx 300 \div 30$ = 10	302 rounds to 300 and 29 rour									
Now you try										
Estimate the answers to the a 31×8	b 97 × 432 c 8	to the leading di 84 ÷ 91	igit.							

6 Use leading digit approximation to estimate the answer.

а	29×4	b	124 + 58	C	232 - 106
d	61 ÷ 5	е	103 ÷ 11	f	32×99
g	59×21	h	279 ÷ 95	i.	394 ÷ 10
j.	97×21	k	1390 + 3244	1	999 - 888



13



Problem-solving and reasoning7–99–127 You purchase 59 tickets at \$21 each. Give an estimate for the
total cost of the tickets.Hint: For questions 7 to 10, use
leading digit approximation to
make your estimate.

- 8 A digger can dig 29 scoops per hour and work 7 hours per day. Approximately how many scoops can be dug over 10 days?
- 9 Most of the pens at a stockyard are full of sheep. There are 55 pens and one of the pens has 22 sheep. Give an estimate for the total number of sheep at the stockyard.
- **10** A whole year group of 159 students is roughly divided into 19 groups. Estimate the number in each group.
- **11** For the given estimates, decide if the approximate answer is going to give a larger or smaller result compared to the true answer.
 - **a** $58 + 97 \approx 60 + 100$
 - **c** $130 79 \approx 130 80$

- **b** $24 \times 31 \approx 20 \times 30$
- **d** $267 110 \approx 270 110$
- 12 It is sensible sometimes to round one number up if the other number is going to be rounded down. Use leading digit approximation to estimate the answers to these problems.
 - **a** 11×19 **b** 129×954 **c** 25×36 **d** 1500×2500

Aboriginal dot painting

13 Many examples of Aboriginal art include dot paintings. Here are two examples. Estimate the number of dots in each one.



1H Order of operations with whole numbers

- To know the convention for determining order of operations in an expression involving more than one operation.
- . To be able to evaluate arithmetic expressions involving more than one operation.
- Key vocabulary: operation, brackets, multiplication, division, addition, subtraction

When combining the operations of addition, subtraction, multiplication and division, a special order needs to be followed. Multiplication and division sit higher in the order than addition and subtraction. This affects how we might make sense of simple mathematical problems put into words. Consider these two statements.

- 2 groups of 3 chairs plus 5 chairs
- 5 chairs plus 2 groups of 3 chairs



In both cases, there are $2 \times 3 + 5 = 11$ chairs. This means that $2 \times 3 + 5 = 5 + 2 \times 3$.

This also suggests that for $5 + 2 \times 3$, the multiplication should be done first.

Lesson starter: Make it true!

Can you insert a pair of brackets to make the following true?

 $2 + 3 \times 5 = 25$

• $20 \div 8 - 3 = 4$

• $3 \times 2 + 6 = 24$

• $7 - 1 \div 3 = 2$

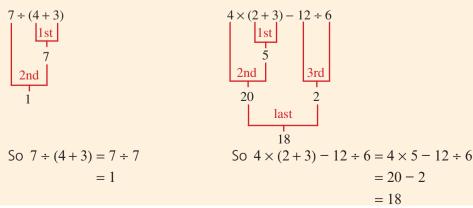
Discuss whether you think the following need brackets to make them true.

 $2 + 6 \times 1 = 8$

 $10 \div 2 + 3 = 2$

Key ideas

- When working with more than one operation:
 - Deal with brackets first.
 - Do multiplication and division next, working from left to right.
 - Do addition and subtraction last, working from left to right.



Exercise 1H

Understanding		1–2	2
 Which goes first? a Addition or multiplication b Brackets or division c Subtraction or brackets d Multiplication or subtraction Which operation (addition, subtraction, multiplication a 2+5-3 b 5÷5×2 d 5×2+3 e 7÷7-1 g (8÷4)-1 h 4+7×2 	C f	one first in these $2 \times 3 \div 6$ $(6+2) \times 3$ $8-10 \div 5$	e problems?
j $10 - 2 + 3$ k $6 + 2 \times 3 - 3$		$5 \times (2+3 \div 3)$	- 1
Fluency		3(1/2)	3-4(½)
Example 13 Using order of operations			
Use order of operations to answer the following. a $5+10 \div 2$ b $3 \times (2+4)$ c $5 \times 2 - 8 \div 4$ d $6 \times (2+10) - 24$ e $18 - 2 \times (4+6) \div 5$			
Solution	Explanation		
a $5 + 10 \div 2 = 5 + 5$ = 10	Do the division befo	re the addition.	
b $3 \times (2+4) = 3 \times 6$ = 18	Deal with brackets b	efore multiplica	tion.
c $5 \times 2 - 8 \div 4 = 10 - 2$ = 8	Do the multiplication subtraction.	n and division b	efore the
d $6 \times (2+10) - 24 = 6 \times 12 - 24$	Deal with brackets f	irst.	
= 72 - 24	Do the multiplication	n before subtrac	tion.
= 48	Do the subtraction la	ast.	
e $18 - 2 \times (4 + 6) \div 5 = 18 - 2 \times 10 \div 5$ = $18 - 20 \div 5$ = $18 - 4$ = 14	Deal with brackets f Do the multiplication from left to right. Do the subtraction la	n and division ne	ext, working
		Continued	on next page

Essential Mathematics for the Victorian Curriculum CORE Year 7

1H

Now you try

Use order of operations to answer the following.

a $9 - 2 \times 3$ **b** $11 \times (8-5)$ **c** $20 \div 10 + 7 \times 3$ d $12 \div (7 - 3) + 13$ **e** $4 \div (13 - 11) \times 3 + 6$

3 Use order of operations to find the answers.

b $5+7 \times 2$

e $21 \div (3+4)$

h $(10 - 4) \times 4$

n $6 \times 3 + 2 \times 7$

q $2 + 3 \times 7 - 1$

t $78 - 14 \times 4 + 6$

b $18 \div (10 - 4)$

d $2 \times (3+2) - 1$

h $2 \times (9 - 4) \div 5$

f $13 \times (10 \div 10) - 13$

 $16 - 2 \times (7 - 5) + 6$

 $14 - (7 \div 7 + 1) \times 2$

n $3 \times (72 \div 12 + 1) - 1$ **p** $20 - (3 \times 5 + 1) \div 4$

k $5 + 8 \times 2$

- **a** $1 + 2 \times 3$ **d** $4 \times (3+2)$ **g** $(7+2) \div 3$ $2 + 3 \times 7$ **m** $22 - 16 \div 4$ **p** $18 \div 9 + 60 \div 3$ **s** $63 \div 3 \times 7 + 2 \times 3$
- 4 Use order of operations to find the answers.
 - **a** $2 \times (3+2)$ **c** $(19 - 9) \div 5$ **e** $10 \div (3+2) + 6$ **q** $(100+5) \div 5+1$ i $50 \div (13 - 3) + 4$
 - **k** $(7+2) \div (53-50)$
 - **m** $(20-10) \times (5+7) + 1$
 - **0** $48 \div (4+4) \div (3 \times 2)$

5 Are these statements true or false?

- **a** $5 \times 2 + 1 = (5 \times 2) + 1$
- **c** $21 7 \div 7 = (21 7) \div 7$

b $10 \times (3+4) = 10 \times 3+4$ **d** $9-3 \times 2 = 9 - (3 \times 2)$

Example 14 Using order of operations in worded problems

Find the result if 6 is multiplied by the sum of 2 and 7.

Solution	Explanation
$6 \times (2+7) = 6 \times 9$ $= 54$	First, write the problem using symbols and numbers.
	Use brackets for the sum since this operation is to be completed first.

Now you try

Find the result if 26 is divided by the difference between 16 and 3.



i.	$(6-5) \div 1$	to right after you have chosen
L	$10 - 20 \div 2$	which operation goes first.
0	$1 \times 8 - 2 \times 3$	
r	$40 - 25 \div 5 + 3$	
u	$300 - 100 \times 4 \div$	- 4

c $9 - 10 \div 5$

 $(6-5) \div 1$

f $18 \div (10 - 1)$



Hint: Deal with brackets first, then \times and \div then + and -.

5-7

Hint: Remember that \times and \div go

before + and -. Work from left



7–10

- 6 Find the answer to these worded problems by first writing the sentence using numbers and symbols.
 - **a** Triple the sum of 3 and 6.
 - **b** Double the result of 20 divided by 4.
 - **c** 44 divided by 11 plus 4.
 - **d** 5 more than the product of 6 and 12.
 - e The result of 60 divided by 12 is subtracted from the product of 5 and 7.
 - f 15 less than the difference of 48 and 12.
 - **g** The product of 9 and 12 is subtracted from double the product of 10 and 15.
- 7 A delivery of 15 boxes of books arrives. Each box contains eight books. The bookstore owner removes three books from each box. How many books still remain in total?



- 8 In a class, eight students have three TV sets at home, four have two TV sets, 13 have one TV set and two students have no TV sets. How many TV sets are there in total?
- **9** Insert brackets into these equations to make them true.

а	$4 + 2 \times 3 = 18$	b	$9 \div 12 - 9 = 3$	C	$2 \times 3 + 4 - 5 = 9$
d	$3 + 2 \times 7 - 3 = 20$	е	$10 - 7 \div 21 - 18 = 1$	f	$4 + 10 \div 21 \div 3 = 2$

10 Decide if the brackets given in each equation are actually necessary. That is, do they make any difference?

e 22 - (11 - 7) = 18

b $(2+3) \times 6 = 30$

- **a** $2 + (3 \times 6) = 20$
- **d** 10 (5+2) = 3

Brackets within brackets

11 These problems involve brackets within brackets. Make sure you work with the inner brackets first. (The first one has already been done.)

a
$$2 \times [(2+3) \times 5 - 1] = 2 \times [5 \times 5 - 1]$$

= $2 \times [25 - 1]$

$$= 2 \times [23]$$
$$= 2 \times 24$$
$$= 48$$

- **b** $[10 \div (2+3)+1] \times 6$
- **c** $26 \div [10 (17 9)]$
- **d** $[6 (5 3)] \times 7$
- **e** $2 + [103 (21 + 52)] (9 + 11) \times 6 \div 12$
- 12 Insert brackets to make the following true. (You may need to use more than one pair.)

a
$$20 - 31 - 19 \times 2 = 16$$

b
$$50 \div 2 \times 5 - 4 = 1$$

c $25 - 19 \times 3 + 7 \div 12 + 1 = 6$

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Hint: *Sum* means add. *Difference* means subtract. *Product* means multiply.

c $(20 \times 2) \times 3 = 120$

f $19 - (10 \div 2) = 14$

11.12





Maths@Work: Stock controller at sports events

The 2019 AFL Grand Final between the Richmond Tigers and the Greater Western Sydney Giants saw an official attendance of 100 014, which is extremely close to the capacity crowd of 100 024 people that can fit into the MCG (Melbourne Cricket Ground).

At large sporting events and concerts, there are many food and beverage stands around the grounds. The stock controllers need to predict the crowd size and make sure that enough water and food is available for each event.



1 Complete the table below for these different stadiums and events from around Australia. Use an allowance of 1.5 bottles of water for each person attending the event. After calculating all answers, round to the nearest whole number.

Hint: Earnings are the total amount from sales, not the profit.



Venue	Event	Attendance	Water bottles required	Total wholesale cost @ \$0.80/bottle	Earnings @ \$3 a bottle
Suncorp Stadium, Brisbane	Brisbane Roar vs Perth Glory	35 200			
MCG, Melbourne Cricket Ground	Hawthorn vs Fremantle	100 007			
WACA, WA Cricket Association	T20 cricket India vs Australia	34 527			
SCG, Sydney Cricket Ground	Sydney Swans vs Western Bulldogs	33 386			
Adelaide Oval	Adelaide Crows vs West Coast Eagles	53 445			
NIB Stadium, Perth	Wallabies vs Argentina	16 202			
Darwin Football Stadium	Brumbies vs Reds	4600			
ANZ Stadium, Sydney	Broncos vs Cowboys	82 758			

2 Attendances are often rounded for convenience of reporting. For the events in question 1, round each of the attendances to the nearest thousand.

3 Average attendance figures help stock controllers predict the needs of events at their venues.

Average = $\frac{\text{Total attendance}}{\text{Number of games}}$

Calculate the average attendance for each of the following events:

- a AFL 2019 season with a total attendance of 7 517 647 with 198 games.
- **b** Big Bash League 2018–19 season with 1 212 596 people attending 59 games.
- c Japanese baseball 2019 season of 429 games with a total attendance of 14867071.
- d Major league baseball with total attendance 68 494 752 over 2 429 games.



A Big Bash League match between the Brisbane Heat and Hobart Hurricanes at the Gabba.

List four factors that could cause variation in attendance figures.

Using technology

Use the following example to help you with the guestion below.

For one MCG cricket event, 6 buckets of hot chips were sold for every 10 people. The following calculation shows how the stock controller predicts the amount of food required for an event.

Total number of food items = seating capacity \times <u>number of food items</u>

number of people

$$= 100\,000 \times \frac{6}{10}$$

 $= 60\,000$ buckets of hot chips

- **5** For the following calculations, you can assume each stadium is filled to capacity.
 - a Copy the table below into a spreadsheet. Select the shaded cells, right click, select Format Cells/Number/0 d.p./OK

4	A	B	с	D	Ε	F	G
1		Food quan	tities needed fo	or sports even	ts		
2	Stadium	Seating capacity	Fruit salad	Hot chips	Pies	Mini pizzas	Fresh wraps
3	WACA, Perth	24500					
4	Adelaide Oval	53500					
5	The Gabba, Brisbane	42000					
6	ANZ Stadium, Sydney	83500					
7	Rod Laver Arena, Melbourne	14820					
8	Blundstone Arena, Hobart	20000					
9	Darwin Football Stadium	6000					

b Insert formulas into the shaded cells to calculate the whole number of serves for each food item in this table.

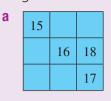
Use these facts to write the formulas:

- 1 in 5 people buy fruit salad
- 3 pies are sold for every 2 fans
- 3 in 8 people buy fresh wraps
- half the fans buy hot chips
- 2 mini pizzas are sold for every 5 people

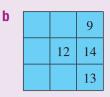
Hint: E3 formula = $B3^* 3/2$ G3 formula = B3* 3/8



38

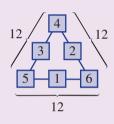


Chapter 1 Whole numbers



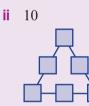
;	3	17		6
		8		11
			13	
	15		4	18

- 2 Decide where brackets should go to make each statement true.
 - **a** $5 + 2 \times 3 = 21$
 - **b** $16 8 \div 10 6 = 2$
 - **c** $4 + 2 \times 7 1 \times 3 = 43$
- **3** Each side on a magic triangle adds up to the same number, as shown in this example with a sum of 12 on each side.



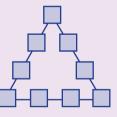
a Place the digits 1 to 6 in a magic triangle with three digits along each side so that each side adds up to the given number.



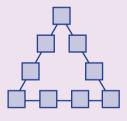


b Place the digits 1 to 9 in a magic triangle with four digits along each side so that each side adds up to the given number.









4 Sudoku is a popular logic number puzzle made up of a 9 by 9 square, where each column and row can use the digits 1, 2, 3, 4, 5, 6, 7, 8 and 9 only once. Also, each digit is to be used only once in each 3 by 3 square. Solve these puzzles.

	4				2		8	7
2	8		7		9		1	
			6			3		5
	3	7		2				8
	6	5	4	7	8			2
			2	6				
					7	5		
		8	3	9		2	7	

	7			6	9	3		
		4	1		8			7
8					2	9	1	
3		1						
	2	8	5		3			
	5	6		9		2		
	3	9			5			
6				8	4			
5			9		7			

5 The sum along each line is 15. Can you place each of the digits 1, 2, 3, 4, 5, 6, 7, 8 and 9 to make this work?

- 6 Find all the missing digits in these products.
 - a $1 \ \times 7$ $5 \ 1 \ b$ b $2 \ 9 \ b$

3

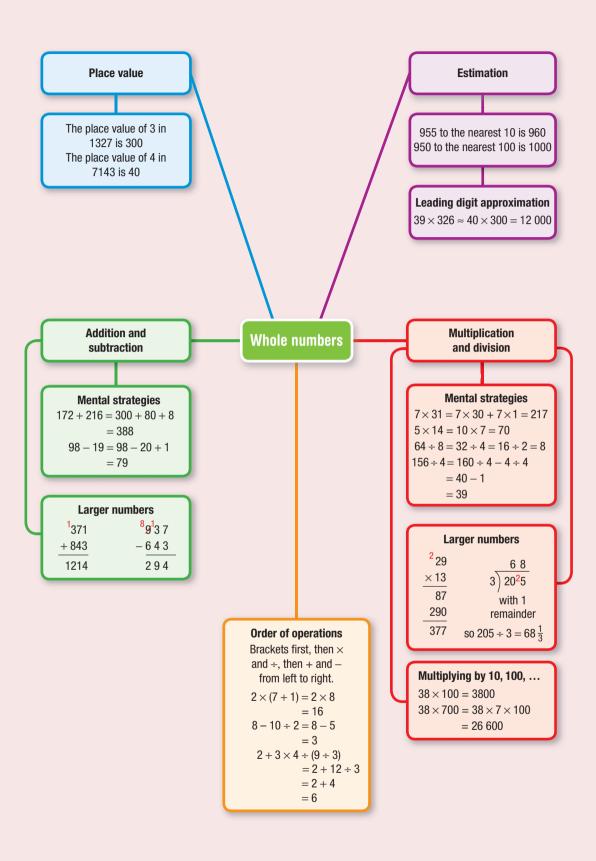
8

7 You decide to start counting backwards by 7, starting at these numbers. If you stop just before passing zero, what is your final number?

a 205

 \times

b 22314



Essential Mathematics for the Victorian Curriculum CORE Year 7

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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

			~
1A	1	I can write down the place value of digits within a number. e.g. Write the place value of the digit 4 in the number 1043.	
1A	2	I can arrange whole numbers from smallest to largest. e.g. Arrange these numbers from smallest to largest: 29, 36, 18, 132, 1001, 99, 592, 123, 952.	
1B	3	I can use mental addition and subtraction techniques effectively. e.g. Mentally find $132 + 156$ (with partitioning) and $56 - 18$ (with compensating).	
10	4	I can use the addition algorithm. e.g. Give the result for this sum $439 + 172$	
10	5	I can use the subtraction algorithm. e.g. Give the result for this difference 526 -138	
10	6	I can use mental multiplication techniques effectively. e.g. Mentally find 4×19 .	
10	7	I can use the multiplication algorithm when one number is less than ten. e.g. Give the result of 197×7 .	
1E	8	I can multiply by powers of ten by adding zeros to the end of a number. e.g. Give the result of 37×100 .	
16	9	I can multiply larger numbers using the multiplication algorithm. e.g. Find $87 \times 13.$	
1F	10	I can use mental strategies to divide whole numbers. e.g. Mentally find 93 ÷ 3.	
1F	11	I can use the short division algorithm. e.g. Use short division to find the quotient and remainder. Give your answer using a fraction. $7)195$	
16	12	I can round whole numbers to a power of ten. e.g. Round 4142 to the nearest 100.	
16	13	I can estimate answers using leading digit approximation. e.g. Estimate 95×326 by rounding each number to the leading digit.	
1H	14	I can use order of operations. e.g. Find the value of $18 - 2 \times (4 + 6) \div 5$.	
1H	15	I can use order of operations in worded problems. e.g. Find the result if 6 is multiplied by the sum of 2 and 78.	

Short-answer questions

1A 1	Arrange these numbers from smallest to largest. a 317, 713, 731, 371, 173, 137 b 1001, 1010, 199, 999, 1000, 1900, 1090				
1A 2	Write down the place value of the digit 5 in these numbers. a 357 b 5249 c 356 612				
1B 3	Use a mental strategy to find these sums and differences. a $124 + 335$ b $687 - 324$ c $59 + 36$ d $256 - 39$				
10 4	Find these sums and differences. c 329 d 926 ± 52 ± 218 -138 -187				
1D 5	Use a mental strategy to work out the following.a 5×19 b 22×6 c 5×44 d $123 \div 3$ e $264 \div 8$ f $96 \div 4$ g 29×1000 h 36×300 i $14678 \div 1$				
1E/F 6	Show your working to find each answer. a 39 \times 4 \times 40 \times 40				
	$\begin{array}{c} \mathbf{c} 157 \\ \times 9 \\ \end{array} \qquad \qquad$				
	e $3\overline{)135}$ f $9\overline{)912}$				
	g $7\overline{\smash{\big)}327}$ h $4\overline{\smash{\big)}30162}$				
1E/F 7	Find the missing digits in these problems. a $2 \ 3$ $+7 \ 3 \ 9 \ 6 \ 1$ b $2 \ -4 \ 3 \ 3$ $2 \ 5 \ 6$				
	c $\boxed{1}$ $\times \frac{7}{2 \ 8 \ }$ d $2 \frac{4 \ 8}{2 \ 1^1 \ 1^1 \ }$ with no remainder				
1G 8	 Round these numbers as indicated. a 72 (nearest 10) b 3268 (nearest 100) c 951 (nearest 100) 				
1G 9	Use leading digit approximation to estimate the answers to these problems. a $289 + 532$ b 22×19 c 452×11 d $99 \div 11$				
1H 1 0	Use order of operations to find the answers to these problems. a $3 \times (2+6)$ b $6-8 \div 4$ c $(7-4) \div 3$ d $20 \div 10+9 \times 10$ e $2 \times 8 - 12 \div 6$ f $40 \div (5+3) - 2$ g $(5+2) \times 3 - (8-7)$ h $0 \times (988234 \div 3)$ i $1 \times (3+2 \times 5)$				

Multiple-choice questions

1A	1	Which of the follow	vina	is not true?						
		A 2 < 3		$12 \le 9$	C	15 > 2	D	13 ≥ 13	Ε	7 ≠ 8
1A	2	The place value of 7								
		A 7	B	70	C	700	D	7000	E	100
1B/D/F	3	Which of the follow A $2+3=3+2$ B $2 \times 3 = 3 \times 2$ C $(2 \times 3) \times 4 = 2 \times 2$ D $5 \div 2 \ne 2 \div 5$ E $7-2=2-7$								
10	4	The sum of 198 and								
		A 301	B	304	C	299	D	199	E	95
10	5	The difference betw A 102	veer B		C	103	D	98	Е	99
1D/E	6	The product of 7 an A 147		1 is: 141	C	21	D	140	E	207
1F	7	The missing digit in A 2	this B	$\begin{pmatrix} 1 \\ 0 \end{pmatrix} (4^{1})^{21}$		4	D	1	E	3
1F	8	The remainder when					_		_	
		A 7	В	5	C	2	D	1	E	0
1G	9	458 rounded to the A 400		arest 100 is: 500	C	460	D	450	E	1000
1H	10	The answer to 4×3					_		_	
		A 10	В	25	C	6	D	12	E	14

Extended-response questions

- 1 A city tower construction uses 450 tonnes of concrete. The concrete is trucked from a factory that is 2 kilometres from the construction site. Each concrete mixer can carry 5 tonnes of concrete. The concrete costs \$350 per truck load for the first 10 loads and \$300 per load after that.
 - a How many loads of concrete are needed?
 - **b** Find the total distance travelled by the concrete mixers to deliver all loads. They need to return to the factory after each load.
 - **c** Find the total cost of concrete needed for the tower construction.
 - d If the price of concrete is always \$350 regardless of the number of loads, how much more would it cost for the concrete?
- 2 One night Ricky and his brother Micky decide to have some fun at their father's sweet shop. In the shop they collected 3 tins of 25 jelly beans, 4 packets of 32 choc buds, 5 boxes of 10 smarties and 12 packets of 5 liquorice sticks.
 - a Find the total number of sweets.
 - **b** Find the difference between the number of choc buds and the number of smarties.
 - **c** Ricky and Micky decide to divide each type of sweet into groups of 7 and then eat any remainder. Which type of sweet will they eat the most of and how many?

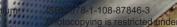
Chapter 2

Geometry

Essential mathematics: why geometry skills are important

Geometry skills are essential for workers in the construction industry. Engineers, architects, surveyors, builders, carpenters, electricians, bricklayers, tilers, glass cutters, plumbers, concreters, sheet metal workers and welders all apply geometry skills in their work.

- Jewellers apply the geometry of angles and symmetry to create gemstone designs.
- Engineers calculate the angles formed by the structural supports on a bridge.
- Carpenters determine the angles to be cut on the framing for windows and doors.
- Builders and carpenters construct parallel roof rafters, parallel ceiling joists and parallel wall studs.
- Surveyors use parallel line geometry to plan parallel streets and parallel lines for angle parking.
- Town planners, architects and civil engineers produce their own geometrical drawings and also use CAD (computer aided design), to create accurate plans for construction workers to follow.



Essential

CORE

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In this chapter

- 2A Basic geometric objects (Consolidating)
- 2B Measuring angles (Consolidating)
- 2C Finding angles at a point
- 2D Transversal lines and parallel lines
- 2E Circles and constructions 🔶
- 2F Using interactive geometry software 🛧

Victorian Curriculum

MEASUREMENT AND GEOMETRY

Geometric reasoning

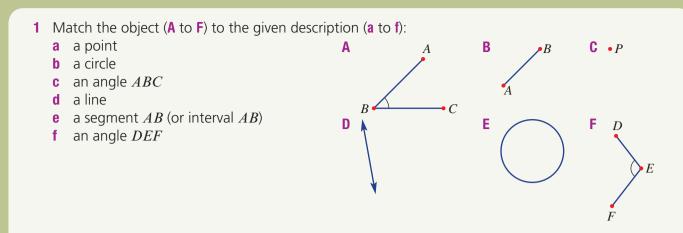
Identify corresponding, alternate and co-interior angles when two straight lines are crossed by a transversal (VCMMG264)

Investigate conditions for two lines to be parallel and solve simple numerical problems using reasoning (VCMMG265)

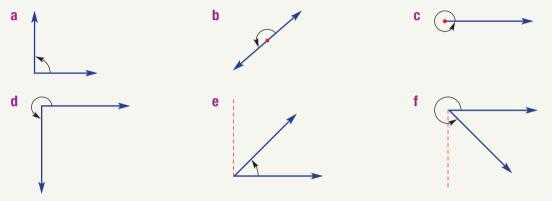
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Online resources

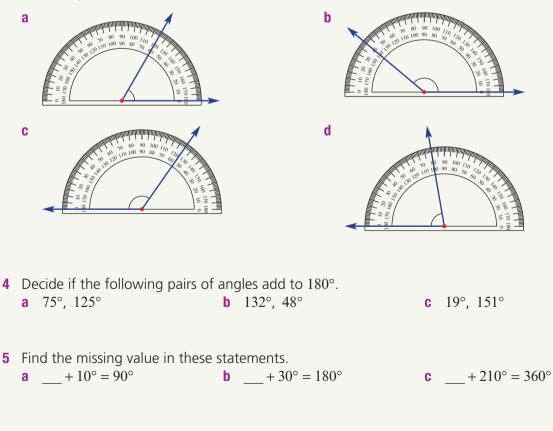
A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.



2 State or estimate the size of these angles. Remember there are 360° in a full circle.



3 What angle measurements are shown on these protractors?



R

С .--

В

Α

line AB

2A Basic geometric objects

CONSOLIDATING

Learning intentions

- To understand that points, lines and the plane are the building blocks of geometry.
- To be able to name lines, segments, rays and angles in terms of labelled points.
- To understand that the order of vertices in the name of an angle, line or segment can be reversed.

Key vocabulary: point, line, plane, collinear, concurrent, segment, ray, vertex

The basic building blocks of geometry are the point, line and plane. They are the objects used to construct angles, triangles and other more complex shapes and objects.

Lesson starter: Can you draw this?

Before you start learning about the geometrical objects in this topic, see if you can remember what each of the following represent. Draw an example of each of these objects:

- line segment AB
- line *AB*

- point P
- angle $\angle FGH$

- angle $\angle ABC$
- ray XY

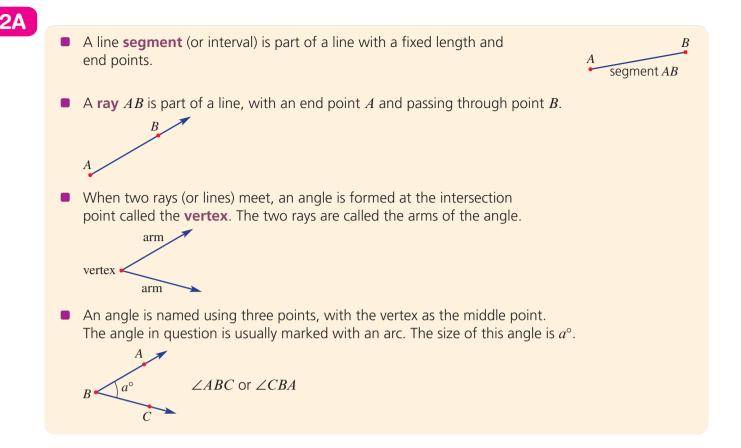


Key ideas

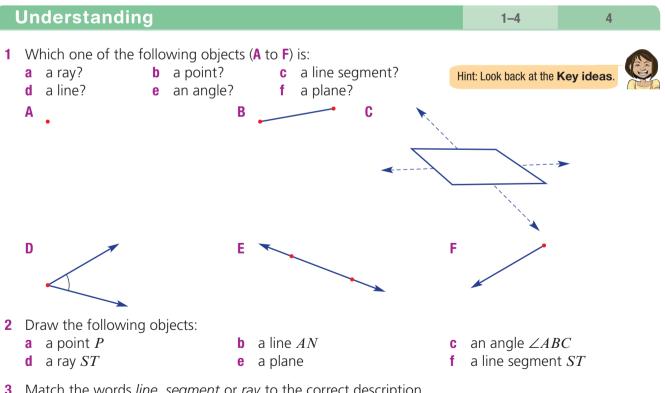
- A point is a position in space, marked with a dot and named with a capital letter.
- A **line** is a set of points forming a straight path that extends forever in opposite directions. It can be named using two points.
- A plane is a flat surface and extends indefinitely.

Points that all lie in a single line are called **collinear**.

More than two lines that meet at the same intersection point are called **concurrent**.



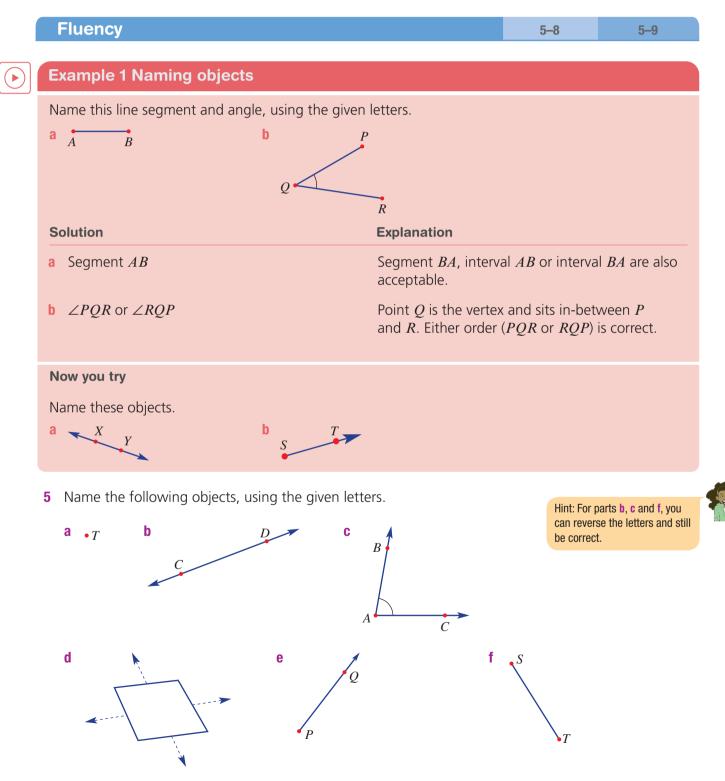
Exercise 2A

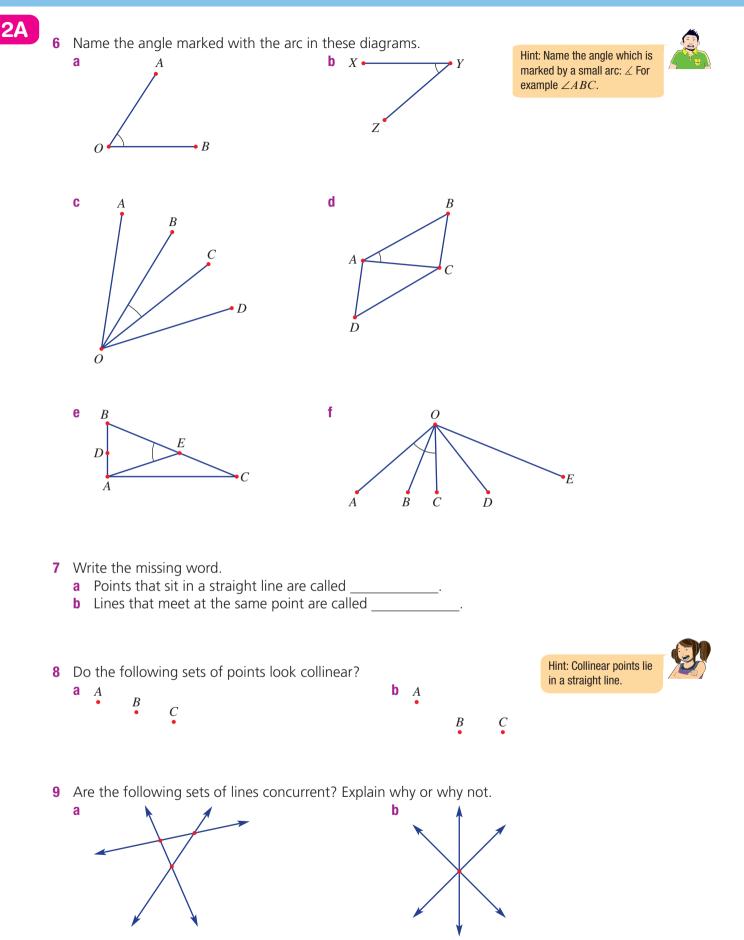


3 Match the words *line*, segment or ray to the correct description.

- a Starts from a point and extends forever in one direction.
- **b** Extends forever in both directions, passing through two points.
- **c** Starts and ends at two points.

- 4 Match the words *point, line* or *plane* with the following descriptions.
 - a the edge of a sheet of paper
 - **b** a flat wall
 - c the surface of a pool of water on a calm day
 - d where two walls and a floor meet in a room
 - e where two walls meet in a room
 - f one side of a cereal packet
 - g where two sides meet on a box
 - **h** where three sides meet on a box





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Hint: There are three angles

CDE

in a corner like this:

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10 Count the number of angles formed inside these diagrams. Count all angles, including those that may be the same size. You should also count those that are divided by another segment. b а

Problem-solving and reasoning

11 How many line segments are there on this line? Do not count AB and BA as separate segments since they are the same segment with two different names.

12 A line contains a certain number of labelled points. For example, this line has three points.

1

2

3

4

d

a Complete this table by counting the total number of segments for the given number of labelled points.

b	Explain any patterns you see in the table. Is there a quick way of finding the next number in the
	table?

5

6

Are they concurrent?

CORE Year 7

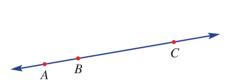
Number of points

Number of segments

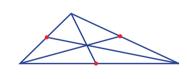
C

- 13 The lines joining each vertex (corner) of a triangle with the midpoint (middle point) of the opposite side are drawn here.
 - a Draw any triangle and use a ruler to measure and mark the midpoints of each side.
 - **b** Join each vertex with the midpoint of the opposite side.
 - **c** Are your segments from part **b** concurrent?
 - **d** Do you think your answer to part **c** will always be true for any triangle? Try one other triangle of a different size to check.





В A



13

10, 11

2B Measuring angles

CONSOLIDATING

Learning intentions

- To be able to classify angles based on their size.
- To be able to measure angles using protractors. •
- To be able to draw angles of a given size using a protractor. .

Key vocabulary: acute, right, obtuse, straight, reflex, revolution, protractor

Angles can be measured using a simple piece of equipment called a protractor. Some protractors can measure from 0° to 360° (a full turn) and others measure from 0° to 180° (a half turn). The unit for angles is the degree and the symbol used is °.

Lesson starter: Estimating angles

How good are you at estimating the size of angles? Estimate the size of these angles and then check with a protractor.

If your protractor only goes to 180°, discuss how you might measure the second angle.





Key ideas

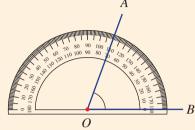
Angles are classified according to their size.

Angle type	Size	Examples
acute	between 0° and 90°	<u> </u>
right	90°	
obtuse	between 90° and 180°	$P \sim$
straight	180°	
reflex	between 180° and 360°	
revolution	360°	•

• A **protractor** is a semicircular or circular tool for measuring or drawing angles. It can be used to measure angles to about half a degree.

To use a protractor:

- Place the centre of the protractor on the vertex of the angle.
- Align the base line of the protractor along one arm of the angle.
- Measure the angle using the other arm and the scale on the protractor.



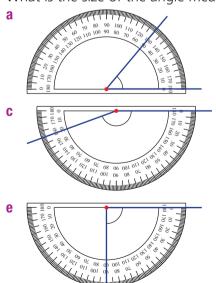
A **reflex** angle can be measured by subtracting a measured angle from 360°.

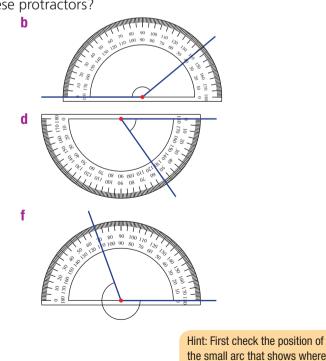
Exercise 2B

Understanding

- 1 Classify the following angles as acute, right, obtuse, straight, reflex or revolution.
 - **a** 31° 127° b **d** 180° е 360°
- 90° С 83° f i. 93°
- **q** 291° **h** 320°
- 2 Without using a protractor, draw an example of the following types of angles.
 - a Acute **d** Straight
 - **b** Right e Reflex
- c Obtuse f Revolution
- 3 What is the size of the angle measured with these protractors?

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1-3

Hint: acute: between 0° and 90° right: 90° obtuse: between 90° and 180° straight: 180° reflex: between 180° and 360° revolution: 360°

3



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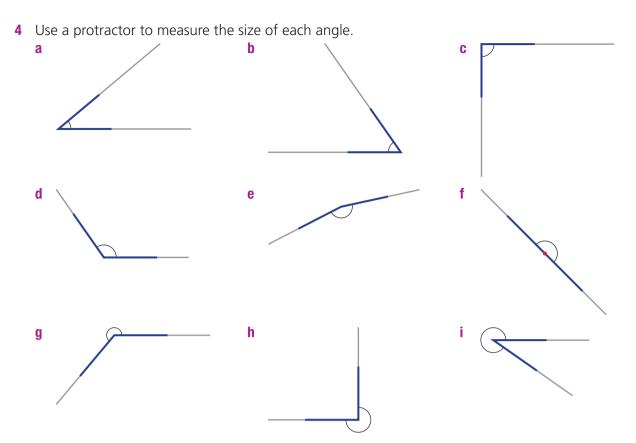
the angle is.

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2B Fluency 4-6(1/2) 4-6(1/2) **Example 2 Measuring with a protractor** Measure the size of each angle. b а G C D E-E B **Solution Explanation** a $\angle AOB = 60^{\circ}$ A 0 **b** $\angle EFG = 125^{\circ}$ G F obtuse $\angle DOE = 130^{\circ}$ С reflex $\angle DOE = 360^\circ - 130^\circ$ $= 230^{\circ}$ FNow you try Measure the size of each angle. b а C CX A Ř

S

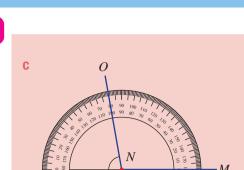
 \mathbf{I}



5 Classify each of the angles in question **4** as acute, right, obtuse, straight, reflex or revolution.

Example 3 Drawing angles				
Use a protractor to draw each of the following ang a $\angle AOB = 65^{\circ}$ b $\angle WXY = 130^{\circ}$				
Solution	Explanation			
a A A A A A A A A A A A A A A A A A A A	 Step 1: Draw a base line <i>OB</i>. Step 2: Align the protractor along the base line with the centre at point <i>O</i>. Step 3: Measure 65° and mark a point, <i>A</i>. Step 4: Draw the arm <i>OA</i>. 			
b Y	Step 1: Draw a base line XW.Step 2: Align the protractor along the base line with the centre at point X.Step 3: Measure 130° and mark a point, Y.Step 4: Draw the arm XY.			





Step 1: Draw an angle of $360^{\circ} - 260^{\circ} = 100^{\circ}$. Step 2: Mark the reflex angle on the opposite side to the obtuse angle of 100° . Alternatively, draw a 180° angle and measure an 80° angle to add to the 180° angle.

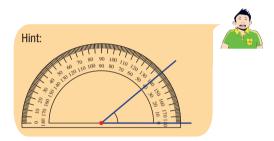
Now you try

Use a protractor to draw each of the following angles.

a $\angle XOY = 50^{\circ}$ **b** $\angle EFG = 145^{\circ}$

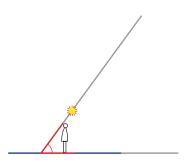
 $\angle UTV = 300^{\circ}$

- 6 Use a protractor to draw each of the following angles.
 - **a** 40° **b** 75°
 - **c** 90° **d** 135°
 - **e** 175° **f** 205°
 - **g** 260°
 - i 295°
- h 270° j 352°



Problem-solving and reasoning

- 7 Use a protractor to measure:
 - a the angle the sun's rays make with the ground



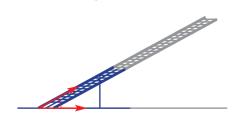
Hint: Place the centre of the protractor at the vertex of the marked angle.

7,8



7–10

b the angle that this ramp makes with the ground



c the angle of this roof d the angle between this laptop screen and the keyboard 8 How many right angles (i.e. angles of 90°) make up: **a** a straight angle? **b** 270°? **c** a revolution? Hint: There are 360° in a full circle. 9 A clock face is numbered 1 to 12. Find the angle the minute hand turns in: **a** 30 minutes **b** 1 hour 15 minutes d 45 minutes С 20 minutes e 5 minutes f a 55 minutes h 1 minute **10** An acute angle $\angle AOB$ is equal to 60°. Explain why you do not need a protractor to work out the size of the reflex angle $\angle AOB$? 60° Hour hand and minute hand angles 11, 12 **11** A clock face is numbered 1 to 12. Find the angle between the hour hand and the minute hand at: Hint: Draw a clock face for each time. Each 5-minute **a** 6 p.m. **b** 3 p.m. turn of the minute hand is **c** 4 p.m. **d** 11 a.m. $360^{\circ} \div 12 = 30^{\circ}$. **12** Find the angle between the hour hand and the minute hand of a clock at these times. **a** 10:10 a.m. **b** 4:45 a.m. Hint: Think carefully! The **c** 11:10 p.m. answer to part a is not **d** 2:25 a.m. 120°.

2C Finding angles at a point

Learning intentions

- To be able to find angles at a point using angle sums of 90°, 180° and 360°.
- To be able to find angles at a point using vertically opposite angles.
- Key vocabulary: adjacent, complementary, supplementary, revolution, vertically opposite, perpendicular

0

B

When lines, segments or rays meet at a point, special pairs or groups of angles are formed.

We name these special groups of angles depending on their geometric relationships. Opposite angles formed by intersecting steel beams, for example, are equal and are called vertically opposite angles.

Ð

A

Lesson starter: Special pairs of angles

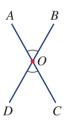
By making a drawing or using computer geometry, construct the diagrams below. Measure the two marked angles. What do you notice about the two marked angles?

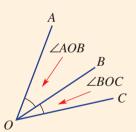
Key ideas

• Adjacent angles are side by side and share a vertex and an arm.

- Angles in a right angle are **complementary**.
 - They sum to 90°
 - *a*° is the complement of *b*°
- Angles on a straight line are **supplementary**.
 - They add to 180°
 - a° is the supplement of b°
- Angles in a revolution sum to 360°.













a + b = 360

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a°

В

С

 $AB \perp CD$

bo

D

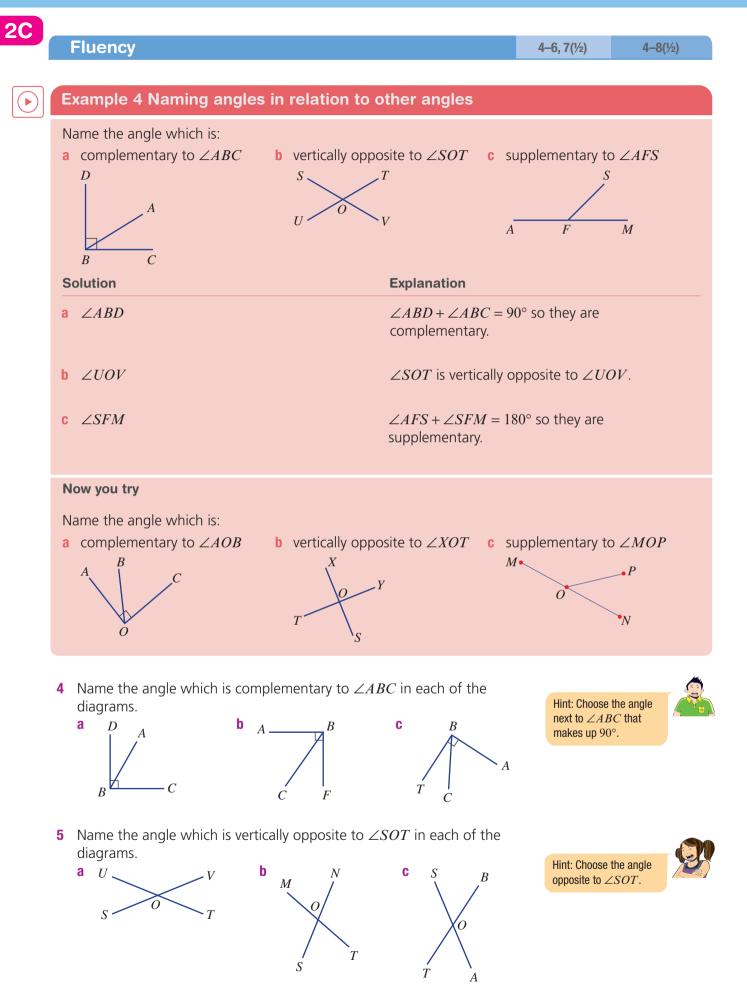
A

• Vertically opposite angles are formed when two lines intersect. The opposite angles are equal.



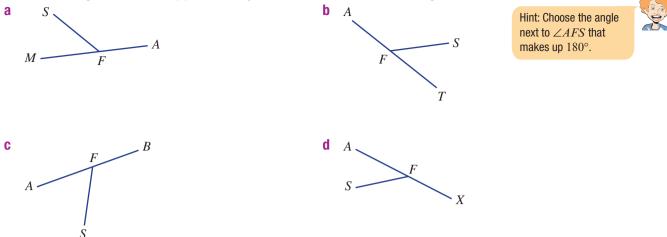
Exercise 2C

	Un	derstanding		1–3	1–3
1	a b c	Measure the angles to find the values of a and b in this Calculate $a + b$. Is your answer 90? If not, check your measurements. Write the missing word: a° and b° are			a° b°
2		Measure the angles to find the values of a and b in this diagram. Calculate $a + b$. Is your answer 180? If not, check your measurements. Write the missing word: a° and b° are angles.	/	a° b°	
3	a b c	Measure the angles to find the values of <i>a</i> , <i>b</i> , <i>c</i> and <i>d</i> in this diagram. What do you notice about the sum of the four angles? Write the missing words: <i>b</i> ° and <i>d</i> ° are angles.		$d^{\circ} c^{\circ} b$	0



Essential Mathematics for the Victorian Curriculum CORE Year 7

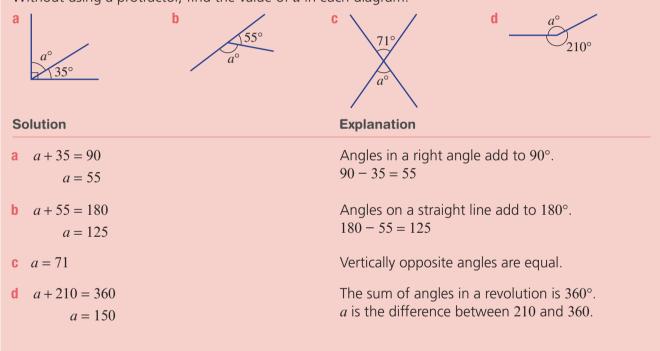
6 Name the angle which is supplementary to $\angle AFS$ in each of the diagrams.





Example 5 Finding angles at a point

Without using a protractor, find the value of *a* in each diagram.

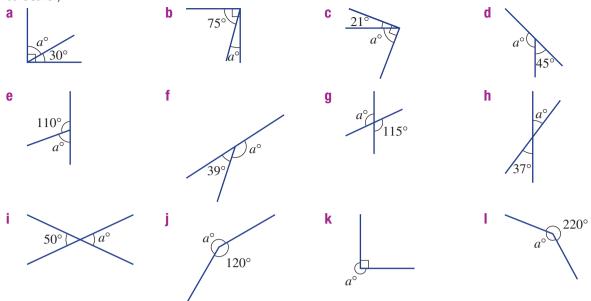


Now you try

Without using a protractor, find the value of *a* in each diagram.



- 2C
- 7 Without using a protractor, find the value of *a* in each diagram. (The diagrams shown may not be drawn to scale.)

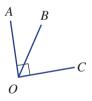


8 For each of the given pairs of angles, write C if they are complementary (add to 90°), S if they are supplementary (add to 180°) or N if they are neither.

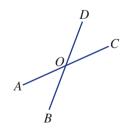
а	21°, 79°	b	130°, 60°	C	98°, 82°	d	180°, 90°
е	17°, 73°	f	31°, 59°	g	68°, 22°	h	93°, 87°

Problem-solving and reasoning

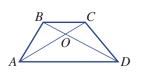
9 a Name the angle that is complementary to $\angle AOB$ in this diagram.



b Name the two angles that are supplementary to $\angle AOB$ in this diagram.



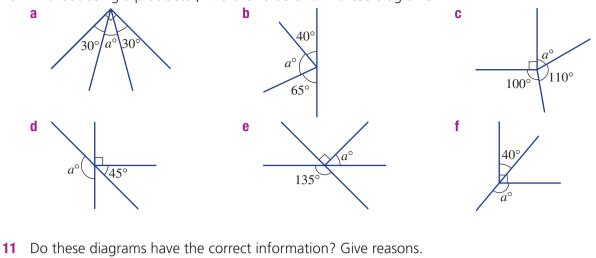
c Name the angle that is vertically opposite to $\angle AOB$ in this diagram.

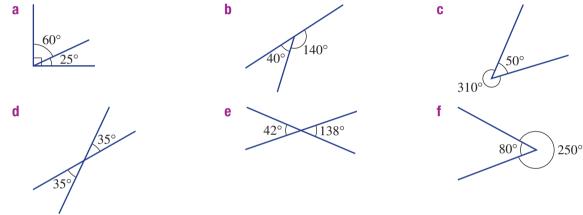


10-12

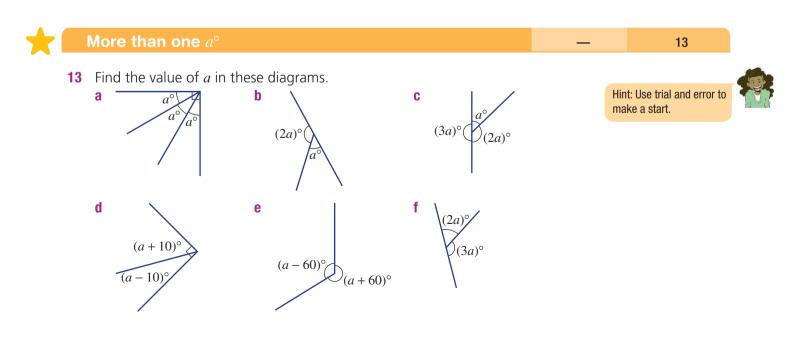
9,10

10 Without using a protractor, find the value of *a* in these diagrams.





12 A pizza is divided between four people. Bella is to get twice as much as Dom. Dom gets twice as much as Rick. Rick gets twice as much as Marie. If the pizza is cut into triangular pieces, find the angle at the centre of the pizza for Marie's piece.



2D Transversal lines and parallel lines

Learning intentions

- To be able to identify angles in relation to another angle (for example, identifying a cointerior angle.)
- To be able to find the size of angles when a transversal crosses parallel lines.
- To be able to determine whether two lines are parallel using angles involving a transversal.

Key vocabulary: transversal, corresponding, alternate, cointerior, parallel, skew, supplementary

When a line cuts two other lines, it is called a transversal and forms eight angles. If the two other lines are parallel, then special pairs of angles are formed.



Lesson starter: What's formed by a transversal?

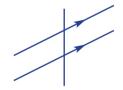
Draw a pair of parallel lines using either:

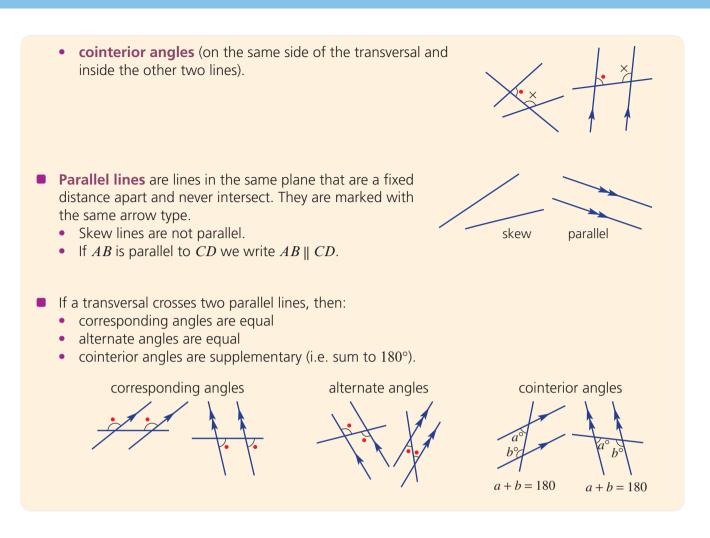
- two sides of a ruler; or
- computer geometry (parallel line tool).

Then cross the two lines with a third line (transversal) at any angle.

Measure each of the eight angles formed and discuss what you find. If computer geometry is used, drag the transversal and see if your observations apply to all the cases that you observe.

Section 1 A transversal is a line intersecting two or more other lines that are usually, but not necessarily, parallel. Image: Section 1 Image: Section 1</td

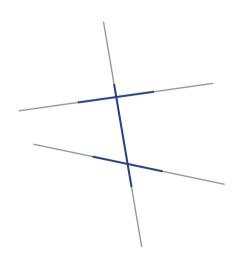




Exercise 2D



- 1 Look at each of the eight angles in this diagram.
 - a How many different-sized angles do you see?
 - **b** Do you think that the two lines cut by the transversal are parallel?



- Look at each of the eight angles in this diagram. 2
 - a How many *different-sized* angles do you see?
 - **b** Do you think that the two lines cut by the transversal are parallel?
- **3** Choose the word *equal* or *supplementary* to complete these sentences. If a transversal cuts two parallel lines, then:
 - a alternate angles are .
 - c corresponding angles are _____
- **b** cointerior angles are
- **d** vertically opposite angles are

Hint: If angles add to 180° they

4, 5, 6-7(1/2)

are called supplementary.

4, 5, 6(1/2)

- Fluency

2D

Name the angle that is:

- a corresponding to $\angle ABF$
- **b** alternate to $\angle ABF$
- **c** cointerior to $\angle ABF$
- **d** vertically opposite to $\angle ABF$

) D	 E

The corresponding angle could also be written as $\angle GFH$.

The alternate angle could also be written as $\angle BFE$ or $\angle CFE$ or $\angle EFC$.

c /HFB

Solution

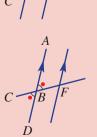
a ∠HFG

∠EFB

b

The cointerior angle could also be written as $\angle BFH$ or $\angle CFH$ or $\angle HFC$.

d $\angle CBD$



Explanation

The vertically opposite angle could also be written as $\angle DBC$.



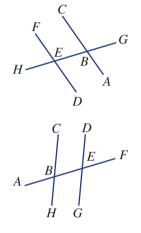
Now you try

Name the angle that is:

- a corresponding to $\angle ABC$
- **b** alternate to $\angle ABF$
- **c** cointerior to $\angle DBF$
- **d** vertically opposite to $\angle HFG$

 $A \xrightarrow{C} D$ $H \xrightarrow{F} E$ G

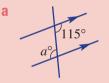
- 4 Name the angle that is:
 - **a** corresponding to $\angle ABE$
 - **b** alternate to $\angle ABE$
 - **c** cointerior to $\angle ABE$
 - **d** vertically opposite to $\angle ABE$
- **5** Name the angle that is:
 - **a** corresponding to $\angle EBH$
 - **b** alternate to $\angle EBH$
 - **c** cointerior to $\angle EBH$
 - **d** vertically opposite to $\angle EBH$



Example 7 Finding angles in parallel lines

Find the value of *a* in these diagrams and give a reason for each answer.

h





Solution

Explanation

- **a** a = 115Alternate angles in parallel lines.
- a = 55
 Corresponding angles in parallel lines.
- Corresponding angles in parallel lines are equal.

Alternate angles in parallel lines are equal.

c a = 180 - 110

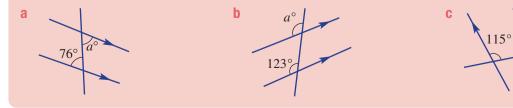
Cointerior angles in parallel lines sum to 180°.

= 70

Cointerior angles in parallel lines.

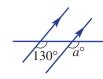
Now you try

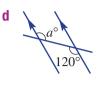
Find the value of *a* in these diagrams and give a reason for each answer.

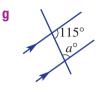


а

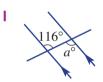
Find the value of *a* in these diagrams, giving a reason. 6

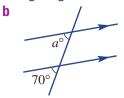


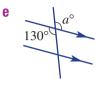




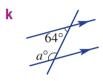










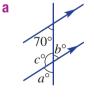


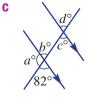
m 70°^a

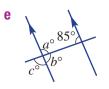
n 132° a

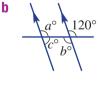
0 117°

7 Find the value of each unknown pronumeral in the following diagrams.

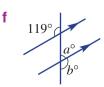




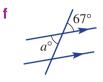


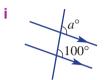










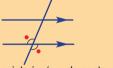


Hint: For Questions 6 and 7, remember the following: corresponding (equal)

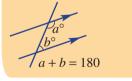




vertically opposite (equal)



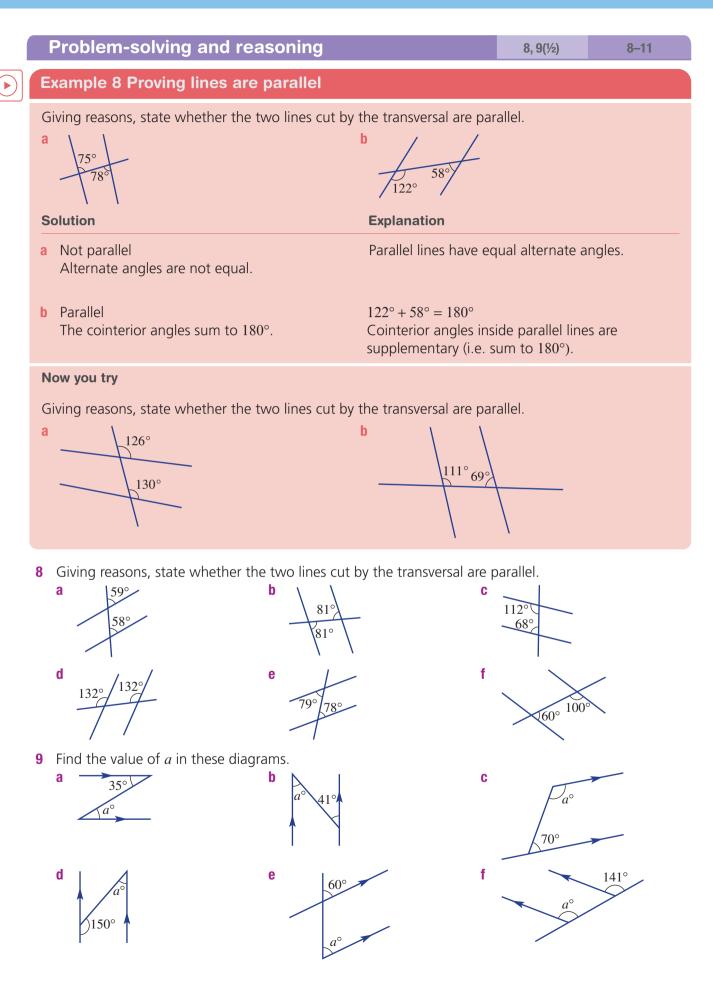
cointerior (supplementary)



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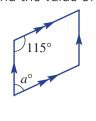
2D

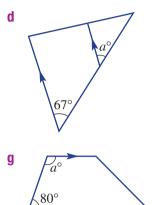


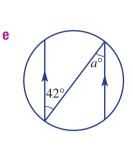
Essential Mathematics for the Victorian Curriculum CORE Year 7

а





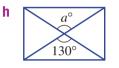


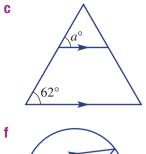


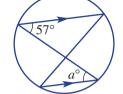
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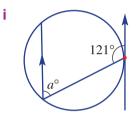
′80°

a°

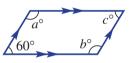






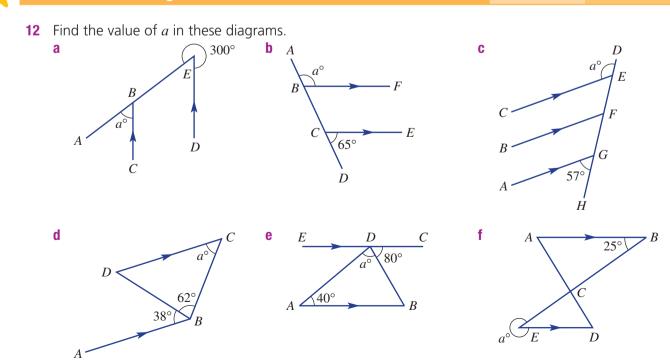


- **11** This shape is a parallelogram with two pairs of parallel sides.
 - **a** Use the 60° angle to find the value of *a* and *b*.
 - **b** Find the value of *c*.
 - c What do you notice about the angles inside a parallelogram?



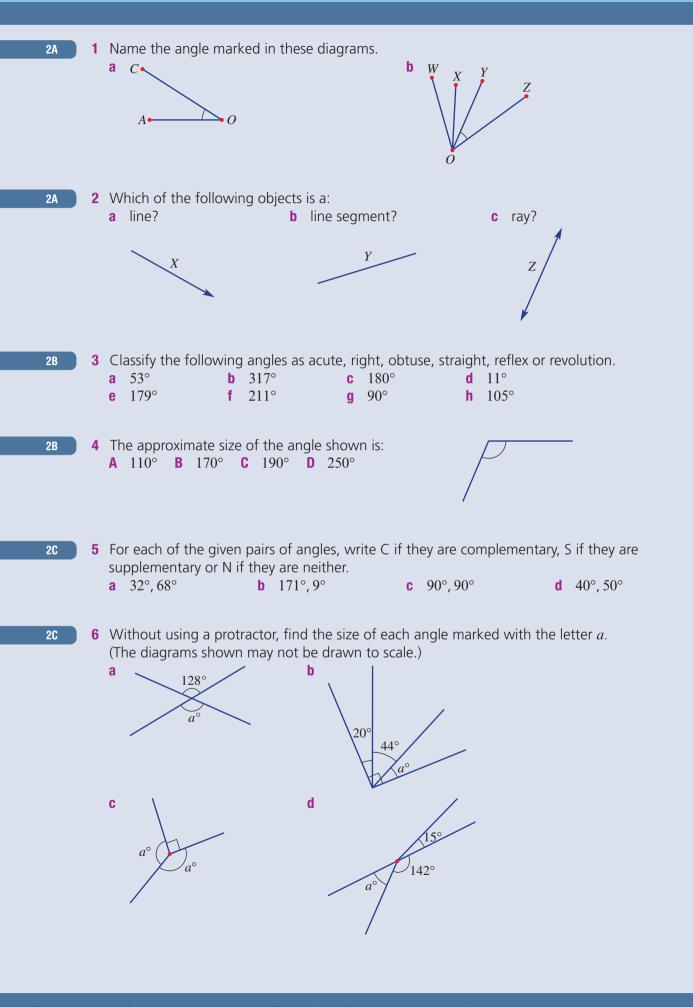
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Parallel challenge

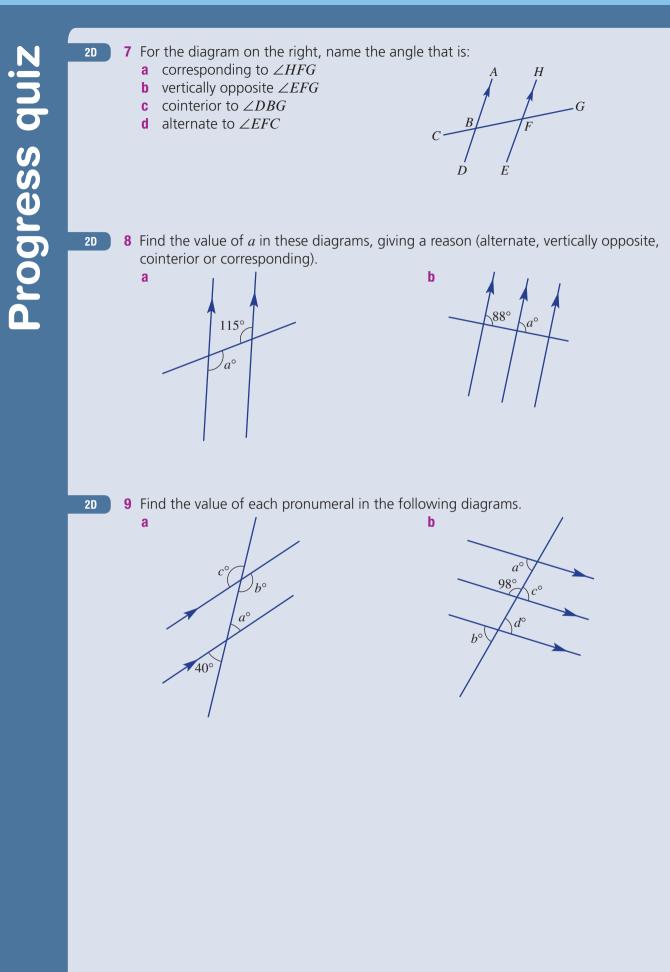


Essential Mathematics for the Victorian Curriculum CORE Year 7

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Essential Mathematics for the Victorian Curriculum CORE Year 7



2E Circles and constructions \star

Learning intentions

- To be able to perform a geometric construction by following instructions involving a pair of compasses and a ruler.
- Key vocabulary: construction, centre, radius, chord, diameter, arc, bisect, perpendicular, pair of compasses

The standard method for constructing accurate geometrical diagrams is with a ruler and a pair of compasses or the equivalent computer software, which will be studied in the next section. Accurate diagrams are important for the design of many objects such as cars and their parts, including the gears in the gearbox.

Lesson starter: Draw it!

Using a pair of compasses and a ruler, see if you can draw:

- a circle with radius 2 cm
- a minor arc

- a circle showing a chord, diameter and radius
- a major arc

Now discuss the following.

- How is the length of the diameter related to the length of the radius?
- How does a major arc differ from a minor arc?

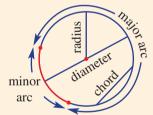
Key ideas

- Common circle features include:
 - centre (point at an equal distance from all points on the circle)
 - **radius** (line interval joining the centre to a point on the circle. Plural: radii)
 - **chord** (line interval joining two points on the circle)
 - **diameter** (longest chord passing through the centre)
 - **arc** (part of a circle. It is possible for a circle to have either a minor or major arc)
- A **pair of compasses** (sometimes called a compass) and a ruler can be used to construct geometrical figures precisely.
- The word **bisect** means to cut in half.
- **Perpendicular** means at right angles (90°).

perpendicular lines



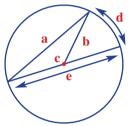




Exercise 2E

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Und	CI 3	lanc	illiy

- 1 Draw the following simple objects.
 - a A segment AB 5 cm long
 - **b** A circle with radius 3 cm
 - **c** A circle with radius 2.3 cm
 - d A circle with diameter 9 cm
- 2 Name the features **a** to **e** in this diagram. Choose from the words: *radius, diameter, minor arc, centre, chord*.

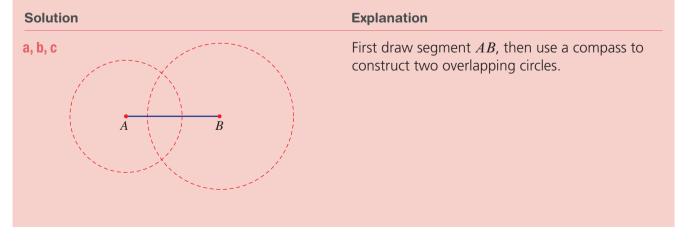


- **3** Use a pair of compasses and a ruler to draw a circle with a radius of about 3 cm. Then mark and label these features.
 - a Centre O
 - **b** Two points, *A* and *B*, at any place on the circle
 - c Radius OA
 - d Chord AB
 - e Minor arc AB

Fluency

Example 9 Constructing a perpendicular line Use a pair of compasses and a ruler to construct a perpendicular line by following these steps. a Use a ruler to draw a line segment *AB* about 5 cm long. b Construct a circle with centre *A* and radius about 3 cm. c Construct a circle with centre *B* and radius about 4 cm.

- **c** Construct a circle with centre *B* and radius about 4 cm.
- d Draw a line connecting the two intersection points of the circles.
- e Measure the angle between the two straight lines. What do you notice?

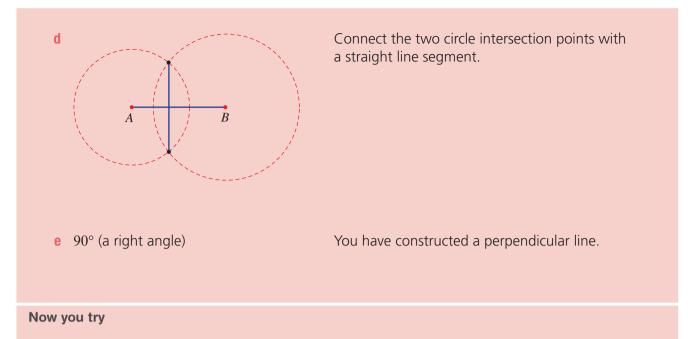


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4, 5

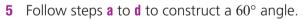
1 - 3

4

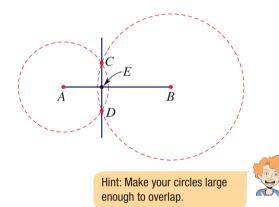


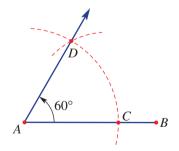
Using a line segment about 7 cm long, construct a perpendicular line.

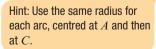
- 4 Follow steps a to e to construct perpendicular lines.
 - **a** Draw a line segment, *AB*, of about 5 cm in length.
 - **b** Construct overlapping circles of different sizes using the two centres *A* and *B*.
 - **c** Mark the intersecting points of the circles and label these points *C* and *D*.
 - **d** Draw the line *CD* and mark the intersection of line *CD* and segment *AB* with the point *E*.
 - e Measure $\angle AEC$ with a protractor. What do you notice?



- **a** Draw a line segment, *AB*, of about 5 cm in length.
- **b** Construct an arc with centre *A* and intersecting the segment *AB* at *C*. Use a radius length less than 5 cm.
- **c** With the same radius construct an arc with centre *C* and intersecting the first arc at *D*.
- **d** Draw the ray AD and measure $\angle DAB$. What do you notice?



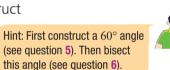




2E Problem-solving and reasoning

- 6 Follow steps a to e to construct an angle bisector.
 - **a** Draw any angle and label $\angle AOB$.
 - **b** Construct an arc with centre *O* so that it cuts OA and OB at points C and D.
 - **c** With the same radius, construct an arc with centre *C* and another with centre D. Ensure these arcs intersect at a point, E.
 - **d** Mark in the ray *OE*.
 - e Measure $\angle AOE$ and $\angle BOE$. What do you notice?
- 7 Use a ruler to draw a segment AB of length 6 cm and then complete the following.
 - a Construct a circle with radius 3 cm with centre A. (Use a ruler to help set the correct length on a pair of compasses.)
 - **b** Construct a circle with radius 3 cm with centre *B*.
 - c Do your two circles miss, touch or overlap? Is this what you expected?
- 8 Use a ruler to draw a line segment, AB, of about 5 cm in length.
 - a Using a pair of compasses, construct arcs with radius 4 cm, as shown, using:
 - i centre A ii centre B
 - **b** Mark point C as shown and use a ruler to draw the segments: i AC BC
 - **c** Measure the angles $\angle BAC$ and $\angle ABC$. What do you notice?

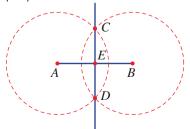




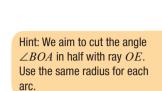
10 Show how you could construct these angles. After each construction, measure the angle using a protractor. (You may wish to use the results from questions 4 and 6 for help.) **a** 45° **b** 22.5°

The perpendicular bisector

- **11 a** Repeat the full construction from question **4** but this time use circles with the same radius.
 - **b** Measure AE and BE. What do you notice?
 - **c** Why do you think the line *CD* is called a perpendicular bisector?



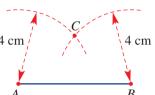




6-10

6-8

4 cm



11

2F Using interactive geometry software \star

Learning intentions

- To be able to use dynamic computer geometry to perform constructions.
- Key vocabulary: construction, drag, measure

Dynamic computer geometry is an effective tool for constructing geometrical figures. Constructing with dynamic computer geometry is like constructing with a ruler and a pair of compasses. The computer gives you the added freedom to drag objects and explore variations of the same construction. With dynamic computer geometry, the focus is on 'construction' as opposed to 'drawing'. Although this can be complicated at first, the results are more precise.

Lesson starter: The disappearing line

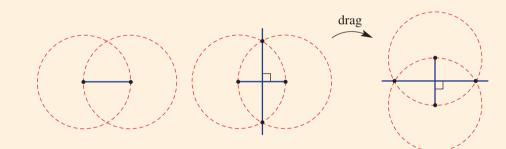
Use computer geometry to construct this figure.

- Add the line *CD* and check that it makes a right angle.
- Drag the points *A* and *B* or increase the size of the circles.
- Can you drag point A or B to make the line CD disappear?

Why would this happen?

Key ideas

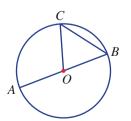
- Using dynamic computer geometry is like using a pair of compasses and a ruler.
- Objects can be **dragged** to explore different cases.
- The same segment can be used to ensure two circles have exactly the same radius.
- Upon dragging, the geometrical construction should retain the desired properties.



Exercise 2F

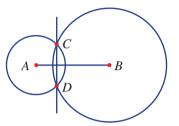
Understanding

- 1 Use computer geometry to construct this diagram.
 - a Measure the lengths of OC, AB and BC.
 - **b** Drag the circle to alter its size.
 - **c** Drag the point *C* to alter the length of chord *BC*.



1.2

2



2F

2

- **a** Use computer geometry to construct an angle $\angle ABC$. Any size will do.
- **b** Mark and measure the angle using computer geometry. Drag the point *A* around *B* to enlarge the angle. See whether you can form all these types of angles.
- Hint: To measure the angle, click on A, then B, then C.

3

3, 4

A

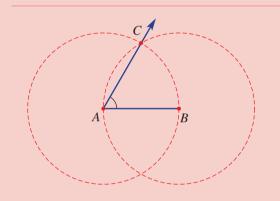
i acute iv reflex ii rightv revolution

Fluency

Example 10 Constructing a 60° angle

Construct an angle of 60° using computer geometry. Then drag one of the starting points to check the construction.

Solution



Explanation

Step 1: Construct and label a segment AB.

Step 2: Construct two circles with radius *AB*, one with centre *A* and one with centre *B*.

Step 3: Mark the intersection C and draw the ray AC.

Step 4: Measure $\angle BAC$ to check.

Now you try

Using computer geometry and starting with a line segment AB of any length, construct a 60° angle.

- 3 Construct each of the following using computer geometry. If necessary, refer back to Section 2E and Exercise 2E to assist you. Check each construction by dragging one of the starting points.
 - a perpendicular line
 - **b** 60° angle
 - c angle bisector
- **4 a** Use the 'parallel line' tool to construct a pair of parallel lines and a transversal.
 - **b** Measure the eight angles formed.
 - c Drag the transversal to change the size of the angles. Check that:
 - i alternate angles are equal
 - ii corresponding angles are equal
 - iii cointerior angles are always supplementary

Hint: Instead of constructing arcs for parts **b** and **c**, just use full circles.





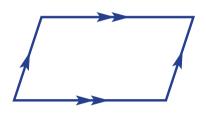
5-7

Problem-solving and reasoning

- **5** Look at the 60° angle construction in Example 10.
 - **a** Why do the two circles have exactly the same radius?
 - **b** What other common geometrical object could be easily constructed simply by adding one more segment?
- **6** Use computer geometry to construct these angles. You may wish to use the 'angle bisector' shortcut tool.
 - **a** 30°

b 15°

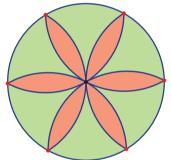
- **c** 45°
- 7 Construct a parallelogram using the 'parallel line' tool.

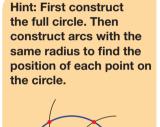


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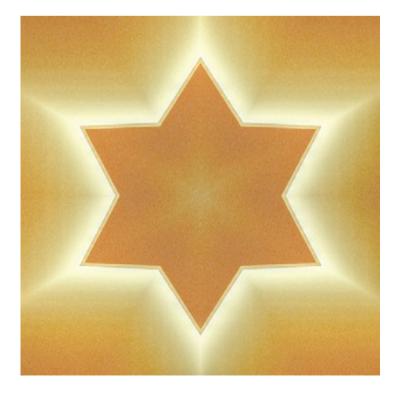
Six-pointed flower

8 Use computer geometry to construct a six-pointed flower. Then drag one of the starting points to increase or decrease its size.





8





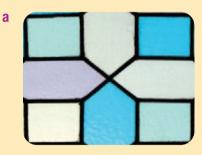
Maths@Work: Glass cutter and design artist for stained-glass windows

Restoration of stained or coloured glass windows and other decorative pieces is a timeless skill requiring artistic ability, a steady hand, good eyesight and fine motor skills. Understanding materials and the ratios of colour combinations when mixing and matching paints and stains is vital.

For the restoration of stained glass and the creation of new designs, it is important to understand and apply the geometry of angles and symmetry.



- 1 Stained-glass windows are made by joining many small pieces of glass. For each stained-glass pattern below, we will copy two of the internal glass pieces.
 - i Use a protractor to measure the vertex angles of a chosen shape inside the glass designs.
 - ii Make a neat, enlarged copy of this shape. Carefully copy the angles (use your protractor again) and label the angles, but make the sides larger.









2 Many stained-glass windows are designed using patterns of circles and arcs. Use a pair of compasses and a ruler to design a stained-glass window pattern using circles and arcs. You may wish to use an idea from one of the designs shown below.



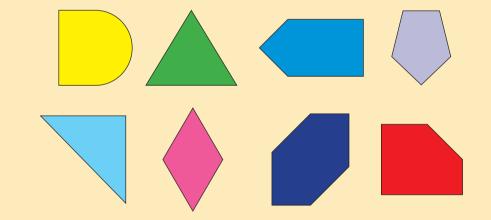


Using technology

Use a word processing program or a geometrical drawing application to create your own design for a stained-glass window by combining geometrical shapes.
 Some shapes you could use are shown below.

Hint: Shapes can be repeated and all shapes need to fit together.

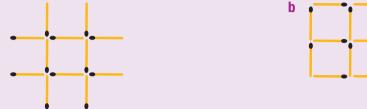






а

- Puzzles and games
- Move three matchsticks to turn the fish to face the opposite direction. 1
- 2 Move three matchsticks to get three squares of the same size.



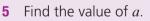
Two circles are the same size. The shaded circle rolls around the other circle. 3 How many degrees will it have turned after returning to its starting position?

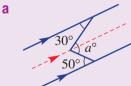
Find the angle between the hour hand and minute hand of a clock at: 4 **b** 9:35 a.m.

b

e





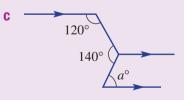


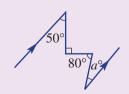
60°



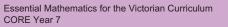
 110°







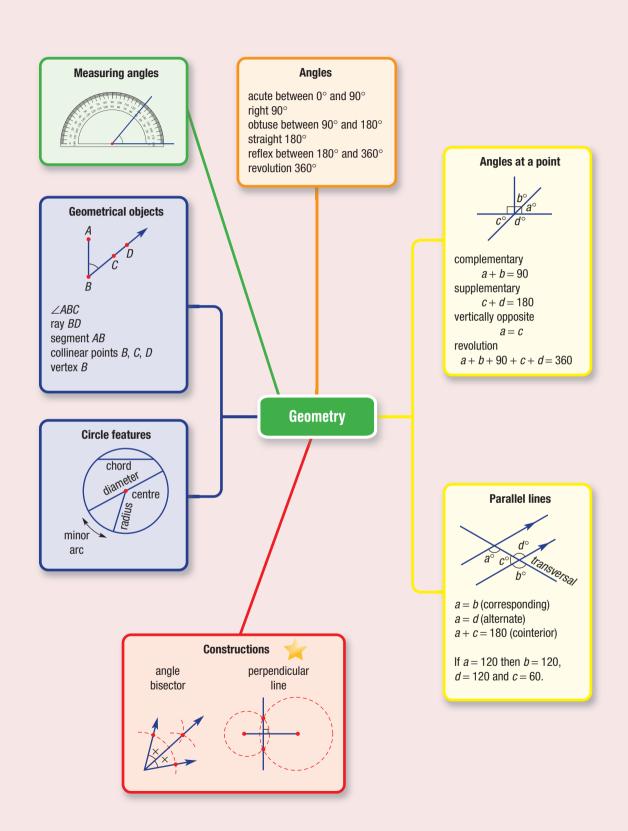




d

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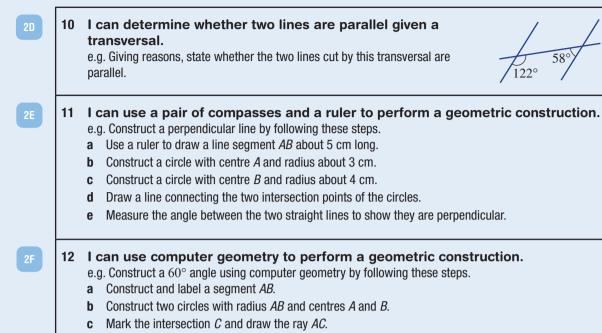
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Chapter checklist

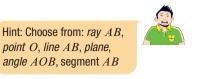
A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

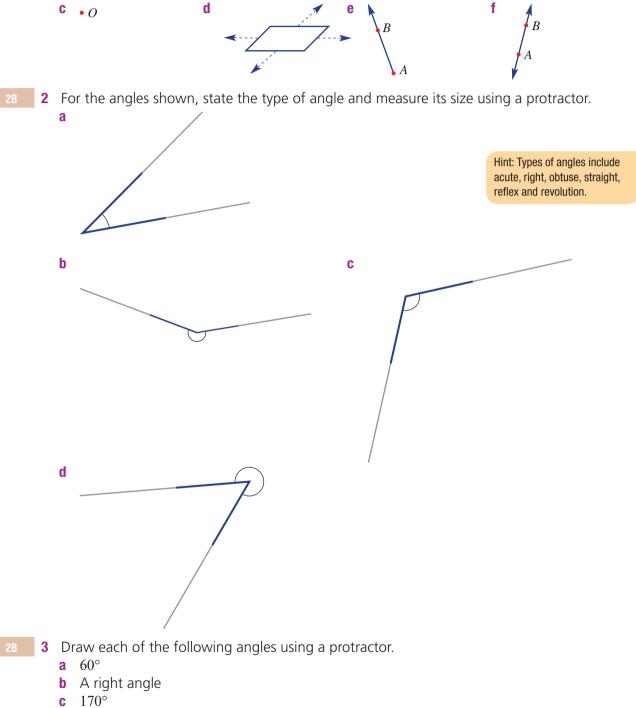
				~
2A	1	I can name lines, rays and segments. e.g. Name this line segment.	A B	
2A	2	I can name angles. e.g. Name the marked angle.	Q R	
28	3	I can classify an angle based on its size. e.g. Classify 47° and 282° as acute, obtuse, straight or reflex.		
28	4	I can measure the size of angles with a protractor. e.g. Use a protractor to measure the angle $\angle EFG$.	G EF	
28	5	I can draw angles of a given size using a protractor. e.g. Use a protractor to draw an angle of size 130° .		
20	6	I can name angles in relation to other angles. e.g. Name the angle which is vertically opposite to \angle SOT.		
20	7	I can find the size of angles without a protractor using a angles at a point. e.g. Find the value of <i>a</i> without a protractor.	other $a^{\circ}_{210^{\circ}}$	
20	8	I can name angles in a relationship to other angles involving a transversal. e.g. Name the angle that is (a) alternate to $\angle ABF$, and (b) cointerior to $\angle ABF$.	$C \xrightarrow{A} H \\ F \\ C \xrightarrow{B} F \\ D E$	
20	9	I can find the size of unknown angles in parallel lines. e.g. Find the value of <i>a</i> , giving a reason for your answer.	$\int_{110^{\circ}}^{a^{\circ}}$	



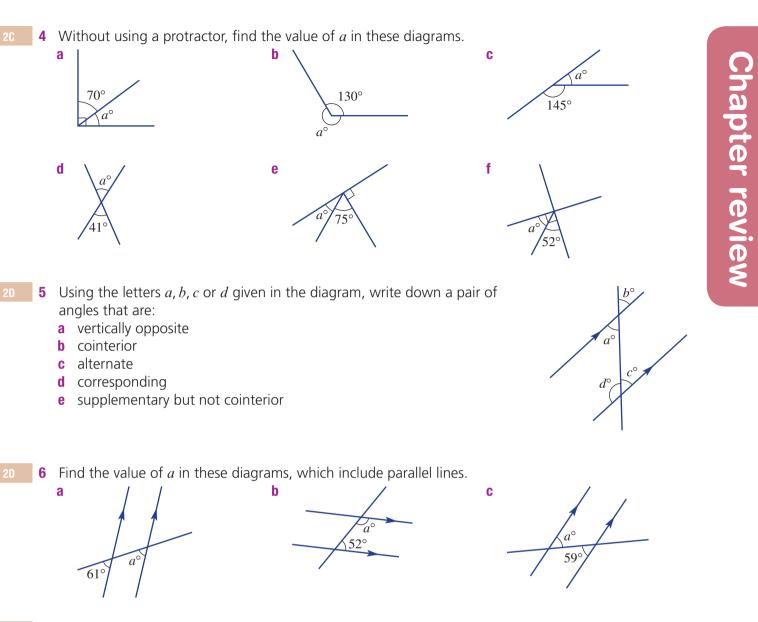
d Measure $\angle BAC$ to check it stays 60° even as the points *A* and *B* are moved.

Chapter checkli

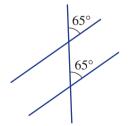




d 265°



For each of the following, state whether the two lines cut by the transversal are parallel. Give reasons 7 for each answer.

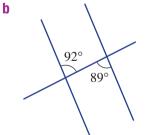


Find the value of *a* in these diagrams.

a°

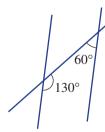
a

8 a

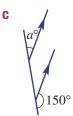


b

85°



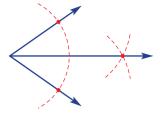
С



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80°

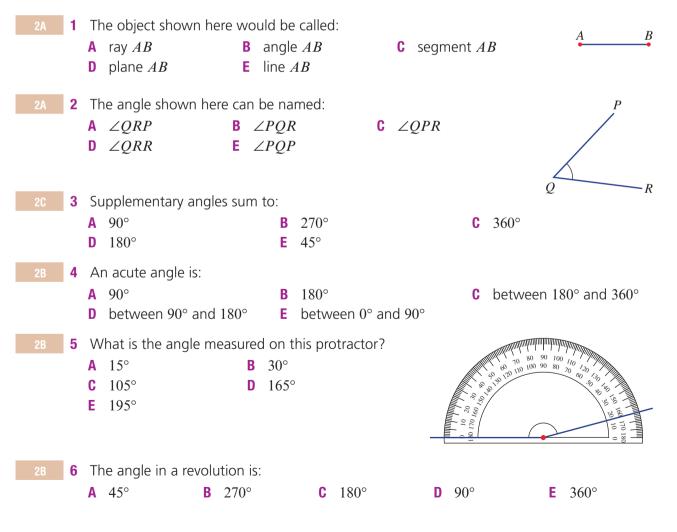
- **9** Use these diagrams to help draw your own construction. You will need a pair of compasses and a ruler or dynamic geometry.
 - a Angle bisector (start with any angle size)





b Perpendicular line (start with a segment of about 6 cm in length)

Multiple-choice questions



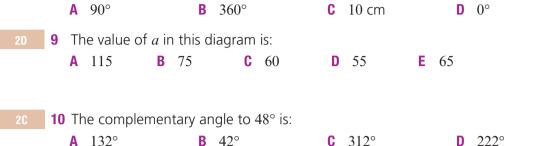
E 180°

115

E 48°



- A cointerior angles are equal
- **B** alternate angles are supplementary (sum to 180°)
- **C** corresponding angles are equal
- **D** vertically opposite angles are supplementary
- **E** supplementary angles add to 90°
- **8** The angle between two perpendicular lines is:

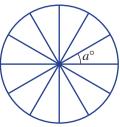


Extended-response questions

- 1 A clock face is numbered 1–12.
 - a Find the angle the minute hand turns in:
 - i 5 minutes
 - ii $\frac{1}{2}$ an hour
 - iii 45 minutes
 - **b** Find the angle the hour hand turns in:
 - i 1 hour
 - ii 7 hours
 - iii $\frac{1}{2}$ an hour
 - **c** Find the angle between the hour and minute hands at these times.
 - i6 p.m.ii3 p.m.iii10 p.m.iv8:30 a.m.
 - **v** 2:30 a.m. **vi** 4:45 p.m.



- 2 A circular birthday cake is cut into pieces of equal size, cutting from the centre outwards. Each cut has an angle of *a* at the centre. Tanya's family takes four pieces. George's family takes three pieces. Sienna's family takes two pieces. Anita's family takes two pieces. Marcus takes one piece.
 - a How many pieces were taken altogether?
 - **b** If there is no cake left after all the pieces are taken, find the value of *a*.
 - **c** Find the value of *a* if:
 - i half of the cake still remains
 - ii one-quarter of the cake still remains
 - iii one-third of the cake still remains
 - iv one-fifth of the cake still remains



B Chapter B Number properties and patterns

Essential mathematics: why understanding number properties and patterns is important

Number properties and patterns are widely applied in science, technology, finance, engineering and the trades.

The Highest Common Factor is commonly used to simplify application rates. Pool owners simplify chlorine usage rates, and landscapers and farmers calculate equivalent fertiliser rates.

- People who work with triangles apply squares and square roots, including engineers, architects, builders, surveyors, navigators, carpenters and graphic designers.
- Cryptography uses very large prime numbers to protect online data.
- Accountants predict possible future annual investment amounts, using an increasing sequence with a common ratio greater than 1.
- Australia's Gouldian finch and pygmy possum are threatened species. The sequence of their annual population numbers is decreasing, with a common ratio less than 1.

In this chapter

- 3A Factors and multiples (Consolidating)
- 3B Highest common factor and lowest common multiple (Consolidating)
- 3C Divisibility 対
- 3D Prime numbers and composite numbers
- **3E** Index form
- **3F** Prime factors
- **3G Squares and square roots**
- 3H Number patterns (Consolidating)
- 3I Patterns with shapes and numbers
- 3J Tables and rules
- 3K The number plane and graphs

Victorian Curriculum

NUMBER AND ALGEBRA Number and place value

Investigate index notation and represent whole numbers as products of powers of prime numbers (VCMNA238)

Investigate and use square roots of perfect square numbers (VCMNA239)

Linear and non-linear relationships

Given coordinates, plot points on the Cartesian plane, and find coordinates for a given point (VCMNA255)

Investigate, interpret and analyse graphs from real life data, including consideration of domain and range (VCMNA257)

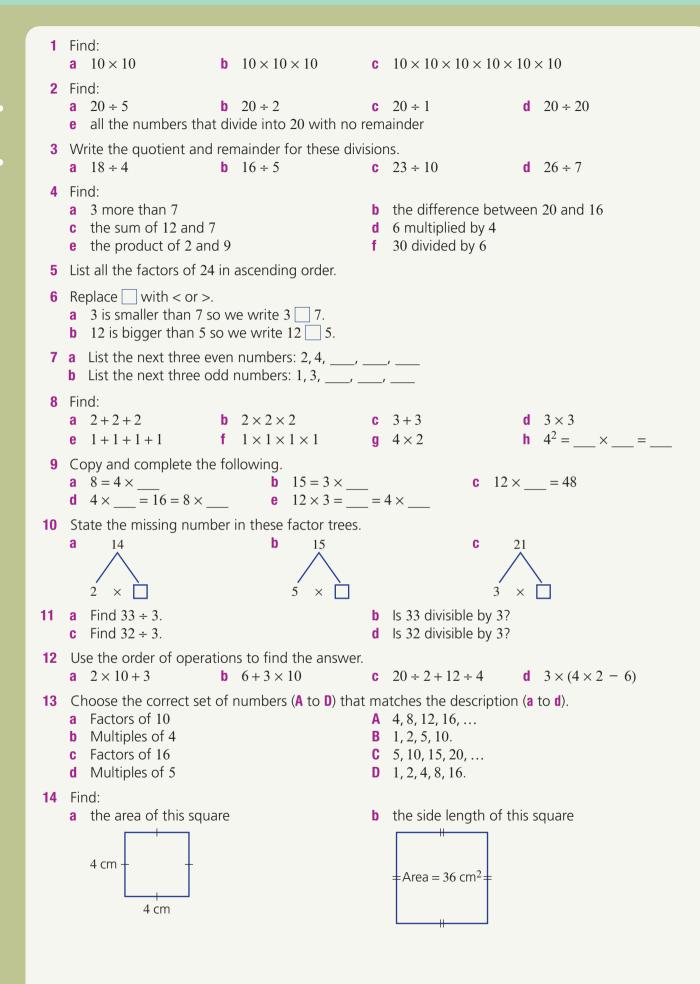
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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

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Warm-up quiz



Essential Mathematics for the Victorian Curriculum CORE Year 7

3A Factors and multiples

CONSOLIDATING

Learning intentions

- To understand that a number has infinitely many multiples.
- To be able to find factors of a number.
- To be able to find multiples of a number.

Key vocabulary: factor, multiple, ascending, remainder

Number patterns can be quite useful when describing groups of objects or relationships between quantities. We start this chapter looking at factors and multiples.

One dozen doughnuts are generally packed into bags or boxes with 3 rows of 4 doughnuts each. Since $3 \times 4 = 12$, we can say that 3 and 4 are **factors** of 12.



Purchasing 'multiple' packs of one dozen doughnuts could result in buying 24, 36, 48 or 60 doughnuts, depending on the number of packs. These numbers are known as **multiples** of 12.

Lesson starter: Using factors to plan a party

Shayna wants everyone at her party (including herself) to have the same number of doughnuts.



- What 'party sizes' are possible so everyone has the same number of doughnuts? For example, a party size of 12 means that Shayna invites 11 friends and everyone gets 3 doughnuts each (12 groups of 3 equals 36).
- List the factors of 36 in ascending (increasing) order. (You could arrange 36 counters into various groups of equal size to find all the possible factors.)
- If Shayna wants just one doughnut, then still wants the remaining friends at the party to have an equal number, how many friends should she invite?

3A

Key ideas

- **Factors** of a number divide exactly into that number.
- For example: $20 \div 4 = 5$ exactly, so 4 is a factor of 20.
 - Factors of 20 listed in pairs: $1 \times 20 = 20, 2 \times 10 = 20, 4 \times 5 = 20$
 - Factors of 20 in ascending order: 1, 2, 4, 5, 10, 20

1 is the smallest factor of any number.

The largest factor of any number is the number itself.

- Multiples of a number are made when that number is multiplied by whole numbers.
 - For example, the multiples of 5 in ascending order are 5, 10, 15, 20, ...
 - Another way to find multiples of 5 is to start with 5 and keep adding 5.



The smallest multiple of a number is the number itself.

Multiples just keep on getting bigger.

• A **remainder** is a number left over from division.

Exercise 3A

Understanding	1–4	4

1 Think about arranging 24 counters into a rectangle with 2 rows of 12 counters.



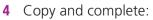
- a Copy and complete the factor pairs for this rectangle. $12 \times \square = 24$ or $\square \times 12 = 24$
- **b** Using all 24 counters each time, think about three different-sized rectangles and write down a factor pair for each.

2 Copy and complete:

- a 1 × _ = 12, 2 × _ = 12, 3 × _ = 12 The factors of 12 are 1, ___, ___, ___, ___, 12
- **b** $1 \times \square = 5$ The factors of 5 are ____, ____

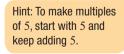
3 Copy and complete:

- **a** The first six multiples of 5 are 5, ____, 15, ____, 25, ____
- **b** The first six multiples of 10 are 10, ___, 30, ___, ___,
- **c** The first six multiples of 7 are 7, ____, 28, ____, 42



- **a** $7 \times 6 = 42$ so 7 and 6 are _____ of 42.
- **b** To make multiples of 6, multiply 6 by whole numbers. For example:
 - $1 \times 6 = 6$, $\square \times 6 = 12$, $\square \times 6 = 18$, $\square \times 6 = 24$
- **c** The first five multiples of 6 are 6,, 18,,
- **d** If you start with 6 and then keep adding 6, you will produce a list of

Hint: List the factors in ascending order (from smallest to largest).



of 6.



	Fl	uency						5–7	′(½)	5-7(½), 8
	Exa	mple 1 Finding	g facto	ors						
	Find a 1	the complete set	of facto	ors for eac b 40		numb	ers.			
		ition		V +0		Exp	lanation			
ł	a F	actors of 15 are 1	, 3, 5, 15			$1 \times$	15 = 15, 3	× 5 = 15		
I	b F	actors of 40 are:				1 ×	40 = 40, 2	$\times 20 = 40$		
	1	, 2, 4, 5, 8, 10, 20, 4	40.			$4 \times$	10 = 40, 5	$\times 8 = 40$		
							ere are no otl h zero remai		s that d	ivide into 40
I		1 you try the complete set 8	of facto	ors for eac b 50		numb	iers.			
5	a d	st the complete se 10 36 80	b e		ach of the fo		ing numbers 17 42 28			ist the factors in ding order (smallest to t).
	g Exa	mple 2 Listing				•	20			
)		e down the first s			ich of these	num	bers			
	a 1			b 35						
9	Solu	ıtion			Explana	tion				
đ	a 1	1, 22, 33, 44, 55, 6	6		Add on ⁻	the g	iple is always iven number rocess to get	to find the	next m	
I	b 3	5, 70, 105, 140, 17	5, 210				e given num lucing multip		eatedly	add 35 to
`		r you try te down the first s	six multi	ples for ea b 21	ich of these	num	bers.			
6		/rite down the firs 5 7	st six mu b e	Iltiples for 8 20	each of the	follc	owing numbe 12 75	ers.		t: List the multiples in ending order.

7 Fill in the gaps to complete the set of factors for each of the following numbers.

1, 2, ____, 6, 9, ____ **a** 18

3A

- **b** 25 1, ____, 25
- **c** 72 <u>, 2, 3, , 8, 10, 18, 36, 72</u> **d** 120 1, 2, <u>, , , , 6, , 10, , 20, , 30, , 60, _</u>

Example 3 Identifying incorrect multiples

Which number is the wrong multiple in the sequence 7, 14, 20, 28, 35? Write the correct sequence.

Solution	Explanation
20 is incorrect.	$14 + 7 = 21$ or $3 \times 7 = 21$
7, 14, 21, 28, 35	A multiple of 7 must be a whole number times 7.

Now you try

Which number is the *wrong* multiple in the sequence 8, 16, 24, 34, 40, 48? Write the correct sequence.

b 5, 10, 15, 20, 24, 30

8 Find the *wrong* multiple in each of the following. Write the correct sequence.

- **a** 3, 6, 9, 12, 15, 18, 22, 24, 27, 30
- **c** 11, 21, 33, 44, 55, 66, 77, 88, 99, 110 **d** 12, 24, 36, 49, 60, 72, 84

	Problem-solving and reasoning		9, 10 9–	11				
E	Example 4 Finding factor pairs							
E:	Express 96 as a product of two factors, both of which are greater than 6.							
_	SolutionExplanation $16 = 8 \times 12$ Divide 96 by numbers greated	ater than 6	to find a large fa	ctor.				
	low you try xpress 72 as a product of two factors, both of which are greater th	an 7.						
9	Express each of the following numbers as a product of two factor both of which are greater than 4. a 30 b 36 c 42 d 40 e 64 f 100	S,	Hint: For some numbers the two factors will be the same number.	s,				
10	Zane and Matt are both keen runners. Zane takes 4 minutes to jog around a running track and Matt takes 5 minutes. They start together at the same time and jog 6 laps for training. a Copy and complete:		Hint: Use a diagram showing 30 minutes $0 \ 1 \ 2 \ \dots \ 30$					
	 i When Zane jogged 6 laps around the track, he crossed the start/finish line after 4, 8,,, and minutes ii Matt crossed the start/finish line after,,,,,, b How many laps had each boy jogged when they crossed the line c For how long had the boys jogged before they crossed the line 	and ne togethe	r?					

- 11 Anson is preparing for his twelfth birthday party. He has invited 5 friends and is making each of them a 'lolly bag' to take home after the party. To be fair, he wants to make sure that each friend has the same number of lollies. Anson has a total of 67 lollies to share among the lolly bags.
 - **a** How many lollies does Anson put in each of his friends' lolly bags?
 - **b** How many lollies does Anson have left over to eat himself?

Anson then decides that he wants a lolly bag for himself also.

- **c** How many lollies will now go into each of the 6 lolly bags?
- d With 6 lolly bags, are there any lollies left over?

Using factors to make squares or rectangles

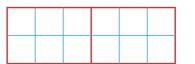
- 12 Joanna is a vet. She wants to buy several pens for separating sick animals. There are square or rectangular pens available, all with sides that are 1, 2, 3 or 4 metres long.
 - **a** Joanna wants to buy at least two equal-sized pens to cover an area of 12 m². Two possibilities are shown below. Find the other four ways Joanna could buy pens.

Option 1: Buy 3 square pens.

Each pen has: L = 2 m, W = 2 m, A = 4 m² Total area = $3 \times 4 = 12 m^2$



Option 2: Buy 2 rectangular pens. Each pen has: L = 2 m, W = 3 m, A = 6 m² Total area = $2 \times 6 = 12 m^2$



Hint: Use grid paper and draw the pens. Note that $2 \text{ m} \times 3 \text{ m}$ pens are the same as $3 \text{ m} \times 2 \text{ m}$ pens, so don't count them twice.

12

- **b** Work out the number of equal-sized *square* pens and their sizes so all these pens join side by side to cover an area of:
 - i 32 m² ii 54 m²
- **c** Work out the number of equal-sized *rectangular* pens and their sizes so all these pens join side by side to cover an area of:
 - i 32 m² ii 54 m²
- **d** A zoo vet wants to buy several larger, equal-sized pens to cover 150 m². Find all the possibilities with whole-number sides from 2 to 25 metres.



3B Highest common factor and lowest common multiple CONSOLIDATING

earning intentions

- To be able to find the highest common factor of two numbers.
- To be able to find the lowest common multiple of two numbers.

Key vocabulary: factor, multiple, highest common factor (HCF), lowest common multiple (LCM)

In the last section, we worked with factors and multiples. In this section, we look at common factors or multiples that are shared by two numbers.

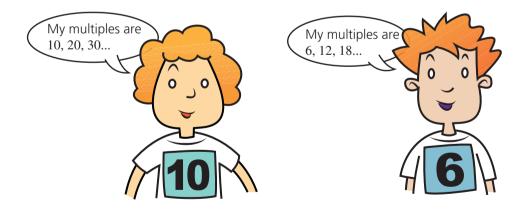
It is often useful to be able to find the highest common factor (HCF) or lowest common multiple (LCM) and these are important in higher levels of mathematics.

Lesson starter: Finding special numbers



We share some common factors. What are they?

Which is the highest (biggest) common factor we share?

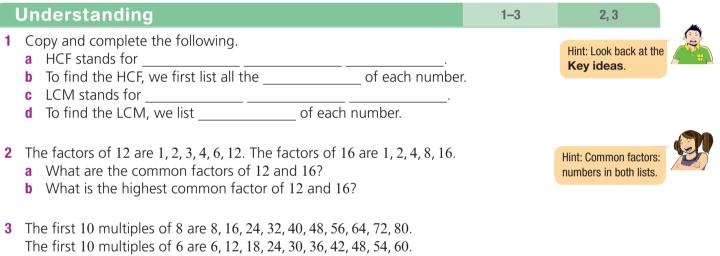


We share some common multiples. What are they? What is the lowest (smallest) multiple we share?

Key ideas

- HCF stands for highest common factor. It is the largest factor shared by the two or more numbers being considered.
 - For example: Find the HCF of 24 and 40.
 Factors of 24 are 1, 2, 3, 4, 6, 8, 12 and 24.
 Factors of 40 are 1, 2, 4, 5, 8, 10, 20 and 40.
 We can see that the highest common factor is 8 so we write HCF = 8.
- LCM stands for lowest common multiple. It is the smallest multiple that two or more numbers divide into evenly.
 - For example: Find the LCM of 20 and 12.
 Multiples of 20 are 20, 40, 60, 80, 100, 120, 140, ...
 Multiples of 12 are 12, 24, 36, 48, 60, 72, 84, 96, ...
 - We can see that the lowest common multiple is 60 so we write LCM = 60.

Exercise 3B



- a What are two common multiples of 8 and 6?
- **b** What is the lowest common multiple of 8 and 6?



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3B

Chapter 3	Number properties and patterns

Fluency		4–5(1⁄2)	4–5(½)	
Example 5 Finding the highest common f	actor (HCF)			
 Find the highest common factor (HCF) of 36 and 48	3.			
Solution	Explanation			
Factors of 36 are: $(1, 2), (3, 4), (6, 9, 12), 18$ and 36.	Find the factors of 30 etc.) and list them in		$2 \times 18 = 36$,	
Factors of 48 are: $(1, 2), (3, 4), (6, 8, 12), 16, 24$ and 48.	Find the factors of 48 ($1 \times 48 = 48$, $2 \times 24 = 48$, etc.) and list them in order. Circle common (shared) factors. Pick the HCF (highest shared factor).			
HCF = 12				
Now you try Find the highest common factor (HCF) of 24 and 32				
 4 Find the HCF of the following numbers. a 4 and 5 b 8 and 13 d 3 and 15 e 16 and 20 g 20, 40 and 50 h 12, 15 and 30 	 c 2 and 12 f 15 and 60 i 5, 7 and 11 	Hint: First list of each num	1.1.2.2.1.5	

Example 6 Finding the lowest common multiple (LCM)

Find the lowest common multiple (LCM) of 6 and 10.			
Solution	Explanation		
6, 12, 18, 24, 30, 36,	List multiples of each number.		
10, 20, (30), 40,	Circle the first common (shared) multiple.		
LCM = 30	This is the LCM.		

Now you try

Find the lowest common multiple (LCM) of 8 and 12.

5 Find the LCM of the following numbers.

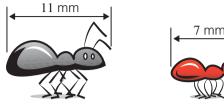
- **a** 4 and 5 **b** 3 and 7
- **d** 8 and 10 **g** 2, 3 and 5
- **e** 4 and 6
- **h** 3, 4 and 5
- **c** 5 and 6 **f** 5 and 10 i 2, 3 and 7
- Hint: First list some multiples of each number.



6-8

Problem-solving and reasoning

6 A trail (line) of red ants runs alongside a trail of black ants. Assume there are no gaps between ants in a trail.

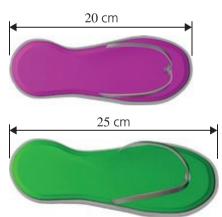


- **a** What is the smallest number of red ants and the smallest number of black ants that would make the trails equal in length?
- **b** How long would that trail be?
- 7 A line of large spoons is next to a line of small spoons.





- **a** What is the smallest number of each type of spoon that would make the lines equal in length?
- **b** How long would that line be?
- **c** The answer to part **b** is called the _____ of 14 and 21.
- 8 A line of pink thongs is next to a line of green thongs.



Hint: Remember that LCM means lowest common multiple.

- **a** Suppose that the two lines of thongs are the same length. How long could each line be? Find three possible answers.
- **b** Which of the answers in part **a** is the LCM of 20 and 25?
- **9** Wendy is a florist who is making up small bunches of roses for sale. She has 36 red roses, 42 pink roses and 30 cream roses.

Wendy uses only one colour for each bunch. She wants to use all the roses. Each bunch must have the same total number of roses.

- **a** What is the largest number of roses Wendy can put in each bunch?
- **b** The answer to part **a** is called the of 36, 42 and 30.
- **c** How many bunches of each colour can she make?

Hint: There can only be whole ants in each trail!

7–10



- **10** Given that the HCF of a pair of different numbers is 8, find the two numbers:
 - **a** if both numbers are less than 20
 - **b** when one number is in the 20s and the other in the 30s

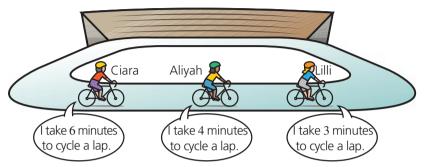
Hint: Remember, HCF means highest common factor.

11

Cycling laps

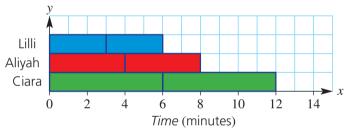
3B

11 Three girls are riding their bikes around a circular track. They all start together.



Lilli takes 3 minutes to cycle each lap. (That is, she crosses the starting line every 3 minutes.) Aliyah takes 4 minutes for each lap and Ciara takes 6 minutes.

This bar graph shows the time each girl takes for the first two laps.



- **a** On grid paper, copy the graph and extend it to show the number of laps each girl completes in 24 minutes. (Draw a rectangle for each lap cycled.)
- **b** When do all three girls first cross the starting line together? (Give your answer as the number of minutes after the start.)
- c How many full laps has each girl completed after 24 minutes? (Count whole laps only.)
- **d** Suppose that each girl rides 15 laps. How many minutes after Lilli will:
 - i Aliyah finish? ii Ciara finish?



3C Divisibility 🕇

Learning intentions

- To understand that tests can be used to check if a number is divisible by another number without actually dividing.
- To be able to test for divisibility by 2, 3, 4, 5, 6, 8, 9 and 10.
- Key vocabulary: factor, divisible, remainder, divisibility test

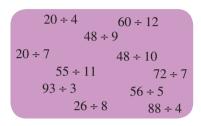
It is often useful to know whether a number is exactly divisible by another number. For example, 20 is divisible by 2 because $20 \div 2 = 10$ with no remainder. However, 20 is not divisible by 3 because $20 \div 3 = 6$ with remainder 2.

There are simple divisibility tests for each of the single-digit numbers, with the exception of 7.

Lesson starter: Exploring remainders

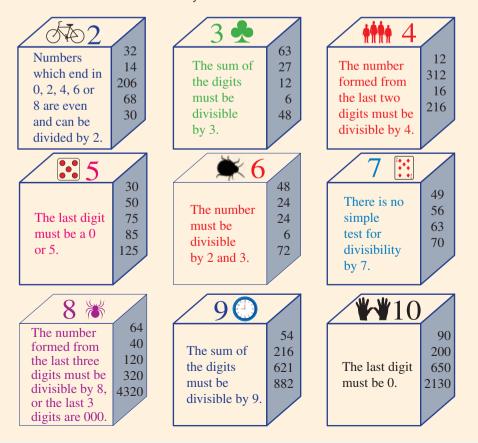
Work with a partner to sort these divisions into two groups:

- Divisions with no remainder
- Divisions with a remainder



Key ideas

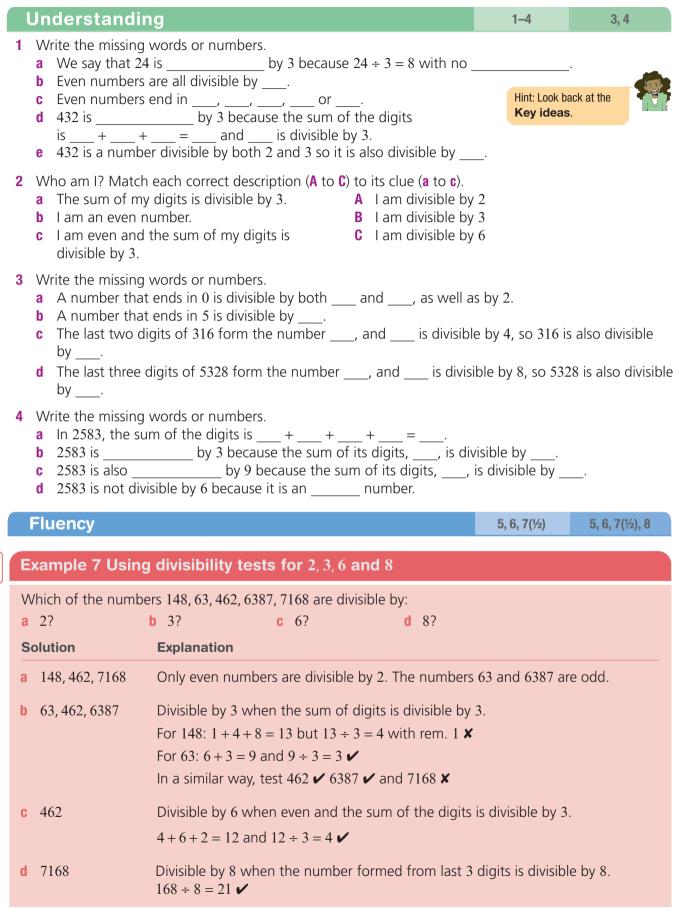
- A number is **divisible** by another number if there is no **remainder** after the division. For example, 84 is divisible by 4 because 84 ÷ 21 = 4 exactly, with no remainder. That is, 4 is a **factor** of 84.
- Divisibility tests are ways to work out whether a whole number is divisible by another whole number, without actually doing the division.
 All numbers are divisible by 1.



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Exercise 3C



Now you try			
Which of the numb	oers 37, 126, 21	6, and 13 914 are div	visible by:
a 2?	b 3?	c 6?	d 8?

- **5 a** Which of these numbers are divisible by 2? 3, 6, 13, 14, 8, 17, 21, 54, 22, 34, 33, 50, 18, 35, 46
 - **b** Which of these numbers are divisible by 3? 12, 14, 18, 20, 22, 30, 27, 23, 54, 50, 36, 42, 13, 24, 43
 - **c** Which of these numbers are divisible by 6? 12, 24, 28, 38, 63, 60, 87, 225, 54, 252, 36, 92, 66, 84, 143
 - d Which of these numbers are divisible by 8? 35, 168, 7168, 40, 5032, 9338, 248, 7831, 6400, 9568

Hint:
Divisibility tests:
2: last digit even
3: sum of digits is divisible by 3
6: divisible by 2 and 3
8: number formed from last
3 digits is divisible by 8 or ends in 000.

Example 8 Using divisibility test	ts for 4, 5, 9 and 10
Which of the numbers 540, 918, 8775, 3	924 are divisible by:
a 10? b 5?	c 4? d 9?
Solution	Explanation
a 540	Divisible by 10 when number ends in 0.
b 540, 8775	Divisible by 5 when number ends in 0 or 5.
c 540, 3924	Divisible by 4 when last two digits divisible by 4.
	For 540: 40 ÷ 4 = 10 ✔
	For 918: 18 ÷ 4 = 4 rem. 2 ≭
	In a similar way, test 75 X and 24 V
d 540, 918, 3924, 8775	Divisible by 9 when sum of digits divisible by 9.
	For 540: $5 + 4 + 0 = 9$ and $9 \div 9 = 1$
	For 918: $9 + 1 + 8 = 18$ and $18 \div 9 = 2 \checkmark$
	In a similar way, test 8775 \checkmark and 3924 \checkmark
Now you try	
Which of the numbers 62, 570, 2112, 56	17 are divisible by:
a 10? b 5?	c 4? d 9?

3C

6

- a Which of these numbers are divisible by 5?
- 35, 52, 125, 13, 15, 100, 113, 112, 32, 515, 408, 730, 105 Which of these numbers are divisible by 10?
- 20, 64, 800, 98, 290, 610, 85, 265, 590, 52, 39, 90, 160
- **c** Which of these numbers are divisible by 4? 16, 32, 220, 10, 12, 28, 213, 432, 72, 316, 424, 1836, 135
- d Which of these numbers are divisible by 9? 27, 432, 456, 88, 99, 387, 63, 55, 720, 85, 253, 2799

Example 9 Applying divisibility tests

Hint:

Divisibility tests: 5: last digit 5 or 0 10: last digit 0 4: number formed from last two digits is divisible by 4 9: sum of digits is divisible by 9

Work out whether the following calculations are possible without leaving a remainder.a 54 327 ÷ 3b 765 146 ÷ 8Solutiona Digit sum = 215+4+3+2+7=21Yes, 54 327 is divisible by 3.21 is divisible by 3.b $8 \frac{1 8}{14^6 6}$ rem. 2Check whether the number formed by the last three digits is divisible by 8.

Now you try

Work out whether the following calculations are possible without leaving a remainder.

a 4168 ÷ 4 **b** 3142 ÷ 9

7 Work out whether the following calculations are possible without leaving a remainder.

a 23 562 ÷ 3	b 39 245 678 ÷ 4	c 1 295 676 ÷ 9	
d 213456 ÷ 8	e 3193457 ÷ 6	f $2000340 \div 10$	Hint: Apply the divisibility
g 51 345 678 ÷ 5	h 215 364 ÷ 6	i 9543 ÷ 6	tests rather than doing the entire division.
j 25756 ÷ 2	k 56 789 ÷ 9	324 534 565 ÷ 5	
m 2 345 176 ÷ 8	n 329 541 ÷ 10	o 225 329 ÷ 3	
p 356 781 276 ÷ 9	q 164 567 ÷ 8	r $2002002002 \div 4$	

8 Copy the table. Carry out the divisibility tests on the given numbers, filling in the table with ticks or crosses.

Hint: ✓ if divisible. ★ if not divisible.

Number	Divisible by 2	Divisible by 3	Divisible by 4	Divisible by 5	Divisible by 6	Divisible by 8	Divisible by 9	Divisible by 10
243 567								
28 080								
189 000								
1 308 150								
1 062 347								

Hint: Think: groups

13

of make 88.

Problem-solving and rea	9, 11	9–12		
 9 Give a reason why: a 8631 is not divisible by 2 c 426 is not divisible by 4 e 87 548 is not divisible by 6 g 3 333 333 is not divisible by 9 	 b 31 313 is not divisible by 3 d 5044 is not divisible by 5 f 214 125 is not divisible by 8 h 56 405 is not divisible by 10 		nt: Think about the rules r divisibility.	
 Give the remainder when: a 326 is divided by 3 b 21154 is divided into groups c 72 is divided into six groups d 45675 is shared into five groups 		am	t: The remainder is the ount left over after the ision.	

11 The game of 'clusters' involves a group getting into smaller-sized groups. Players get into groups as quickly as possible once the cluster size has been called out. If a year level consists of 88 students, which cluster sizes would mean that no students are left out of a group? Give all possible answers.



12 Blake's age is a two-digit number. It is divisible by 2, 3, 6 and 9. How old is Blake if you know that he is older than 20 but younger than 50?

A very large number

- **13** a Is the number 968 362 396 392 139 963 359 divisible by 3?
 - **b** Many of the digits in the number above can actually be ignored when calculating the digit sum. Which numbers can be ignored and why?
 - **c** To determine if the number above is divisible by 3, only five of the 21 digits actually need to be added together. Find this 'reduced' digit sum.
 - **d** Make a list of large numbers. Include some numbers that are divisible by 3 and other numbers that are not.
 - e Swap lists with a classmate. See how quickly you can find each other's numbers that are divisible by 3.

3D Prime numbers and composite numbers

Learning intentions

- To be able to determine whether a number is prime by considering its factors.
- To be able to find the prime factors of a given number.
- To know that 1 is neither prime nor composite.

Key vocabulary: factor, prime number, composite number

A prime number has only two factors. For example, 5 is a prime number because its complete list of factors includes only 1 and 5.

Composite numbers have more than two factors. For example, 9 is a composite number because its factors are 1, 3 and 9.

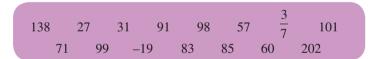
Prime numbers have many important uses in everyday life, such as internet security. There are some interesting prime numbers with remarkable patterns in their digits, such as 12 345 678 901 234 567 891. You can also get primes such as 111 191 111 and 123 494 321 which are the same if you read them forwards or backwards. These are called palindromic primes. Below is a palindromic prime number that reads the same upside down or when viewed in a mirror.



1888081808881

Lesson starter: Find the prime numbers

Elise is trying to decide which of the following are prime numbers.



- Which numbers could she eliminate straight away? Why?
- How could Elise use divisibility tests to eliminate some of the other numbers?
- Which of the numbers do you think are prime?

37	36	35	34	33	32	31	
38	17	16	15	14	13	30	
39	18	5	4	3	12	29	
40	19	6	1	2	11	28	
41	20	7	8	9	10	27	
42	21	22	23	24	25	26	
43	44	45	46	47	48	49	

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Key ideas

- A **prime number** is a positive whole number that has only two **factors**: 1 and itself.
 - The smallest prime numbers include 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, ...
- A number that has more than two factors is called a **composite number**.
- The number 1 has only one factor $(1 \times 1 = 1)$. It is neither prime nor composite.

Exercise 3D

Understanding	1–4	4	
 1 Copy and complete the following. a A number has only two factors: and b A number that has more than two factors is a 	in complexity of the second	at the Key ideas .	
2 a The factors of 12 are 1, 2, 3, 4, 6 and 12. Is 12 a prime numberb The factors of 13 are 1 and 13. Is 13 a prime number?	?		
a List the first 10 prime numbers.b List the first 10 composite numbers.			
4 a What is the first prime number greater than 10?b What is the first composite number greater than 10?			
Fluency	5–6(½), 7	5–6(½), 7, 8	
Example 10 Deciding if a number is prime or composit	te		
Which of these numbers are prime and which are composite: 22, 35SolutionExplanation	5, 17, 11, 9, 5?		
Prime: 5, 11, 17 5, 11, 17 have c	only two factors (1 a	nd itself).	
Composite: 9, 22, 35 $9 = 3 \times 3, 22 = 3$	$2 \times 11, 35 = 5 \times 7$		
Now you try Which of these numbers are prime and which are composite: 7, 25,	39, 43, 58, 73?		
i 8 j 49 k 99 l :	37 H 3 H	Hint: A prime number nas only two factors: 1 and itself.	

30

	nd the prime numbers that are fac olution	tors of 30.	Evel	onotion		
			•	anation		
	actors of 30 are:			all the fa		
	2, 3, 5, 6, 10, 15, 30			$30, 2 \times 15,$		
Ρ	rime factors are 2, 3 and 5.					ctors are prime.
				not a prin		
			2 = 2	$2 \times 1, 3 =$	$3 \times 1, 5$	$5 = 5 \times 1$
	ow you try	_				
	ow you try nd the prime numbers that are fac	tors of 48.				
				60 36		Hint: List all the factors first.
Fi	Find the prime numbers that are factors for the prime numbers that are factors and the prime numbers and the prime numbers that are factors and the prime numbers that are factors and the prime numbers and the prime number	actors of:			C	Hint: List all the factors first.

Problem-solving and reasoning

- 9 The following are not prime numbers, yet they are the product (×) of two primes. Find the two primes that multiply to give:
 a 15
 b 21
 c 35
 - **a** 15 **d** 55

C f

- 10 Which one of the following numbers has factors that are all prime numbers, except itself and 1?12, 14, 16, 18, 20
- Hint: First list all the factors of each number.

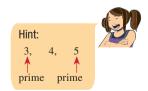
9,10

133

11 Twin primes are pairs of primes that are separated from each other by only one whole number. For example, 3 and 5 are twin primes. Find three more pairs of twin primes.

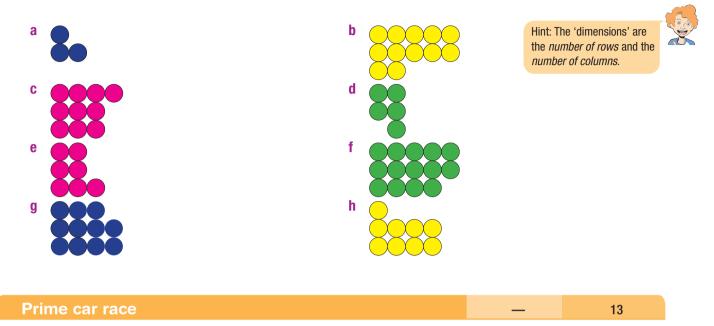
143

е

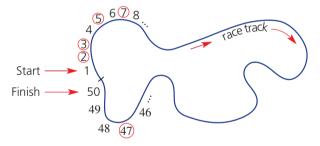


9–12

- 12 Answer these questions for each of the arrays (a to h) below.
 - i Is it possible to rearrange the counters into a rectangle with two or more equal rows?
 - **ii** If it is possible, state the dimensions of the new rectangle.
 - iii State the number of counters and whether this is a prime or a composite number.



- **13** Play this game with a classmate. You will need a large sheet of paper, a die and two 'race cars' (counters or erasers).
 - On the sheet of paper, draw a curvy line for your race track.
 - Write the numbers 1 to 50 along your track and circle all the prime numbers. For example:



- Start with both cars on 1. Take turns to roll the die and drive your car that number of places along the track.
- If your car lands on a prime number, it needs a pit stop (flat tyre, low fuel, etc.) and you miss a turn.
- The car that wins reaches the finish line first. (You must roll the correct number to land exactly on 50.)



3E Index form

Learning intentions

- To understand what an expression like 8⁵ means.
- To be able to write a product in index form if there are repeated factors.
- To be able to evaluate numeric expressions involving powers using multiplication.
- Key vocabulary: base, power, index (plural: indices), expanded form, factor form, index form, raised

When a number is multiplied by itself, we often write that product in index form. For example:

 $1000 = 10 \times 10 \times 10$ (expanded form)

 $=10^3$ (index form)

For 10^3 we say '10 to the power of 3'.

Lesson starter: An easier way

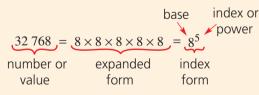
What is an easier way of writing:

- $10 \times 10 \times 10 \times 10$, other than 10000?
- $10 \times 10 \times 10 \times 10 \times 10 \times 10$, other than 1 000 000?
- Computer memory and hard-drive storage are measured in bytes. Do you know the size of the hard drive of your computer at school? How many bytes does it have? Copy and complete this table of computer storage units.

Number of bytes					
kilobyte kB 1 thousand					
megabyte	MB				
	GB	1 thousand million $= 1$ billion	109		
terabyte		1 million = 1 trillion	10 ¹²		

Key ideas

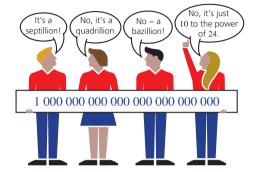
 We can write the product of repeated factors with a **base** number and an **index** number. This is called writing an expression in **index form**. For example:



- The power or index shows the number of repeated factors. It is the number that a base is raised to. 8⁵ reads '8 to the power of 5'.
- Numbers in index form are evaluated first in the order of operations.

For example: $3 + 2 \times 4^2 = 3 + 2 \times 16$ = 3 + 32= 35

• Note that $2^3 = 2 \times 2 \times 2 = 8$. 2^3 does *not* mean $2 \times 3 = 6$.



4

Hint: Choose from the words:

index, expanded, base, power

1-4

Exercise 3E

Understanding

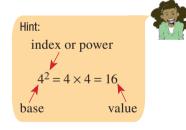
1 Write the missing words.

- **a** The product $2 \times 2 \times 2$ is called the _____ form of 8.
- **b** 2^3 is called the _____ form of 8.
- **c** 2^3 reads: '2 to the _____ of 3'.
- **d** In 2³, the special name for the 2 is the _____ number.
- e In 2³, the special name for the 3 is the _____ or _____.
- 2 Copy and complete each product of repeated factors.
 - **a** $3^2 = 3 \times$ **b** $2^4 = 2 \times \times \times \times \times$ **c** $5^3 = 5 \times \times \times$
 - $\mathbf{d} \quad 8^5 = \boxed{\mathbf{x} \times \mathbf{x}} \times \mathbf{x} \times \mathbf{x}$
- **3** Copy and complete the table.

Expanded form	Index form	Base	Index or power
	7 ³		
$5 \times 5 \times 5$			
		2	6
	6 ⁴		

4 Copy and complete the table.

Index form	Base number	Index or power	Value
2 ³	2	3	8
5 ²			
104			
27			
1 ¹²			
121			
05			





Essential Mathematics for the Victorian Curriculum CORE Year 7

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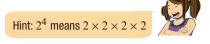
3E				
	Fluency		5–7(½)	5-8(1/2)
	Example 12 Converting to index form			
	Simplify these products by writing them in index for a $5 \times 5 \times 5 \times 5 \times 5 \times 5$ b $3 \times 3 \times 2 \times 3 \times 3$			
	Solution	Explanation		
	a $5 \times 5 \times 5 \times 5 \times 5 \times 5 = 5^6$	The factor 5 is repeated	l six times.	
	b $3 \times 3 \times 2 \times 3 \times 2 \times 3 = 2^2 \times 3^4$	2 is repeated two times 3 is repeated four times		
	Now you try			
	Simplify these products by writing them in index fo			
	a $7 \times 7 \times 7 \times 7 \times 7$ b $5 \times 2 \times 2 \times 5 \times 2 \times 2$	$(2 \times 2 \times 5)$		
	 5 Simplify these products by writing them in index a 3×3×3 b 2×2×2×2×2 d 10×10×10×10 e 6×6 g 1×1×1×1×1×1 h 4×4×4 j 3×3×5×5 k 2×2×7×7×7 m 8×8×5×5×5 p 4×13×4×4×7 q 10×9×10×9×9 	c $15 \times 15 \times 15 \times 15$ f $20 \times 20 \times 20$ i 100×100 i $9 \times 9 \times 12 \times 12$ o $13 \times 7 \times 13 \times 7 \times 7$		wer is the 🖉 🔫 🎙
	Example 13 Expanding expressions in ind	ex form		
	Write each of the following in factor form and find a 2^4 b $2^3 \times 5^2$	the value.		
	Solution	Explanation		
	a $2^4 = 2 \times 2 \times 2 \times 2$ = 16	The digit 2 is repeated to Calculate the value.	four times.	
	b $2^3 \times 5^2 = 2 \times 2 \times 2 \times 5 \times 5$ = 8 × 25 = 200	The digit 2 is repeated t multiply 5 by 5. Calculate the value.	three times, th	nen
	Now you try Write each of the following in factor form and find a 3^4 b $7^2 \times 2^3$	the value.		

6 Write in expanded factor form and find the value.

а	2 ⁵	b	8 ²	C	10 ³	d	$3^2 \times 2^3$
е	10 ⁴	f	$2^{3} \times 5^{3}$	g	$1^{6} \times 2^{6}$	h	$11^2 \times 1^8$

7 Copy and complete the following.

- **a** $3 \times 2 =$ ____ but $3^2 =$ ____ × ___ = ___ **b** $2 \times 4 =$ ____ but $2^4 =$ ____ × ___ × ___ × ___ = ___
- **c** $5 \times 2 =$ _____ but $5^2 =$ _____ × ____ = ____
- **d** $6 \times 2 =$ _____ but $6^2 =$ ____ × ____ = ____
- 8 Write in expanded form. (Do not find the value.)
 - **a** 2^4 **b** 17^2 **c** 9^3 **d** 3^7 **e** $3^5 \times 2^3$ **f** $4^3 \times 3^4$ **g** $7^2 \times 5^3$ **h** $4^6 \times 9^3$



Problem-solving and reason	ling	9, 10	9–12
Example 14 Evaluating expressio	ns with index for	m	
Evaluate: a $7^2 - 6^2$ b 2 ×	$3^3 + 10^2 + 1^7$		
Solution	Explanat	tion	
a $7^2 - 6^2 = 7 \times 7 - 6 \times 6$	Write po	wers in factor form.	
= 49 - 36 = 13	Do multi	plication before subtractio	n.
b $2 \times 3^3 + 10^2 + 1^7$ = $2 \times 3 \times 3 \times 3 + 10 \times 10$	Write po	wers in expanded form.	
$+ 1 \times 1 \times 1 \times 1 \times 1 \times 1 \times 1$ $= 54 + 100 + 1$ $= 155$	Do multi	plication first, then additio	n.
Now you try			
Evaluate: a $2^3 + 3^2$ b $7^2 - 3^2$	$-9 + 1^6 \times 2^4$		
d $(9-5)^3$ e 2	$2 \times 5^2 - 7^2$ $2^4 \times 2^3$ $0^3 - 10^2$	c $8^2 - 2 \times 3^3$ f $2^7 - 1 \times 2 \times 3$ i $(1^{27} + 1^{23}) \times 2$	
10 Find the index number for each of the a $16 = 2$ b $16 = 4$ c $27 = 3$ c $100 = 10$ b $100 = 10$		4 d 64 =	2

Write one of the symbols <, = or > in the box to make the following statements true. **b** $8^3 \square 8^2$

a $2^6 \square 2^9$ $2^4 \Box 4^2$

С

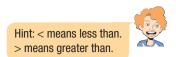
3E

- $6^4 \Box 5^3$ e
- $11^2 \square 2^7$ q

d $3^2 \Box 4^2$ $12^2 \square 3^4$

 2^{3}

18



12 Five friends receive the same text message at the same time. Each of the five friends then forwards it to five other friends and each of these people also sends it to five other friends. How many people does the text message reach?

The power of email

13 **13** A chain email is sent to 10 people. Five minutes later, each of them sends it to 10 other people. That is, after 10 minutes, 110 people (10 + 100)Hint: Assume that will have received the email. Five minutes later, each of them sends it on to ten other people, etc.

everyone uses email and everyone can read!

- **a** How many people will have received the email after:
 - i 15 minutes? ii 30 minutes?
- **b** If the email always goes to a new person, how long would it take until everyone in Australia has received the message? (Australia has approximately 24.5 million people.) Round up to the next 5 minute mark.
- c How long would it take until everyone in the world has received the message? (The world population is approximately 7 billion people.)



3F Prime factors

- To understand that composite numbers can be broken down into prime factors. •
- To be able to use a factor tree to find the prime factors of a number (including repeated factors).
- To be able to express a prime decomposition using powers of prime numbers.

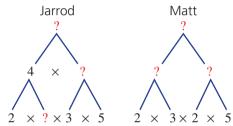
Key vocabulary: factor, composite number, prime factor, factor tree

Every composite number can be written as the product of prime number factors.

Factor trees help us to work out the prime number factors. When there are repeated factors, we write that product in index form.

Lesson starter: Factor trees

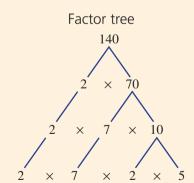
For homework, Jarrod and Matt each drew a factor tree. Then their little brother rubbed out some of the numbers.



- Can you find the missing numbers? Copy and complete each factor tree.
- What was the boys' homework question? •
- How is Jarrod's factor tree different from Matt's?
- What is the same about both factor trees?
- Can you draw a different factor tree that answers the homework question correctly? •

Key ideas

- Every composite number can be written as a product of its prime factors.
- We can use a factor tree or repeated division to find the prime factors of a composite number. It is a diagram showing the breakdown of a number into its prime factors.



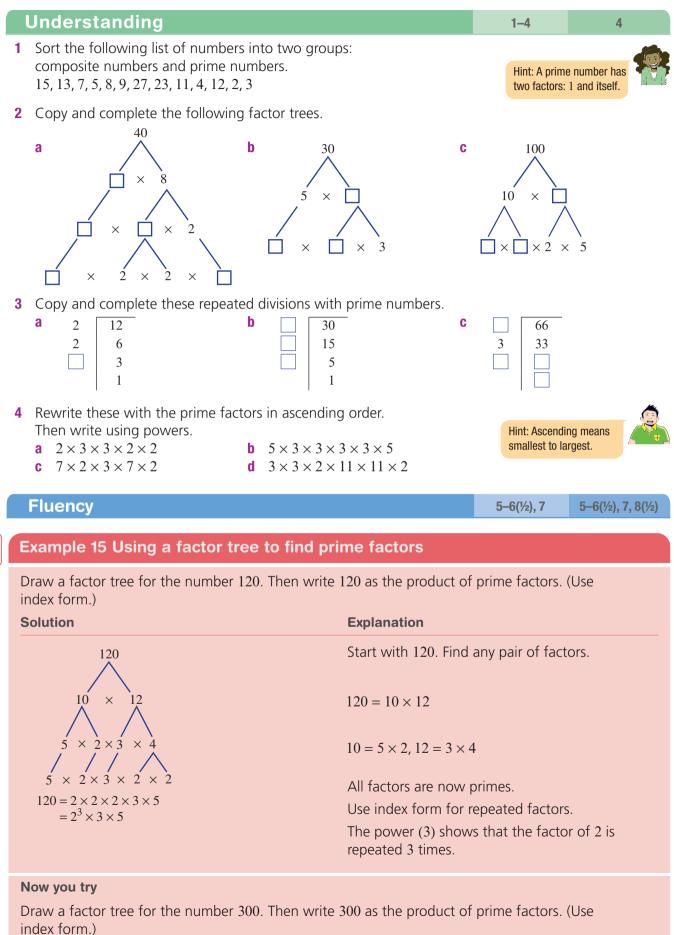
Repeated division with prime factors 2 140 70 2

2	/0
5	35
7	7
	1

It is helpful to write the prime factors in ascending (increasing) order, using powers. For example: $140 = 2 \times 2 \times 5 \times 7$

$$= 2^2 \times 5 \times 7$$

Exercise 3F



5	For each numb	er, draw a factor tre	e. Then write the nu	ımber as a	
	product of prim	ne factors, using po	wers.		Hint: Write prime factors in
	a 72	b 24	c 38	d 44	ascending order. Use powers
	e 124	f 80	g 96	h 16	for repeated factors.
	i 75	j 111	k 64	56	
6	For each numb using powers.	er, draw a factor tre	ee. Then write the nu	umber as a product	of prime factors,
	a 600	b 800	c 5000	d 2400	
	e 1 000 000	f 45000	g 820	h 690	

Example 16 Using repeated division to find prime factors

Use repeated division with prime numbers to find the prime factors of 126. Then write 126 as a product of prime factors with powers.

Solution	Explanation
2 126	$126 \div 2 = 63$
3 63	$63 \div 3 = 21$
3 21	$21 \div 3 = 7$
7 7 1	$7 \div 7 = 1$
$126 = 2 \times 3 \times 3 \times 7$ $= 2 \times 3^2 \times 7$	Write prime factors in ascending order. $3 \times 3 = 3^2$

Now you try

Use repeated division with prime numbers to find the prime factors of 495. Then write 495 as a product of prime factors with powers.

7 Use repeated division with prime numbers to find the prime factors of 96. Then write 96 as a product of prime factors with powers.

Hint: You could start by dividing 96 by 2.

9–12

9,10

8 Use repeated division with prime numbers to help you write each of these numbers as a product of prime factors with powers.

а	32	b	40	С	81	d	144
е	120	f	500	g	1800	h	1250

Problem-solving and reasoning

9 Match the correct composite number (a to d) to its set of prime factors (A to D). a 120 b 150 c 144 d 180 A $2 \times 3 \times 5^2$ B $2^2 \times 3^2 \times 5$ c $2^4 \times 3^2$ D $2 \times 3 \times 2 \times 5 \times 2$ Hint: Look for easy ways to multiply 10 $2 \times 3 \times 5 \times 5$ 15 3F

- 10 Draw four different factor trees that each show the prime factors of 24. (For two trees to be different, they must show different combinations of factors, not just the same factors in a different order.)
 - **11 a** Express 144 and 96 in prime factor form.
 - **b** Determine the HCF of 144 and 96. The prime factor form may help.
 - 12 Only one of the following is the correct set of prime factors for 424. **B** $2 \times 3^2 \times 5^2$
 - **A** $2^2 \times 3^2 \times 5$
 - **D** $2^3 \times 53$ **C** 53×8
 - **a** Explain why **A** and **B** are wrong.
 - **b** Why is option **C** wrong?
 - **c** Show that option **D** is the correct answer.

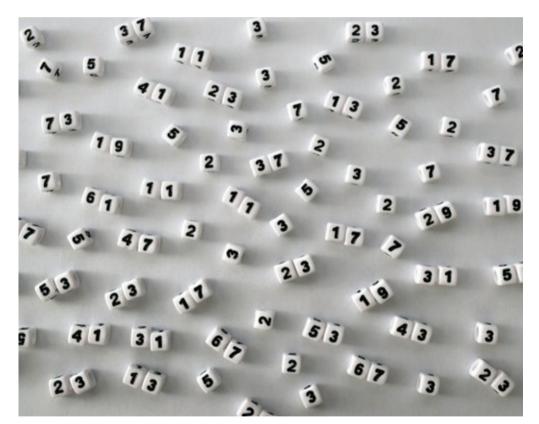
Four different prime factors



13

13 Only 16 composite numbers smaller than 1000 have four prime factors. For example: $546 = 2 \times 3 \times 7 \times 13.$

By considering the prime factor possibilities, see how many of the other 15 composite numbers you can find. Express each of them in prime factor form.



3G Squares and square roots

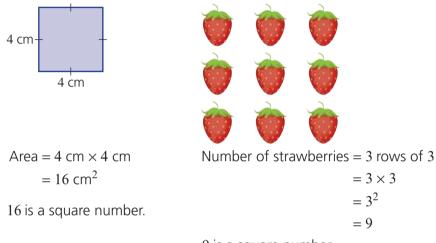
Learning intentions

- To understand that a square number can be thought of in terms of the area of a square, or the number of items in a square array.
- To be able to find the square of a number.
- To be able to find the square root of a perfect square.

Key vocabulary: square number, square root, perfect square

We can picture a square number as the area of a square or the number of objects in a square array.

For example:



9 is a square number.

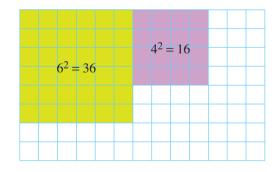
Finding a square root of a number is the opposite of squaring a number. We use the symbol $\sqrt{}$ to show the square root of a number.

The pictures above show that $\sqrt{16} = 4$ and $\sqrt{9} = 3$.

Lesson starter: Shading squares

You will need a sheet of 1-cm grid paper.

- Shade as many different-sized squares as you can fit onto the page.
- Write each area in index form. For example, $6^2 = 36$, $4^2 = 16$, etc.
- Finally, on each square write the side length as the square root of the area. For example, $6 = \sqrt{36}$, $4 = \sqrt{16}$, etc.



Key ideas

- If you multiply a whole number by itself, the result is a **square number**. For example: $5^2 = 5 \times 5 = 25$, so 25 is a square number.
 - Square numbers are also known as perfect squares.
 - The first 12 square numbers are:

Index form	12	22	32	4 ²	5 ²	62	72	82	9 ²	10 ²	11 ²	12 ²
Value	1	4	9	16	25	36	49	64	81	100	121	144

3G

- The square root of a given number multiplied by itself results in the given number.
 - The symbol for square root is $\sqrt{}$.
 - Finding a square root of a number is the opposite of squaring a number. For example: $4^2 = 16$, so $\sqrt{16} = 4$.

We read this as '4 squared equals 16, so, the squ	uare root of 16 equals 4'.
---	----------------------------

Square root form	$\sqrt{1}$	$\sqrt{4}$	$\sqrt{9}$	$\sqrt{16}$	$\sqrt{25}$	$\sqrt{36}$	$\sqrt{49}$	√64	$\sqrt{81}$	$\sqrt{100}$	√121	$\sqrt{144}$
Value	1	2	3	4	5	6	7	8	9	10	11	12

- Order of operations
 - Squares are powers, so evaluate first. For example: $2 \times 3^2 + 4 = 2 \times 9 + 4$
 - Square roots act like brackets. For example: $\sqrt{16+9} = \sqrt{25} = 5$

Exercise 3G

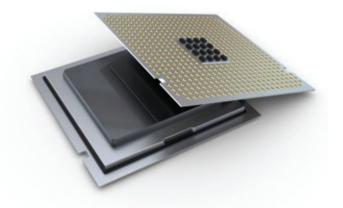
Understanding

- 1 State the missing word or number.
 - **a** $3^{-} = 9$
 - **b** The_____ of 9 equals 3.
 - $\sqrt{\Box} = 6$
 - **d** 9 _____ equals 81.
- 2 Copy and complete this table of square numbers.

Index form	12			4 ²	5 ²		72		92	
Value		4	9			36		64		100

3 Copy and complete this table of square roots.

Square root form	$\sqrt{1}$	$\sqrt{4}$		$\sqrt{16}$		$\sqrt{36}$			$\sqrt{81}$	
Value			3		5		7	8		10



Essential Mathematics for the Victorian Curriculum ISI CORE Year 7 Ph



3

1–3

Fluency			4, 5, 6–8	(1/2) 4, 5, 6–8(1/2)
Example 17 Fir	nding squares and	l square roots		
Write the value of a 4 ² e Square root of Solution		of square with are	d 5 to the power c a 64 cm ² nation	of 2
a $4^2 = 16$		$4^2 = 4$	↓×4	
b 7 squared = 49		7 squ	ared is the same as 7 ²	
c $(3)^2 = 9$		$(3)^2 =$	$3 \times 3 = 9$	
d 5 to the power	of 2 = 25		the power of 2 is the same $2^2 = 5 \times 5 = 25$	e as 5 ² ,
e square root of	36 = 6	$\sqrt{36} =$	6 because $6 \times 6 = 36$	
f side length = 8	cm	side le	ength = $\sqrt{64}$ and $8 \times 8 =$	64
			d 8 to the power of a 4 m ²	of 2
4 Evaluate:	_			
 a 6² d 10 to the po 		5 squared 7 ²	c $(11)^2$ f 12×12	
5 Evaluate: a $\sqrt{25}$ d the side length	b gth of a square that ha	square root of 16 as an area of 49 cm	$c \sqrt{100}$	
6 Find the value of a 8 ²	of: b 7^2 f 15^2	c 1 ² g 5 ²	d 12^2 h 0^2	Hint: $8^2 = 8 \times 8 = 64$
e 3 ² i 11 ²	j 100 ²	k 30 ²	40^2	



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3G

Exam	ala 10	Eve	luctica	00	ULO KO	root	
	ие ю	EVal					-
							-

Find the value of: a $\sqrt{64}$ Solution a $\sqrt{64} = 8$ b $\sqrt{1600} = 40$			on ecause 8 × 8 =) because 40 ×	
Now you try Find the value of: a $\sqrt{36}$		b √4900		
7 Find the value of: a $\sqrt{25}$ e $\sqrt{0}$ i $\sqrt{4}$ m $\sqrt{2500}$	b $\sqrt{9}$ f $\sqrt{81}$ j $\sqrt{144}$ n $\sqrt{6400}$	c $\sqrt{1}$ g $\sqrt{49}$ k $\sqrt{400}$ o $\sqrt{8100}$	d $\sqrt{121}$ h $\sqrt{16}$ l $\sqrt{169}$ p $\sqrt{729}$	Hint: For $\sqrt{25}$, think: \times = 25

Example 19 Evaluating expressions involving squares and square roots

Evaluate: a $\sqrt{64} + \sqrt{36}$ Solution	b $\sqrt{8^2 + 6^2}$	c $3^2 - \sqrt{9} + 1^2$ Explanation
a $\sqrt{64} + \sqrt{36} = 8 + 6$ = 14		Find square roots first. Then add.
b $\sqrt{8^2 + 6^2} = \sqrt{64 + 36}$ = $\sqrt{100}$ = 10		The square root sign is like a bracket: $\sqrt{(8^2 + 6^2)} = \sqrt{(8 \times 8 + 6 \times 6)}$ Multiply and add to give: $\sqrt{64 + 36} = \sqrt{100}$
c $3^2 - \sqrt{9} + 1^2 = 9 - 3 + 1$ = 7		Evaluate squares and square roots first. $3^2 = 3 \times 3, \sqrt{9} = 3, 1^2 = 1 \times 1$
Now you try Evaluate: a $\sqrt{100} - \sqrt{9}$	b $\sqrt{5^2 - 4^2}$	c $5^2 - \sqrt{64} - 2^2$

10-12

13, 14

8	Evaluate:			Hint: Remember the order of
	a $\sqrt{9} + \sqrt{16}$	b $\sqrt{3^2 + 4^2}$	c $\sqrt{9} \times \sqrt{16}$	operations.
	d $3^2 + 5^2 - \sqrt{16}$	e 4×4^2	f $8^2 - 0^2 + 1^2$	
	g $1^2 \times 2^2 \times 3^2$	h $\sqrt{5^2 - 3^2}$	i $\sqrt{81} - 3^2$	
	j $6^2 \div 2^2 \times 3^2$	$\mathbf{k} \sqrt{9} \times \sqrt{64} \div \sqrt{36}$	$\sqrt{12^2+5^2}$	

Problem-solving and reasoning	9, 10
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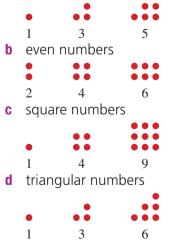
9 This arrangement of dots shows that 9 is a square number.

•	•	•	
•	٠	٠	
•	•	•	

- a Show, using dots, that 6 is not a square number.
- **b** Show, using dots, that 16 is a square number.
- **10** List all the square numbers between 50 and 101.
- 11 List all the square numbers between 101 and 200. Hint: There are only four.
- **12** a Show that $3^2 + 4^2 = 5^2$.
 - **b** Does $5^2 + 6^2 = 7^2$?
 - **c** Does $6^2 + 8^2 = 10^2$?
 - d Find some other true sums of square numbers like the one in part a.

Number dot patterns

- **13** For each of the following:
 - i Copy the dot pattern and draw the next three terms.
 - ii How many dots are added each time?
 - iii What patterns did you notice?
 - a odd numbers



14 Can you see a connection between triangular numbers and square numbers?

3A	1	Find the complete set of factors for each of these numbers. a 20 b 36
3A	2	Write down the first five multiples of each of these numbers. a 12 b 21
38	3	 Find the highest common factor (HCF) of the following numbers. a 24 and 40 b 35 and 70 c 18 and 42
38	4	 Find the lowest common multiple (LCM) of the following numbers. a 8 and 12 b 11 and 7 c 3, 5 and 10
30	5	Which of the numbers 75, 14, 141, 52, 88, 1234 are divisible by: a 2? b 3? c 4? d 5?
30	6	 Work out whether the following calculations are possible without leaving a remainder. a 32 689 ÷ 3 b 456 336 ÷ 8
3D	7	Which of these numbers are prime (P) and which are composite (C)? 15, 23, 31, 39, 51, 80, 91
3D	8	Find the prime numbers that are factors of: a 24 b 72
3E	9	Simplify these products by writing them in index form. a $4 \times 4 \times 4 \times 4 \times 4$ b $6 \times 5 \times 5 \times 6 \times 5 \times 5 \times 6$
3E	1() Write each of the following in expanded form and find the value. a 3^4 b $2^3 \times 5^2$ c $6^2 - 2^3$
3F	1	 Write the following numbers as a product of their prime factors, using powers. a 40 b 108 c 128
3G	12	2 Find the value of: a 13^2 b 30^2 c $\sqrt{49}$ d $\sqrt{2500}$ e $\sqrt{36} \times \sqrt{9}$ f $\sqrt{10^2 - 8^2}$

3H Number patterns

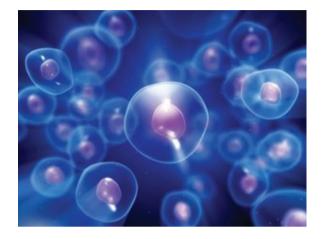
CONSOLIDATING

- To understand what a number pattern (or number sequence) is.
- To be able to describe a pattern where numbers are increasing or decreasing by a fixed amount.
- To be able to describe a pattern where numbers are multiplied or divided by a fixed amount.

Key vocabulary: pattern, sequence, term, rule, increasing, decreasing

Number patterns can be found in all sorts of natural and artificial situations. For example, if bacteria cells divide in two every hour, then the number of bacteria follows the pattern 1, 2, 4, 8, 16, 32, 64, 128, and so on. A scientist could use this pattern to predict the number of bacteria after a certain time.

It is helpful to find the rule that describes a number pattern. Entering rules into a spreadsheet makes it easy to perform calculations with large numbers. Scientists, accountants and many other people use number patterns and rules to help them analyse data and make predictions.



Lesson starter: Which rule is which?

Work with a partner to match each of these number patterns to the correct rule. Discuss the thinking vou used.

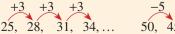
Number pattern

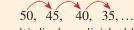
- Rule
- **A** 7, 12, 17, 22, 27, ...
- **P** Start with 96 and keep dividing by 2.

- A 7, 12, 17, 22, 27, ...
 P Start with 96 and keep dividing by 2.
 B 96, 48, 24, 12, 6, ...
 Q Start with 7, add 5, add 6, add 7, etc.
 C 96, 92, 88, 84, ...
 D 7, 12, 18, 25, 33, 42, ...
 P Start with 96, add 4, take 10, etc.
- **E** 96, 100, 90, 94, 84, 88, 78, ... **T** Start with 96 and keep subtracting 4.
- Make up some number patterns of your own. Then swap patterns with another group. See if you can work out each other's rules

Key ideas

- A list of numbers arranged in order according to some rule is called a number pattern or a **sequence**.
- Each separate number in the sequence is called a **term**.
- To find the terms of a sequence, follow the pattern rule. For example: the rule 'start with 3 and add 2 to each term' gives 3, 5, 7, 9, 11, ...
- To find the pattern rule for a sequence, ask:
 - Is the sequence increasing or decreasing by a fixed amount?

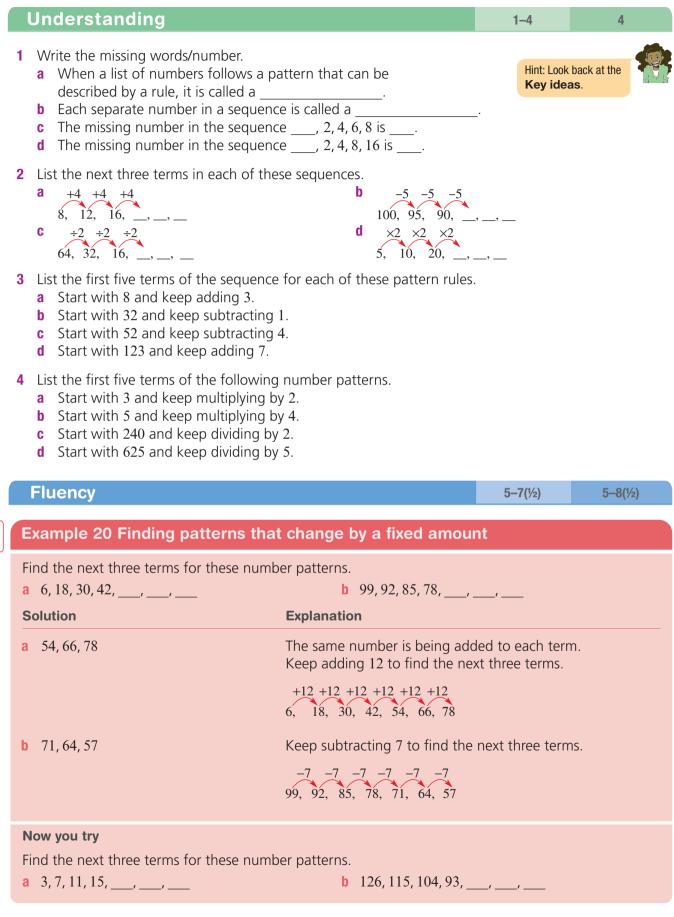




Is each term being multiplied or divided by the same amount?

 $\begin{array}{c} x^3 \ x^3 \$

Exercise 3H



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- **5** Find the next three terms for these sequences.
 - **a** 3, 8, 13, 18, ___, ___, ___
 - **c** 26, 23, 20, 17, ___, ___,
 - e 63, 54, 45, 36, ___, ___,
 - **g** 101, 202, 303, 404, ___, ___, ___
- b
 4, 14, 24, 34, ___, ___, ___

 d
 106, 108, 110, 112, ___, ___, ___

 f
 9, 8, 7, 6, ___, ___, ____

 h
 75, 69, 63, 57, ___, ___, ____

SolutionExplanationa 162, 486, 1458Each term is being multiplied by the same nur Keep multiplying by 3 to find the next three term	
×3 ×3 ×3 ×3 ×3 ×3 2, 6, 18, 54, 162, 486, 1458	
b 16, 8, 4 Keep dividing by 2 to find the next three term	ns.
$\dot{+2}$ $+2$	
Now you try Find the next three terms for the following number patterns.	
Now you try	
 Now you try Find the next three terms for the following number patterns. a 5, 20, 80, 320,,, b 729, 243, 81, 27,,, Find the next three terms for the following number patterns. 	Hint: Is each tei
Now you try Find the next three terms for the following number patterns. a 5, 20, 80, 320,,, b 729, 243, 81, 27,,, 6 Find the next three terms for the following number patterns. a 2, 4, 8, 16,,, b 5, 10, 20, 40,,	being multiplied
Now you try Find the next three terms for the following number patterns. a 5, 20, 80, 320,,, b 729, 243, 81, 27,,, 6 Find the next three terms for the following number patterns. a 2, 4, 8, 16,,, b 5, 10, 20, 40,,, c 96, 48, 24,,, e 11, 22, 44, 88,,,	being multiplied divided by the same number?
Now you try Find the next three terms for the following number patterns. a 5, 20, 80, 320,,, b 729, 243, 81, 27,,, 6 Find the next three terms for the following number patterns. a 2, 4, 8, 16,,, b 5, 10, 20, 40,,, c 96, 48, 24,,,	being multiplied divided by the same number?
Now you try Find the next three terms for the following number patterns. a 5, 20, 80, 320,,, b 729, 243, 81, 27,,, 6 Find the next three terms for the following number patterns. a 2, 4, 8, 16,,, b 5, 10, 20, 40,,, c 96, 48, 24,,, e 11, 22, 44, 88,,	being multiplied divided by the same number?

3H

Example 22 Describing patterns in wor	rds
For each of these sequences, write the pattern r a 2, 10, 50, 250, c 32, 16, 8, 4,	ule in words. b 6, 10, 14, 18, d 32, 28, 24, 20,
Solution	Explanation
a Start with 2 and multiply each term by 5.	×5 ×5 ×5 2, 10, 50, 250,
b Start with 6 and add 4 to each term.	$\begin{array}{c} +4 & +4 & +4 \\ 6, & 10, & 14, & 18, \dots \end{array}$
c Start with 32 and divide each term by 2.	÷2 ÷2 ÷2 32, 16, 8, 4,
d Start with 32 and subtract 4 from each term.	-4 -4 -4 32, 28, 24, 20,
Now you try	
For each of these sequences, write the pattern r	ule in words.
a 3, 12, 48, 192,	b 11, 14, 17, 20,
c 625, 125, 25,	d 123, 114, 105, 96,

8 Use words to write the pattern rule for each sequence.

а	19, 17, 15, 13,	b	48, 24, 12, 6,
C	50, 56, 62, 68,	d	1, 3, 9,
е	10 000, 1000, 100, 10,	f	75, 72, 69, 66,

Pr	oblem-solving and reasoning	9, 10	9–12
a b	'rite the next three terms in each of the following sequences. 3, 5, 8, 12,,, 1, 2, 4, 7, 11,,,	Hint: Look a each term i decreases.	
d	 10, 8, 11, 9, 12,,, 25, 35, 30, 40, 35,,, frog has fallen to the bottom of a well that is 6 metres deep. On the first day the frog climbs 3 metres up the wall of the well. 	Hint: Draw a the well. Use show the m the frog.	e arrows to
	On the second day it slides back 2 metres.On the third day it climbs up 3 metres.		

On the fourth day it slides back 2 metres.

The frog continues following this pattern until it reaches the top of the well and hops away.

- **a** Write a sequence of numbers to show the frog's height above the bottom of the well at the end of each day.
- **b** How many days does it take the frog to get out of the well?



- 11 For each of the following sequences, describe the pattern rule.
 - **a** 4, 12, 36, 108, 324, ...
 - **c** 212, 223, 234, 245, 256, ...
 - **e** 64, 32, 16, 8, 4, ...
 - **g** 2, 3, 5, 7, 11, ...

- **b** 19, 17, 15, 13, 11, ... **d** 8, 10, 13, 17, 22, ...
- **f** 5, 15, 5, 15, 5, ...
- **h** 75, 72, 69, 66, 63, ...
- **12** Copy and complete each of the following. Give the special name for each type of numbers.
 - **a** 1, 4, 9, 16, 25, 36, ___, ___,
 - **b** 1, 1, 2, 3, 5, 8, 13, <u>,</u>, <u>,</u>, <u>,</u>
 - **c** 1, 8, 27, 64, 125, ____, ____,
 - **d** 2, 3, 5, 7, 11, 13, <u>17</u>, <u>,</u> , <u>,</u>
 - **e** 4, 6, 8, 9, 10, 12, 14, 15, ____, ___,
 - f 121, 131, 141, 151, ___, ___,

Human pyramids

13 When making a human pyramid, each row has one less person than the row below. The pyramid is complete when there is a row of only one person on the top.

Write down a number pattern for a human pyramid with 10 students on the bottom row. How many people are needed to make this pyramid?



Hint:

Choose from: composite numbers, cube numbers, even numbers, Fibonacci numbers, negative numbers, odd numbers, palindromes, prime numbers, square numbers, triangular numbers

13

Hint: Draw a diagram



Essential Mathematics for the Victorian Curriculum CORE Year 7

3I Patterns with shapes and numbers

Learning intentions

- To understand that spatial patterns are related to number patterns.
- To know that a spatial pattern starts with a starting design and has a repeating design.
- To be able to continue a spatial pattern given the first few shapes.
- To be able to describe and use a rule relating the number of shapes and the number of objects required to make them.

Key vocabulary: spatial pattern, geometrical shapes, pattern rule, number sequence, table of values

Repeated geometric shapes form interesting spatial patterns. Architects often use spatial patterns in the design of buildings. Artists also use repeated geometric shapes in designs to be printed on curtains, tiles and wallpaper.

Lesson starter: Stick patterns

Copy these shapes using matchsticks or toothpicks. Then build the next three shapes in the pattern.





How many sticks would you need to make the shape with:

- 10 triangles?
- 100 triangles?

If you know the number of triangles, how could you find the number of sticks? Discuss this with a partner and then write your answer.

Use similar steps to explore the number of squares in the following pattern.



Key ideas

• A **spatial pattern** is a sequence of **geometrical shapes**. For example:



- The number of 'diamonds' in each term makes a **number sequence**.
- The number of sticks in each term makes another number sequence.
- A table of values shows the number of shapes and the number of sticks.

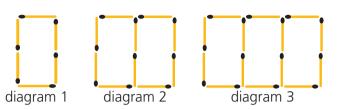
Number of shapes	1	2	3	4	5
Number of sticks	4	8	12	16	20

A pattern rule tells how many sticks are needed for a certain number of shapes. For example: number of sticks = 4 × number of shapes

3I Patterns with shapes and numbers

Exercise 31 Understanding

1 Jack used matchsticks to begin a pattern of rectangles.



Write the missing words or numbers for each of these.

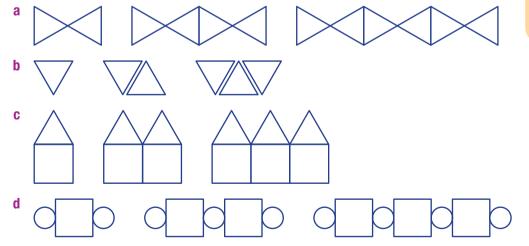
- a The shape of the first diagram is called a ____
- **b** Diagram 1 has _____ rectangle, diagram 2 has _____ rectangles and diagram 3 has _____ rectangles.
- **c** Diagram 1 has _____ sticks, diagram 2 has _____ sticks and diagram 3 has _____ sticks.
- **d** These diagrams follow a sequence that is called a _____ pattern.
- 2 Jane used matchsticks to make a spatial pattern of houses.

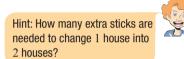


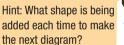
Copy and complete this table.

Number of houses	1	2	
Number of sticks			

3 Draw the next two terms for each of these spatial patterns.





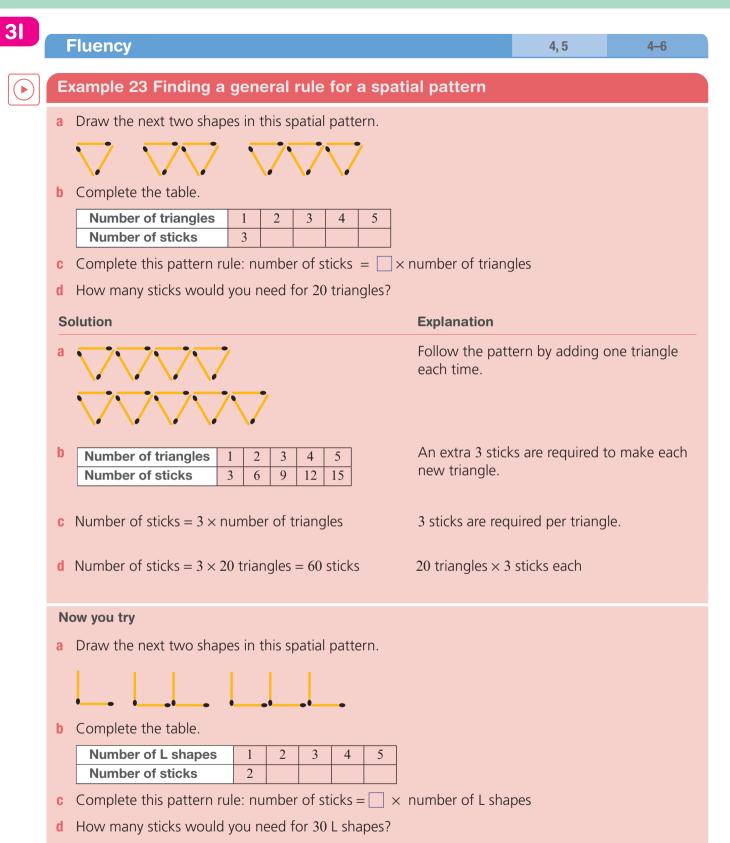




133

3

1–3



4 a Draw the next two shapes for this spatial pattern.



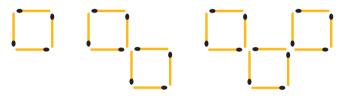
b Copy and complete this table.

Number of crosses	1	2	3	4	5
Number of sticks					

Hint: For part **c**, check that your pattern rule works for all values in the table.



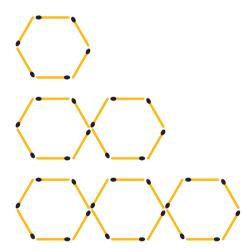
- **c** Copy and complete this pattern rule: number of sticks = $\square \times$ number of crosses.
- **d** How many sticks would you need for 10 crosses?
- **5 a** Draw the next two shapes for this spatial pattern.



b Copy and complete this table.

Number of squares	1	2	3	4	5
Number of sticks					

- **c** Copy and complete the pattern rule: number of sticks = $\square \times$ number of squares
- d How many sticks would you need for 12 squares?
- 6 a Draw the next two shapes for this spatial pattern.



b Copy and complete this table.

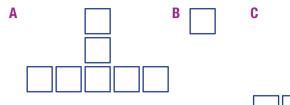
Number of hexagons	1	2	3	4	5
Number of sticks					

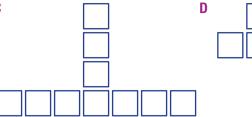
- **c** Copy and complete the pattern rule: number of sticks = $\square \times$ number of hexagons
- d How many sticks would you need for 20 hexagons?

Hint: How many extra sticks would you need to add another hexagon?

Problem-solving and reasoning

7 List the shapes (A to D) in the correct order to make a spatial pattern. (Start with the smallest shape.) Then draw the next shape in the sequence.





31

Example 24 Finding more-challenging rules

a Draw the next two shapes for this spatial pattern.



b Copy and complete the table.

Number of squares	0	1	2	3	4
Number of sticks	1	1 + 🗌 × 1 = 🗌	1 + 🗌 × 2 = 🗌	$1 + \square \times 3 = \square$	1 + 🗌 × 4 = 🗌

- **c** Copy and complete the rule for the pattern: number of sticks = $1 + 1 \times 10^{10} \times 10^{10}$ complete the rule for the pattern:
- d How many sticks are needed to make 30 squares this way?
- e How many squares could be made from 25 sticks?

Solution



b	Number of squares	0	1	2	3	4
	Number of sticks	1	$1 + 3 \times 1 = 4$	$1 + 3 \times 2 = 7$	$1 + 3 \times 3 = 10$	$1 + 3 \times 4 = 13$

- **c** Number of sticks = $1 + 3 \times$ number of squares
- d 91 sticks
- e 8 squares

Explanation

Add 3 sticks at a time to complete each new square.

9–12

7-9

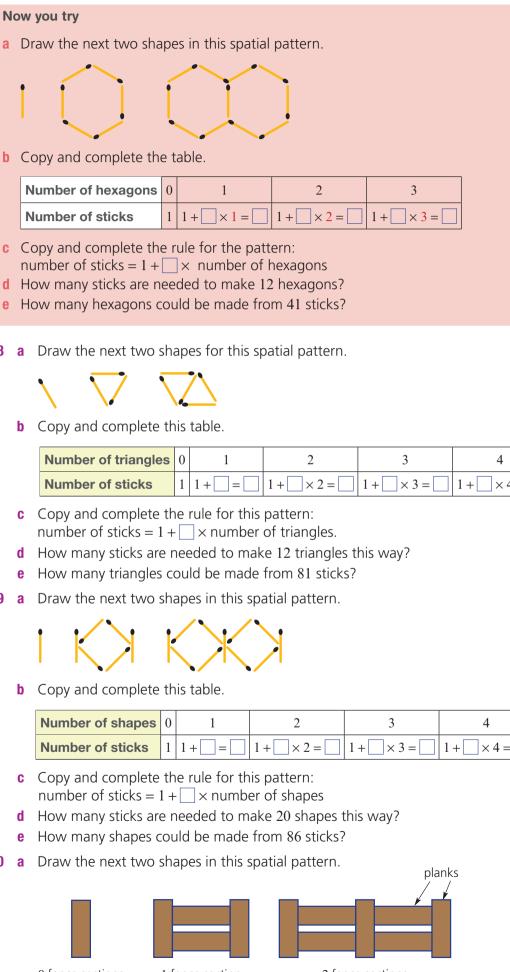
Count the squares. Complete the calculations, then count sticks in the diagrams to check.

The number of sticks is 1 more than 3 times the number of squares.

$$1 + 3 \times 30 = 91$$

$$25 - 1 = 24$$
,

 $24 \div 3 = 8$



0 fence sections 1 fence section Essential Mathematics for the Victorian Curriculum ISBN 978-1-108-87846-3 CORE Year 7

8

е

b

9

10

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Hint: How many extra sticks are needed to make 1 stick into a triangle?

4

 $\times 4 =$



Hint: Copy the last shape and add more sticks to make the next shape.



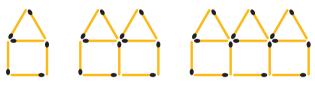
b Copy and complete this table.

Number of fence sections	0	1	2	3	4
Number of planks	1	1+	$1 + \square \times 2 = \square$	$1 + \square \times 3 = \square$	1 + 🗌 × 4 = 🗌

- **c** Copy and complete the pattern rule: number of planks = $1 + \square \times$ number of fence sections.
- d How many planks would you need to make 9 fence sections?
- e How many fence sections can be made from 43 planks?
- 11 Which rule correctly describes this spatial pattern?



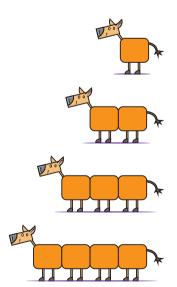
- A Number of sticks = $7 \times$ number of 'hats'
- **B** Number of sticks = $7 \times \text{number of 'hats'} + 1$
- **C** Number of sticks = $6 \times$ number of 'hats' + 2
- **D** Number of sticks = $6 \times$ number of 'hats'
- 12 Which rule correctly describes this spatial pattern?



- A Number of sticks = $5 \times$ number of houses + 1
- **B** Number of sticks = $6 \times$ number of houses + 1
- **C** Number of sticks = $6 \times$ number of houses
- **D** Number of sticks = $5 \times$ number of houses

Design your own spatial pattern

- **13** Design a spatial pattern to fit the following number patterns.
 - **a** 4, 7, 10, 13, ...
 - **b** 4, 8, 12, 16, ...
 - **c** 3, 5, 7, 9, ...
 - **d** 3, 6, 9, 12, ...
 - **e** 5, 8, 11, 14, ...
 - **f** 6, 11, 16, 21, ...



13

31

3J Tables and rules

Learning intentions

- To understand that a rule connects two varying quantities.
- To be able to complete an input-output table given a rule.
- To be able to find a rule in the form input = $? \times \text{output} + ?$ for an input-output table.

Key vocabulary: input, output, table of values, rule, substitute

In the last section, we investigated rules for spatial patterns. Rules are also useful for many other everyday situations.

It can be helpful to think of a rule as a 'machine'. You feed in one number (the input), and another number (the output) comes out. For example, Mary was 3 years old when her brother Tim was born. If you know Tim's age (the input), what is a rule for finding Mary's age (the output)?

Showing some values in a table makes it easy to 'see' the rule.

Tim's age (input)	0	1	7	3	
Mary's age (output)	3	4	10	6	+3

Rule: Mary's age = Tim's age + 3 *output* = *input* + 3

Lesson starter: What's the story?

Each of the following stories tells how an input and output are related.

Story	input	output
1 Connor is 5 years younger than his brother Declan.	Declan's age	Connor's age
2 Liam earns \$5 for every car he washes.	number of cars washed	amount (\$) earned
3 Jayce and 4 friends share some lollies equally.	total number of lollies	number of lollies each person gets

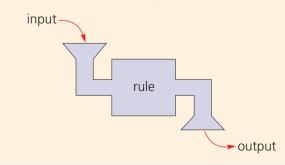
• Which story matches the following table of input and output values? How did you decide?

input	2	1	7	3	6	?
output	10	5	35	15	?	50

- How would you find the missing values?
- Pick one of the other stories and make up your own table of values.

Key ideas

A rule shows the relationship between two amounts that can vary. It is used to calculate the **output** (answer) from the **input** (starting number).



3J

- A table of values shows inputs and outputs. To make a table of values:
 - choose some input values
 - use the rule to calculate the output values.
- To find the rule from a table of values, try different operations (+, -, ×, ÷) until you find a rule that works for *all* the values. For example:

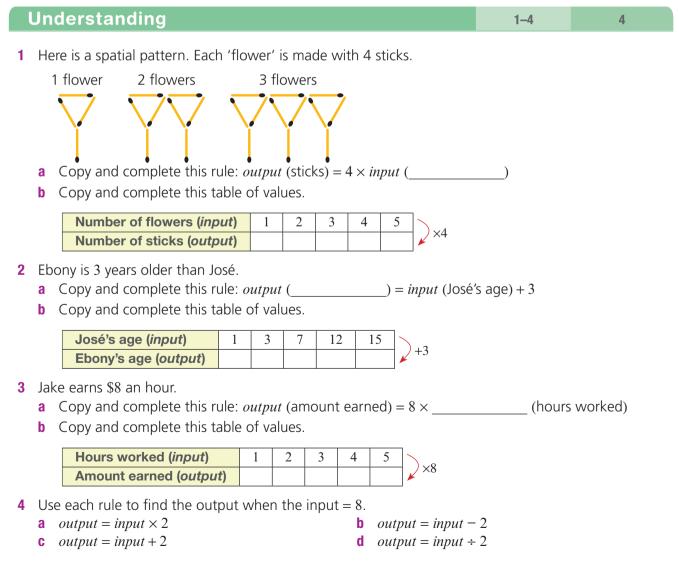
input	output
5	15
8	24
12	36

To get the outputs in the table above, has the same number been:

- added to each input? (no)
- subtracted from each input? (no)
- multiplied by each input? (yes)

The rule is: $output = 3 \times input$

Exercise 3J



Fluency 5.6 5-7 Example 25 Completing a table of values Complete each table for the given rule. a output = input - 2**b** $output = (3 \times input) + 1$ input 3 5 7 12 20 input 4 2 9 12 0 output output **Solution Explanation** Put each *input* value, in turn, into the rule. a output = input - 2When *input* is 3: input 3 5 7 12 20 e.g. 1 3 5 10 18 output output = 3 - 2 = 1Put each *input* value, in turn, into the rule. **b** $output = (3 \times input) + 1$ input 4 2 9 12 e.g. When *input* is 4: 0 13 7 28 37 1 output $output = (3 \times 4) + 1 = 13$ Now you try Complete each table for the given rule. a output = input + 5**b** $output = (input \div 3) + 1$ input 0 5 10 12 input 9 3 21 90 33 1 output output **5** Copy and complete each table for the given rule. Hint: Substitute each input number into the rule. **b** $output = input \times 2$ a output = input + 3input 4 5 6 7 10 input 5 1 3 21 0 output output

- **c** output = input 8input 11 18 9 44 100 output
- 6 Copy and complete each table for the given rule.
 - a $output = (10 \times input) 3$

-		-	·		
input	1	2	3	4	5
output					
output -	$(3 \times i)$	unut)	<u>⊥ 1</u>		

C	$output = (3 \times input) + 1$							
	input	5	12	2	9	0		
	output							

d $output = input \div 5$

input	5	15	55	0	100
output					

Hint: Remember to calculate brackets first.

b $output = (input \div 2) + 4$

input	6	8	10	12	14
output					

 $output = (2 \times input) - 4$ d

input	3	10	11	7	50
output					

3J		
	Example 26 Finding a rule from a table	of values
	Find the rule for each of these tables of values.	
	a input 3 4 5 6 7 output 12 13 14 15 16	b input 1 2 3 4 5 output 7 14 21 28 35
	Solution	Explanation
	a $output = input + 9$	Each <i>output</i> value is 9 more than the <i>input</i> value.
	b $output = input \times 7$ or $output = 7 \times input$	By inspection, it can be observed that each <i>output</i> value is 7 times bigger than the <i>input</i> value.
	Now you try	
	Find the rule for each of these tables of values.	
	a input 2 3 4 5 6	b input 1 2 3 4 5
	<i>output</i> 0 1 2 3 4	output 6 12 18 24 30
	7 State the rule for each of these tables of values	5. Hint: The same rule must work for each input/
	a input 4 5 6 7 8 b inpu	t 1 2 3 4 5 output pair in a table.
	output 5 6 7 8 9 output b input 10 8 3 1 14 d input	
	D input 10 8 3 1 14 0 input output 21 19 14 12 25 output	
	Problem-solving and reasoning	8–10 9 –12
	8 Copy and complete the missing values in the ta	5 11 2
	output 4 10 15 24 output 39 42 9	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
		of values (a to d). ut = input + 1 ut = 5 + input Hint: The rule must be true for each input number in the table.
	a <i>input</i> 20 14 6	b <i>input</i> 8 10 12
	output 15 9 1	output 13 15 17
	output 15 9 1 c input 4 5 6	output 13 15 17 d input 4 3 2
	output 15 9 1 input 4 5 6 output 5 6 7	output 13 15 17

a Copy and complete this table for Zac's birthday account:

Zac's age in years (input)	0	1	2	3
Amount (\$) in account (output)				

b Copy and complete this rule for Zac's birthday account:

output = × input +

- c How much will be in the account when Zac turns 18?
- 11 Cindy has \$64 saved so far for the school ski trip. She has just started working at the local vets, helping to clean out pens and feed the animals. Cindy gets paid \$8 an hour and saves all her wages towards the ski trip.
 - a Copy and complete this table for Cindy's savings:

Hours worked (input)	0	2	5	10
Cindy's total savings (output)				

- **b** Copy and complete this rule for Cindy's savings: $output = \square \times input + \square$
- c Cindy wants to save \$200 to pay for the ski trip. How many hours will she need to work?
- 12 Complete these two different rules so that they each give an output of 7 when the input is 3.
 - a $output = \square \times input + \square$
 - **b** $output = \square \times input \square$

Finding harder rules

- 13 The following rules all involve two operations. Find the rule for each of these tables of values.
 - a $output = \square \times input$ input 4 5 6 7 8 5 7 9 output 11 13 **c** $output = \times input$ input 10 8 3 1 14
 - e output = × input + input 4 5 6 7 8 output 43 53 63 73 83

4

69

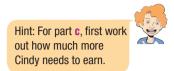
output 49 39 14

- **b** $output = \bigcirc \times input + \bigcirc$ input 1 2 3 4 5 output 5 9 13 17 21 **d** $output = input \div$ + 6 18 30 24 66 input 3 5 7 output 6 13 f output = × input – input 2 5 1 3 4 output 0 4 8 12 16
- 14 Use a spreadsheet to make each of the tables in Question 13. Each time, enter a formula so that the computer calculates all the output values. Here is an example of the formulas for **a** above. Try extending your tables by using other input numbers.

1	A	В
1	13a	
2	input	output
3	4	=2*A3-3
4	5	=2*A4-3
5	6	=2*A5-3
6	7	=2*A6-3
7	8	=2*A7-3
8		

Hint:

- When entering formulas:
- always start with =
- use * for \times
- instead of typing 'A3' just click on cell A3
- to copy the formula into other cells, fill down by dragging.



13, 14

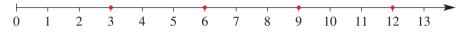
3K The number plane and graphs

Learning intentions

- To be able to interpret the location of a point described by its coordinates, e.g. (2, 4).
- To be able to plot one or more points given their coordinates.
- To be able to draw a graph of a rule using a table.

Key vocabulary: number plane (or Cartesian plane), x-axis, y-axis, origin, plot, coordinates, input, output

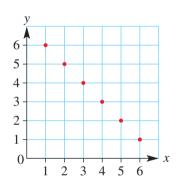
In earlier sections we looked at number sequences and spatial patterns. We used rules and tables of values to describe them. Another way of showing a pattern is by plotting points. For example, we could use a number line to show the simple pattern 3, 6, 9, 12, ...



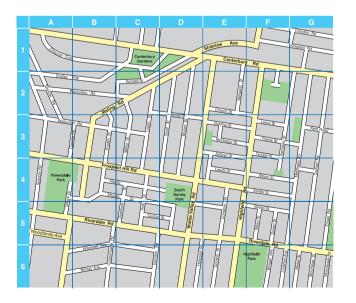
However, when we work with two sets of values (inputs and outputs) we need two dimensions. Instead of a number line, we use a number plane.

Lesson starter: Locating points

This grid shows a pattern of points on a number plane.

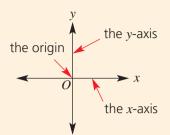


- Describe the behaviour of the *y* values as the *x* values increase.
- By continuing the pattern, what would be the y value for x = 7 or x = 0?
- How would you write a rule linking *y* (the output) with *x* (the input)?
- How is the number plane like a street map? How is it different?

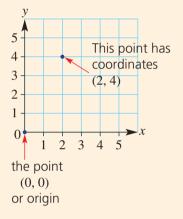


Key ideas

- A **number plane** is a grid for **plotting** points. Important features of a number plane are:
 - The *x*-axis and *y*-axis: these are horizontal and vertical number lines.
 - The **origin**: where the *x*-axis and *y*-axis meet at (0, 0).



- Points are located by a grid-reference system of **coordinates**.
 - The point (*x*, *y*) means (*x* units across from the origin, *y* units up).
 - For (2, 4) the *x*-coordinate is 2 and the *y*-coordinate is 4. To plot this point, start at the origin and go 2 units across, then 4 units up.
- For a rule describing a pattern with **input** and **output**, the *x*-value is the *input* and the *y*-value is the *output*.



Exercise 3K

Understanding	1–2	2	
 1 Copy and complete the following sentences. a The horizontal axis is known as the b The is the vertical axis. c The point at which the axes intersect is called the d The <i>x</i>-coordinate is always written e The second coordinate is always the f The letter comes before in the dictionary, and thecoordinate on the number plane. 	rdinate come:	Hint: Look at the Key ideas .	
2 Match each point on the grid with its correct coordinates. $ \begin{array}{c} y \\ 6 \\ 5 \\ 6 \\ 7 \\ 6 \\ 7 \\ 7 \\ 7 \\ 7 \\ 7 \\ 7 \\ 7 \\ 7 \\ 7 \\ 7$		Hint: Start at 0 and then nove across and up.	

Fluency

3K

Example 27 Plotting points on a number plane

Draw a number plane and plot these points on it. A(2, 5) = B(4, 3) = C(0, 2)

Solution y 5 4 4 3 2 C 1 0 1 2 3 4 5 x

Explanation

Draw a number plane with both axes labelled from 0 to 5. The numbers go on the grid lines, not in the spaces.

Label the horizontal axis x and the vertical axis y.

(2, 5) means go across 2 from 0 (along the *x*-axis) and then go up 5 units. Plot the point and label it *A*.

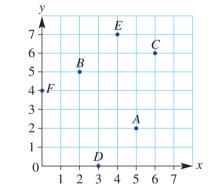
B(4, 3) means (4 across, 3 up).

C(0, 2) means (0 across, 2 up) so C is on the y-axis.

Now you try

Draw a number plane and plot these points on it. A(1, 4) = B(5, 0) = C(3, 3)

- 3 Copy and complete the coordinates for each point shown on this number plane.
 - **a** A(5,?) **b** B(?,5)
 - **C** C(?, ?)
 - **d** D(3, ?)
 - **e** E(?,?)
 - **f** F(?, 4)



4 On grid paper, draw a number plane, with the numbers 0 to 6 marked on each axis. Plot and label these points:

A(3,5) B(4,2) C(0,3) D(1,0) E(6,6)

- **5** Use grid paper to draw a number plane with the *x* and *y*-axis numbered from 0 to 10. Plot each group of points and join them in order, using a ruler.
 - **a** (4, 10), (2, 8), (5, 9)
 - **b** (2, 6), (4, 6), (4, 3)
 - **c** (6, 8), (8, 8), (8, 5), (6, 5), (6, 8)
 - **d** (5, 1), (6, 4), (7, 1), (5, 1)
 - $e \quad (0,0), (0,3), (3,0), (0,0)$
 - **f** (7, 3), (9, 3), (10, 6)

Name this type of angle, less than 90°. Name this type of angle, equal to 90°. Name this shape. Name this type of triangle. Name this type of triangle. Name this type of angle, less than 180°.

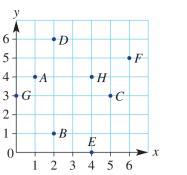
6 Draw a number plane from 0 to 8 on both axes. Plot the following points on the grid and join them in the order they are given.
(2,7), (6,7), (5,5), (7,5), (6,2), (5,2), (4,1), (2,2), (1,5), (2,5), (2,7).

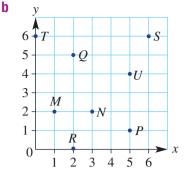
(2, 7), (6, 7), (5, 5), (7, 5), (6, 2), (5, 2), (4, 1), (3, 2), (2, 2), (1, 5), (3, 5), (2, 7)

Hint: The coordinates are

(x, y) or (across, up).

7 Write down the coordinates of each of these labelled points.





Example 28 Drawing a graph

For the rule output = input + 1:

- a Copy and complete the table of values.
- **b** List the coordinates of each point.
- c Plot each pair of points on the number plane.

input (x) output (y) 0 1 1 2 3 3

Solution

►

а

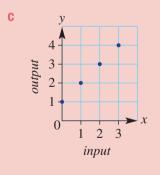
a	input (x)	output (y)
	0	1
	1	2
	2	3
	3	4

Explanation

Use the rule to find each *output* value for each *input* value. The rule is:

output = input + 1, so add 1 to each input value.

b (0, 1), (1, 2), (2, 3) and (3, 4)



The coordinates of each point are (input, output).

Plot each (*x*, *y*) pair as a point: (*x* units across from 0, *y* units up).

Now you try

For the rule output = input - 1:

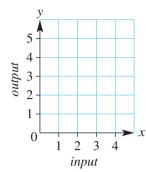
- a Copy and complete the table of values.
- **b** List the coordinates of each point.
- **c** Plot each pair of points on the number plane.

input (x)	output (y)
1	0
2	
3	
4	

3K

- 8 For the given rule output = input + 2:
 - a Copy and complete the given table of values.
 - **b** List the coordinates of each point.
 - c Plot each point on a number plane like the one below.

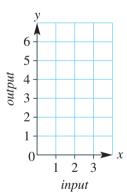
input (x)	output (y)
0	2
1	
2	
3	



- **9** For the given rule $output = input \times 2$:
 - a Copy and complete the given table of values.

input (x)	output (y)
0	
1	
2	
3	

- List the coordinates of each point. b
- Plot each point on a number plane like the one below. С



Problem-solving and reasoning

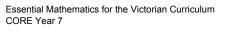
10, 11

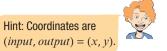
10-12

10 Draw a number plane from 0 to 5 on both axes. Place a cross on each point with coordinates that have the same x value and y value.





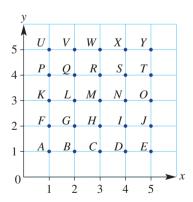




- **11 a** Which of the following is the correct way to describe the position of point *X*?
 - **A** 21
 - **B** 2, 1
 - C(2,1)
 - **D** (x2, y1)
 - **E** $(2_x, 1_y)$
 - **b** Which of the following is the correct set of coordinates for point *Y*?
 - **A** (2, 4)
 - **B** 4, 2
 - **C** (4, 2)
 - **D** (2, 4)
 - **E** x = 4, y = 2
- **12** a Plot the following points on a number plane. Join the points in the order given to draw the basic shape of a house. (1, 5), (0, 5), (5, 10), (10, 5), (1, 5), (1, 0), (9, 0), (9, 5)
 - **b** Draw a door and list the coordinates of the four corners of the door.
 - **c** Draw a window and list the coordinates of the four corners of the window.
 - d Draw a chimney and list the coordinates of the four points needed to draw the chimney.

Secret messages

13 A grid system can be used to make secret messages. Jake decides to arrange the letters of the alphabet on a number plane in the following manner.





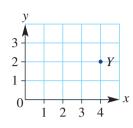
- a Decode Jake's following message: (3, 2), (5, 1), (2, 3), (1, 4)
- **b** Code the word 'secret'.

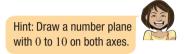
To increase the difficulty of the code, Jake does not include brackets or commas and he uses the origin to indicate the end of a word.

c What do the following numbers mean?

13515500154341513400145354001423114354.

d Code the phrase: 'Be here at seven'.





13

Maths@Work: Computer technician

Computer technicians and computer engineers are people who love technology and its uses. Their jobs range in difficulty, hours and pay. But they all need to have an understanding of patterns and mathematics.

The computer industry is always evolving. New devices and applications require larger and larger storage. Electronic data is represented in digital form using the digits 0 and 1, which are called 'bits' of data. A 'byte' is 8 bits, for example, the capital letter B is 1 byte stored as '01000010', which has 8 bits of data.

- A 'bit' (1 b) is the smallest data unit (either a 1 or 0).
- A 'byte' (1 B) is 8 bits.

Because there are only two possible bits (i.e. 0 or 1), computer storage data is called binary data and can be written as powers of 2. Note that 'bi' means two of something, for example, a bicycle has 2 wheels.

1	Remembering that a byte	e has 8 bits, wri	te each of the following in bytes.	
	a 16 bits (i.e. 16 b)	b 32 b	c 64 b	Hint: number of bits ÷
	d 256 b	e 1024 b	f 1048576b	8 = number of bytes

2 Other units are also used in file storage. Complete the table below to find the number of bytes for each of these storage amounts.

Name	Symbol	Powers of 2	Number of bytes
Byte	В	20	
Kilobyte	kB	2 ¹⁰	
Megabyte	MB	2 ²⁰	
Gigabyte	GB	2 ³⁰	
Terabyte	TB	2 ⁴⁰	

Hint: Use the power button on your calculator.



- **3** Use a factor tree or repeated division to determine the following storage amounts as powers of 2.
 - **a** 64 GB
 - **b** 512 GB
 - **c** 2048 GB (= 2TB)



Hint: Convert 56 kb/s to kB/s $56 \div 8 = ?$ kiloBytes/s

Hint: Convert MB to kiloBytes $21 \text{ MB} = 21 \times 1024$ = ? kiloBytes

 $=\frac{102^{2}}{102^{2}}$

Hint:

4 Use the question **2** answers to help you write each of the following in kilobytes (kB).

a 1 MB **b** 3 MB **c** 25 MB **d** 100 GB

5 Before Broadband, download speeds were quite slow. A dial-up internet speed could be 56 kb/s (kilobits per second).

Determine the unknown values in the following table to find the download times for the given data files.

			1			
		Speed	File size	File size	Download	Download
	Speed in	in kB/s	in MB	in kB	time in	time to the
	kilobits/s	(kiloBytes/s)	(MegaBytes)	(kiloBytes)	seconds	nearest hour
а	56		26 MB music			
			video			
b	56		152 MB game			
С	56		740 MB movie			

Using technology

Computer download times depend on the speed of the ISP (Internet Service Provider), the size of the file, the type and quality of the internet connection, the amount of traffic using a website, etc.

- 6 In this question, you will use a spreadsheet to calculate the download times for various Broadband internet speeds, which are measured in Mb/s (Megabits per second).
 - a Set up the following spreadsheet. Format all the shaded cells as Number/1 d.p.

Å,	A	B	c	D	E	F	G	н
1			Download times	for vario	ous files			
2			[Dow	nload spee	ds in Mega	bits per se	cond
3				8	20	30	50	100
4	Media type	File size in MB MegaBytes	File size in Mb Megabits	Download times				
5	Арр	16						
6	Music	24						
7	Short Video	45						
8	Gaming	120						
9	Movie	600						

- **b** In column C, enter formulas to calculate Megabits. Recall that there are 8 bits for each byte, so 8 Megabits for each Megabyte.
- **c** In columns D to H, enter formulas to calculate the download times in seconds for each data file for each of the different speeds.
- d How much faster, in seconds, is the App download time at 100 Megabits/s compared to 8 Megabits/s?
- e How much faster, in minutes and seconds, is the movie download time at 100 Megabits/s compared to 8 Megabits/s?

Hint: Cell C5 formula = B5*8



Hint: Formulas for download times: Use \$ signs to fix the address of the speed cell for each column. Cell D5 formula = C5/\$D\$3Cell E5 formula = C5/\$E\$3To fill formulas down the column, drag the fill handle down.



Start

1 To play *Prime Drop* with a partner, you will need a number chart (with circles around the prime numbers, and square numbers coloured in) and a die.

¥									
1	(2)	3	4	5	6	$\overline{7}$	8	9	10
(11)	12	(13)	14	15	16	(17)	18	(19)	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37)	38	39	40
41	42	43	44	45	46	(47)	48	49	50

Finish

- Each player must roll a 1 to start.
- Take turns to roll the die and move that number of places on the chart.
- If you land on a prime number, move back to the previous prime number (or to 1).
- If you land on a square number, have another turn.
- To finish, you must land on 50. (If the number you roll is too big, move forward to 50 and then move backwards.)
- 2 Why did the elephant go, 'Baa, baa'?

To find out, work out the following powers and square roots. Then decode the answer below.



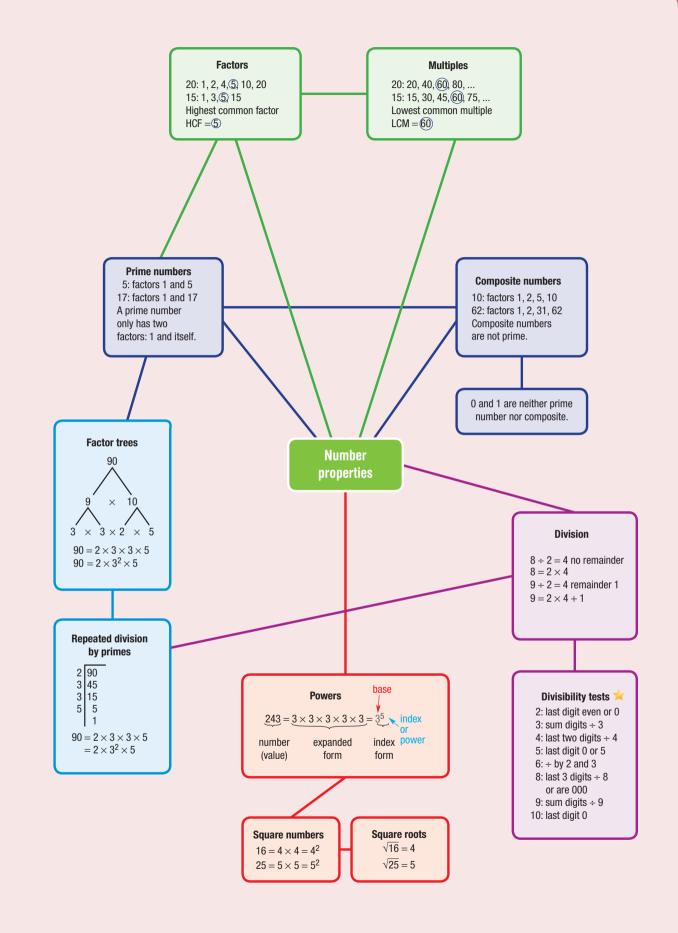
3 What number am I?

a Read the following clues to work out each mystery number.

- I have three digits.
 I am divisible by 5.
 I am odd.
 The product of my digits is 15.
 The sum of my digits is less than 10.
 I am less than 12 × 12.
- iii I have three digits.
 - I am odd and divisible by 5 and 9. The product of my digits is 180.
 - The sum of my digits is less than 20.
 - I am greater than 30^2 .

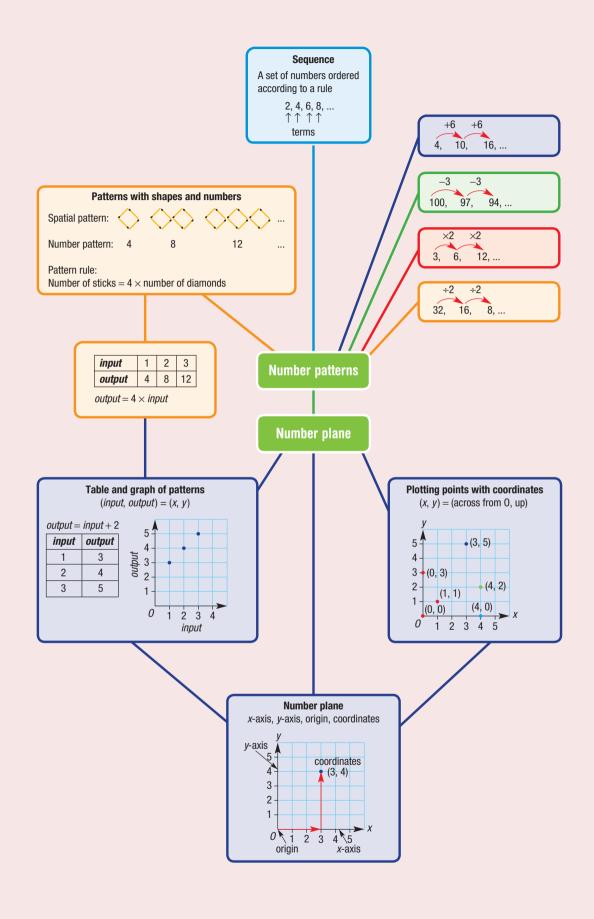
ii I have three digits. The sum of my digits is 12. My digits are all even. My digits are all different. I am divisible by 4. The sum of my units and tens digits equals my hundreds digit.

b Make up two of your own mystery number puzzles and submit your clues to your teacher.



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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

1 I can list pairs of factors of a number. e.g. Write the pairs of factors for 18. 2 I can list the factors of a number. e.g. Find the complete set of factors for the number 40. 3 I can list the multiples of a number (up to a certain limit). e.g. Write down the first six multiples of the number 11. I can identify an incorrect multiple within a sequence. e.g. Which number is the wrong multiple in the sequence 7, 14, 20, 28, 35? 5 I can list common factors and common multiples of two numbers. e.g. a List the common factors of 8 and 20. b List two common multiples of 2 and 3. 6 I can find the highest common factor (HCF) of two numbers. e.g. Find the highest common factor (HCF) of 36 and 48. 7 I can find the lowest common multiple (LCM) of two numbers. e.g. Find the lowest common multiple of 6 and 10. 8 I can determine if a number is divisible by 2, 3, 5 and/or 10. e.g. State whether 2, 3, 5 and/or 10 are factors of 48 569 412. 9 I can determine if a number is divisible by 4, 6, 8 and/or 9. e.g. State whether 4, 6, 8 and/or 9 are factors of 48 569 412. 10 I can determine whether a number is prime by considering its factors. e.g. Explain why 17 is prime but 35 is not prime. 11 I can find the prime factors of a number. e.g. Find the prime factors of 30. 12 I can convert an expression to index form. e.g. Write $3 \times 3 \times 2 \times 3 \times 2 \times 3$ in index form. 13 I can convert an expression to expanded form. e.g. Write 2^4 in expanded form. 14 I can evaluate expressions involving powers using the order of operations. e.g. Evaluate $7^2 - 6^2$.

3F 15	I can express a composite number in prime factor form using a factor tree. e.g. Draw a factor tree for the number 120. Then write 120 as the product of prime factors in index form.	~
3F 16	I can express a composite number in prime factor form using repeated division. e.g. Use repeated division with prime numbers to find the prime factors of 126. Then write 126 as a product of prime factors in index form.	
g 17	I can find the square of a number. e.g. Write the value of 4^2 .	
18	I can find the square root of a number. e.g. Find $\sqrt{64}$, the square root of 64.	
19	I can evaluate expressions involving squares and/or square roots. e.g. Evaluate $\sqrt{8^2+6^2}$	
20	I can find the next terms in a number pattern that change by a fixed amount. e.g. Find the next three terms for the number pattern 6, 18, 30, 42,	
21	I can find the next terms in a number pattern that involve multiplication or division. e.g. Find the next three terms for the number pattern 256, 128, 64, 32,	
22	I can describe a pattern in terms of the starting value and the operation used to get from each value to the next. e.g. Write the pattern rule in words for the sequence 2, 10, 50, 250,	
23	I can draw and describe terms within a spatial pattern. e.g. Draw the next two shapes in this spatial pattern and describe the rule in terms of how many sticks are required to make the first term, and how many are added each time.	
24	I can describe and use a rule for spatial patterns. e.g. By first drawing a table, find a pattern rule connecting the number of sticks required to the number of triangles. Then use this rule to find the number of sticks for 20 triangles.	
25	I can complete a table of values for a given rule. e.g. Fill out the table for the rule $output = (3 \times input) + 1$ input 4 2 9 12 0 output	

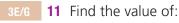
Chapter checklist 🔇

~

3J	26	I can find a rule for a table of values.e.g. Find the rule for the table of values shown.input12345output714212835	
ЗК	27	I can plot points on a number plane. e.g. Plot the points A(2, 5), B(4, 3) and C(0, 2).	
ЗК	28	I can draw a graph of a rule by completing a table of values. e.g. For the rule $output = input + 1$, construct a table of values using <i>input</i> values of 0, 1, 2 and 3. Use the table of coordinates to plot a graph.	

Short-answer questions

				-	400									
3A	1	а		pairs	of 12				12, 🗌 × 6 = 12, 🗌 × er are:,,			_,		
3A	2		List all the factors of 24 in ascending order. (Hint: First write the factor pairs.) List the first 6 multiples of 5. (Hint: Start with 5 and count in fives.)											
3B	3	b C d	List the fac List the fac Circle the c What do the Write the F	ctors comn he let	of 20. non (s tters l	share HCF s	tand		rs of 16 and 20. ?					
3B	4		List the firs What do t						b List the r? d State th			•		
30	5	a b	264 is is is 576 is is and is	that divis	ends by ible b by	in 0 i / 3 be / 9 be _ by 9	s divis ecause ecause 9.	sibl e th e th	e by both and _ ne sum of the digits i ne sum of the digits i ne last two digits are	s	+	_+ _+	_=_	
30	6	Frc a	6, 48, 56, 62 om the list o 2 6		nbers b			rite	the numbers that an c 4 g 9	re divis	sible	by: d 5 h 10		
3D	7	a b c	List the fac Sort these	ber 1 ber 1 two tors num factor	a pri a co factor of 10 bers i rs of 2	me n mpos rs, 1 a . ls 10 nto p 20 in	site nu and 5) a pri prime two g	um . Is ime or gro	5 a prime number? or composite numb composite numbers: ups, prime and comp	2, 3, 8			0.	
3E/F	8	Ar a b c d	Write the p	², wh produ 3² in	at nu ict 5 : facto	mber × 5 × or for	7 × 7 m an	′×′ d fi	ase? What number i 7 in index form. nd the number value ps).		nde>	or pov	ver?	
		е	Find the m	issing	g pov	vers:	125 =	5	; $32 = 2^{-1}$; 100000	= 10				
3F	9	Fo a	r each num				or tre		Then write the numb				f prin	ne factors.
3G	10	Сс	ppy and com	nplete	e each	n of t	hese	tab	les.					
		I	ndex form	4 ²		7 ²			Square root form	$\sqrt{16}$		$\sqrt{100}$]
		V	/alue		36		81		Value		5		12]



d

199 а

 $\sqrt{3^2} \times \sqrt{4^2}$

b $\sqrt{3^2} + \sqrt{4^2}$

b

d 44, 40, 36, ...

- e $4^2 \sqrt{25} + \sqrt{7^2}$
- 8 to the power of 2 **h** 11 squared q

the side length of a square that has area = 25 cm^2

- the side length of a square that has area = 400 cm^2 k
- **12** List the next four terms for these sequences.
 - а Start with 3 and keep adding 4.
 - 3, 6, 12, ... C
 - e 1, 4, 9, ... (Hint: These are square numbers.)
 - 13 a Draw the next two shapes in this spatial pattern.



b Copy and complete this table.

Number of triangles	1	2	3	4	5
Number of sticks	3				

- Write the pattern rule. С
- **d** How many sticks would be needed for 12 triangles?
- 14 Look at this spatial pattern.



Copy and complete this table. а

Number of squares	0	1	2	3	4
Number of sticks	1	1+=	1 + 🗌 × 2 = 🗌	$1 + \square \times 3 = \square$	1+ × 4 =

b

input

output

Copy and complete the rule for this pattern: b

number of sticks = $1 + 1 \times 1$ x number of squares

- How many sticks are needed to make 10 squares this way? С
- **d** How many squares could be made from 82 sticks?
- **15** Copy and complete each table for the given rule.
 - a output = input + 5

-	-				
input	3	5	7	12	20
output					

16 Write the pattern rule for each of these tables.

25

a $output = | \times input$ input 3 5 4

15

output

b	output =	inpu	t — [
	input	15	20	28	
	output	9	14	22	

 $output = 2 \times input + 7$

2 4

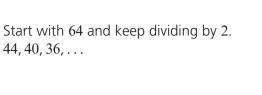
9 12 0



- 17 State the coordinates of each point plotted on this number plane. а
 - b State the coordinates of the origin.

20

- Which axis is point (0, 5) on? С
- **d** Name the vertical axis.
- Which axis is the point (3, 0) on? е
- Name the horizontal axis. f
- State the coordinates of a point *C* so that *ABCD* is a square. q

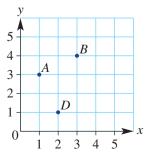


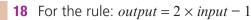
c $\sqrt{3^2 + 4^2}$

f

 $10^3 \div \sqrt{3^2 + 4^2}$

the square root of 81

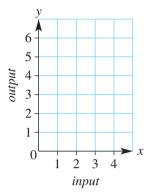




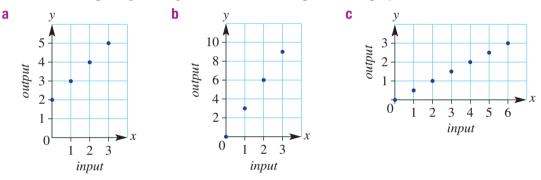
a Copy and complete this table of values.

input (x)	output (y)
1	
2	
3	
4	

- **b** List the coordinates of each point.
- **c** Plot each point on a number plane like the one to the right.



19 Write a rule (e.g. $output = input \times 2$) that would give these graphs.



Multiple-choice questions

3A 1	Which number is 24, 27, 30	the wrong m	nultiple for the following	g sequence? 3, 6,	9, 12, 15, 18, 22,				
	A 18	B 22	C 30	D 6	E 3				
3A 2	3A 2 Which group of numbers contains every factor of 20?								
	A 2, 4, 5, 10, 20		B 2, 4, 5, 15, 20	C 1, 2, 4	, 5, 10				
	D 1, 2, 4, 8, 5, 10		E 1, 2, 4, 5, 10, 20						
3D 3	Which of the foll	owing numb	ers is a prime number?						
	A 21	B 77	C 11	D 22	E 1				
3D 4	Which of the foll	owing group	s of numbers includes o	ne prime and two	o composite				
	numbers?								
	A 2, 10, 7	B 54, 7, 11	C 9, 32, 44	D 5, 17, 23	E 18, 3, 12				
3E 5	$7 \times 7 \times 7 \times 7 \times 7$	•	fied to:						
	A 5 ⁷	B 7 ⁵	C 7 × 5	D 75	E 77777				
3G 6	Evaluate $\sqrt{3^2 + 4^2}$								
	A 7	B 5	C 14	D 25	E 6				
3B 7	The HCF and LCM	√ of 12 and 1	8 are:						
	A 6 and 18	B 3 and 12	C 2 and 54	D 6 and 36	E 3 and 18				

Chapter review

6

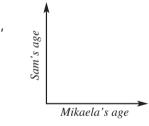
3F	8 T	he prime factor fo	rm of 48 is:							
		$2^4 \times 3$			C 2×3^3	D	3×4^2		E	$2^3 \times 6$
3E	9 E	valuate $4^3 - 3 \times (2)$	$(2^4 - 3^2).$							
	A	427	B 18		C 43	D	320		E	68
3A	10 F	actors of 189 inclu	ıde:							
	A	3, 7, 9, 18, 21, 27		B	3, 9, 18, 21		C	3, 9, 18		
	D	3, 7, 9, 17, 21		Е	3, 7, 9, 21, 27, 63					
3C	11 V	Vhich number is <i>n</i>	ot divisible by i	3?						
•	A	25 697 403		B	31 975		C	7 297 008		
	D	28 650 180		Е	38 629 634 073					
3K	12 V	Vhich set of points	s is in a horizor	ntal	line?					
	A	(5, 5), (6, 6), (7, 7)		В	(3, 2), (3,	4), (3, 1	1)		
	C	(2, 4), (3, 6), (4, 8)		D	(5, 4), (6,	4), (8, 4), (12, 4)		
	E	(1, 5), (5, 1), (1, 1), (5, 5)							

Extended-response questions

- 1 Sam is five years older than his sister Mikaela.
 - a Copy and complete this rule for their ages: Sam's age = Mikaela's age +
 - **b** Copy and complete this table showing Sam's age and Mikaela's age in years.

Mikaela's age	0	3	7	13
Sam's age				

c On grid paper, draw horizontal and vertical axes and label each with the numbers from 0 to 20. (Be careful to mark the numbers next to the grid lines, not in the spaces.) Label the axes as follows.



- **d** On your graph, plot the points from the table above. (Hint: Mikaela's age goes *across*, Sam's age goes *up*.)
- 2 At North Park Primary School, the classrooms have trapezium-shaped tables. Mrs Greene arranges her classroom's tables in straight lines, as shown.



a Copy and complete this table for up to 5 tables joined together.

Number of tables	1	2	3	4	5
Number of students					

b Copy and complete this rule:

number of students = $\square \times$ number of tables + \square

Check that the rule works for the numbers in your table.

- **c** The room allows seven tables to be arranged in a straight line. How many students can sit around the tables?
- **d** There are 80 students in Grade 6 at North Park Primary School. Mrs Greene would like to arrange the tables in one straight line for an outside picnic lunch. How many tables will she need?

Chapter

Fractions and percentages

Essential mathematics: why working with fractions and percentages is important

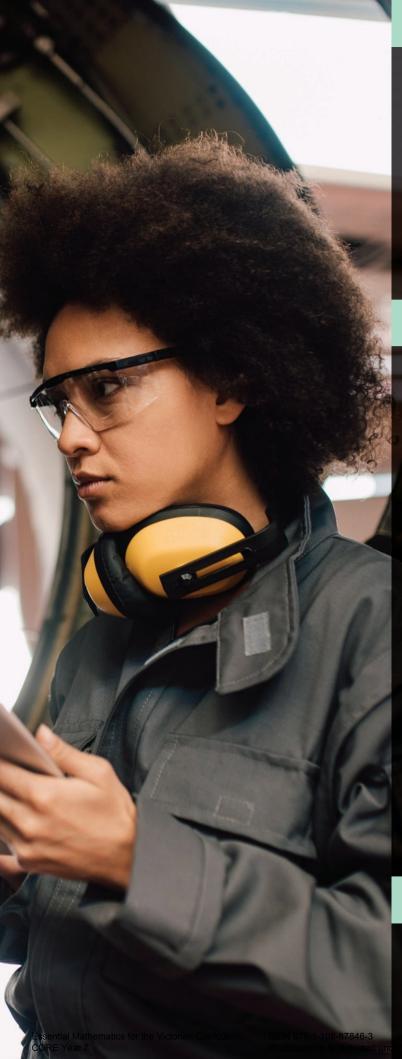
Fraction and percentage skills are used in many of the calculations needed in the skilled trades. Accuracy is essential for successful outcomes, such as a plane that flies or a patient who lives.

• Aviation engineers and mechanics regularly work with fractions of an inch, as many aircraft parts are from America which uses Imperial measurements. Calculations need to be accurate

to $\frac{1}{1000}$ of an inch.

- Chefs and cooks multiply fractions to increase recipe quantities, e.g. $3\frac{3}{4}$ cups \times 7 = $26\frac{1}{4}$ cups.
- Nurses use fraction skills to calculate the time for an intravenous drip, e.g. $\frac{23}{4} = 5\frac{3}{4}$ hours.
- Retail assistants and accountants use percentage calculations to find discounted prices, e.g. if a \$40 shirt is discounted by 25%, the sale price is \$30.
- Bricklayers use a ratio for the proportions in a dry mortar mix, e.g. sand : cement = 4 : 1.

SBN 978



In this chapter

- 4A Introduction to fractions (Consolidating)
- 4B Equivalent fractions and simplified fractions
- 4C Mixed numbers (Consolidating)
- 4D Ordering fractions
- 4E Adding fractions
- 4F Subtracting fractions
- 4G Multiplying fractions
- 4H Dividing fractions
- 4I Fractions and percentages
- 4J Finding a percentage of a number
- 4K Expressing a quantity as a proportion
- 4L Ratios, rates and best buys

Victorian Curriculum

NUMBER AND ALGEBRA Real numbers

Compare fractions using equivalence. Locate and represent positive and negative fractions and mixed numbers on a number line (VCMNA242)

Solve problems involving addition and subtraction of fractions, including those with unrelated denominators (VCMNA243)

Multiply and divide fractions and decimals using efficient written strategies and digital technologies (VCMNA244)

Express one quantity as a fraction of another, with and without the use of digital technologies (VCMNA245)

Connect fractions, decimals and percentages and carry out simple conversions (VCMNA247)

Find percentages of quantities and express one quantity as a percentage of another, with and without digital technologies. (VCMNA248)

Recognise and solve problems involving simple ratios (VCMNA249)

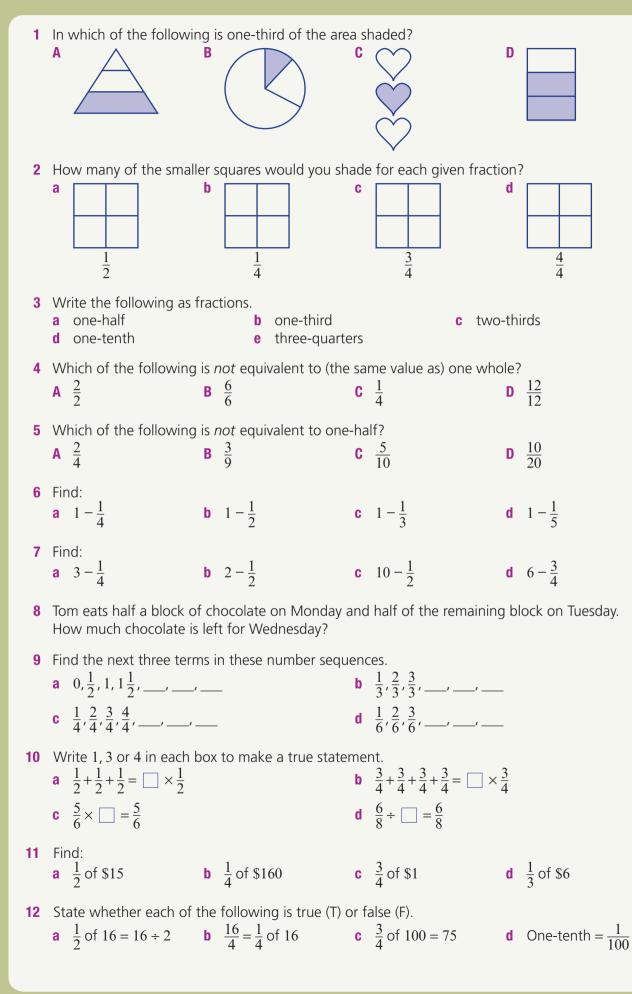
Money and financial mathematics

Investigate and calculate 'best buys', with and without digital technologies (VCMNA250)

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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more. Warm-up quiz



4A Introduction to fractions

CONSOLIDATING

Learning intentions

- To understand what a fraction is.
- To know what the numerator and denominator of a fraction represent in different situations.
- To understand how a fraction relates to the shaded area of a shape.
- To be able to represent fractions on a number line.

Key vocabulary: fraction, denominator, numerator, vinculum, proper fraction, improper fraction, mixed number

The word fraction comes from the Latin word 'frangere', which means 'to break into pieces'. Fractions are parts of a whole.

We all use fractions every day. They are used in cooking, shopping, sport and building construction.



Lesson starter: What strength do you like your cordial?

- Tom uses 40 mL of cordial and 120 mL of water.
- Sally uses 40 mL of cordial with 200 mL of water.
- Who likes their drink the strongest? How can fractions be used to describe the strengths of cordial?

Key ideas

 A fraction is a number made up of a numerator (up) and a denominator (down).

For example: $\frac{3}{5}$ — numerator denominator

- The **denominator** tells you how many parts the whole is divided up into.
- The **numerator** tells you how many parts we are talking about.
- The horizontal line separating the numerator and the denominator is called the **vinculum**.
- A **proper fraction** has the numerator less than the denominator. For example: $\frac{2}{7}$ is a proper fraction.
- An **improper fraction** has the numerator greater than or equal to the denominator. For example: $\frac{5}{2}$ is an improper fraction.
- Whole numbers can be represented as fractions. For example: $1 = \frac{4}{4}$, $1 = \frac{3}{3}$, $2 = \frac{8}{4}$
- **Mixed numbers** have a whole number and a fraction. For example: $1\frac{2}{3}$ is a mixed number.
- We can represent fractions on a number line. This number line shows the whole numbers 0, 1 and 2. Each unit has then been divided equally into four segments, therefore creating 'quarters'.





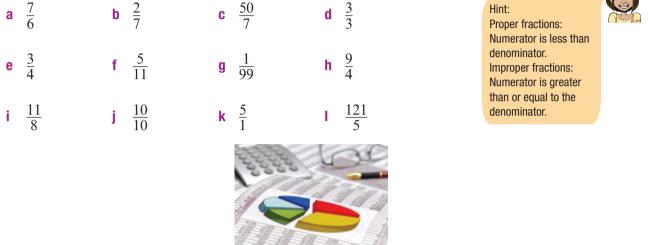
Exercise 4A

Understanding

- **1** a State the denominator of this proper fraction: $\frac{2}{9}$
 - **b** State the numerator of this improper fraction: $\frac{7}{5}$
- 2 Group the following list of fractions into proper fractions or improper fractions. Also state which ones are whole numbers.

1-4

4

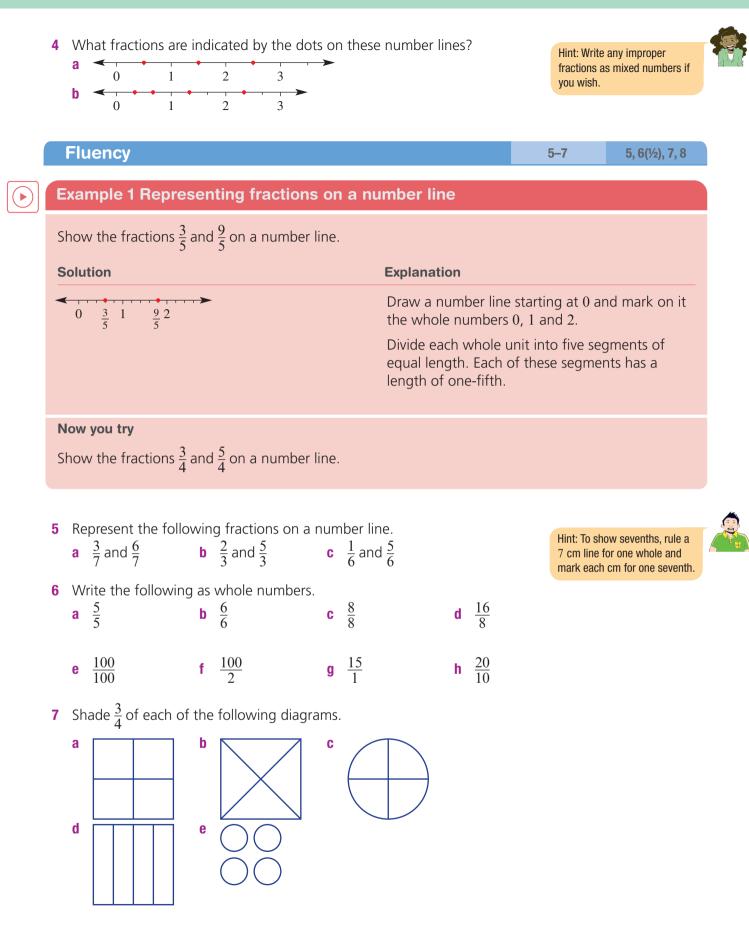


3 State the missing parts in the following table.

The whole (divided into equal parts)	Number of equal parts in the whole (denominator)	Number of shaded equal parts (numerator)	Fraction shaded	Name of fraction
	4			one-quarter
		2	$\frac{2}{3}$	
		8		one whole

Essential Mathematics for the Victorian Curriculum CORE Year 7

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4A

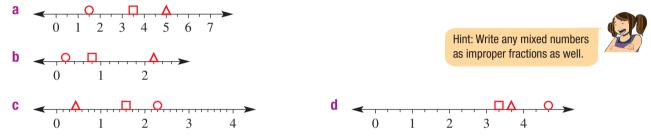


- **a** $\frac{3}{5}, \frac{4}{5}, \frac{5}{5}, \frac{6}{5}, \dots, \dots, \dots$
- **b** $\frac{5}{8}, \frac{6}{8}, \frac{7}{8}, \frac{8}{8}, \dots, \dots, \dots$
- **c** $\frac{1}{3}, \frac{2}{3}, \frac{3}{3}, \frac{4}{3}, \dots, \dots, \dots$
- **d** $\frac{11}{7}, \frac{10}{7}, \frac{9}{7}, \frac{8}{7}, \dots, \dots, \dots$

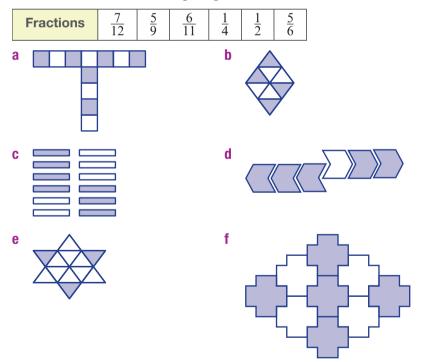
Problem-solving and reasoning

9, 10 9–12

9 What fraction matches each of the different shapes (\bigcirc , \square and \triangle) on these number lines?



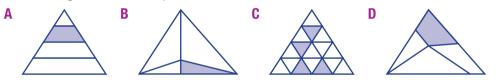
10 Match each of the following diagrams to one of the fractions in the box below.



- **11** For each of the following, write the fraction that is describing part of the total.
 - a After one day of a 43-kilometre hike, the students had completed 12 kilometres.
 - **b** From 15 starters, 13 went on and finished the race.
 - **c** Rainfall for 11 months of the year was below average.
 - **d** One egg is broken in a carton that contains a dozen eggs.
 - e Two players in the soccer team (with 11 players) scored a goal.
 - f The lunch stop was 144 kilometres into the 475-kilometre trip.
 - g Seven members in the class of 20 have visited Australia Zoo.
 - **h** One of the car tyres (not including the spare) is worn and needs replacing.
 - i It rained three days this week.



12 Which diagram has one-quarter shaded?



Adjusting concentration

- **13 a** Callum pours 20 mL of water into this beaker. What fraction of 200 mL is that?
 - **b** Callum adds acid to the same beaker until it holds 200 mL. How much acid did he add? What fraction of 200 mL is that?
 - **c** Rosa has a 200 mL beaker that is $\frac{1}{4}$ full of water. How much acid will she need to add to fill the beaker?



13

4B Equivalent fractions and simplified fractions

Learning intentions

- To understand what it means for two fractions to be equivalent.
- To be able to simplify fractions.

Key vocabulary: equivalent fractions, highest common factor, simplify

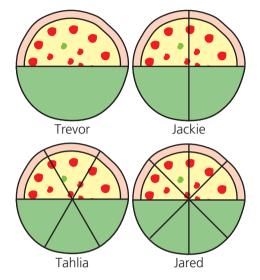
Fractions may look very different but still have the same value. For example, in an AFL football match, 'half-time' is the same as 'the end of the second quarter'. We can say that

 $\frac{1}{2}$ and $\frac{2}{4}$ are equivalent fractions.

Consider a group of friends eating pizzas during a sleepover. The pizzas are homemade and each person cuts up their pizza as they like. The green shading shows the amount eaten before it is time to start the second movie.

By looking at the pizzas, it is clear to see that Trevor, Jackie, Tahlia and Jared have all eaten the same amount of pizza.

This means that $\frac{1}{2} = \frac{2}{4} = \frac{3}{6} = \frac{4}{8}$.



Lesson starter: Odd one out

• Pick the fraction that is the odd one out.

 $\frac{25}{100}$, $\frac{4}{16}$, $\frac{2}{8}$, $\frac{2}{5}$, $\frac{5}{20}$

• What could we call the other four fractions?

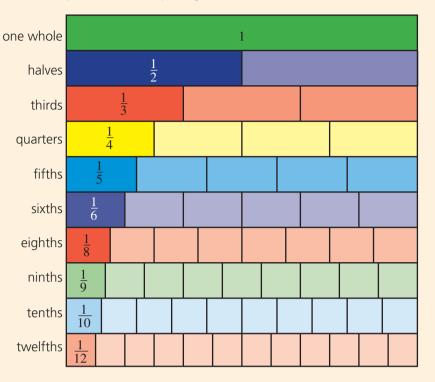
Key ideas

Equivalent fractions are fractions that mark the same place on a number line.

For example: $\frac{1}{2}$ and $\frac{2}{4}$ are equivalent fractions.

- Equivalent fractions are produced by multiplying the numerator and denominator by the same number.
- Equivalent fractions can also be produced by dividing the numerator and denominator by the same number.
- Simplifying fractions involves writing a fraction in its 'simplest form'. To do this, the numerator and the denominator must be divided by their highest common factor (HCF), the largest number which divides into both numbers.
 - You should usually write fraction answers in their simplest form.

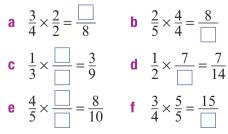
A fraction wall can be helpful when comparing fractions.



Exercise 4B

Understanding

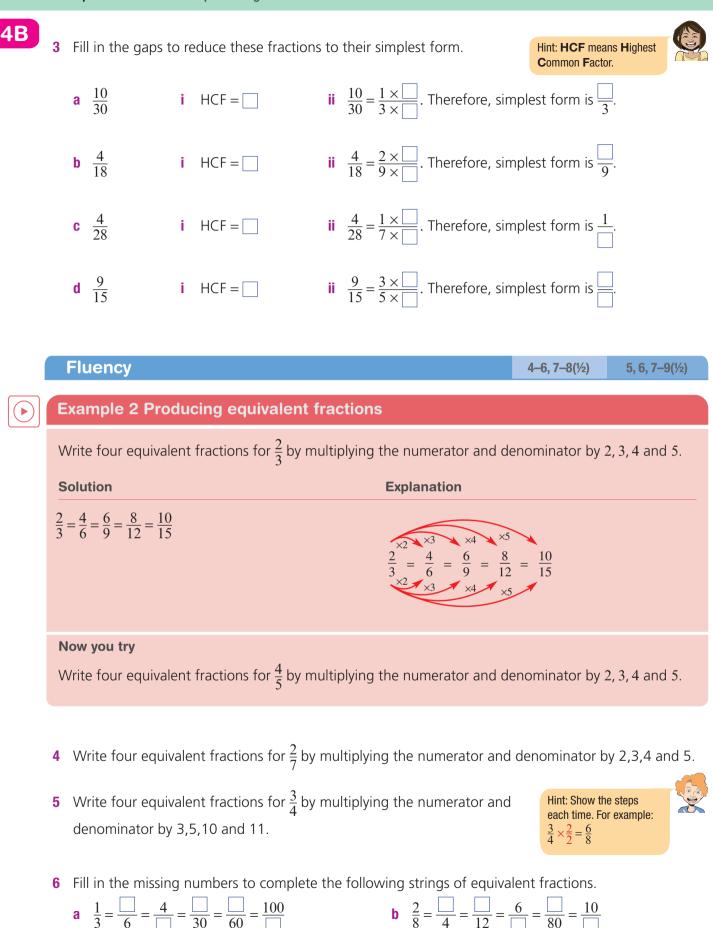
- 1 Use the fraction wall in the Key ideas to find:
 - **a** five fractions equivalent to (equal to) $\frac{1}{2}$.
 - **b** two fractions equivalent to $\frac{1}{4}$
 - **c** three fractions equivalent to $\frac{1}{3}$
 - **d** one fraction equivalent to $\frac{4}{5}$
- 2 Copy and complete the following.

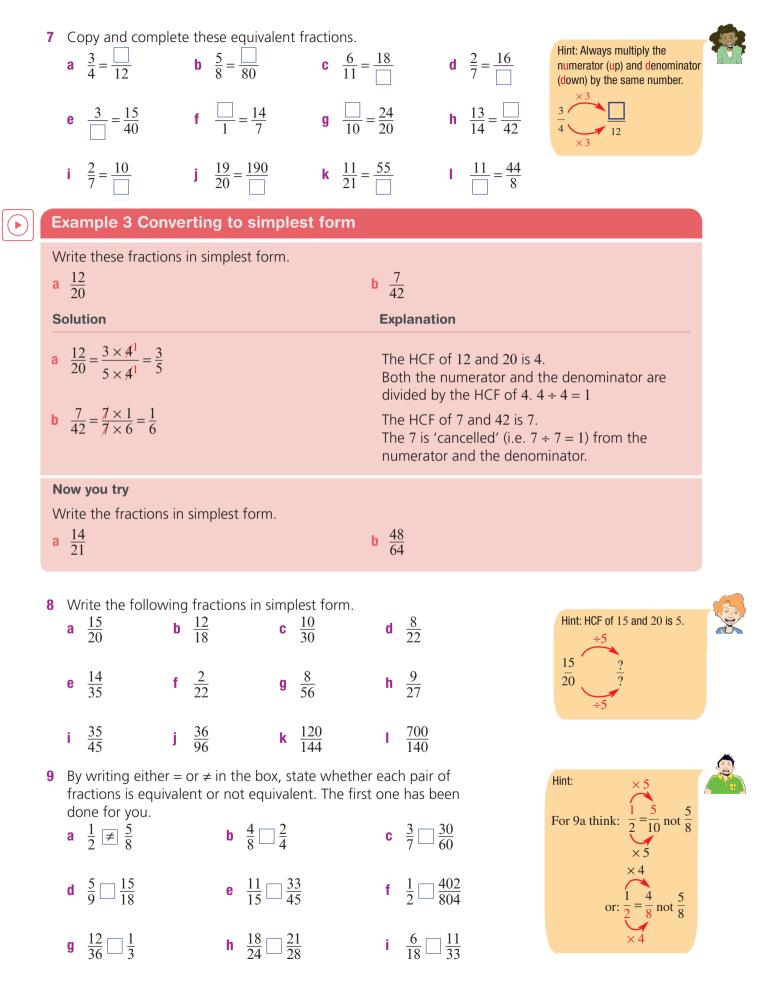




1-3

3





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4B

Problem-solving and reasoning

11 - 13

10.11

- 10 In each group, choose the fraction that is not in its simplest form. What should it be?
 - $\frac{1}{3}, \frac{3}{8}, \frac{5}{9}, \frac{7}{14}$ а

 - **b** $\frac{2}{5}, \frac{12}{16}, \frac{15}{19}, \frac{13}{37}$
 - **c** $\frac{12}{19}, \frac{4}{42}, \frac{5}{24}, \frac{6}{61}$

 - **d** $\frac{7}{63}, \frac{9}{62}, \frac{11}{81}, \frac{13}{72}$
- 11 Which of the following fractions are equivalent to $\frac{8}{20}$?

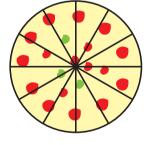
 $\frac{4}{10}$, $\frac{1}{5}$, $\frac{6}{20}$, $\frac{8}{10}$, $\frac{16}{40}$, $\frac{2}{5}$, $\frac{4}{12}$, $\frac{12}{40}$, $\frac{80}{200}$, $\frac{1}{4}$

12 A family block of chocolate consists of 6 rows of 6 individual squares. Tania eats 16 individual squares. What fraction of the block, in simplest terms, has Tania eaten?



13 Jason, Joanna and Jack are sharing a large pizza for dinner. The pizza has been cut into 12 equal pieces. Jason would like $\frac{1}{3}$ of the pizza, Joanna would

like $\frac{1}{4}$ of the pizza and Jack will eat whatever is remaining. How much does Jack eat?



14

Mystery fraction

14 A fraction when simplified is written as $\frac{3}{5}$.

What could the fraction have been before it was simplified? Show your fraction on a diagram. Is your fraction the same as the fraction of the student sitting next to you?

4C Mixed numbers

CONSOLIDATING

Learning intentions

- To understand what improper fractions and mixed numbers are.
- To be able to convert from a mixed number to an improper fraction.
- To be able to convert from an improper fraction to a mixed number.

Key vocabulary: proper fractions, improper fractions, mixed numbers, whole numbers, remainder

As we have seen in this chapter, a fraction is a common way of representing part of a whole. For example, a particular car trip may require

 $\frac{2}{3}$ of a tank of petrol.

On many occasions, you may need whole numbers plus a part of a whole number.

For example, a long interstate car trip may require

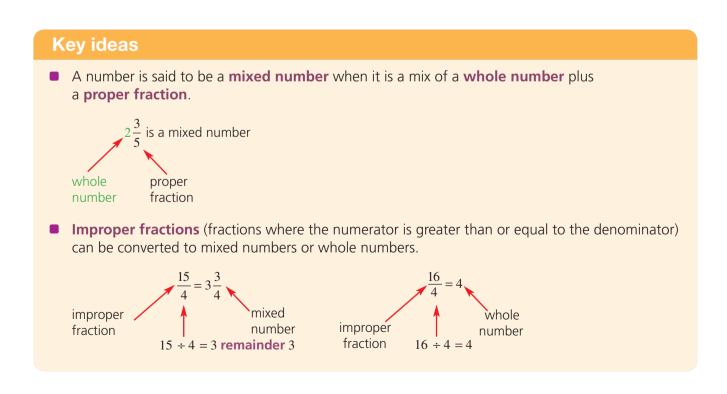
 $2\frac{1}{4}$ tanks of fuel. When you have a combination

of a whole number and a fraction, we call this a mixed number.



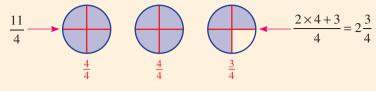
Lesson starter: Pizza frenzy

Tom ate $1\frac{1}{2}$ pizzas. Chandra ate $\frac{3}{2}$ of a pizza. Who ate the most? Discuss, showing each person's pizzas on a separate diagram.

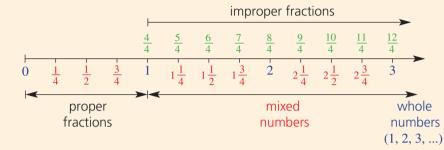


4C

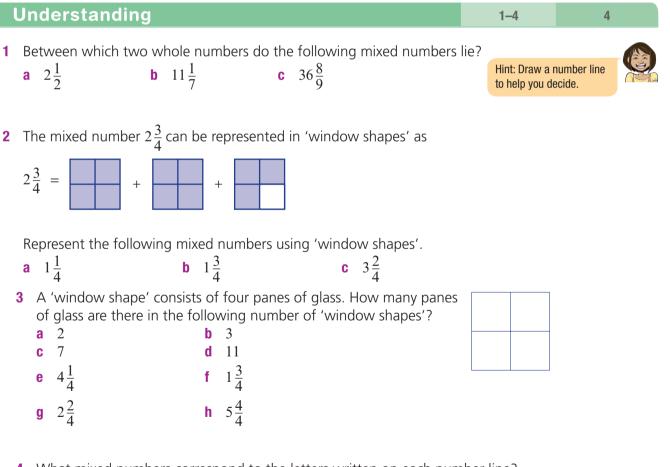
Mixed numbers can be converted to improper fractions.



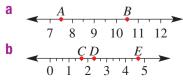
A number line helps show the different types of fractions.

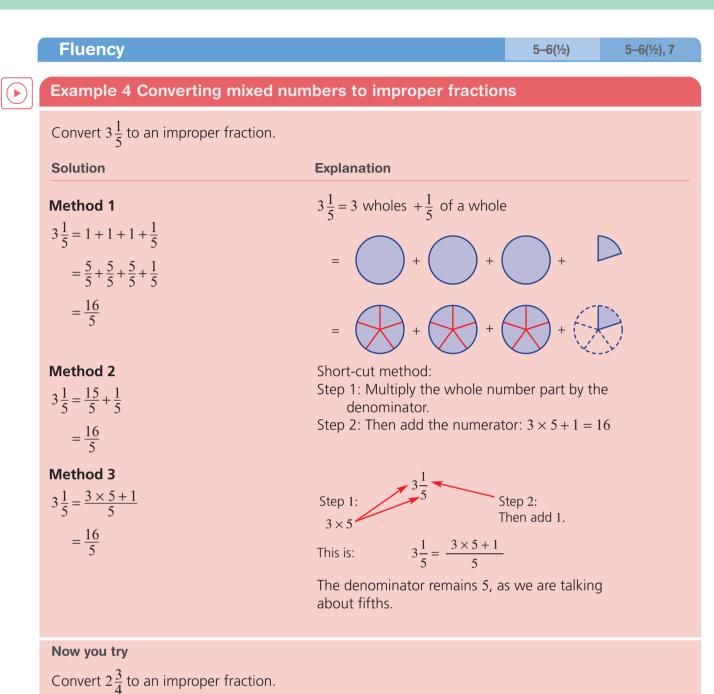


Exercise 4C



4 What mixed numbers correspond to the letters written on each number line?





5	Сс	onvert these mixed nui	mbe	ers to improper fractior	าร.			
	а	$2\frac{1}{5}$	b	$1\frac{3}{5}$	C	$3\frac{1}{3}$	d	$5\frac{2}{3}$
	е	$4\frac{1}{7}$	f	$3\frac{3}{7}$	g	$2\frac{1}{2}$	h	$6\frac{1}{2}$
	i	$4\frac{2}{5}$	j	$11\frac{1}{2}$	k	$8\frac{2}{5}$	I.	$10\frac{3}{10}$
	m	$6\frac{1}{9}$	n	$2\frac{7}{9}$	0	$5\frac{2}{8}$	р	$2\frac{5}{8}$
	q	$1\frac{11}{12}$	r	$3\frac{5}{11}$	S	$4\frac{5}{12}$	t	$9\frac{7}{12}$

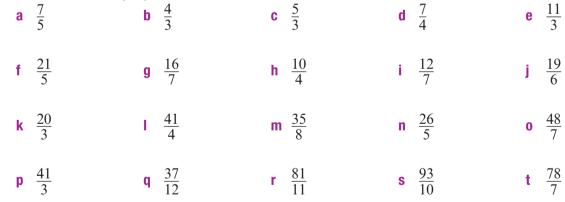
4**C**

Example 5 Converting improper fractions to mixed numbers

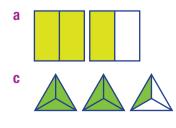
Convert $\frac{11}{4}$ to a mixed number.

4 Solution	Explanation
Method 1 $\frac{11}{4} = \frac{8+3}{4}$ $= \frac{8}{4} + \frac{3}{4}$ $= 2 + \frac{3}{4}$ $= 2\frac{3}{4}$ Method 2 $4\frac{2}{11}$ rem. 3 $= 2\frac{3}{4}$	$\frac{11}{4} = 11 \text{ quarters}$ $= ++++++++++++++++++++++++++++++++++++$
Now you try Convert $\frac{22}{7}$ to a mixed number.	

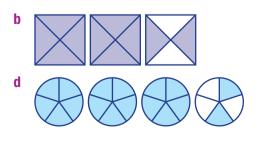
6 Convert these improper fractions to mixed numbers.

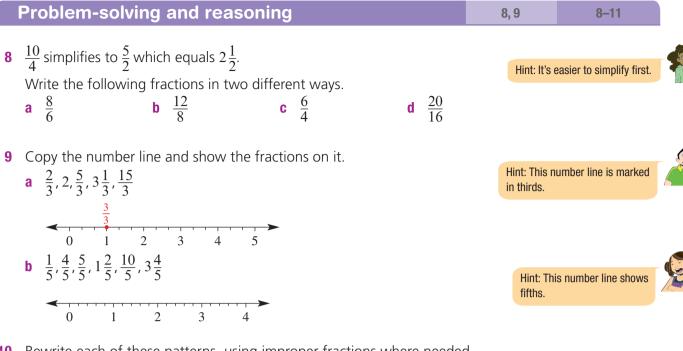


7 For each of these diagrams, write:i the mixed number



ii the improper fraction





- **10** Rewrite each of these patterns, using improper fractions where needed.
 - **a** $\frac{1}{2}$, 1, $1\frac{1}{2}$, 2, $2\frac{1}{2}$, 3

- **b** $\frac{1}{4}, \frac{2}{4}, \frac{3}{4}, 1, 1\frac{1}{4}, 1\frac{2}{4}, 1\frac{3}{4}, 2$
- **11** Four friends order three large pizzas for their dinner. Each pizza is cut into eight equal slices. Simone has three slices, Izabella has four slices, Mark has five slices and Alex has three slices.
 - a Draw circles to show the three pizzas ordered.
 - **b** How many pizza slices do they eat in total?
 - c How much pizza do they eat in total? Give your answer as a mixed number.
 - d How many pizza slices are left uneaten?
 - e How much pizza is left uneaten? Give your answer as a mixed number.

Writing fractions

12 What different fractions can you write using only the digits 1, 2 and 3? Who in your class wrote the most? Assume that each digit can only be used once in each fraction.



Hint: You can include improper fractions and mixed numbers. You don't need to use all three digits.

12

Hint: Remember, each pizza has

8 equal slices.



4D Ordering fractions

Learning intentions

- To be able to compare two fractions and decide which one is bigger.
- To be able to use the symbols < or > to compare two numbers.
- To be able to order a list of fractions in ascending or descending order.

Key vocabulary: lowest common denominator (LCD), equivalent fractions, ascending, descending

Just like whole numbers, fractions can be written in order. We can use the ideas from section 4B to help. Remember that > means *is greater than* and < means *is less than*.

A fraction is greater than another fraction if it lies to the right of that fraction on a number line.



Lesson starter: The order of five

- As a warm-up activity, ask five volunteer students to arrange themselves in alphabetical order, then in height order and, finally, in birthday order.
- Each of the five students receives a large fraction card and displays it to the class.

(For example, $\frac{1}{2}$, $\frac{1}{10}$, $\frac{2}{10}$, $\frac{10}{2}$, $\frac{2}{3}$.)

• The rest of the class must then attempt to order the students in ascending order, according to their fraction card. It is a group decision and none of the five students should move until the class agrees on a decision.



Key ideas

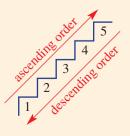
- To order (or arrange) fractions we must know how to compare different fractions. There are three cases to consider.
 - 1 If the numerators are the same, the smallest fraction is the one with the largest denominator, as the whole has been divided up into the most pieces. For example: $\frac{1}{2} < \frac{1}{2}$

For example: $\frac{1}{7} < \frac{1}{2}$

2 If the denominators are the same, the smallest fraction is the one with the smallest numerator.

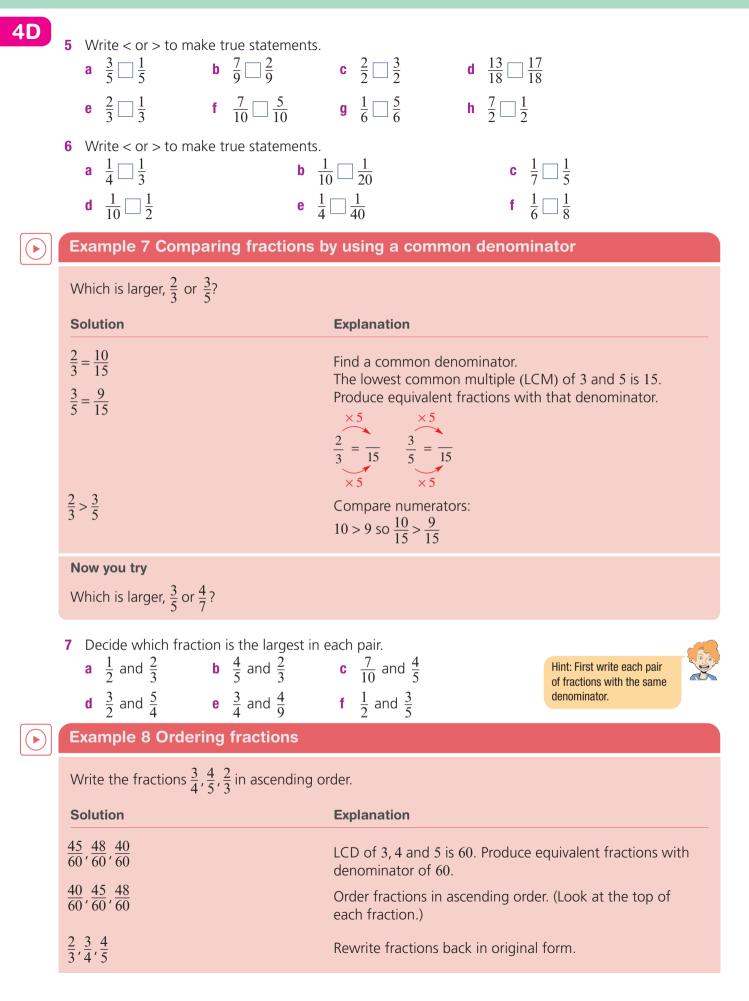
For example: $\frac{3}{10} < \frac{7}{10}$

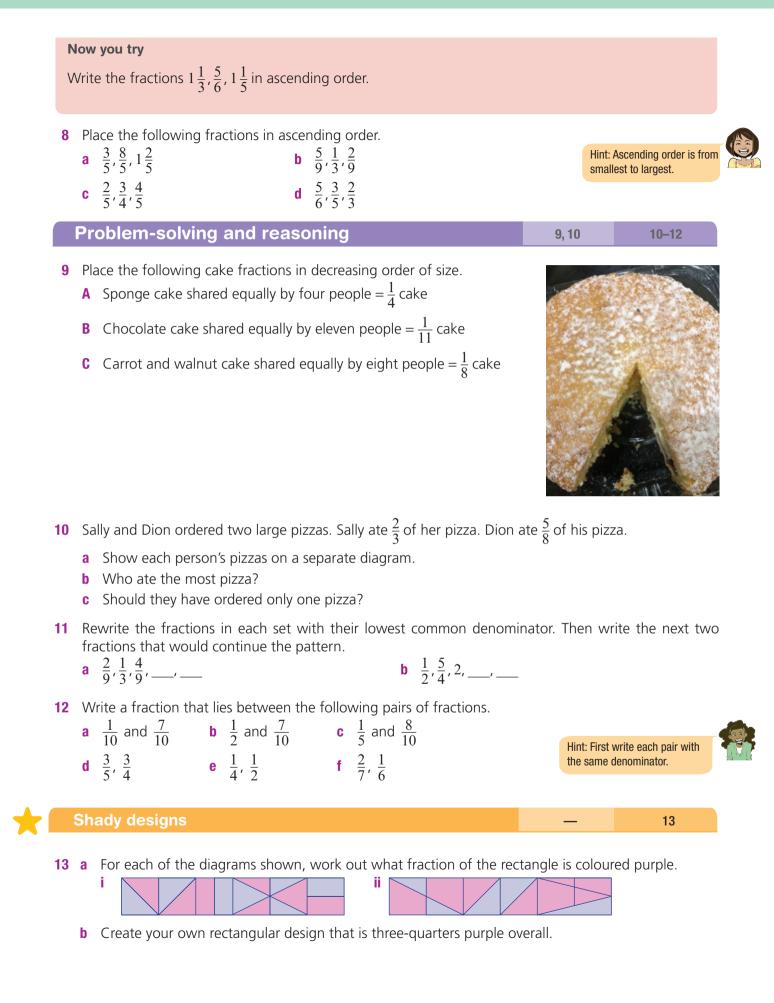
- **3** Otherwise, use **equivalent fractions** to make fractions with the same denominator. (The **lowest common denominator (LCD)** is best.) Then compare numerators as above.
- Ascending order is when numbers are ordered going up, from smallest to largest.
- Descending order is when numbers are ordered going *down*, from largest to smallest.



Exercise 4D

Understandi	ng		1	1–4	4
	fraction in each of t b $\frac{4}{3}, \frac{2}{3}, \frac{7}{3}, \frac{5}{3}$ c	he following lists. $\frac{5}{11}, \frac{9}{11}, \frac{3}{11}, \frac{4}{11}$ d $\frac{8}{5}, \frac{4}{5}$	$\frac{1}{5}, \frac{7}{5}$ the same	en the denominat e, compare nume han <u>5</u> , just as 6 is	rators: $\frac{6}{7}$
 2 State the lowest of a 2, 5 e 3, 6 i 2, 3, 5 	common multiple of b 3, 7 f 2, 10 j 3, 4, 6	f the following sets of n c 5,4 g 4,6 k 3,8,4	umbers. d 6, 5 h 8, 6 l 2, 6, 5	Hint: 2, 4, 6, 7 5, (10), 15, 2 The LCM of 2	
a $\frac{1}{3}, \frac{3}{5}$	b $\frac{2}{4}, \frac{3}{5}$	tor of the following sets c $\frac{4}{7}, \frac{2}{3}$ g $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}$	d $\frac{2}{10}, \frac{1}{5}$	Hint: Fin denomin	d the LCM of the nators.
4 Fill in the gaps to a $\frac{2}{5} = \frac{\square}{15}$ d $\frac{3}{7} = \frac{\square}{14}$		fractions. $\frac{2}{3} = \frac{\square}{12}$ $\frac{3}{8} = \frac{\square}{40}$	$c \frac{1}{4} = \frac{1}{1}$ $f \frac{5}{6} = \frac{1}{1}$	-	
Fluency			5-	-7(½)	5-7(½), 8
Example 6 Com	paring fractions	i			
Write < or > in each a $\frac{2}{5}$ $\boxed{\frac{4}{5}}$) box to make a true	e mathematical statement b $\frac{1}{3}$ $\boxed{\frac{1}{5}}$	nt.		
Solution		Explanation			
a $\frac{2}{5} < \frac{4}{5}$		Denominators are th numerators. $2 < 4$ so $\frac{2}{5} < \frac{4}{5}$	e same, therefor	e compare	
b $\frac{1}{3} > \frac{1}{5}$		Numerators are the s The smaller fraction So $\frac{1}{3} > \frac{1}{5}$		enominator.	





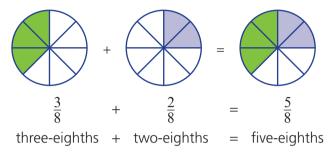
4E Adding fractions

Learning intentions

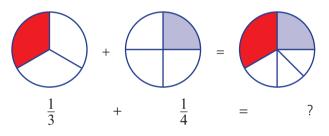
- To understand that adding fractions requires a common denominator.
- To be able to add two fractions by considering their lowest common denominator.
- To be able to add two mixed numbers.

Key vocabulary: lowest common denominator (LCD), equivalent fractions, simplify

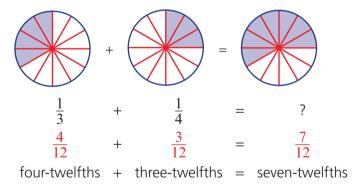
Fractions with the same denominator can be easily added together.



Fractions with different denominators cannot be added together so easily.



But with a common denominator it is possible.



Lesson starter: 'Like' addition

As a class, discuss which of the following pairs of numbers can be simply added together without having to change them in some way.

- **a** 6 goals, 2 goals
- d 6 hours, 5 minutes
- **g** 15 cm, 3 m
- $j = \frac{2}{7}, \frac{3}{7}$

- **b** 11 goals, 5 behinds
- e 21 seconds, 15 seconds
- **h** 2.2 km, 4.1 km
- $k \frac{1}{4}, \frac{1}{2}$

- **c** 56 runs, 3 wickets
- f 47 minutes, 13 seconds
 - i 5 kg, 1680 g
 - $1 \quad 2\frac{5}{12}, \ 1\frac{1}{3}$

You can see that, when adding, the units need to be the same. With fractions, the 'units' are the denominators.

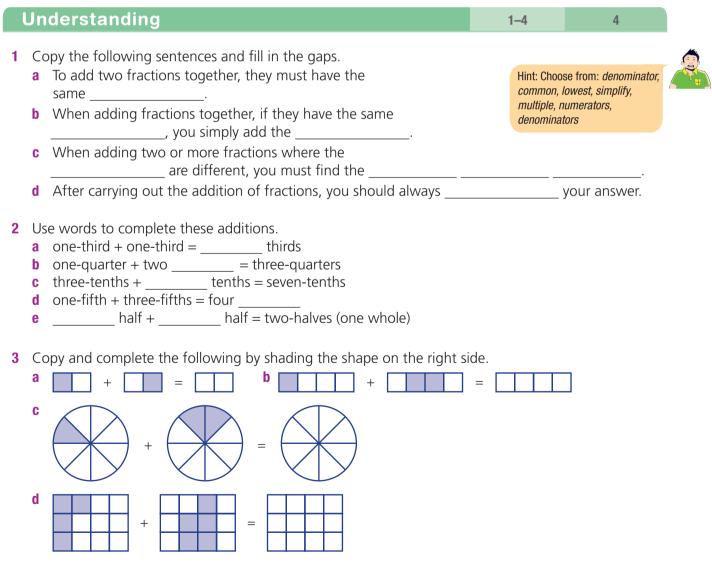
Key ideas

- Fractions can be simplified using addition if they are 'like' fractions; that is, if they have the same denominator.
- If the denominators are equal, add the numerators and retain the denominator. For example: $\frac{3}{7} + \frac{2}{7} = \frac{5}{7}$
- If the denominators are not the same:
 - find the lowest common denominator (LCD)
 - convert fractions to equivalent fractions using the LCD
 - add the numerators and retain the LCD
 - simplify the answer if possible.

For example:
$$\frac{2}{3} + \frac{4}{5} = \frac{10}{15} + \frac{12}{15}$$

= $\frac{22}{15}$ or $1\frac{7}{15}$

Exercise 4E



4E

	4 Answer true (T) or false a $\frac{1}{6} + \frac{3}{6} = \frac{4}{6}$ e $\frac{2}{7} + \frac{2}{7} = \frac{2}{7}$	e (F) for each of the follo b $\frac{2}{5} + \frac{4}{5} = \frac{6}{10}$ f $\frac{7}{12} + \frac{4}{12} = \frac{11}{12}$	powing. c $\frac{1}{11} + \frac{3}{11} = \frac{4}{11}$ g $\frac{3}{10} + \frac{4}{10} = \frac{7}{10}$	d $\frac{3}{5} + \frac{4}{5} =$ h $\frac{1}{100} +$	$=1\frac{2}{5}$ $\frac{2}{100} = \frac{3}{200}$
	Fluency			5–9(½)	5–10(1/2)
)]	Example 9 Adding 'li	ke' fractions			
	Add the following fractio	ns together.			
	a $\frac{1}{5} + \frac{3}{5}$		b $\frac{3}{11} + \frac{5}{11} + \frac{6}{11}$		
	Solution		Explanation		
	a $\frac{1}{5} + \frac{3}{5} = \frac{4}{5}$		The denominators a simply add the nume one-fifth + three-fift	erators.	e'), so
	b $\frac{3}{11} + \frac{5}{11} + \frac{6}{11} = \frac{14}{11}$ = $1\frac{3}{11}$		Denominators are th numerators. We are adding eleve		the

Now you try

Add the following fractions together.

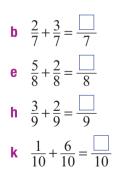
a $\frac{2}{9} + \frac{5}{9}$

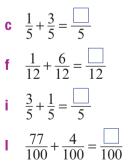
b $\frac{5}{13} + \frac{2}{13} + \frac{11}{13}$

Convert to a mixed number if required.

5 Copy and complete.

а	$\frac{1}{8} + \frac{4}{8} = \frac{1}{8}$
d	$\frac{3}{11} + \frac{6}{11} = \frac{1}{11}$
g	$\frac{3}{15} + \frac{4}{15} = \frac{1}{15}$
j	$\frac{2}{7} + \frac{4}{7} = \frac{2}{7}$





6 Add these fractions and write your answers using mixed numbers.

a $\frac{6}{7} + \frac{3}{7}$	b $\frac{7}{10} + \frac{6}{10}$	c $\frac{2}{5} + \frac{3}{5} + \frac{4}{5}$
d $\frac{12}{19} + \frac{3}{19} + \frac{8}{19}$	e $\frac{7}{10} + \frac{4}{10}$	f $\frac{4}{5} + \frac{3}{5}$
g $\frac{6}{7} + \frac{4}{7}$	h $\frac{8}{11} + \frac{6}{11}$	$i \frac{99}{100} + \frac{2}{100}$

Hint: When you add these fractions, the denominator stays the same.



Example 10 Adding 'unlike' fract	ions
Add the following fractions together. a $\frac{1}{5} + \frac{1}{2}$	b $\frac{3}{4} + \frac{5}{6}$
Solution	Explanation
a $\frac{1}{5} + \frac{1}{2} = \frac{2}{10} + \frac{5}{10}$ = $\frac{7}{10}$	LCD is 10. Write equivalent fractions with the LCD. $\frac{1}{5} \times \frac{2}{2} = \frac{2}{10} \frac{1}{2} \times \frac{5}{5} = \frac{5}{10}$ Denominators are the same, so add numerators.
b $\frac{3}{4} + \frac{5}{6} = \frac{9}{12} + \frac{10}{12}$ = $\frac{19}{12}$ = $1\frac{7}{12}$	LCD is 12. Write equivalent fractions with the LCD. $\frac{3}{4} \times \frac{3}{3} = \frac{9}{12}$ $\frac{5}{6} \times \frac{2}{2} = \frac{10}{12}$ Denominators are the same, so add numerators. Write as a mixed number, if required.

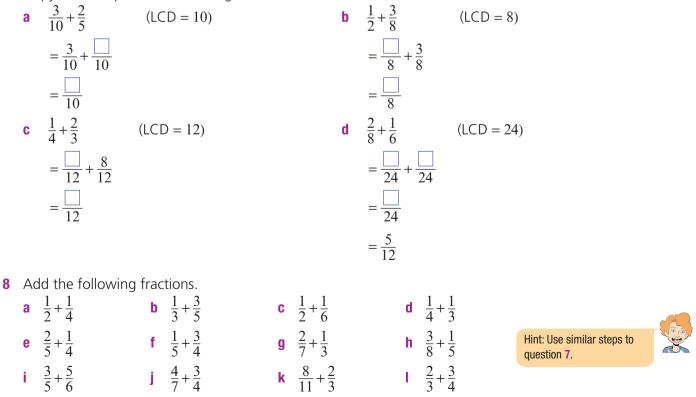
Now you try

Add the following fractions together.

a $\frac{1}{3} + \frac{3}{4}$

b
$$\frac{7}{10} + \frac{11}{15}$$

7 Copy and complete the following additions.



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40	Example 11 Adding mixed number	rs
	Simplify:	
	a $3\frac{2}{3}+4\frac{2}{3}$	b $2\frac{5}{6} + 3\frac{3}{4}$
	Solution	Explanation
	a $3+4+\frac{2}{3}+\frac{2}{3}=7+\frac{4}{3}$	Add the whole number parts together.
	$= 8\frac{1}{3}$	Add the fraction parts together. Noting that $\frac{4}{3} = 1\frac{1}{3}$, simplify the answer.
	Alternatively	$3^{-1}3^{,3}$ simplify the distribution
	$3\frac{2}{3} + 4\frac{2}{3} = \frac{11}{3} + \frac{14}{3}$	First convert to an improper fraction.
	$=\frac{25}{3}$ or $8\frac{1}{3}$	Add the numerators.
	b $2+3+\frac{5}{6}+\frac{3}{4}$	Add the whole number parts together. LCD of 6 and 4 is 12.
	$= 5 + \frac{10}{12} + \frac{9}{12}$	Write equivalent fractions with LCD.
	$=5+\frac{19}{12}$	Add the fraction parts together.
	$= 5 + 1 \frac{7}{12}$	Noting that $\frac{19}{12} = 1\frac{7}{12}$, simplify the answer.
	$= 6\frac{7}{12}$	
	Alternatively	
	$2\frac{5}{6} + 3\frac{3}{4} = \frac{17}{6} + \frac{15}{4}$	First convert to an improper fraction.
	$=\frac{34}{12}+\frac{45}{12}$	Convert using an LCD of 12.
	$=\frac{79}{12}$ or $6\frac{7}{12}$	Add the numerators.
	Now you try	
	Simplify: a $1\frac{2}{5} + 3\frac{1}{5}$	b $2\frac{1}{2} + 3\frac{3}{4}$
	$a = 1\frac{5}{5} + 3\frac{5}{5}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{3}$ $\frac{1}{4}$
	9 Simplify: $1 - 3 - 2 - 1$	12
	5 5 1 1	c $11\frac{1}{4} + 1\frac{2}{4}$ d $1\frac{3}{9} + 4\frac{2}{9}$
	e $5\frac{2}{3}+4\frac{2}{3}$ f $8\frac{3}{6}+12\frac{4}{6}$	g $9\frac{7}{11} + 9\frac{7}{11}$ h $4\frac{3}{5} + 7\frac{4}{5}$
	10 Simplify: $2 \cdot 2^2 + 1^3$ b $5^2 + 1^5$	$a^{1} a^{2}$ $a^{5} 4 a^{3}$
	a $2\frac{2}{3}+1\frac{3}{4}$ b $5\frac{2}{5}+1\frac{5}{6}$	
	e $8\frac{1}{2} + 6\frac{3}{5}$ f $12\frac{2}{3} + 6\frac{4}{9}$	g $17\frac{8}{11} + 7\frac{3}{4}$ h $9\frac{7}{12} + 5\frac{5}{8}$

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a What fraction of the company do they own together?

c If the ticket cost \$10, how much did you pay?

11 Dad gave you $\frac{2}{5}$ of the money for a movie ticket and Mum gave you $\frac{1}{5}$.

a What fraction of the ticket did your parents pay for?

b What fraction of the company is left?

12 Julie owns $\frac{1}{3}$ of a company and Sean owns $\frac{1}{4}$.

Problem-solving and reasoning

b What fraction was left for you to pay?

- **13** Mark spends $\frac{1}{3}$ of the day at school and $\frac{3}{8}$ of the day asleep.
 - **a** What fraction of the day has been used?
 - **b** What fraction of the day is left for fun?
 - **c** How many hours of fun does he get?

6

Fraction networks

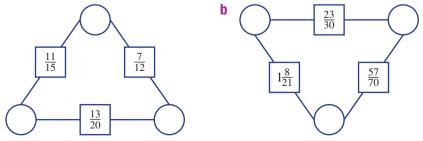
а

а

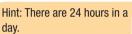
 $\frac{2}{3}$

14 To find the number in each square, add the fractions in the two circles that are joined to it. Fill in the following fraction networks.

15 Now find the fractions in the circles within the following fraction networks.

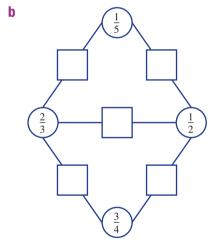






14, 15







4F Subtracting fractions

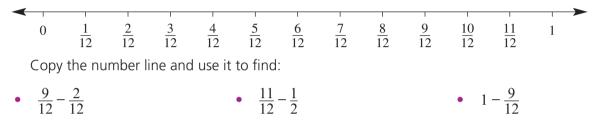
Learning intentions

- To understand that subtracting fractions requires a common denominator.
- To be able to subtract two fractions by considering their lowest common denominator.
- To be able to subtract two mixed numbers.

Key vocabulary: lowest common denominator (LCD), equivalent fractions, simplify

The rules for subtracting fractions are very similar to adding fractions. Before you can subtract, we aim to write the fractions with the same denominator.

Lesson starter: Subtraction on a number line



Key ideas

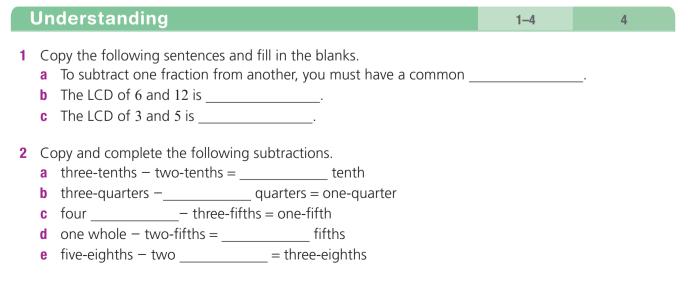
- Fractions can be **simplified** easily using subtraction if they are 'like' fractions with the same denominator.
- The rules for subtracting fractions are similar to those for adding fractions.
- When subtracting mixed numbers, you may need to borrow a whole. For example:

$$7\frac{1}{8} - 2\frac{3}{8} = \frac{1}{8}$$
 is not big enough to have $\frac{3}{8}$ subtracted from it.

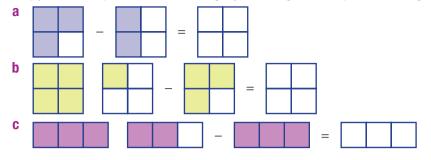
 $6\frac{9}{8} - 2\frac{3}{8}$ Therefore, we choose to borrow a whole from the 7. (6 + 1 = 7)

Alternatively, first convert the mixed numbers to improper fractions.

Exercise 4F



3 Copy and complete the following by shading the shape on the right side.



4 Copy and complete these equations.



-

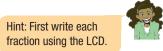
Fluency				5–7(½)	5-8(1/2)	
Example 12 Subt	racting 'like' and	l 'unlike' fractio	ns			
Simplify: a $\frac{7}{9} - \frac{2}{9}$ Solution a $\frac{7}{9} - \frac{2}{9} = \frac{5}{9}$ b $\frac{5}{6} - \frac{1}{4} = \frac{10}{12} - \frac{3}{12}$ $= \frac{7}{12}$		b $\frac{5}{6} - \frac{1}{4}$ Explanation Denominators are the same, therefore we are ready to subtract the second numerator from the first. Find the LCD, which is 12. Write equivalent fractions with the LCD. $\frac{5}{6} \times \frac{2}{2} = \frac{10}{12}$ $\frac{1}{4} \times \frac{3}{3} = \frac{3}{12}$ We have the same denominators now, so subtract second numerator from the first. The denominator stays the same (twelfths).				
Now you try Simplify: a $\frac{8}{11} - \frac{3}{11}$		b $\frac{5}{8} - \frac{1}{2}$				
5 Simplify: a $\frac{5}{7} - \frac{3}{7}$ e $\frac{3}{5} - \frac{3}{5}$ i $\frac{84}{100} - \frac{53}{100}$	f $\frac{6}{9} - \frac{2}{9}$	c $\frac{12}{18} - \frac{5}{18}$ g $\frac{5}{19} - \frac{2}{19}$ k $\frac{23}{25} - \frac{7}{25}$	d $\frac{2}{3} - \frac{1}{3}$ h $\frac{17}{23} - \frac{1}{2}$ l $\frac{7}{10} - \frac{1}{1}$			

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4F

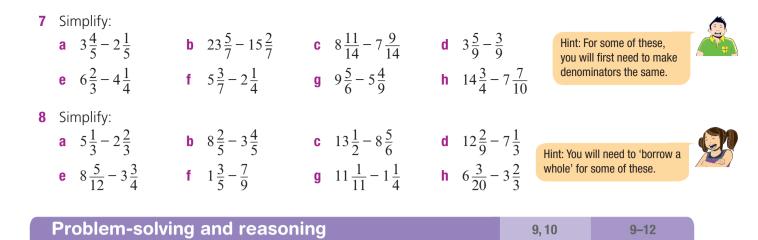
Simplify:			
a $\frac{2}{3} - \frac{1}{4}$	b $\frac{3}{5} - \frac{1}{2}$	c $\frac{3}{5} - \frac{3}{6}$	d $\frac{4}{7} - \frac{1}{4}$
e $\frac{1}{2} - \frac{1}{3}$	f $\frac{3}{4} - \frac{1}{9}$	g $\frac{8}{11} - \frac{1}{3}$	h $\frac{4}{5} - \frac{2}{3}$
i $\frac{3}{4} - \frac{5}{8}$	j $\frac{11}{20} - \frac{2}{5}$	k $\frac{5}{12} - \frac{7}{18}$	$\frac{7}{9} - \frac{2}{3}$



Example 13 Subtracting mixed numbers Simplify: **b** $8\frac{1}{5} - 4\frac{3}{4}$ a $5\frac{2}{3} - 3\frac{1}{4}$ Solution **Explanation a** $5\frac{2}{3} - 3\frac{1}{4} = \left(5 + \frac{2}{3}\right) - \left(3 + \frac{1}{4}\right)$ A mixed number is the addition of a whole number and a proper fraction. $=(5-3)+\left(\frac{2}{3}-\frac{1}{4}\right)$ Group whole numbers and group proper fractions. Simplify whole numbers. $=2+\left(\frac{8}{12}-\frac{3}{12}\right)$ Make denominators the same. $\frac{2}{3} \times \frac{4}{4} = \frac{8}{12}, \frac{1}{4} \times \frac{3}{3} = \frac{3}{12}$ $=2\frac{5}{12}$ Borrowing a whole was not required. Alternatively $5\frac{2}{3} - 3\frac{1}{4} = \frac{17}{3} - \frac{13}{4}$ First convert to improper fractions. $=\frac{68}{12}-\frac{39}{12}$ Find and use the LCD. $=\frac{29}{12}$ or $2\frac{5}{12}$ Subtract the numerators. **b** $8\frac{1}{5} - 4\frac{3}{4} = 8\frac{4}{20} - 4\frac{15}{20}$ Convert to twentieths: $\frac{1}{5} \times \frac{4}{4} = \frac{4}{20}, \frac{3}{4} \times \frac{5}{5} = \frac{15}{20}$ $=7\frac{24}{20}-4\frac{15}{20}$ Borrow a whole from the 8 so that the numerators can be subtracted. $=3\frac{9}{20}$ $8\frac{4}{20} = 7 + 1 + \frac{4}{20} = 7 + \frac{20}{20} + \frac{4}{20} = 7\frac{24}{20}$ Subtract whole numbers, subtract fractions. Alternatively $8\frac{1}{5} - 4\frac{3}{4} = \frac{41}{5} - \frac{19}{4}$ First convert to improper fractions. $=\frac{164}{20}-\frac{95}{20}$ Find and use the LCD. $=\frac{69}{20}$ or $3\frac{9}{20}$ Subtract the numerators. Now you try

Simplify: **a** $2\frac{4}{5} - 1\frac{1}{2}$

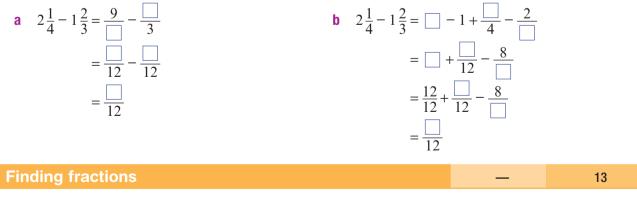
b $5\frac{3}{5} - 1\frac{3}{4}$



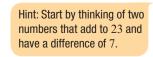
- **9** A family block of chocolate is made up of 60 small squares of chocolate. Marcia eats 10 squares, Jon eats 9 squares and Holly eats 5 squares. What fraction of the block of chocolate is left?
- **10** Three friends split a restaurant bill. One pays $\frac{1}{2}$ of the bill and one pays $\frac{1}{3}$ of the bill. What fraction of the bill must the third friend pay?



- 11 A full container of flour weighs $\frac{4}{5}$ kg. The empty container weighs $\frac{1}{20}$ kg. How much does the flour weigh?
- **12** Copy and complete these two subtractions, which use two different techniques. State which technique you prefer, giving reasons.



```
13 Two fractions have a sum of \frac{23}{24} and a difference of \frac{7}{24}.
Can you find the two fractions?
```



4G Multiplying fractions

Learning intentions

- To understand that multiplying fractions is easier if you first cancel common factors from numerators and denominators in each fraction.
- To know that a whole number can be written as a fraction with a denominator of 1.
- To be able to multiply fractions, mixed numbers and/or whole numbers, giving an answer in simplest form.

Key vocabulary: factor, simplify, mixed number, improper fraction

When we multiply whole numbers together, we end up with a number larger than (or equal to) the ones we started with.

 $2 \times 3 = 6$ $5 \times 7 = 35$ $15 \times 1 = 15$

But when we multiply fractions together, things can be different. Consider half of half an apple, for example, which results in a smaller fraction compared to the original fractions.





Lesson starter: Parts of a circle

• How does this diagram show half of half a circle?



• What is half of three-quarters of a circle?



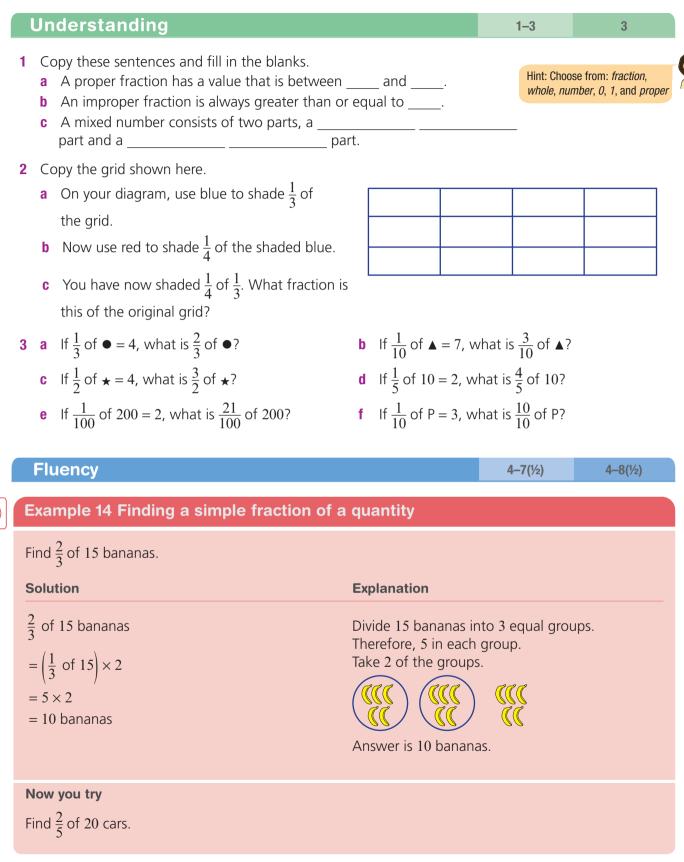
Use diagrams to investigate other fraction multiplications.

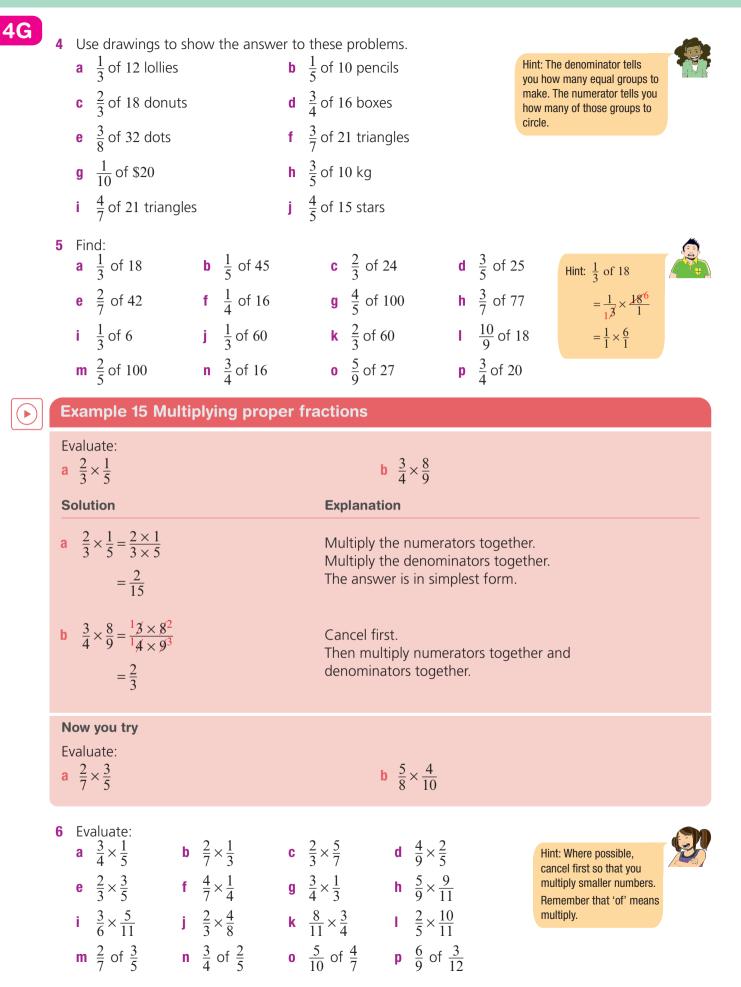
What shortcut (or rule) can you find to help multiply fractions together?

Key ideas

- Fractions do *not* need to have the same denominator to be multiplied together.
- To multiply fractions, multiply the numerators together and multiply the denominators together.
 - In symbols: $\frac{a}{b} \times \frac{c}{d} = \frac{a \times c}{b \times d}$
- If possible, 'simplify' or 'cancel' fractions before multiplying. (Remember, you can only cancel numerators with denominators.)
- Mixed numbers must be changed to improper fractions before multiplying.
- Final answers should be written in simplest form.

Exercise 4G





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7	Find:			
	a $\frac{5}{2} \times \frac{7}{3}$	b $\frac{6}{5} \times \frac{11}{7}$	c $\frac{6}{4} \times \frac{11}{5}$	$d \frac{9}{6} \times \frac{13}{4}$
	e $\frac{8}{5} \times \frac{10}{3}$	f $\frac{21}{4} \times \frac{8}{6}$	g $\frac{10}{7} \times \frac{21}{5}$	h $\frac{14}{9} \times \frac{15}{7}$
	i $\frac{8}{5} \times \frac{1}{2}$	$\mathbf{j} \frac{4}{3} \times \frac{1}{5}$	k $\frac{3}{2} \times \frac{1}{4}$	$\frac{3}{4} \times \frac{5}{3}$

Example 16 Multiplying mixed numbers

Hint: Multiply improper fractions just as if they were proper fractions, then simplify your answer.

A
REP

Find: a $2\frac{1}{3} \times 1\frac{2}{5}$ **b** $6\frac{1}{4} \times 2\frac{2}{5}$ **Solution Explanation a** $2\frac{1}{3} \times 1\frac{2}{5} = \frac{7}{3} \times \frac{7}{5}$ Convert mixed numbers to improper fractions. Multiply numerators together. $=\frac{49}{15}$ Multiply denominators together. $=3\frac{4}{15}$ Write the answer as a mixed number if required. **b** $6\frac{1}{4} \times 2\frac{2}{5} = \frac{525}{14} \times \frac{12^3}{5^1}$ Convert to improper fractions. Simplify fractions by cancelling. Multiply numerators and denominators together. $=\frac{15}{1}$ = 15Write the answer in simplest form. Now you try Find: a $1\frac{3}{4} \times 2\frac{2}{3}$ **b** $4\frac{2}{5} \times 2\frac{1}{2}$ 8 Find: **a** $1\frac{3}{5} \times 2\frac{1}{3}$ **b** $1\frac{1}{7} \times 1\frac{2}{9}$ **c** $3\frac{1}{4} \times 2\frac{2}{5}$ **d** $4\frac{2}{3} \times 5\frac{1}{7}$ Hint: First convert mixed numbers to improper fractions. **e** $\frac{6}{5} \times \frac{8}{3}$ **f** $\frac{1}{2} \times \frac{3}{8}$ **g** $\frac{3}{4}$ of $5\frac{1}{3}$ **h** $7\frac{1}{2} \times 4\frac{2}{5}$ i $\frac{3}{7} \times \frac{2}{3}$ j $1\frac{1}{2} \times 2\frac{1}{4}$ k $\frac{8}{9} \times \frac{6}{20}$ l $\frac{15}{4} \times \frac{8}{5}$

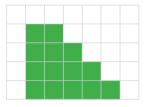
Problem-solving and reasoning

- 9, 10 10–12
- 9 At one secondary college, $\frac{2}{5}$ of the Year 7 students are boys.
 - a What fraction of the Year 7 students are girls?
 - **b** If there are 120 Year 7 students, how many boys and girls are there?

- 4<u>G</u>
- 10 Julie was injured during the netball season. She was able to play only $\frac{2}{3}$ of the matches. The season consisted of 21 matches. How many games did Julie miss as a result of injury?



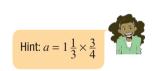
- **11** a Blake spends $\frac{3}{4}$ of an hour on his Maths homework. How many minutes is this?
 - **b** Perform this calculation: $60 \div 4 \times 3$. What do you notice?
 - **c** Now find the number of minutes in $\frac{2}{3}$ of an hour in a similar way.
- 12 The diagram shows a plan of Joel's garden. The shaded section is grass. The rest is paved.



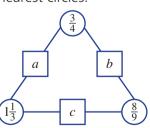
- **a** What fraction of the garden is grass?
- **b** If half the grass is removed and replaced with pavers, what fraction of the garden will remain grass?

Missing products

13 a To find the number in each square, multiply the numbers in the two nearest circles.



13



b Challenge yourself. What does a + b + c equal? Check using a calculator.

H

4H Dividing fractions

- To understand that dividing fractions involves multiplying by a reciprocal. •
- To be able to find the reciprocal of a fraction or a mixed number.
- To be able to divide fractions, mixed numbers and/or whole numbers, giving an answer in simplest form.

Key vocabulary: reciprocal, mixed number, improper fraction

Remember that division is the opposite operation to multiplication. Thinking of division as 'how many' helps us to understand dividing fractions.

For example, to find $\frac{1}{2} \div \frac{1}{4}$, think: How many quarters are in a half?

Consider a strip of paper that is divided into four equal sections. Half the strip is shaded.

There are two quarters in our half. Therefore, $\frac{1}{2} \div \frac{1}{4} = 2$.

When it is half-time in an AFL game, you have played two quarters. This is another way of showing that $\frac{1}{2} \div \frac{1}{4} = 2.$

Lesson starter: Using division patterns

Use patterns to help you find the missing numbers.

$$20 \div 4 = 5$$
$$20 \div 2 = 10$$
$$20 \div 1 = 20$$
$$20 \div \frac{1}{2} = 20$$
$$20 \div \frac{1}{4} = 20$$

Can you see an easy way to find the following?

• $12 \div \frac{1}{4}$ • $20 \div \frac{1}{8}$ • $10 \div \frac{1}{3}$ $30 \div \frac{1}{2}$

Key ideas

CORE Year 7

- We use multiplication to help with the division of fractions.
 - Dividing by $\frac{1}{2}$ is like multiplying by 2.

For example: $20 \div \frac{1}{2} = 40$ and $20 \times 2 = 40$

- A reciprocal is a fraction in which the numerator and denominator have changed places.
 - The reciprocal of x is $\frac{1}{x}$.
 - 2 is the reciprocal of $\frac{1}{2}$ (and vice versa).
 - The reciprocal of $\frac{3}{5}$ is $\frac{5}{3}$.

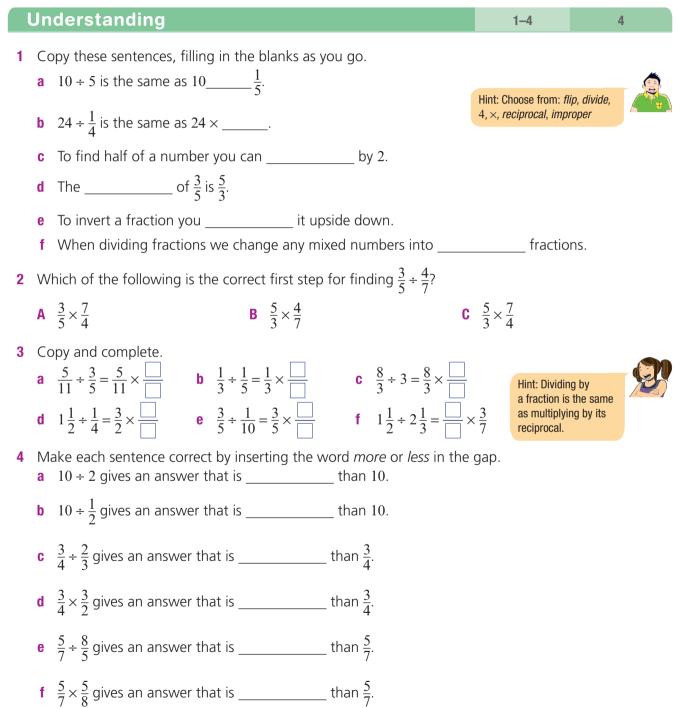
Essential Mathematics for the Victorian Curriculum

• The reciprocal of $\frac{1}{4}$ is $\frac{4}{1} = 4$.

4H

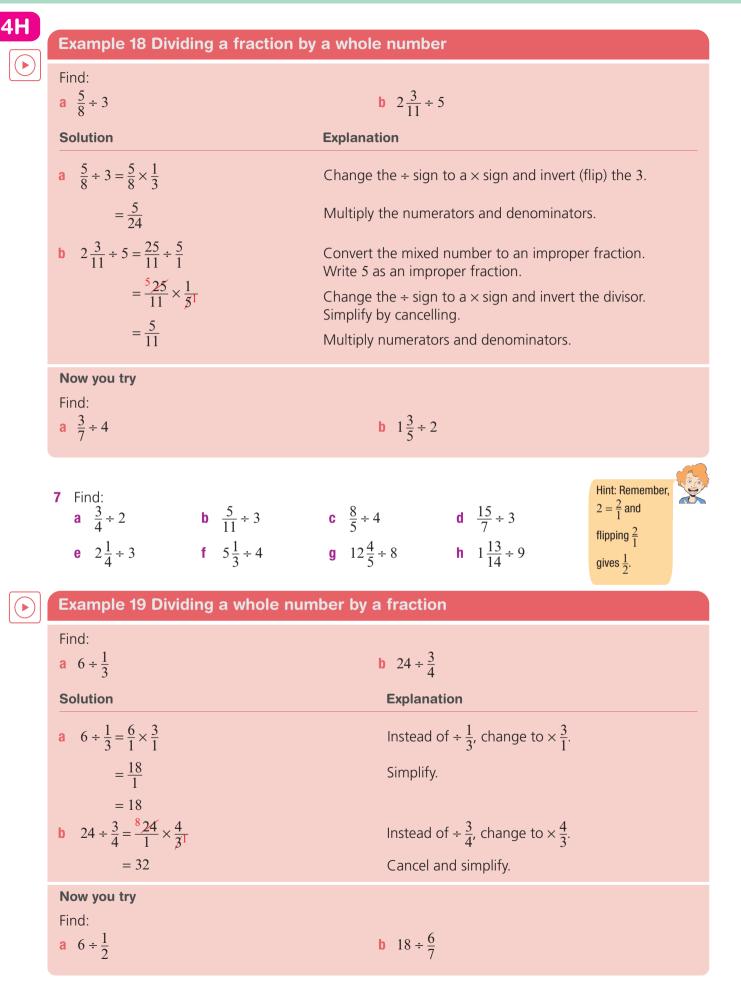
- Finding a reciprocal is called inverting, flipping or turning the fraction upside down.
- To divide by a fraction, you can multiply by its reciprocal. For example: $\frac{1}{2} \div \frac{3}{4} = \frac{1}{2} \times \frac{4}{3}$ $\frac{2}{5} \div \frac{1}{3} = \frac{2}{5} \times \frac{3}{1}$
- When dividing, or finding reciprocals, mixed numbers must be changed to improper fractions.

Exercise 4H



1	Fluency			5-8(1/2)	5-9(1/2)	
	Example 17 Finding re	eciprocals				
	State the reciprocal of the following.					
	a $\frac{2}{3}$	b 5	c 1 $\frac{3}{7}$			
	Solution		Explanation			
	a Reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$.		The numerator and denominator are swapped. (Flip the fraction upside down.)			
	b Reciprocal of 5 is $\frac{1}{5}$.		Think of 5 as $\frac{5}{1}$ and then invert (flip) it.			
	c Reciprocal of $1\frac{3}{7}$ is $\frac{7}{10}$.		Convert $1\frac{3}{7}$ to the improper fraction $\frac{10}{7}$, and then invert.			
	Now you try State the reciprocal of the following.					
	a $\frac{7}{9}$	b 13	c $2\frac{3}{8}$			
	5 What is the reciprocal of each of the following?					
	a $\frac{5}{7}$	b $\frac{3}{5}$	c $\frac{2}{9}$	d $\frac{1}{8}$		
	e $\frac{1}{3}$	f $\frac{1}{10}$	g $\frac{3}{10}$	h $\frac{5}{4}$		
	i $\frac{12}{1}$	j $\frac{101}{1}$	k $\frac{1}{9}$	I 1		
	6 First change each of the following to an improper fraction, then find its reciprocal.					
	a $1\frac{1}{2}$	b $1\frac{1}{5}$	c $2\frac{1}{2}$	d $1\frac{2}{5}$		
	e $2\frac{3}{4}$	f $2\frac{1}{3}$	g $4\frac{3}{5}$	h $1\frac{5}{6}$		

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8	Find: a $5 \div \frac{1}{4}$	b $7 \div \frac{1}{3}$	c $10 \div \frac{1}{10}$	d $24 \div \frac{1}{5}$
	e $12 \div \frac{2}{5}$	f $15 \div \frac{3}{8}$	g $14 \div \frac{7}{2}$	h $10 \div \frac{3}{2}$

 (\mathbf{b})

Example 20 Dividing a fraction by a fraction

Example 20 Dividing	a fraction by a	Traction					
Find: a $\frac{3}{5} \div \frac{3}{8}$		b $2\frac{2}{5} \div 1\frac{3}{5}$					
Solution	Ex	Explanation					
a $\frac{3}{5} \div \frac{3}{8} = \frac{13}{5} \times \frac{8}{3^1}$ $= \frac{8}{5}$	af	Change the \div to \times and invert the divisor (the fraction <i>after</i> the division sign). Cancel and simplify.					
$= 1\frac{3}{5}$ b $2\frac{2}{5} \div 1\frac{3}{5} = \frac{12}{5} \div \frac{8}{5}$ $= \frac{312}{15} \times \frac{51}{8^2}$		onvert mixed numbers to im nange the ÷ sign to a × sign					
$=\frac{3}{2}=1\frac{1}{2}$	Ca	ancel, multiply and simplify.					
Now you try							
Find: a $\frac{4}{7} \div \frac{3}{14}$		b $2\frac{1}{2} \div 1\frac{1}{4}$					
9 Find: a $\frac{2}{7} \div \frac{2}{5}$ d $\frac{2}{3} \div \frac{8}{9}$	b $\frac{1}{5} \div \frac{1}{4}$ e $2\frac{1}{4} \div 1\frac{1}{3}$	c $\frac{3}{7} \div \frac{6}{11}$ f $4\frac{1}{5} \div 3\frac{3}{10}$	Hint: First convert any mixed numbers to improper fractions.				
g $12\frac{1}{2} \div 3\frac{3}{4}$	h $9\frac{3}{7} \div 12\frac{4}{7}$	i $1\frac{1}{4} \div \frac{5}{6}$					

4H

Problem	n-solving	and rea	asoning
---------	-----------	---------	---------

10 If $2\frac{1}{4}$ leftover pizzas are to be shared between three friends, what fraction of pizza will each friend receive?



11 A car travels 180 km in $1\frac{1}{2}$ hours. Calculate this car's speed. Your answer will be in km/h.



10-12

10, 11

12 Ceanna colours $\frac{1}{4}$ of her circle pink.



She divides the rest of the circle into three equal sectors and colours them blue, purple and green. What fraction of the circle is purple?

A puzzling question!

13 Why do I love fractions?

To find out, work out the value of each of these 15 letters.

$$A = \frac{2}{3} + 1\frac{1}{3} \qquad 0 = \frac{2}{7} + \frac{2}{7} \qquad E = \frac{1}{4} + \frac{1}{5}$$

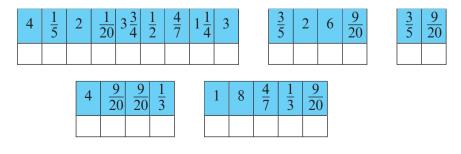
$$N = 2 - \frac{3}{4} \qquad M = \frac{1}{10} + \frac{1}{2} \qquad C = \frac{1}{4} - \frac{1}{5}$$

$$F = \frac{2}{3} \text{ of } 6 \qquad R = \frac{1}{2} - \frac{3}{10} \qquad S = \frac{1}{9} \text{ of } 27$$

$$T = 2\frac{1}{2} + 1\frac{1}{4} \qquad I = \frac{5}{6} - \frac{1}{3} \qquad L = \frac{7}{12} - \frac{1}{4}$$

$$K = 1\frac{1}{2} \times 4 \qquad W = \frac{5}{6} \times \frac{6}{5} \qquad H = 2 \div \frac{1}{4}$$

Now use those values to decode the answer.



Want to know why love fractions?

13

Essential Mathematics for the Victorian Curriculum CORE Year 7



4A	1 For the follo	owing list of fraction	ons determin	e if they are r	oroner fract	ions (P) impr	oper fractions (I)
TA	or whole n	umbers (W).					
	a $\frac{3}{7}$	b $\frac{13}{9}$	C 25	5	d $\frac{4}{2}$	e	$\frac{1}{100}$
4B		bllowing fractions			45		32
	a $\frac{14}{20}$	b $\frac{12}{21}$	c 1	00	d $\frac{45}{30}$	е	48
4B	3 Which of th	ne following fraction	ons is equivale	ent to $\frac{5}{35}$?			
	A $\frac{5}{70}$	B $\frac{15}{70}$	5	C $\frac{1}{5}$		D $\frac{1}{7}$	
40	2	ese mixed numbers	4	fractions.			
	a $3\frac{2}{7}$	b 11	49				
40		ese improper fracti	-	numbers.			
	a $\frac{33}{10}$	b $\frac{23}{3}$	-				
4D	6 Decide whi a $\frac{3}{8}$ and $\frac{5}{8}$	ch fraction is the la	argest in each	pair. b $\frac{1}{3}$ an	d 1		
	0 0			5	'		
	c $\frac{5}{11}$ and	5		d $\frac{3}{4}$ an	$\frac{10}{16}$		
4D	7 Place the fo	llowing fractions i	n ascending o	order. $\frac{2}{3}, \frac{3}{5}, \frac{5}{6}$	$\frac{8}{15}$		
4E		lowing fractions to	-			a 1	
	a $\frac{4}{13} + \frac{5}{13}$		b $\frac{3}{7} + \frac{1}{3}$		C	$3\frac{2}{5} + 2\frac{1}{4}$	
4F	9 Simplify:		7 0			2 5	
	a $\frac{9}{11} - \frac{5}{11}$		b $\frac{7}{8} - \frac{2}{3}$		C	$15\frac{3}{4} - 9\frac{5}{12}$	
4G	10 Evaluate:		10 0			1 2	
	a $\frac{3}{7} \times \frac{3}{4}$		b $\frac{10}{3} \times \frac{9}{5}$		C	$3\frac{1}{3} \times 1\frac{2}{5}$	
4H		ciprocal of the fol				- 3	
	a $\frac{2}{9}$		b 5		C	$3\frac{3}{4}$	
	12 Evaluate: a $\frac{6}{11} \div 3$	b 8	<u>+ 1</u>	c $\frac{2}{7} \div \frac{2}{7}$	3	d $5\frac{1}{4}$ ÷	$-2\frac{1}{2}$
	11 1		4	7 2	5	- 4	-3

Essential Mathematics for the Victorian Curriculum CORE Year 7

4I Fractions and percentages

Learning intentions

- To understand that a percentage can be thought of as a fraction with a denominator of 100.
- To be able to convert a percentage to a fraction in simplest form.
- To be able to convert a fraction to a percentage.

Key vocabulary: per cent, percentage, denominator, equivalent fraction

Percentages are used in many day-to-day situations including test results, discounts and food ingredients.

A percentage is another way of writing a fraction with a denominator of 100. For example, 87 per cent simply means 87 out of 100, so:

$$87\% = \frac{87}{100}$$

Lesson starter: Student ranking

Five students each completed a different Mathematics test.

- Matthew scored 15 out of a possible 20 marks.
- Mengna scored 36 out of a possible 50 marks.
- Maria scored 17 out of a possible 25 marks.
- Marcus scored 7 out of a possible 10 marks.
- Melissa scored 128 out of a possible 200 marks.

Change these test results to equivalent scores out of 100, and therefore state the percentage test score for each student. Why are percentages useful in this situation?

Key ideas

The % symbol means per cent. This comes from the Latin per centum which means 'out of 100'.

For example: 75 per cent means 75 out of 100. That is, $75\% = \frac{75}{100}$

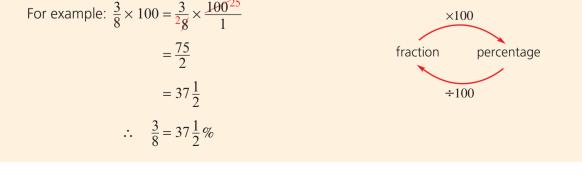
We can write percentages as fractions by changing the % sign to a denominator of 100 (meaning out of 100).

For example: $37\% = \frac{37}{100}$

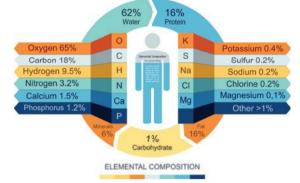
We can use equivalent fractions to convert fractions to percentages.

For example:
$$\frac{1}{4} = \frac{25}{100} = 25\%$$

To convert any fraction to a percentage, multiply by 100.



THE HUMAN BODY



4

Hint: The total is 100%

1-4

It is useful to know the following common percentages and their equivalent fractions.

Fraction	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{4}$	$\frac{1}{5}$	$\frac{1}{8}$	$\frac{2}{3}$	$\frac{3}{4}$	1
Percentage	50%	$33\frac{1}{3}\%$	25%	20%	$12\frac{1}{2}\%$	$66\frac{2}{3}\%$	75%	100%

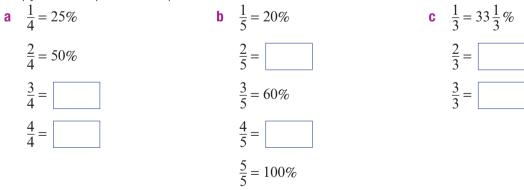
Exercise 4I

Understanding

- 1 Change these test results to equivalent scores out of 100, and therefore state the percentage.
 - **a** 7 out of 10 =_____ out of 100 =_____ %
 - **b** 24 out of 50 =____ out of 100 =____ %
 - **c** 12 out of 20 =_____ out of 100 =_____ %
 - **d** 1 out of 5 =_____ out of 100 =_____ %
 - **e** 80 out of 200 = _____ out of 100 = _____ %
 - **f** 630 out of 1000 =_____ out of 100 =_____ %



2 Copy and complete these patterns.



- **3** a If 14% of students in Year 7 are absent due to illness, what percentage of Year 7 students are at school?
 - **b** If 80% of the Geography project has been completed, what percentage still needs to be finished?
- 4 Zoe scored 100% on her fractions test. The test was out of 25. What was Zoe's mark?

41	Fluency			5-7(1/2) 5-8(1/2)
	Example 21 Convertir	ng percentages to f	ractions	
	Express these percentages a 17%	as fractions in their sim	olest form. c 140%	
	Solution	0 3070	Explanation	
	a $17\% = \frac{17}{100}$		Change % sign to a deno	ominator of 100.
	b $36\% = \frac{36}{100}$		Change % sign to a deno	ominator of 100.
	$=\frac{9\times4}{25\times4}$		Cancel HCF.	
	$=\frac{9}{25}$		Answer is now in simples	st form.
	c $140\% = \frac{140}{100}$		Change % sign to a dence	ominator of 100.
	$=\frac{7\times20}{5\times20}$		Cancel HCF.	
	$=\frac{7}{5}=1\frac{2}{5}$		Convert answer to a mixe required.	ed number if
	Now you try Express these percentages a 29%	as fractions in their sim b 60%	olest form. c 190%	
	 5 Express these percentage a 11% b 71% g 15% h 88% m 70% n 90% 	c 43% d 4	49% e 25% f 19% k 21% I	30% 50%
	6 Express these percentag a 120% b 180% g 316% h 840%	c 237% d 4	their simplest form. 101% e 175% f 205% k 310% l	110% 350%
	Example 22 Convertin	ng to percentages t	hrough equivalent fra	ctions
	Convert the following frace a $\frac{5}{100}$	tions to percentages.	b $\frac{11}{25}$	
	Solution		Explanation	
	a $\frac{5}{100} = 5\%$		Denominator is already 1 write the number as a pe	
	b $\times 4$ $\frac{11}{25} = \frac{44}{100} = 44\%$ $\times 4$		We need the denominate Therefore, multiply nume by 4 to get an equivalent	or to be 100. erator and denominator

Essential Mathematics for the Victorian Curriculum CORE Year 7

	ollowing fraction:	s to percentages.		
a $\frac{37}{100}$			b $\frac{27}{25}$	
100			20	
	ese fractions to p		equivalent fractions.	
9 8	ь 9		-	Hint: First write with
a $\frac{98}{100}$	b $\frac{9}{100}$	c $\frac{79}{100}$	d $\frac{56}{100}$	Hint: First write with denominator of 100.
9 8	ь 9		-	
a $\frac{98}{100}$	b $\frac{9}{100}$	c $\frac{79}{100}$	d $\frac{56}{100}$	

Example 23 Converting to perce	entages by multiplying by 100
Convert the following fractions to perce	entages.
a $\frac{3}{8}$	b $3\frac{3}{5}$
Solution	Explanation
a $\frac{3}{28} \times \frac{100^{25}}{1} = \frac{75}{2}$ = $37\frac{1}{2}$	Multiply by 100. Simplify by cancelling HCF.
$\therefore \frac{3}{8} = 37\frac{1}{2}\%$ b $3\frac{3}{5} \times \frac{100}{1} = \frac{18}{15} \times \frac{100^{20}}{1}$	Convert mixed number to improper fraction. Cancel and simplify.
= 360 $\therefore 3\frac{3}{5} = 360\%$	
Now you try	

Convert the following fractions to percentages.

a $\frac{5}{12}$	b $2\frac{3}{4}$	

8 Convert these fractions to percentages by multiplying by 100.

а	$\frac{1}{8}$	b	$\frac{1}{3}$	C	$\frac{4}{15}$	d	$\frac{10}{12}$
е	$1\frac{3}{20}$	f	$4\frac{1}{5}$	g	$2\frac{36}{40}$	h	$\frac{13}{40}$

41

Problem-solving and reasoning

10-12

13

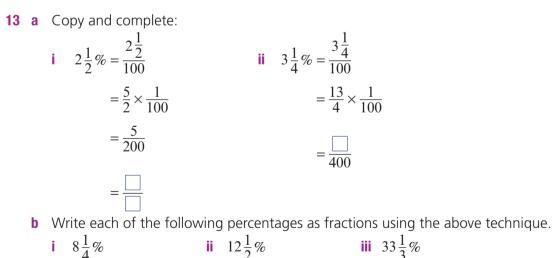
9,10

- **9** A bottle of lemonade is only 25% full.
 - a What fraction of the bottle has been consumed?
 - **b** What percentage of the bottle has been consumed?
 - **c** What fraction of the bottle is left?
 - d What percentage of the bottle is left?



- 10 A lemon tart is cut into eight equal pieces. What percentage of the tart does each piece represent?
- 11 Petrina scores 28 out of 40 on her fractions test. What is her percentage score?
- **12** The Heathmont Hornets basketball team have won 14 out of 18 games. They still have two games to play. What is the smallest and the largest percentage of games the Hornets could win for the season?

More-challenging conversions



10 A lemon tart is cut into e

'of' means \times

 $25\% \text{ of } 60 = \frac{25}{100} \times \frac{60}{1}$

= 15

4J Finding a percentage of a number

Learning intentions

- To understand that finding percentages of a number generally involves multiplying by a fraction.
- To be able to find a percentage of a number.
- To be able to apply percentages to worded problems.

Key vocabulary: percentage, 'of', fraction

Throughout life you will come across many examples where you need to calculate percentages of a quantity. Examples include retail discounts, interest rates, personal improvements and salary increases.

Lesson starter: Percentages in your head

It is a useful skill to be able to calculate percentages mentally. Calculating 10% or 1% is often a good starting point. You can then multiply or divide these values to quickly arrive at other percentage values.

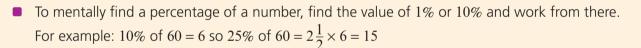
With a partner, and using mental arithmetic only, calculate 10% of each of these amounts.

а	\$120	b	\$35	C	\$160	d	\$90	е	\$300	f	\$40
g	\$80	h	\$420	i.	\$1400	j	\$550	k	\$200	1	\$60

How did you find 10% of an amount mentally?

Key ideas

- To find the **percentage** of a number:
 - 1 Express the required percentage as a **fraction**.
 - 2 Change the 'of' to a multiplication sign.
 - **3** Express the number as a fraction.
 - **4** Follow the rules for multiplication of fractions.



Exercise 4J

Understanding 1 - 43, 4 1 Copy and complete the following. **a** To find 10% of \$20, you can use $20 \div \square = 2$. **b** To find 25% of \$20, you can use $20 \div 4 = \square$. **c** To find 50% of \$20, you can use $20 \div$ = . **2** a If 10% of $\star = 3$, find 20% of \star . **b** If 1% of \blacktriangle = 7, find 5% of \blacktriangle . **c** If 50% of $\bullet = 8$, find 100% of \bullet . **3** Use mental strategies to find: a 10% of \$500 **b** 1% of \$900 c 25% of 84 kilograms **d** 50% of 7 days e 75% of 84 kilograms f 20% of 35 minutes What is 100% of 8 hours?

1	п
-	

4J	Fluency		5–6(½), 7 5–6(½), 7, 8(½)
	Example 24 Finding the percer	tage of a number	
	Find: a 30% of 50 Solution	b 15% of 400 Explanation	
	a 30% of $50 = \frac{30}{2100} \times \frac{50^{1}}{1}$ = $\frac{30}{2} = 15$	Write 30% as a fracti The word 'of' tells us Cancel and simplify.	
	Alternatively 10% of 50 = 5 30% of 50 = 15 b 15% of 400 = $\frac{15}{1.100} \times \frac{400^4}{1}$ $= \frac{15 \times 4}{1} = 60$ Alternatively 10% of 400 = 40, 5% of 400 = 20	10% is easy to find m Multiply 10% by 3 to Write 15% as a fracti 'Of' means ×. Cancel and simplify. Find 10% mentally. H	find 30%. on.
	15% of 400 = 60 Now you try Find:	Add 10% and 5% to	
	a 60% of 80	b 35% of 260	
	 5 Find: a 50% of 140 b 10% of 360 e 25% of 40 f 25% of 28 j 5% of 80 m 11% of 200 n 21% of 400 	c 20% of 50 d 30% of g 75% of 200 h 80% of k 5% of 880 l 2% of o 12% of 300 p 9% of	f 250 9500 = $\frac{50}{100} \times \frac{140}{1}$
	6 Find: a 120% of 80 b c 110% of 60 d e 125% of 12 f g 146% of 50 h	150% of 400 400% of 25 225% of 32 3000% of 20	Hint: $120\% = \frac{120}{100}$

7 Match each question with the correct answer.

Questions	Ansv	vers
a 10% of \$200 b 5% of \$500	\$8	\$30
c 20% of \$120 d 30% of \$310	\$16	\$40
e 10% of \$80 f 10% of \$160	\$20	\$44
g 50% of \$60 h 1% of \$6000	\$24	\$60
i 20% of \$200 j 50% of \$88	\$25	\$93

Hint: Remember that the

9,10

answers need to include units

10-12

- 8 Find:
 - **a** 30% of \$140
 - c 15% of 60 kilograms
 - e 20% of 40 minutes
 - g 5% of 30 grams
 - i 120% of 120 seconds

Problem-solving and reasoning

9 Harry scored 70% on his percentages test. If the test is out of 50 marks, how many marks did Harry score?

b 10% of 240 millimetres

f 80% of 500 centimetres

d 2% of 4500 tonnes

h 25% of 12 hectares



- **10** In a student survey, 80% of students said they received too much homework. If 300 students were surveyed, how many students felt they get too much homework?
- 11 25% of teenagers say their favourite fruit is watermelon. In a survey of 48 teenagers, how many would write watermelon as their favourite fruit?



- **12** At Gladesbrook College, 10% of students walk to school, 35% of students catch public transport and the rest are driven to school. If there are 1200 students at the school, find how many students:
 - a walk to school
 - **b** catch public transport
 - c are driven to school

Percentage challenge

13

- **13 a** Which is larger: 60% of 80 or 80% of 60?
 - **b** Tom did the following calculation: $120 \div 4 \div 2 \times 3$. What percentage of 120 did Tom find?
 - c i If 5% of an amount is \$7, what is 100% of the amount?
 - ii If 25% of an amount is \$3, what is $12\frac{1}{2}\%$ of the amount?

4K Expressing a quantity as a proportion

Learning intentions

- To understand that finding one number as a proportion of a total generally involves dividing and converting to a fraction.
- To be able to find one value as a proportion or as a percentage of a total. **Key vocabulary:** proportion, 'out of', fraction

Sometimes we want to know the proportion of a certain quantity compared to a given total or another quantity. Proportions can be expressed using a fraction, percentage or ratio. The Earth's surface, for example, is about 70% ocean. So, the proportion of land could be written as 30% (as a percentage) or $\frac{3}{10}$ (as a fraction).



S Lesson starter: Municipal parkland

A municipal area is set aside in a new suburb and is to be divided into three main parts. The total area is $10\,000$ m² and the three parts are to be divided as follows:

Parkland: 6000 m² Shops: 2500 m² Playground and skate park: 1500 m²

- Express each area as a proportion of the total, first as a fraction and then as a percentage.
- If $\frac{3}{5}$ of the parkland is to be a lake, what percentage of the total area is the lake?

Key ideas

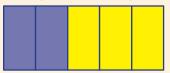
- A **proportion** is a part of a whole and can be expressed as a fraction or percentage.
- To express one quantity as a fraction of another:

```
Fraction = \frac{\text{amount}}{\text{total}}
```

• To express one quantity as a percentage of another:

```
\mathsf{Percentage} = \frac{\mathsf{amount}}{\mathsf{total}} \times \frac{100}{1} \%
```

An object or quantity divided into parts can be analysed using fractions and percentages.



Purple fraction =
$$\frac{2}{5}$$

Purple percentage = $\frac{2}{5} \times \frac{100}{1}\% = 40\%$

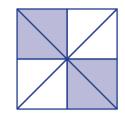
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Exercise 4K

Understanding

- 1 Write these fractions as percentages by multiplying by 100.
 - **a** $\frac{1}{4}$ **b** $\frac{10}{50}$ **c** $\frac{12}{25}$
- 2 This square shows some coloured triangles and some white triangles.
 - a How many triangles are coloured?
 - **b** How many triangles are white?
 - **c** What fraction of the total is coloured?
 - d What percentage of the total is coloured?
 - e What fraction of the total is white?
 - f What percentage of the total is white?
- **3** A farmer's pen has 2 black sheep and 8 white sheep.
 - a How many sheep are there in total?
 - **b** What fraction of the sheep are black?
 - c What fraction of the sheep are white?
 - d What percentage of the sheep are black?
 - e What percentage of the sheep are white?
- 4 A cake contains 7 grams of fat. The cake has a mass of 350 grams.
 - **a** Write the fraction of the cake which is fat.
 - **b** Simplify the fraction in part **a**.
 - **c** Use this simplified fraction to find the percentage of fat in the cake.

Fluency		5–6(½), 7	5–6(½), 7, 8
Example 25 Expressing a propo	rtion		
Express 24 green ducks out of a total o	f 30 ducks as a fraction and then	as a percentage	
Solution	Explanation		
Fraction = $\frac{24}{30}$	24 out of 30 is $\frac{24}{30}$.		
$=\frac{4}{5}$	Simplify the fraction.		
Percentage = $\frac{24}{30} \times \frac{100}{1}$ = 80%	Start with the same fraction a	and multiply by 1	00.
Now you try			
Express 21 students out of a total of 28	students as a fraction and then	as a percentage	

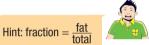


1-4

99

100

d





5 Express each of these proportions as a fraction and then as a percentage.a 30 out of a total of 100b 3 out of a total of 5

c \$10 out of a total of \$50

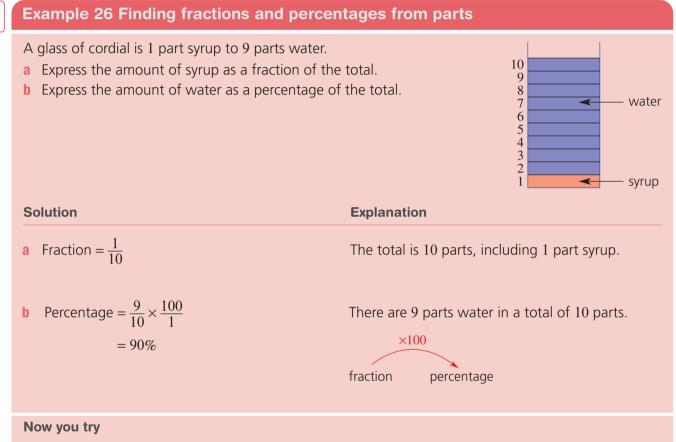
d \$60 out of a total of \$80

e 2 kg out of a total of 40 kg

f 14 g out of a total of 28 g

g 3 L out of a total of 12 L

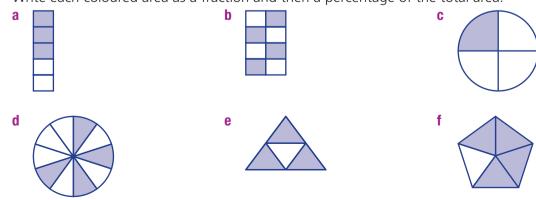
h 30 mL out of a total of 200 mL



A bottle of insecticide is 5 parts poison to 15 parts water.

- a Express the amount of poision as a fraction of the total.
- **b** Express the amount of water as a percentage of the total.

6 Write each coloured area as a fraction and then a percentage of the total area.



- 7 A jug of lemonade is made up of 2 parts of lemon juice to 18 parts of water.
 - **a** Express the amount of lemon juice as a fraction of the total.
 - **b** Express the amount of lemon juice as a percentage of the total.
- 8 A mix of concrete is made up of 1 part of cement to 4 parts of sand.
 - **a** Express the amount of cement as a fraction of the total.
 - **b** Express the amount of cement as a percentage of the total.
 - c Express the amount of sand as a fraction of the total.
 - **d** Express the amount of sand as a percentage of the total.

Problem-solving and reasoning 9, 10

- **9** Gillian pays \$80 tax out of her income of \$1600.
 - a What fraction of her income is tax?
 - **b** What percentage of her income is tax?
 - c What percentage of her income does she keep?
- **10** Over summer, a dam's water volume reduces from 20 megalitres to 4 megalitres.

11 In a new subdivision involving $20\,000$ m², specific areas are set

- a How many megalitres of water were used?
- **b** What fraction of the water was used?
- c What percentage of the water was used?



10-13



iii Park

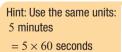
- Dwellings: 12 000 m²
 Shops: 1000 m²
 Roads/Paths: 3000 m²
 Park: 2500 m²
 Factories: Remainder
- a What area is set aside for factories?

aside for the following purposes.

- **b** Express the area of the following as both a fraction and a percentage of the total area.
 - i Shops

ii Dwellings

- c What fraction of the total area is either dwellings, shops or factories?
- d What percentage of the total area is park or roads/paths?
- **12** Express the following as a fraction and percentage of the total.
 - a 20 cents out of 500 cents
 - **b** 14 days out of 35 days
 - c 15 centimetres out of 3 metres (300 centimetres)
 - d 15 seconds out of 5 minutes
 - e 50 centimetres from a total of 2 metres
 - f 1500 metres from 2 kilometres
- **13** For a recent class test, Ross scored 45 out of 50 and Maleisha scored 72 out of 100. Use percentages to show that Ross obtained the higher mark.



= 300 seconds

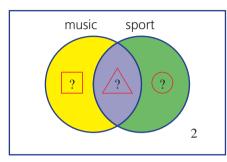
4K

Sport and music

14 Of 20 students, 10 play sport and 12 play a musical instrument, with some of these students playing both sport and music. Two students do not play any sport or musical instrument.

14

- a How many of the 20 students played music and sport?
- **b** Find the missing numbers in this Venn diagram.



c What fraction of the students play both sport and a musical instrument?



d What percentage of the students play a musical instrument but not a sport?



4L Ratios, rates and best buys

Learning intentions

- To understand what ratios and rates are.
- To understand that a best buy relates to finding the best value for money.
- To be able to simplify ratios and rates.
- To be able to determine the best buy.

Key vocabulary: ratio, rate, best buy

Ratios are used to show the relationship between two (or more) related quantities. In general, ratios compare quantities of the same type given in the *same* unit. Therefore a ratio is generally not written with a unit of measurement.

Rates show the relationship between two different types of quantities with *different* units. Therefore, all rates must be expressed with appropriate units, which often include the symbol / to represent the word 'per'. For example, speed is a rate comparing distance and time. Typical units of speed include metres per second (m/s) and kilometres per hour (km/h).

There are many everyday situations where it is useful to convert rates to the same unit for easy comparison. This can be a good way to determine the best value or best buy.



Lesson starter: Fair shares

Assuming that everyone gets an equal share, work out how much each person receives in each of the following situations.

- 40 potato gems for 5 children
- 24 party pies for 6 preschoolers at a party
- 480 mini chocolate bars for 160 students

Assuming that the adults need twice as much food as the children, work out how much each child and adult receives in each of the following situations.

- 12 sausages for 2 adults and 2 children
- 80 strawberries for 1 adult and 3 children
- 44 biscuits for 5 adults and 1 child

4L

Key ideas

Ratios

 Ratios show the relationship between two (or more) numbers or quantities measured in the same unit.

For example: Fleur wrote the ratio 16 : 8 to relate the number of hours she spends awake each day to the number of hours she sleeps.

- The colon : is the mathematical symbol used to represent ratios.
- The ratio a : b is read 'a to b' or 'a is to b'.
- If each value in a ratio is multiplied or divided by the same number, an equivalent ratio is formed.

For example: 2 : 3 and 4 : 6 and 10 : 15 are equivalent ratios.

• A ratio is in its simplest form when it contains only whole numbers with a highest common factor (HCF) of 1.

Rates

- Rates compare quantities measured in different units.
- Every rate has a unit that compares the two quantities. For example, speed compares distance and time in units such as kilometres per hour (km/h) or metres per second (m/s).
- We usually write rates in their simplest form, giving the amount for one unit of the second quantity. For example: Travelling 150 km in 3 hours would not usually be written as 150 km/3 hours. Instead, it is simplified to 50 km/1 hour, which we write as 50 km/h.

'Best buy'

- The concept of best buy relates to comparing rates to determine the best value for money, the best performance and so on.
- It is easy to compare rates that have the same units. For example, the same cheese is sold in packets of 600 g for \$9 and 1.75 kg for \$29. Converting both rates to price per kilogram gives \$15/kg and \$16.57/kg. Now we can see that the smaller packet is the better buy.

Exercise 4L

1Which of the following is an example of aA3.75 secondsBB5 m/s	c \$5000	D 3:7	
2 Which of the following is an example of aA \$7.50/kgB 2:4:5	rate? C 12:37 p.m.	D $\frac{3}{4}$	
3 Find the HCF for each of the following paira 5 and 15b 3 and 7	irs of numbers. c 4 and 9	d 12 and 8	3
 4 Using your answers from Question 3, state a 5:15 b 3:7 	e whether the following rati c 4 : 9	os can be simpli d 12 : 8	fied.
 5 Teddy's resting heart rate is 60 beats per m beat in: a 1 minute? b 5 minutes? 	ninute (60 bpm). How many c 1 hour?	times will Teddy d 1 day?	's heart

...

Fluency	6-7(½), 8 6-9(½)
Example 27 Writing a ratio in s	
Simplify the following ratios.	
a 3:9	b 60:24
Solution	Explanation
a $3:9$ $\div 3$ $3:9$ $1:3$ $\div 3$	The HCF of 3 and 9 is 3. Therefore divide both numbers by 3 to write the ratio in its simplest form.
b $\div 12$ $60:24$ $\div 12$ $\div 12$ $5:2$	The HCF of 60 and 24 is 12. Therefore divide both numbers by 12 to write the ratio in its simplest form.
Now you try Simplify the following ratios. a 12:9	b 180 : 45
 6 Simplify the following ratios. a 3:9 b 5:10 e 27:9 f 16:4 i 10:25 j 14:21 	c 2:18 d 6:18 g 100:10 h 60:12 k 32:40 I 50:70

7 There is one mistake in each of the following groups of equivalent ratios. Find the non-equivalent ratio in each group and replace one of its numbers to make a correct ratio.

0 55:35

p 60 : 48

- **a** 2 : 8, 5 : 20, 4 : 24, 10 : 40, 50 : 200
- **b** 11:66, 3:18, 7:42, 10:600, 40:240

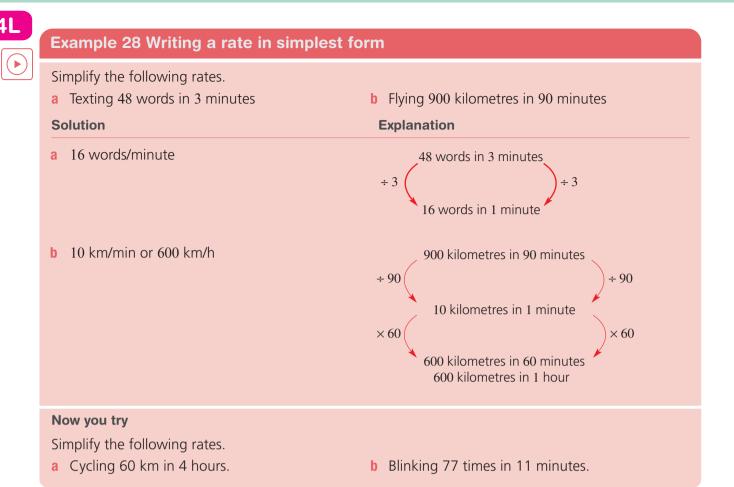
n 36 : 15

 $\textbf{c} \quad 6:9,2:3,20:30,8:24,14:21$

m 18 : 14

d 9:15,3:5,15:20,24:40,36:60





- 8 Simplify the following rates.
 - a Riding 24 kilometres in 2 hours
 - **b** Clapping 120 times in 30 seconds
 - c Spending \$28 on 4 kilograms of lollies
 - d Running 140 metres in 20 seconds
 - e Scoring 24 goals in 8 games
 - f Travelling 180 kilometres in 90 minutes

9 Solve the following rate problems.

- a How much will 3 kg of salami cost at \$8/kg?
- **b** A radio station plays songs at a rate of 9 songs per hour. How many songs would you hear in 8 hours?
- **c** A surfer catches 8 good waves per hour. How many waves would she catch if she surfed for $2\frac{1}{2}$ hours?
- **d** A teenager buys 4 pairs of shoes per year. How many pairs of shoes does he buy during his teenage years?



13

Problem-solving and reasoning		10, 11	10–12
Example 29 Determining the best buy			
By calculating a common rate, determine the best • A 5 kg bag of King for \$35	buy for the following l • A 12 kg bag of Th	0	ood.
Solution	Explanation		
King dog food costs \$7/kg.	\$35 for 5 kg ÷ 5 \$7 for 1 kg	- 5	
Thrive dog food costs \$5/kg.	\$60 for 12 kg ÷ 12 \$5 for 1 kg	÷ 12	
The best buy is Thrive dog food.			
Now you tryDetermine the best buy.6 kg bag of Grow for \$30	• 10 kg bag of Spro	ut for \$40	

- **10** By calculating a common rate, determine the best buy for each of the following.
 - a 2 kg of flour for \$3.60 or 5 kg of flour for \$8.50
 - **b** 12 kg of potatoes for \$14.40 or 5 kg of potatoes for \$5.50
 - **c** 500 g of ham for \$9.50 or 2 kg of ham for \$39
 - d 20 L of cooking oil for \$120 or 12 L of cooking oil for \$84

11 Washing powder can be purchased in many different quantities. By calculating a common rate (\$/kg), rank the following options in order of best buy to worst buy.

A 500 g for \$2.09

B 2 kg for \$7.90

C 5 kg for \$19.95

- **D** 10 kg for \$38.00
- **12** Shaun is an apprentice chef. He is required to make a large amount of pastry. The recipe shows the ratio of butter to flour is 1 : 3.
 - a How much flour will Shaun need if he has 7.5 kg of butter?
 - **b** How much butter will Shaun need if he has 7.5 kg of flour?

Reading rates

Ħ

13 When Diviesh was 12, he had been learning English for only 3 years and was able to read at a rate of 96 words per minute. Now he is 14, he is able to read at a rate of 160 words per minute.

- a Express Diviesh's reading rates at 12 and at 14 as a ratio in simplest form.
- **b** How much quicker would it be for Diviesh to read a 12 288-word novel now that he is 14 than when he was 12?
- **c** At age 14, it took Diviesh a total of 15 hours and 10 minutes to read his longest novel ever. Assuming he read at 160 words per minute, how many words were in the novel?



Maths@Work: Building construction apprentice

The construction industry in Australia is huge, and property developers employ many thousands of workers. Apprentices must complete hours of on-the-job training as well as achieve TAFE qualifications. Number and measurement skills are very important, as construction workers apply these skills in everyday projects.

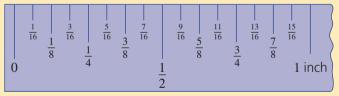
Fractions are studied both at school and at TAFE. Measuring and calculating with fractions is a vital skill in the building industry. Many building components are from the United States, which still uses Imperial measurements, so inches and fractions of an inch often feature in the workplace.



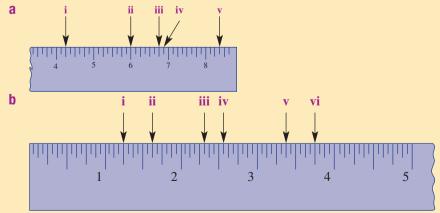
1 Given that 1 inch is 25.4 mm, find the length in millimetres to 1 d.p. for the following.

a $\frac{1}{2}$ inch b	$\frac{1}{4}$ inch	c $\frac{1}{8}$ inch	d $\frac{1}{32}$ inch	e $\frac{3}{4}$ inch
--------------------------------------	--------------------	-----------------------------	------------------------------	----------------------

2 Make a neat, enlarged copy of this 1-inch ruler and its scale. Start by ruling an 8 cm line and mark 16 equal spaces on it. Label the ends 0 and 1 inch, label the centre $\frac{1}{2}$ inch, then carefully mark in all the other fractions of an inch as shown on this image.



3 Tape measures can show units in both inches and centimetres. What are the fractional measurements in inches indicated on the following tape measures?



Imperial units

- 4 TAFE courses for construction apprentices include fraction skills. Write a list in inches for each of the following sets of measurements:
 - **a** Increasing in quarters from $10\frac{1}{4}$ inches to 1 foot.
 - **b** Decreasing in eighths from 1 foot to $11\frac{1}{4}$ inches.
 - **c** $\frac{3}{8}$ of an inch less than each of 1 inch, 5 inches and 1 foot.
 - **d** $4\frac{5}{16}$ inches less than each of 1 foot and 1 yard.
- **5** Travis, a first-year apprentice, is asked to cut off one third of a 12-inch pipe. What length of the pipe in mm is remaining after he cuts it?

Construction workers calculate and measure using fractions.

- 6 Holly is asked to cut $8\frac{1}{4}$ inches from a pipe $41\frac{1}{4}$ inches long. What proportion of the pipe is cut (as a fraction)?
- 7 Murray has eight lengths of pipe to join together. If each pipe is $4\frac{3}{4}$ inches long, how many mm is the final length of pipe?

Using technology

8 Many older buildings have pipes that were installed before Australia changed to the metric system. The replacement of old pipes requires exactly the same length of pipe measured in mm.

Set up the following spreadsheet to add fractions and convert inches to mm.

Select all the cells using inches (columns A, B, C) and Format/Fraction/up to two digits.

Enter formulas in the shaded cells.

В

				-	-
	1	F	Pipe lengths in	n inches and mr	n
	2	Pipe A in inches	Pipe B in inches	Total A + B in inches	Total A + B mm
	3	5 1/2	4 1/16		
	4	9 15/16	17 3/16		
	5	12 3/16	46 13/32		
	6	14 7/8	42 3/4		
Essential Ma	athema	atics for the Vic	torian Curricul	um ISBN 9	978-1-108-87

CORE Year 7

e.g. 5 1/2 means $5\frac{1}{2}$

the fraction.

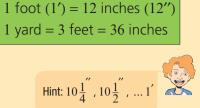
Hint: Formula for C3 = A3 + B. Formula for D3 = C3*25.4

Hint: To type a fraction into a spreadsheet, insert a space

between the whole number and



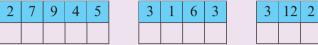
in



1 Three cities are known as India's Golden Triangle. To find the names of these cities, complete the puzzle.

Match each of the fractions in the middle row with the equivalent fraction in the bottom row. Place the letter in the code below.

1	2	3	4	5	6	7	8	9	10	11	12
$\frac{4}{24}$	$\frac{28}{35}$	$\frac{100}{120}$	$\frac{5}{7}$	$\frac{21}{36}$	$\frac{1}{2}$	$\frac{22}{77}$	$\frac{2}{3}$	$4\frac{2}{5}$	$\frac{81}{90}$	$\frac{25}{3}$	$\frac{43}{9}$
$U = 8\frac{1}{3}$	$A = \frac{5}{6}$	$H = \frac{15}{21}$	$D = \frac{4}{5}$	$G = \frac{1}{6}$	$N=4\frac{7}{9}$	$I = \frac{7}{12}$	$E = \frac{2}{7}$	$P = \frac{18}{27}$	$J = \frac{9}{10}$	$R = \frac{48}{96}$	$L = \frac{22}{5}$



How many words with three or more letters can you and a partner make from the word

You have 15 minutes to come up with as many words as you can. Score your results as follows:

- 3 points for every word with five or more letters

Compare your list with those of other students in the class.

3 Fraction dice game

Two different-coloured dice are required. Choose one die for the numerator and one die for the denominator.

For example: $\frac{\text{red die result}}{\text{blue die result}} = \frac{5}{3} \text{ or } \frac{\text{red die result}}{\text{blue die result}} = \frac{4}{1}$.

Players take turns to throw both dice and record their fraction results.

After an equal number of turns, each player then adds all their results together and the winner is the player with the largest number.

b

In a magic square, the sum of the fractions in each row, column and diagonal is the same. 4 Find the value of each letter in these magic squares.

ſ				ľ
I			۰	L
			п	L
l		۰	U	L
	-		_	

а

	$\frac{2}{5}$	А	$\frac{4}{5}$	
	В	С	D	
	Е	$\frac{1}{2}$	1	
(Magic	sum i	is $2\frac{1}{10}$.)

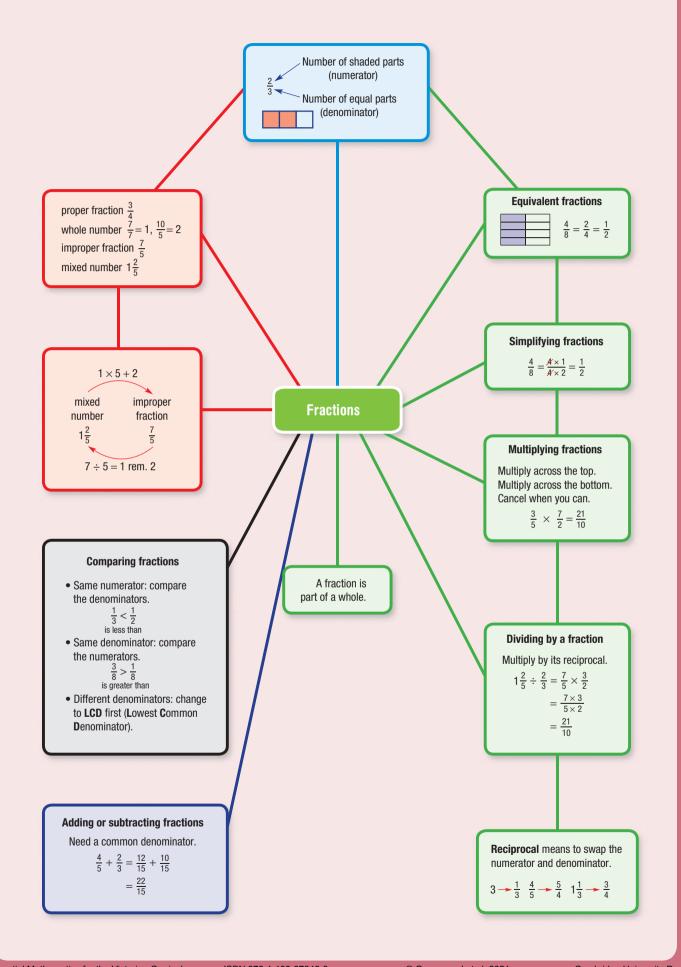
А	В	$2\frac{1}{4}$	
С	$1\frac{7}{8}$	D	
Е	$1\frac{1}{8}$	3	
(Magi		is $5\frac{5}{8}$	

8 11 6

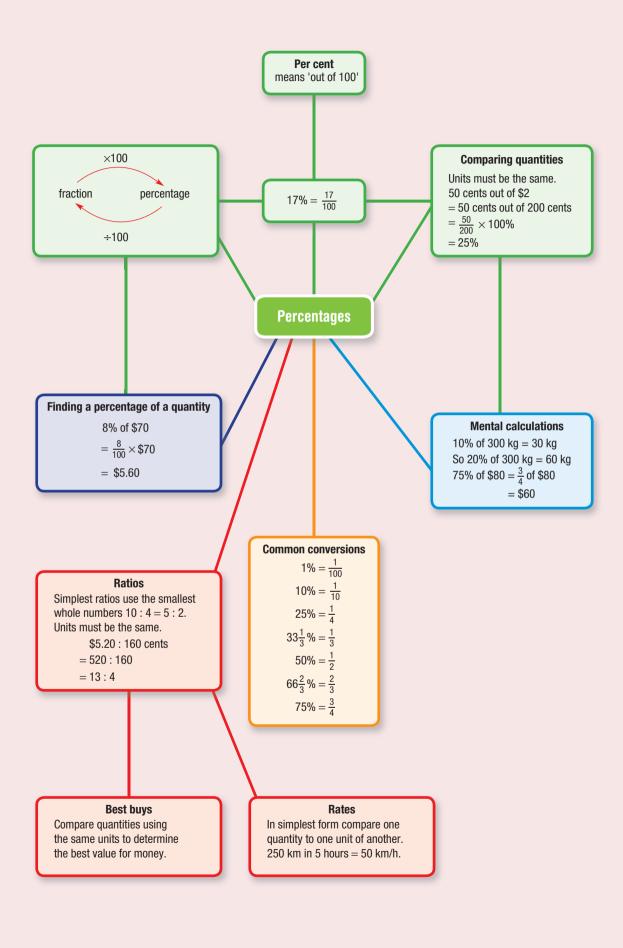
10 3 5

2 PERCENTAGES?

Puzzles and games 1 point for every three-letter word 2 points for every four-letter word • •



Essential Mathematics for the Victorian Curriculum CORE Year 7



Essential Mathematics for the Victorian Curriculum CORE Year 7

Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

			~
4A	1	I can identify the numerator and denominator of a fraction described in words. e.g. A pizza has been cut into eight pieces, with three of them selected. Write the selection as a fraction and state the numerator and denominator.	
4A	2	I can represent fractions on a number line. e.g. Represent the fractions $\frac{3}{5}$ and $\frac{9}{5}$ on a number line.	
4B	3	I can list fractions that are equivalent to a given fraction. e.g. Write four fractions that are equivalent to $\frac{2}{3}$.	
4B	4	I can write fractions in simplest form. e.g. Write the fraction $\frac{12}{20}$ in simplest form.	
C	5	I can convert mixed numbers to improper fractions. e.g. Convert $3\frac{1}{5}$ to an improper fraction.	
С	6	I can convert from an improper fraction to a mixed number. e.g. Convert $\frac{11}{4}$ to a mixed number.	
D	7	I can compare two fractions to decide which is bigger. e.g. Decide which of $\frac{2}{3}$ and $\frac{3}{5}$ is bigger, and write a statement involving > or < to summarise your answer.	
D	8	I can order fractions in ascending or descending order. e.g. Place the following fractions in ascending order: $\frac{3}{4}, \frac{4}{5}, \frac{2}{3}$.	
Æ	9	I can add two fractions by converting to a common denominator if required. e.g. Find the value of $\frac{3}{4} + \frac{5}{6}$.	
3	10	I can add two mixed numbers. e.g. Find the sum of $2\frac{5}{6}$ and $3\frac{3}{4}$.	
F	11	I can subtract two fractions by converting to a common denominator if required. e.g. Find the value of $\frac{5}{6} - \frac{1}{4}$.	
F	12	I can subtract two mixed numbers. e.g. Find the value of $5\frac{2}{3}-3\frac{1}{4}$.	
G	13	I can find a simple fraction of a quantity. e.g. Find $\frac{2}{3}$ of 15 bananas.	

Chapter checklist <

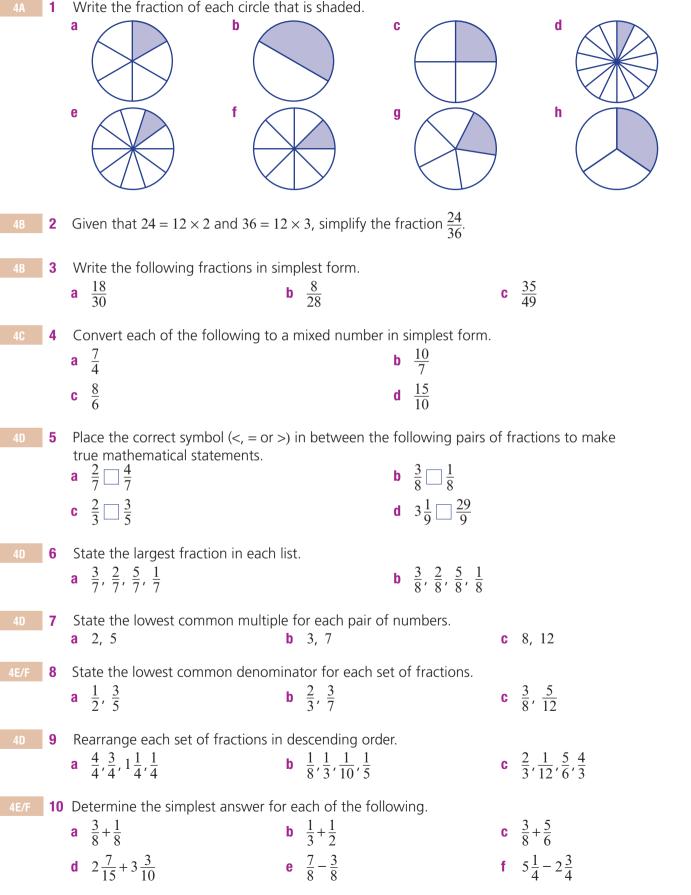
		~
14	I can express a whole number as a fraction. e.g. Write 21 as a fraction.	
15	I can multiply proper fractions. e.g. Find $\frac{3}{4} \times \frac{8}{9}$.	
16	I can multiply mixed numbers. e.g. Find $6\frac{1}{4} \times 2\frac{2}{5}$.	
17	I can find the reciprocal of a fraction, whole number or mixed number. e.g. Find the reciprocal of (a) $\frac{2}{3}$, (b) 5, and (c) $1\frac{3}{7}$.	
18	I can divide a fraction by a whole number and I can divide a whole number by a fraction. e.g. Find $\frac{5}{8} \div 3$ and $24 \div \frac{3}{4}$.	
19	I can divide fractions (proper and/or improper fractions). e.g. Find $\frac{3}{5} \div \frac{3}{8}$.	
20	I can divide mixed numbers. e.g. Find $2\frac{2}{5} \div 1\frac{3}{5}$.	
21	I can convert a percentage to a fraction or mixed number. e.g. Express 36% as a fraction in simplest form.	
22	I can convert a fraction to a percentage. e.g. Convert $\frac{11}{25}$ and $\frac{3}{8}$ to percentages.	
23	I can find the percentage of a number. e.g. Find 15% of 400.	
24	I can find one number as a proportion of a total, represented as a fraction. e.g. What proportion is 24 green ducks out of a total of 30 ducks? Answer as a fraction.	
25	I can find one number as a percentage of a total. e.g. What percentage is 24 green ducks out of a total of 30 ducks?	
26	I can simplify a ratio. e.g. Write 60 : 24 in simplest form.	
27	I can simplify a rate. e.g. Simplify the rate 48 words in 3 minutes.	
28	I can find a best buy. e.g. Which is the best buy out of 5 kg for \$35 and 12 kg for \$60?	

Chapter review

Short-answer questions

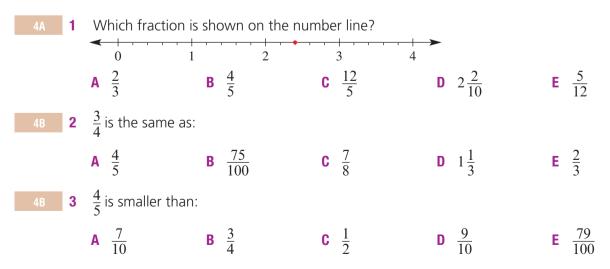


Write the fraction of each circle that is shaded.



4G	11	Find:								
	1	a $\frac{1}{3} \times 21$		b	$\frac{4}{5}$ of	100		C	$\frac{3}{4}$ of 1	6
		d $\frac{8}{10} \times \frac{25}{4}$		е	$\frac{2}{3}$ of	$\frac{1}{4}$		f	$3\frac{1}{8}$ ×	$2\frac{2}{5}$
4H	12	Determine the recipro	ocal of e	ach c	of the	followi	ng.			
	i	a $\frac{3}{4}$	b $\frac{7}{12}$			C	$2\frac{3}{4}$		d	8
4H	13	Perform these divisio	ns.							
	;	a $\frac{6}{10} \div 3$	b 64	$\div 3\frac{1}{5}$		C	$\frac{2}{3} \div \frac{1}{3}$	$\frac{1}{6}$	d	$1\frac{1}{2} \div \frac{3}{4}$
41	14	Find the missing perc	entages	and	fracti	ons.				
		Percentage form	10%	А	В	75%	С	150%]	
		Fercentage form	1070		0	1370	Ŭ	15070		
		Fraction	D	$\frac{1}{4}$	$\frac{1}{2}$	E	$\frac{7}{25}$	F		
4J			D				$\frac{7}{25}$ Find			
4J 4K	16	Fraction a Find 10% of \$200. c Find 50% of 96 gr	D ams. as both	$\frac{1}{4}$	$\frac{1}{2}$	E ti C	Find Find Find rcentae	F 25% of \$ 20% of \$	total.	
	16 17	Fraction a Find 10% of \$200. c Find 50% of 96 gr e Find 150% of \$6. Express the following a 6 out of 10	D ams. as both	$\frac{1}{4}$	$\frac{1}{2}$	E t and pe	7 25 Find Find rcenta \$4 c 600 \$4 c 600 \$2 : 60 k	F 25% of \$ 20% of \$ ge of the out of \$20 mL out o	total. f 2 L	S

Multiple-choice questions



Chapter review

Chapter review

4D 4	Which is the lowest	t common denomina	ator for this set of fra	actions? $\frac{1}{3}$, $\frac{1}{4}$, $\frac{5}{6}$	
	A 3	B 4	C 6	D 72	E 12
4A 5	Maria has 15 red ap			of the apples are gree	
	A 5	B $\frac{1}{3}$	C $\frac{2}{3}$	D $\frac{1}{4}$	E $\frac{3}{4}$
4D 6	Which of the follow	-			
	A $\frac{1}{2} > \frac{4}{5}$	B $\frac{1}{2} < \frac{3}{8}$	c $\frac{1}{2} > \frac{2}{5}$	D $\frac{1}{2} > \frac{9}{10}$	E $\frac{1}{2} < \frac{4}{11}$
4D 7	Which set of fraction	ons is ordered from s	mallest to largest (as	scending order)?	
	A $\frac{1}{2}, \frac{2}{3}, \frac{5}{12}$	B $\frac{1}{2}, \frac{13}{24}, \frac{1}{4}$	c $\frac{2}{3}, \frac{1}{2}, \frac{7}{12}$	D $\frac{7}{12}, \frac{1}{2}, \frac{1}{4}$	E $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}$
4E/F/G 8	Which problem has	an incorrect answe	r?		
	A $\frac{1}{6} + \frac{3}{6} = \frac{4}{6}$		$+\frac{5}{12} = \frac{5}{16}$	C $\frac{3}{4} \times \frac{1}{3} = \frac{1}{4}$	
	D $1\frac{3}{4} - \frac{1}{2} = 1\frac{1}{4}$	E $\frac{3}{4}$	$\times \frac{4}{5} = \frac{3}{5}$		
4l 9	Which fraction is g	reater than 75%?			
	A $\frac{1}{4}$	B $\frac{3}{4}$	c $\frac{15}{24}$	D $\frac{4}{5}$	$E \frac{6}{8}$
4K 10	What is \$5 as a per	-			
	A 50%	B 20%	C 25%	D 5%	E 10%
4C 11	$\frac{60}{14}$ can be written a	as:			
	A $4\frac{2}{7}$	B $2\frac{4}{7}$	C $4\frac{2}{14}$	D $7\frac{4}{7}$	E $5\frac{1}{7}$
4G 12	$\frac{17}{25}$ of a metre of m	aterial is needed for	a school project. Ho	w many centimetres i	is this?
	A 65 cm	B 70 cm	C 68 cm	D 60 cm	E 75 cm

Extended-response question

- 1 A printer produces 1200 leaflets. One-quarter of the leaflets are on green paper. Half the remaining leaflets are on white paper. There are smudges on 10% of the leaflets for each colour of paper.
 - a How many leaflets were on green paper?
 - **b** What percentage of the leaflets were *not* on green paper?
 - c How many white leaflets were printed?
 - **d** Of the white leaflets, how many had smudges?
 - e How many leaflets did not have any smudges?

Chapter

Algebra

Essential mathematics: why skills in algebra are important

Using algebra we can write a mathematical relationship between variables and state results. Algebra skills are essential when applying formulas and finding solutions to problems.

- A farmer uses the formula $V = \frac{D}{1000} \times A$ to calculate the volume V litres of irrigation water, required for a depth D mm of water on a paddock of area A m².
- An electrician uses many algebraic formulas that relate voltage V, current I, resistance R and power P. Formulas such as: V = IR, $P = RI^2$ and $V = \sqrt{PR}$.
- A fitness instructor can estimate the safe maximum heart rate, MHR, for a person of age a years, using the formula: *MHR* = 207 0.67a.
- A plumber uses the formula $V = \pi r^2 h$ to calculate the volume V litres of water contained in a pipe of height h and radius r.



In this chapter

- 5A Introduction to algebra
- 5B Substituting and evaluating
- 5C Equivalent expressions
- 5D Like terms
- 5E Multiplying and dividing expressions
- 5F Applying algebra 🛧

Victorian Curriculum

NUMBER AND ALGEBRA Patterns and algebra

Introduce the concept of variables as a way of representing numbers using letters (VCMNA251)

Create algebraic expressions and evaluate them by substituting a given value for each variable (VCMNA252)

Extend and apply the laws and properties of arithmetic to algebraic terms and expressions (VCMNA253)

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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

A AM AND AND AND A

Warm-up quiz

1	Find the value of: a $3+6$ c 12×4		12 - 5 20 ÷ 5
2	 Write the answer to each of the following prob a 4 and 9 are added b 3 is multiplied by 7 c 12 is divided by 3 d 10 is halved 	lem	IS.
3	If $=$ 7, write the value of each of the following a $+4$ c $12 -$	b	$\boxed{-2} \\ 3 \times $
4	Write the value of $x \le 4$ if: a $x \le 2$ c $x \le 10$	b d	= 9 = 2.5
5	If $\blacktriangle = 10$, write the value of: a $\bigstar + 7$ b $\bigstar - 2$ c $\bigstar \div 2$ d $\bigstar + \bigstar$		
6	Find the value of each of the following. a $4 \times 3 + 8$ c $4 \times 3 + 2 \times 5$		$4 \times (3+8)$ $4 \times (3+2) \times 5$
7	Find the value of each of the following. a $50 - (3 \times 7 + 9)$ c $24 \div 6 - 2$		24 ÷ 2 - 6 24 ÷ (6 - 2)
8	If $\Box = 5$, write the value of each of the following		
	a -4 c $\div 5+2$	b d	
9	 Find the value of each of the following. a 5 more than 12 c 4 added to 7 e 15 subtracted from 22 g The product of 7 and 5 	b d f h	The sum of 8 and 6 12 less than 20 Double 9 4 is tripled, then 5 is added
10	Find the perimeter (distance around the outside a $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$	2) O	f each of these shapes.

5A Introduction to algebra

Learning intentions

- To know the basic terminology of algebra.
- To be able to identify coefficients, terms and constant terms within expressions.
- To be able to write expressions from word descriptions.

Key vocabulary: pronumeral, variable, term, constant term, expression, coefficient, sum, product

In algebra, letters can be used to stand for unknown numbers. For example:

- *h* might stand for someone's height (in cm).
- T might stand for the temperature outside (in °C).
- *n* could stand for the number of people in Australia.

Letters and numbers can be combined:

- h + 5 (cm) is the height of someone 5 cm taller than a person of height h cm.
- T 12 (°C) is the temperature outside if it drops 12°C.
- $5 \times n$ is the number of rabbits in 5 cages if there are n rabbits in each cage.

• Lesson starter: Algebra stories

In the left column are three expressions. An example story is given for the first expression. Try to make a short story for each of the others.

Expression	Story
$3 \times b$	Packets of biscuits each have <i>b</i> biscuits in them. (<i>b</i> is not known.) Ahmed opens three packets of biscuits to serve at a party. The number of biscuits is $3 \times b$.
$3 \times c - 5$	
$2 \times d + 10$	

Key ideas

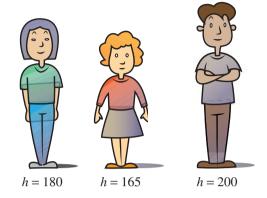
- In algebra, letters called pronumerals or variables stand for numbers.
- $a \times b$ is written ab and $a \div b$ is written $\frac{a}{b}$.

For example: 5*n* means $5 \times n$ and $\frac{a}{3}$ means $a \div 3$.

A term consists of numbers and pronumerals combined with multiplication or division. For example:

5 is a term, x is a term, 9a is a term, abc is a term, $\frac{4xyz}{3}$ is a term.

- A term that does not contain any pronumerals is called a constant term. All numbers by themselves are constant terms.
- An **expression** is a mathematical statement that consists of numbers and pronumerals combined with any mathematical operations. For example: 3x + 2yz is an expression and $8 \div (3a 2b) + 41$ is also an expression. Any single term is also an expression.



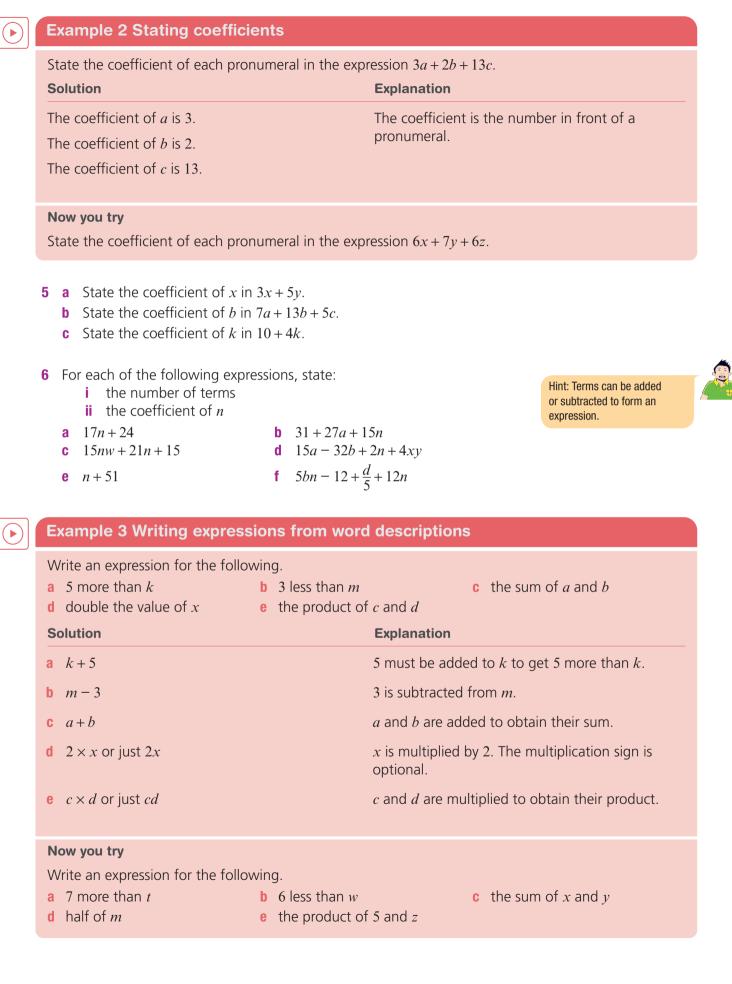
• A **coefficient** is the number in front of a pronumeral. For example, the coefficient of y in the expression 8x + 2y + z is 2. If there is no number in front, then the coefficient is 1, since 1z and z are equal.

expressi	ion
first term coefficient of b is 4	2c + 5 — constant term terms are combined using addition and/or subtraction

Exercise 5A

	Un	nderstanding	g				1–3	2, 3	
1	Sta a b	-	rs are called s not have any p	 onumerals is called	а	wo	t: Choose from t rds: <i>expression</i> , <i>numerals</i> and <i>c</i>	constant,	
	c d	An pronumerals.	is a mathema	tical statement that front of a pronume		numbe	ers and		
2	A B C	Seven times <i>a</i> 7 <i>a</i> <i>a</i> ⁷	ving is the comm	on way to write 7 ×	a?		Hint: In algebr written 5b.	$a, 5 \times b$ is	
3		which of the follow $\frac{m}{5}$	ving is the comm B five divid	on way to write 5 \div ded by m	m? C	$\frac{5}{m}$		D 5m	
	Flu	uency					4–8	4, 5, 6(½), 7	7, 8
E	Exa	mple 1 Listing	terms						
		the individual terr ition	ns in the expressi	on $3a + b + 13$. Explanation					
Т	here	e are three terms:	3 <i>a</i> , <i>b</i> and 13.	Each part of an	expression	is a teri	m.		
		/ you try the individual terr	ns in the expressi	on $2xy + y + 3$.					

- 4 List the individual terms in each of the following.
 - **a** 2x + 7y
 - **b** 3a + 2c + e
 - **c** 5q + 3r + 2s
 - **d** 7d + 5f + 17



5A

Write an expression for the following.

- a 3 more than x
- **c** 2 is added to *b*
- e 4 is subtracted from H

- **b** The sum of k and 5
- **d** 3 less than g
- **f** 6 is subtracted from M

8 Write an expression for the following without using \times or \div .

- a Double the value of u
- **c** 3 is multiplied by x
- **d** The product of k and 10 f Half of z

b 4 lots of v

- e y is divided by 8
- **g** *a* is tripled, then 4 is added **h** *p* is doubled, then 12 is added

Problem-solving and reasoning

- 9 In a room there are k people, and then 5 people leave. How many people are now in the room? A k+5**B** 5 **C** k - 5D = 5k
- **10** Nicholas buys 10 lolly bags from a supermarket.
 - a If there are 7 lollies in each bag, how many lollies does he buy in total?
 - **b** If there are *n* lollies in each bag, how many lollies does he buy in total?
- 11 Mikayla is paid x per hour at her job. Write an expression for each of the following.
 - a How much does Mikayla earn if she works 8 hours?
 - b If Mikayla gets a pay rise of \$3 per hour, what is her new hourly wage?
 - c If Mikayla works for 8 hours at the increased hourly rate, how much does she earn?
- **12** Recall that there are 100 centimetres in 1 metre and 1000 metres in 1 kilometre. Write expressions for each of the following.
 - a How many metres are there in x kilometres?
 - **b** How many centimetres are there in *x* metres?
 - **c** How many centimetres are there in x kilometres?
- **13** If *b* is an even number greater than 3, decide whether these statements are true or false.
 - **a** b+1 must be even.
 - **c** 5+b could be greater than 10.
 - **e** 2b must be greater than 10.

- **d** 5*b* must be greater than *b*.
- $\frac{b}{2}$ is a whole number.

b b+2 could be odd.

Restaurant algebra

- 14 A group of people go out to a restaurant and the total amount they must pay (in dollars) is A. They split the bill equally. Write expressions to answer the following questions.
 - a If there are 4 people in the group, how much do they each pay?
 - **b** If there are *n* people in the group, how much do they each pay?
 - **c** One of the *n* people has a voucher that reduces the total bill by \$20.
 - i How much does each person pay now?
 - ii If the bill is \$200 and n = 6, how much does each person end up paying?



14



Hint: For part b, write an

expression involving *n*.

Hint: 'Product' tells you to use

The product of 3 and 10 is

multiplication.

 $3 \times 10 = 30.$



10 - 13

9-11

5B Substituting and evaluating

Learning intentions

- To know that pronumerals can be replaced with numbers.
- To understand that multiplication symbols are often removed in algebra, so a term like 4a means 4 × a.
- To be able to substitute numbers for pronumerals.
- To be able to evaluate an expression using order of operations once all pronumeral values are known.

Key vocabulary: evaluate, substitute, pronumeral

To evaluate an expression, replace the pronumerals (such as x and y) with numbers then simplify to find the answer.

For example, when a = 11 we can evaluate 4 + a to get 15.

Lesson starter: Sum to 10

The variables X and Y could stand for any number.

- If X = 3 and Y = 7, what is X + Y?
- If X + Y = 10, what other numbers could X and Y be? Try to list as many pairs as possible.
- Can you make $X \times Y$ equal 10 instead?



Key ideas

- To evaluate an expression or to substitute values, replace each pronumeral in an expression with a number to obtain a final value. For example: if x = 3 and y = 8, evaluating x + 2y gives $3 + 2 \times 8 = 19$.
- A term like 4a means $4 \times a$. When substituting a number we must include the multiplication sign, since the number 42 is very different from the product 4×2 .

Exercise 5B

	Understanding			1-	5	5	
1	State the value of: a $12+5$ b	40 - 2	c 30 ÷ 2	d	3×7	,	
2	If $\square = 4$, find the value of: a $\square + 2$ b	7 × 🗌	c - 3	d	÷	2	
3	If $\blacktriangle = 3$, find the value of: a $\blacktriangle + 7$ b		c 8 − ▲	d	12 ÷		
4	Use the correct order of op a $4+2 \times 5$ c $3 \times 6 - 2 \times 4$	b	to evaluate the following. $7 - 3 \times 2$ $(7 - 3) \times 2$		Division	member order: Brackets and Multiplication, and Subtraction	
5	Complete the following. a If <i>a</i> is 4, what is $a + 3$? c If <i>x</i> is 10, what is $12 \times x$		If <i>b</i> is 5, what is $b + 12$? If <i>r</i> is 7, what is $r - 2$?		Hint	<i>a</i> +3=4+3=?	

	Fluency				6–10(½)	6–11(½)
E	xample 4 Substituting	for a single	e pronu	meral		
G	iven that $t = 5$, evaluate:					
а	<i>t</i> + 7	b 8 <i>t</i>		c]	10t + 4 - t	
S	olution			Explanation		
а	t + 7 = 5 + 7 = 12			Replace <i>t</i> with 5 an expression, which r pronumerals.		the
b	$8t = 8 \times t$ $= 8 \times 5$ $= 40$			Insert a \times between in 5. If the multiplic included, we might answer of 85.	ation sign is not	
C	$10t + 4 - t = 10 \times 5 + 4 - 5$ = 50 + 4 - 5 = 49	5		Replace <i>t</i> with 5 be the multiplication (2 the addition and su	10×5) is calculat	
G	low you try given that $c = 7$, evaluate: c - 4	b		C S	5c + 2 - c	
6	Given that $a = 6$, evaluate: a $a + 2$ b	$7 \times a$		c <i>a</i> – 3	d <i>a</i> ÷ 2	
7	If $b = 5$, find the value of: a $4b$ b $10b$	Ь	c 7 <i>b</i>	d 20 <i>b</i>	Hint: 4b mea	$ns 4 \times b.$
8	Calculate the value of $12 + a$ $b = 5$ b	b if: b = 8		c <i>b</i> = 60	d $b = 0$	
9	d $2x + 4$ e	evaluate each $x \times 2$ 3x + 2 $20 \div x + 3$	of the fo	llowing. c $14 - x$ f $13 - 2x$ i $4x - 2$	Hint: Substitute replace x with x	
10	If $y = 3$, state the value of: a $5y + 2 - y$ c $y \times 7 + 5 - y$ e $y + 2y + 3y$			b $3 + 4y + 2y$ d $y \times (1 + y)$ f $(10 - y) \times y$		

12

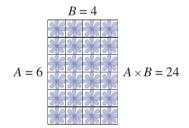
12, 13

14

Substitute $x = 4$ and y	= 7 to evaluate $5x + y + 8$.	
Solution		Explanation
$5x + y + 8 = 5 \times 4 + 7 + = 20 + 7 + 8 = 35$	8	Insert the implied multiplication sign betwee and 4 before completing the calculation.
Now you try		
Substitute $a = 5$ and b	= 3 to evaluate $3a - 2b - 1$.	
Substitute $a = 2$ and	b = 3 and then evaluate: b $2b - 2$ e $5a - 2b$	c <i>a</i> + <i>b</i> f <i>ab</i>

- **12** A number is substituted for b in the expression 7 + b and gives the result 12. What is the value of b?
- 13 Assume A and B are two numbers, where AB = 24.What values could A and B equal if they are whole numbers? Try to list as many pairs as possible.

Problem-solving and reasoning



Working backwards

14 Copy and complete the table.

x	5	9	12			
<i>x</i> + 6	11			7		
4x	20				24	28

5C Equivalent expressions

Learning intentions

- To know what it means for two expressions to be equivalent.
- To be able to determine whether two expressions are equivalent.
- Key vocabulary: equivalent expressions, substitute, pronumeral

Sometimes two expressions will evaluate to give the same result, no matter what numbers the pronumerals stand for.

For example, B + B and $2 \times B$ will always give the same result. For example:



This means that B + B and $2 \times B$ are equivalent.

Lesson starter: Odd one out

Here are four expressions:

 $2 \times B + 6$ 6 + B + B $(B + 3) \times 2$ B + 6

One of them is not equivalent to the others.

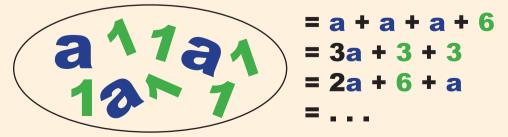
• Copy and complete the table to help you find the odd one out. (The first row has already been done.)

	$2 \times B + 6$	6+B+B	$(B+3) \times 2$	B +6
B = 0	$2 \times 0 + 6 = 6$	6 + 0 + 0 = 6	$(0+3) \times 2 = 6$	0 + 6 = 6
<i>B</i> = 1				
<i>B</i> = 2				

• Can you draw pictures to show why the 'odd one out' in the table is not equivalent to the other three expressions? (For example, if *B* is the number of marbles in a bag, you could draw 2 bags and 6 extra marbles to show $2 \times B + 6$.)

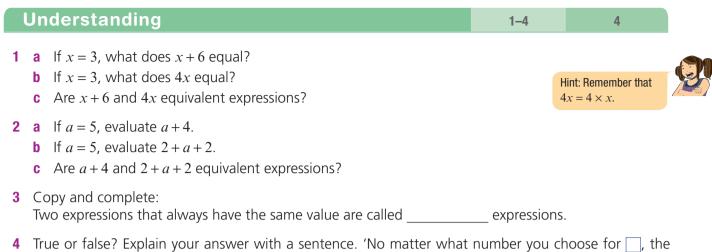
Key ideas

- Equivalent expressions are always equal in value, no matter what numbers are substituted for the pronumerals.
- For example: 3a + 6 is equivalent to 6 + 3a and to 3a + 3 + 3.



This collection of terms can be arranged into many different equivalent expressions.

Exercise 5C



Fluency						5–7	5, 7, 8
Example 6 Using tables to decide equivalence							
Fill in a table to help you decide if $3a + 6$ and $(a + 2) \times 3$ are equivalent. Use $a = 0$, $a = 1$, $a = 2$, $a = 3$. Solution Explanation							
$3a+6$ $(a+2)\times 3$	<i>a</i> = 0 6 6	<i>a</i> = 1 9 9	<i>a</i> = 2 12 12	<i>a</i> = 3 15 15		$(a+2) \times 3$ are of a , so they a t.	
They are equivalent.					Note $(a+2) \times 3$	$= 3 \times (a+2) = a+2+a+2 = 3a+6$	2 + <i>a</i> + 2

Now you try

Fill in a table to help you decide if 2(x - 1) and 2x - 1 are equivalent. Use x = 1, x = 2, x = 3 and x = 4.

5 a Copy and complete the following table.

values of -+6 and 6+- are equal.'

	<i>a</i> = 0	<i>a</i> = 1	<i>a</i> = 2	<i>a</i> = 3
2a + 2				
$(a+1) \times 2$				

b Fill in the gap: 2a + 2 and $(a + 1) \times 2$ are ______ expressions.

6 a Copy and complete the following table.

	B = 0	<i>B</i> = 1	<i>B</i> = 2	<i>B</i> = 3
5 <i>B</i> + 3				
6 <i>B</i> + 3				

b Are 5B + 3 and 6B + 3 equivalent expressions?

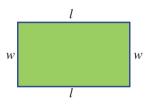
- 5C
- **a** Copy and complete this table.

	6x + 5	4x + 5 + 2x
<i>x</i> = 1		
<i>x</i> = 2		
<i>x</i> = 3		
<i>x</i> = 4		

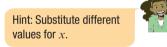
- **b** Are 6x + 5 and 4x + 5 + 2x equivalent?
- 8 For each of the following pairs, decide if they are equivalent (E) or not equivalent (N).
 - **a** k + 6 and $k \times 4$
 - **b** $k \times 3$ and $2 \times k + k$
 - **c** k+2 and 1+k+1
 - **d** k + 10 and $k \times 10$

Problem-solving and reasoning

- **9** Give an example of an expression that is equivalent to 4y.
- **10** The perimeter of this rectangle is given by w + l + w + l. Write an equivalent expression for the perimeter.



- 11 The expressions a + b and b + a are equivalent and only contain two terms. How many expressions are equivalent to a + b + c and contain only three terms and use only a, b and c and addition?
- **12** Prove that no two of these expressions are equivalent: 4 + x, 4x, x = 4, $x \div 4$.



13

Hint: Try making k stand for

k = 2, etc.) in a table.

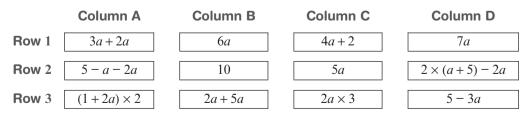
9.10

different numbers (k = 0, k = 1,

10-12

Matching pairs

13 On the following game board, each box has a partner box. Write all the matches. (For example, A1 and C2 match because 3a + 2a is equivalent to 5a.)



5D Like terms

Learning intentions

- To know what like terms are.
- To be able to identify like terms.
- To be able to simplify expressions using like terms.

Key vocabulary: like terms, simplifying, equivalent

Consider boxes of chocolates produced at a factory, with each box containing 12 chocolates. Then 3 boxes added to 5 boxes would contain the same number of chocolates as 8 boxes. So $3 \times 12 + 5 \times 12 = 8 \times 12$.

Similarly, if each box contained *n* chocolates, then 3 boxes added to 5 boxes would be the same as 8 boxes. So 3n + 5n = 8n. The terms 3n and 5n would be considered 'like' terms and can therefore be collected when they are added or subtracted.



Lesson starter: Simplifying expressions

- Show that 4a + 3a is equivalent to 7a. (For example, you could use a table of values.)
- Is 4a + 3b equivalent to 7ab? Choose values of a and b to substitute and check.
- What is the difference between 4a + 3a and 4a + 3b?
- Write a sentence to explain why 4a + 3b can't be simplified.

Key ideas

Like terms have exactly the same pronumerals, although not necessarily in the same order.

Like	Not like
3x and $5x$	3x and $5y$
-12a and $7a$	11d and $4c$
5ab and 6ba	-8ab and $5a$

 Like terms can be combined. This is called **simplifying** like terms. For example: 3x + 5x simplifies to 8x 12a - 7a simplifies to 5a

Exercise 5D

Understanding

5

1-5

- 1 True or false?
 - a If you add 5a to 3a you get 8a.
 - **b** If you add 5*b* to 6*a* you get 11*b*.
 - **c** If you take 6c away from 10c you have 4c left.
 - **d** If you add 6c to 3a you get 9c.

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51

5D	2	a If $a = 7$, what is $2a$? b If $a = 7$, what is $3a$? c If $a = 7$, what is $2a + 3a$? d If $a = 7$, what is $5a$?		Hint: $2a = 2 \times a$ = 2×7 = 14		
	3	Evaluate the following, using $x = 5$. a $10x$ b $4x$	c $10x - 4x$ d	6 <i>x</i>		
	4	For each of the following terms, list all the pro a $4xy$ b $3abc$	numerals it contains. c $2k$ d	pq		
	5	Copy and complete the following sentences. a $3x$ and $5x$ are terms. b $4x$ and $3y$ are not c $4xy$ and $4yx$ are like d $12a$ and $5ab$ are not like because		erals.		
		Fluency	6–9	(1/2) 6-10(1/2)		
\bigcirc	Ε	xample 7 Identifying like terms				
	a d	Vhich of the following pairs are like terms? $3x$ and $2x$ b $3a$ and $3b$ $2a$ and $4ab$ e $7ab$ and $9ab$		iba		
	S	olution	Explanation			
	a	3x and $2x$ are like terms.	The pronumerals are the sar			
	b	3a and $3b$ are not like terms.	The pronumerals are different.			
	C	2 <i>ab</i> and 5 <i>ba</i> are like terms.	The pronumerals are the same, even though they are written in a different order (one <i>a</i> and one <i>b</i>). The pronumerals are not exactly the same (the first term contains only <i>a</i> and the second term has <i>a</i> and <i>b</i>).			
	d	2a and 4ab are not like terms.				
	е	7 <i>ab</i> and 9 <i>aba</i> are not like terms.	The pronumerals are not exactly the same (the first term contains one a and one b , but the second term contains two a terms and one b).			
		Iow you tryVhich of the following pairs are like terms?5a and 4b5m and 4b7m and 4mne2xyz and 9z	c 5xy and 3 xxy	3yx		
	6	Classify the following pairs as like terms (L) or a $7a$ and $4b$ b $3a$ and 1 d $4a$ and $4b$ e 7 and 10 g $5x$ and 5 h $12ab$ and j $3abc$ and $12abc$ k $3ab$ and	Da c 18x an b f x and 4 4ab i 7cd and 4	4 <i>x</i> d 12 <i>cd</i>		

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Simplify:	
a $10x + 4x$	b $7a - 2a$
Solution	Explanation
a $10x + 4x = 14x$	10x and $4x$ are like terms, so they are combined $(10 + 4 = 14)$.
b $7a - 2a = 5a$	7 <i>a</i> and 2 <i>a</i> are like terms, so they are combined $(7 - 2 = 5)$.
Now you try	
Simplify:	
a 12 <i>m</i> – 7 <i>m</i>	b 14 <i>ab</i> + 20 <i>ba</i>
7 Simplify the following by collecting like terms. a $3x + 2x$ b $4a + 2a$ c $6q + 10q$ e $6cd + 3cd$ f $2qr + 4qr$ g $8ab + ab$	
8 Simplify the following by collecting like terms. a $7x - 3x$ b $8a - 5a$ c $10cd - 2cd$ f $8qr - 6qr$	c $12q - 2q$ g $8ab - ab$ d $7b - b$ h $10cf - 7cf$
Example 9 Simplifying by combining like	
Example 5 Simplifying by combining like	terms
	terms
Simplify the following by collecting like terms. a $7b+2+3b$ b $12d-4d+d$	terms c $5 + 12a + 4b - 2 - 3a$
Simplify the following by collecting like terms.	
Simplify the following by collecting like terms. a $7b+2+3b$ b $12d-4d+d$	c $5+12a+4b-2-3a$
Simplify the following by collecting like terms. a $7b+2+3b$ b $12d-4d+d$ Solution	c $5+12a+4b-2-3a$ Explanation 7 <i>b</i> and 3 <i>b</i> are like terms, so they are combined. They cannot be combined with 2 because it
Simplify the following by collecting like terms. a $7b+2+3b$ b $12d-4d+d$ Solution a $7b+2+3b = 10b+2$	 c 5+12a+4b-2-3a Explanation 7b and 3b are like terms, so they are combined. They cannot be combined with 2 because it contains no pronumerals. All the terms here are like terms. Remember that
Simplify the following by collecting like terms. a $7b + 2 + 3b$ b $12d - 4d + d$ Solution a $7b + 2 + 3b = 10b + 2$ b $12d - 4d + d = 9d$ c $5 + 12a + 4b - 2 - 3a$ = 12a - 3a + 4b + 5 - 2	 c 5+12a+4b-2-3a Explanation 7b and 3b are like terms, so they are combined. They cannot be combined with 2 because it contains no pronumerals. All the terms here are like terms. Remember that <i>d</i> means 1<i>d</i> when combining them. 12a and 3a are like terms. We subtract 3a because it has a minus sign in front of it. We can also combine the 5 and the 2 as they are

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- **5D**
- Simplify the following by collecting like terms.
- **a** 2a + a + 4b + b**b** 5a + 2a + b + 8b
 - **c** 3x 2x + 2y + 4y**d** 4a + 2 + 3a
 - **e** 7 + 2b + 5b
- **10** Simplify the following by collecting like terms.
 - **a** 7f + 12 2f**b** 4a - 4 + 5b + b**c** 3x + 7x + 3y - 4x + y **d** 10a + 3 + 4b - 2a**e** 4 + 10g - 3gf 10x + 4x + 31y - y**g** 10 + 7y - 3x + 5x + 2y**h** 11a + 4 - 3a + 9
 - 3b+4b+c+5b-c

f 3k - 2 + 3k

8+3d-5+2d

Hint: For 7f + 12 - 2f, the sign in front of 2f tells us to subtract that term.

11.12



12-13

- **Problem-solving and reasoning**
 - 11 Ravi and Marissa each work for *n* hours per week. Ravi earns \$30 per hour and Marissa earns \$35 per hour.
 - a Write an expression for the amount Ravi earns in one week.
 - **b** Write an expression for the amount Marissa earns in one week.
 - c Write a simplified expression for the total amount Ravi and Marissa earn in one week.
 - **12** The length of the line segment shown could be expressed as a + a + 3 + a + 1.

3 a 1 a a

- a Write the length as a simplified expression.
- **b** What is the length of the segment if *a* is equal to 5?
- **13** a Show, using a table of values, that 3x + 2x is equivalent to 5x.
 - **b** Prove that 3x + 2y is not equivalent to 5x.
 - **c** Prove that 3x + 2y is not equivalent to 5xy.



- 14 Let x represent the number of marbles in a standard-sized bag. Xavier bought 4 bags and Cameron bought 7 bags.
 - a Write simplified expressions for:
 - i the number of marbles Xavier has.
 - ii the number of marbles Cameron has.
 - iii the total number of marbles that Xavier and Cameron have.
 - iv the number of *extra* marbles that Cameron has compared to Xavier.
 - **b** If x is 12, how many marbles do they each have?

Hint: For part b, try choosing different values for x and y.



14

5A	1	 a State the coefficient of b in the expression 7a + 11b + 4c. b State the coefficient of x in the expression 13x + 3y.
5A	2	 Write an expression for the following. a 7 more than x b 8 less than t c Triple the value of f d Half the value of p, then 4 is added
5A	3	In a room there are p people, and then 7 more people arrive. How many people are now in the room?
		A $p-7$ B $7-p$ C $7p$ D $p+7$
58	4	Given that $y = 4$, evaluate: a $y + 11$ b $5 \times y$ c $9 - y$ d $24 \div y$
5B	5	Substitute $x = 7$ and then evaluate each of the following. a $x+6$ b $73-x$ c $3x-5$ d $35 \div x+18-x$
5B	6	Substitute $a = 5$ and $b = 3$ and then evaluate: a $3a + b$ b $a + 4b$ c ab d $7a - 11b - 2$
5C	7	Copy and complete. Two or more expressions that are always equal are called expressions.
50	8	For each of the following pairs, decide if they are equivalent (E) or not equivalent (N). a $r+5$ and $r \times 5$ b $r \times 3$ and $r+r+r$ c $r+4$ and $2+r+2$ d $6r+3$ and $4r+4+2r-1$
50	9	Classify the following pairs as like terms (L) or not like terms (N). a 6c and 5d b 21x and 3x c 5 and 5t d 7xy and xy e 3abc and 3ab f 6wk and 3kw
50	10	Simplify the following by collecting like terms if possible. a $5x + 12x$ b $11kt - 4k$ c $16x + 4y + 7y$ d $5p + 8 - 3p$ e $10a + 4a + 5b + b$ f $17 + 3g - 12 - g$

5E Multiplying and dividing expressions

Learning intentions

- To know the different ways multiplication and division can be written.
- To be able to simplify expressions with multiplication.
- To be able to simplify expressions with division.

Key vocabulary: factors, pronumerals, simplify

When we simplify and write expressions involving multiplication and division we usually do not use the \times or \div symbols.

Remember that 4*a* means $4 \times a$ and $6xy = 6 \times x \times y$. Also, we write fractions like $\frac{b}{3}$ to mean $b \div 3$.

Lesson starter: Putting in the multiplication symbol

- Rewrite the following expression by putting in all the \times signs. 7abc + 2de + 3f
- How can the following expression be written without × signs? Put the pronumerals in alphabetic order within each term to find a hidden message.
 s × i × m × c × h × p + v × l × u + s × p × c × i × h

Key ideas

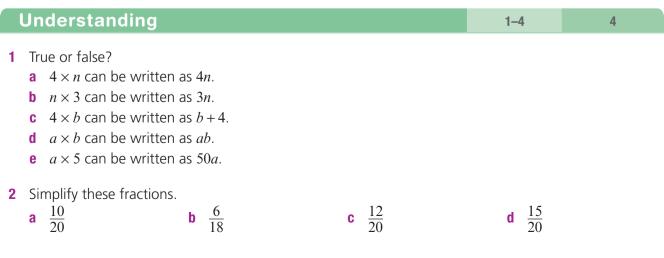
- $a \times b$ is written ab.
- $a \div b$ is written $\frac{a}{b}$.
- For multiplication, numbers should be written first and pronumerals are usually written in alphabetical order.
 For example: a × 2 × b is written 2ab

For example: $a \times 2 \times b$ is written 2ab.

When dividing, we write division using fraction form and any common factors in the numerator and denominator can be cancelled.

For example: $\frac{{}^{2}\mathcal{A}a\mathscr{b}^{1}}{{}^{1}\mathscr{L}\mathscr{b}^{1}c} = \frac{2a}{c}$

Exercise 5E



3	a Simplify the fraction $\frac{12}{18}$.				
	10			Hint: $\frac{12}{18} = \frac{2 \times 6}{3 \times 6}$	
	b Simplify the fraction $\frac{2000}{3000}$.			$\frac{2000}{3000} = \frac{2 \times 1000}{3 \times 1000}$	
	c Simplify $\frac{2a}{3a}$.			$\frac{2a}{3a} = \frac{2 \times a}{3 \times a}$	
4	Match these expressions (a to e) with the conventi write them (A to E).	ona	al way to		
	a $2 \times u$	Α	3и		
	b $7 \times u$	В	$\frac{5}{u}$		
	c $5 \div u$	C	2 <i>u</i>		

 $\frac{u}{5}$

E 7*u*

D

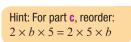
Fluency Example 10 Simplifying expressions	5–8(½) 5–9(½) with multiplication
a Write $4 \times a \times b \times c$ without multiplication s b Simplify $4a \times 2b \times 3c$, giving your final answ	
Solution	Explanation
a $4 \times a \times b \times c = 4abc$	When pronumerals are written next to each other, they are being multiplied.
b $4a \times 2b \times 3c = 4 \times a \times 2 \times b \times 3 \times c$ = $4 \times 2 \times 3 \times a \times b \times c$ = $24abc$	First insert the missing multiplication signs. Rearrange to bring the numbers to the front. $4 \times 2 \times 3 = 24$ and $a \times b \times c = abc$
Now you try	
a Write $3 \times x \times y$ without multiplication sign b Simplify $2a \times 5b \times 4c$, giving your answer v	

5 Write each of these expressions without multiplication signs.

а	$2 \times x$	b	$5 \times p$	C	$7 \times r$
d	$11 \times s$	е	$10 \times a \times b$	f	$5 \times c \times d$

6 Write each of these expressions without any multiplication signs.

а	$5 \times 2 \times a \times b$	b	$2 \times 8 \times x \times y$
С	$2 \times b \times 5$	d	$x \times 7 \times z \times 4$
е	$2 \times a \times 3 \times b \times 6 \times c$	f	$8 \times d \times 2 \times e \times 3 \times f$
g	$7 \times 3 \times a \times 2 \times b$	h	$a \times 2 \times b \times 7 \times 3 \times c$
i.	$7 \times a \times 12 \times b \times c$	j	$x \times 2 \times 3y$



d $u \times 3$

e *u* ÷ 5

7

- **5**E
- Simplify these expressions.
- a $3a \times 12$
- c $2 \times 4e$
- e $4a \times 3b$
- **g** $8a \times bc$
- $a \times 3b \times 4c$
- **k** $4d \times 3e \times 5fg$

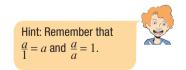
- **b** $7d \times 9$
- d $3 \times 5a$
- f $7e \times 9g$ h $4d \times 7af$
- $j \quad 2a \times 4b \times c$
- Т
- $2cb \times 3a \times 4d$
- Example 11 Simplifying expressions with division
- a Write $x \div 3$ without a division sign.
- **b** Simplify the expression $\frac{8ab}{12b}$.

Solution	Explanation
a $x \div 3 = \frac{x}{3}$	Divisions are written as fractions in algebra.
b $\frac{8ab}{12b} = \frac{8 \times a \times b}{12 \times b}$	Insert multiplication signs to help spot common factors.
$=\frac{2\times\cancel{4}^{1}\times a\times\cancel{b}^{1}}{3\times\cancel{4}^{1}\times\cancel{b}^{1}}$	8 and 12 have a common factor of 4. $4 \div 4 = 1, b \div b = 1$
$=\frac{2a}{3}$	Cancel out the common factors of 4 and b .

Now you try

- a Write $6 \div m$ without a division sign.
- **b** Simplify the expression $\frac{10xy}{25y}$
- 8 Write each expression without a division sign.
 - **b** z ÷ 2 **a** *x* ÷ 5 **d** *b* ÷ 5 **c** *a* ÷ 12
 - f $5 \div d$ e $2 \div x$
 - **h** $a \div b$ **g** $x \div y$
- Simplify the following expressions by dividing by any common factors. 9

а	$\frac{2x}{5x}$	b	$\frac{5a}{9a}$	C	$\frac{9ab}{4b}$
d	$\frac{2ab}{5a}$	e	$\frac{2x}{4}$	f	$\frac{9x}{12}$
g	$\frac{10a}{15a}$	h	$\frac{30y}{40y}$	i	$\frac{4a}{2}$
j	$\frac{21x}{7x}$	k	$\frac{4xy}{2x}$	I	$\frac{9x}{3xy}$



Hint: Multiply the numbers

alphabetical order.

and write the pronumerals in

10, 11

width \times length

а

11 Five friends go to a restaurant. They split the bill evenly, so each pays the same amount.

- a If the total cost is \$100, how much do they each pay?
- **b** If the total cost is \$*C*, how much do they each pay? Write an expression.
- **12** The expression $3 \times 2p$ is the same as the expression 2p + 2p + 2p. (1)(2)(3)
 - **a** What is a simpler expression for 2p + 2p + 2p?
 - **b** $3 \times 2p$ is shorthand for $3 \times 2 \times p$. How does this relate to your answer in part a?



CORE Year 7

13 The area of this rectangular paddock is 3*a*.

Both the length and the width of the paddock are now doubled.

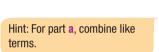
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- a Draw the new paddock, showing its dimensions.
- **b** Write a simplified expression for the area of the new paddock.
- **c** Divide the area of the new paddock by the area of the old paddock. What do you notice?
- **d** What happens to the area of the original paddock if you triple both the length and the width?

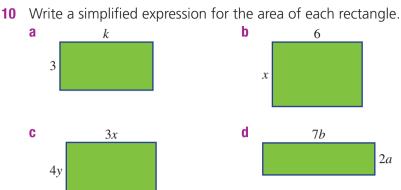


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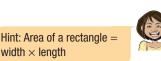




Problem-solving and reasoning

а

С



10-12

13

5F Applying algebra 🕇

Learning intentions

- To know that algebra can model a variety of situations.
- To be able to apply an expression in a modelling situation.
- To be able to construct an expression from a problem description.

Key vocabulary: model, expression, substitute, evaluate

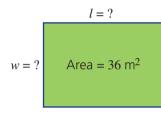
An algebraic expression can be used to describe problems relating to many different everyday situations, including costs, speeds and sporting results.



Lesson starter: Garden bed area

The garden shown below has an area of 36 m^2 , but the width and length are unknown.

- What are some possible values that *w* and *l* could equal?
- Try to find the dimensions of the garden that make the fencing around the outside as small as possible.

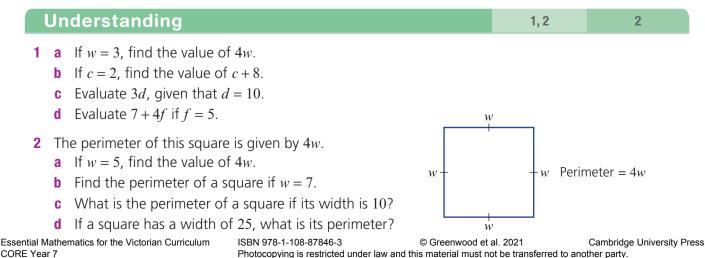


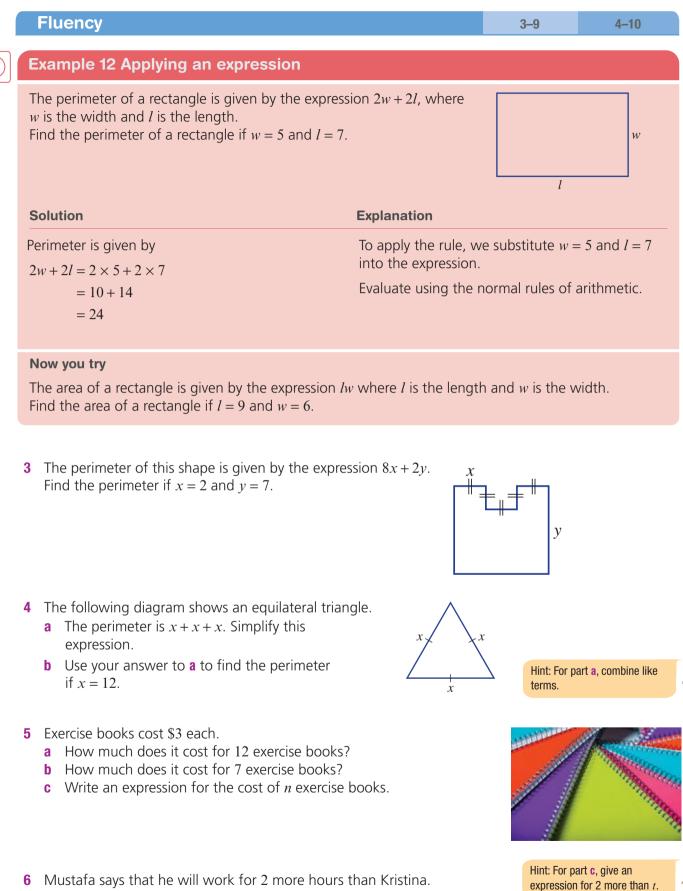
Key ideas

- Many different situations can be modelled with algebraic expressions.
- For example: an algebraic expression for perimeter of a rectangle is 2l + 2w.
- To apply an expression, the pronumerals should be defined clearly. Then known values should be substituted for the variables.
 For example: If *l* = 10 and *w* = 5,
 Perimeter = 2 × 10 + 2 × 5

= 30

Exercise 5F





- - a If Kristina works for 4 hours, how long will Mustafa work?
 - **b** If Kristina works for 9 hours, how long will Mustafa work?
 - **c** If Kristina works for *t* hours, how long will Mustafa work? Give an expression.

	r
\mathbf{J}	

Example 13 Constructing expressions from situations

Write expressions for each of the following.

- a The total cost, in dollars, of 10 bottles, if each bottle costs x.
- **b** The total cost, in dollars, of hiring a plumber for *n* hours. The plumber charges a \$30 call-out fee plus \$60 per hour.

Solution	Explanation
a 10 <i>x</i>	Each of the 10 bottles costs x , so the total cost is $10 \times x = 10x$.
b 30 + 60 <i>n</i>	For each hour, the plumber charges \$60, so you must pay $60 \times n = 60n$. The \$30 call-out fee is added to the total bill.

Now you try

Write expressions for each of the following.

- **a** The total cost, in dollars, for each person if a bill of \$100 is split between *n* people.
- **b** The total cost, in dollars, of an electrician for *t* hours who charges an \$80 call-out fee and \$100 per hour.
- 7 If pencils cost x each, write an expression for the cost of:
 - a 10 pencils.
 - **b** 3 packets of pencils, if each packet contains 5 pencils.
 - **c** k pencils.
- 8 If pens cost \$2 each, write an expression for the cost of *n* pens.
- 9 A car travels at 60 km/h, so in *n* hours it has travelled 60*n* kilometres.
 - **a** How far does the car travel in 3 hours (i.e. n = 3)?
 - **b** How far does the car travel in 30 minutes?
 - **c** Write an expression for the total distance travelled in n hours for a motorbike with speed 70 km/h.
- **10** A carpenter charges a \$40 call-out fee and then \$80 per hour. This means the total cost for x hours of work is 40 + 80x.
 - **a** How much would it cost for a 2-hour job (i.e. x = 2)?
 - **b** How much would it cost for a job that takes 8 hours?
 - **c** The call-out fee is increased to \$50. What is the new expression for the total cost of *x* hours?

Problem-solving and reasoning

- 11 A plumber charges a \$50 call-out fee and \$100 per hour.
 - **a** Copy and complete the table below.

Hours	1	2	3	4	5
Total cost (\$)					

- **b** Find the total cost if the plumber works for *t* hours. Give an expression.
- **c** Substitute t = 30 into your expression to find how much it will cost for the plumber to work 30 hours.





	1	2,	1	3

11, 12

14

- **12** To hire a tennis court, you must pay a \$5 booking fee plus \$10 per hour.
 - **a** What is the cost of booking a court for 2 hours?
 - **b** What is the cost of booking a court for *x* hours? Write an expression.
 - **c** A tennis coach hires a court for 7 hours. Substitute x = 7 into your expression to find the total cost.



- 13 In Australian Rules football, a goal is worth 6 points and a behind is worth 1 point. This means the total points scored for a team is 6g + b, if g goals and b behinds are scored.
 - a What are the total points scored for a team that has scored 5 goals and 3 behinds?
 - **b** What are the values of g and b for a team that has scored 8 goals and 5 behinds?
 - **c** If a team has scored 20 points, this could be because g = 2 and b = 8. What are the other possible values of g and b?

Mobile phone mayhem

14 Rochelle and Emma hire two different satellite phones for an extended mountain trek. The costs to make calls on these phones are outlined in this table below.

Rochelle's plan	Emma's plan
20 cents connection fee	80 cents connection fee
60 cents per minute	40 cents per minute

- **a** Write an expression for the cost of making a *t*-minute call using Rochelle's phone.
- **b** Write an expression for the cost of making a *t*-minute call using Emma's phone.
- **c** Whose phone plan would be cheaper for a 7-minute call?
- d What length of call would cost exactly the same for both phones?



S Maths@Work: Office designs

Planning the design and structure of office spaces requires skill with geometry and number patterns. A business will employ experts to plan their office work and meeting areas. Designing an office or conference space to hold the best arrangement of people and computers is important for productivity and progress.

Algebra skills help in this planning process, using patterns for layouts as well as formulas for costings.

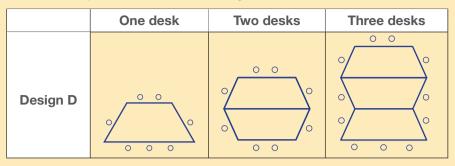


1 Below are some table designs. For each table design, answer the following four questions.

- i List the sequence for the number of people at 1, 2, 3 and 4 desks. You can draw extra groups of desks if you wish.
- ii Write a formula (i.e. a rule) for the number of people that could sit at *n* desks with each design.
- iii Calculate the number of people sitting at 10 desks.
- iv If each desk costs \$890, each office chair costs \$345, and there is a delivery fee of \$199 per order, calculate the total cost for 10 desks and accompanying chairs of each design.
- Hint: For Designs *B* and *C*
- How many people are always sitting on the ends?
- people sit in the middle for 2 desks, 3 desks, *n* desks. Formula Number of people = $2 + 1 \times n$

	One desk	Two desks	Three desks
Design A			
Design B			
Design C	0 0 0 0 0 0		

2 Answer the questions below for Design D.

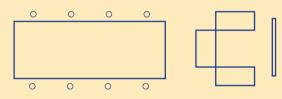


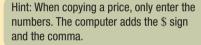
- a Draw 4 desks of Design D showing the chairs as small circles.
- **b** List the number sequence for the number of people at 1, 2, 3 and 4 desks.
- **c** Following this number pattern in part **b**, extend the sequence to find the number of people sitting at 10 desks.

Using technology

3 Office designs can include areas for staff to meet and discuss plans in a more relaxed setting. Design E:

Each row has one table for 8 people, 3 lounge chairs and a large video screen.







a Set up the following spreadsheet for Design E. Select all the cost cells (in columns B to H), right click, select Format/Currency/0 d.p.

1	Α	В	c	D	E	F	G	н
1				Cost of	f office furniture			
2	Office	Cost of one large table	Cost of one office chair	Cost of one lounge chair	Cost of one row of furniture	Number of rows	Cost of large video screen	Total cost
,	1	\$2,541	\$345	\$1,500		4	\$2,100	
	н	\$4,320	\$548	\$2,300		9	\$2,460	
5	ш	\$3,875	\$470	\$1,750		15	\$2,040	
6	IV	\$2,758	\$275	\$1,200		24	\$1,750	

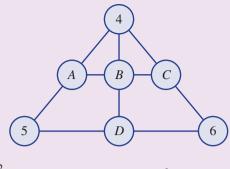
b Enter formulas into the shaded cells to calculate the total furniture cost for each office.

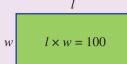


а

- Puzzles and games
- Each line of three numbers in the triangle adds to 12.
 Find the value of A, B, C and D.

2 A rectangular paddock must have an area of 100 metres². What is the minimum amount of fencing required?





3 Find the values of the pronumerals in the following tables.

			Sum	b				Product
	a	b	С			а	b	18
	d	24	32			2	С	d
Sum	12	е	48		Product	12	е	180

4 Copy and complete the following table in which *x* and *y* are always whole numbers.

x	2				
У	7	6		12	
3 <i>x</i>		6	9		
x + 2y			9		7
xy				0	5

5 In a mini-Sudoku, the digits 1 to 4 occupy each square. No row, column or 2×2 block has the same digit twice. Find the value of each of the pronumerals in the following mini-Sudoku.

a	3	2	С
С	d	е	f
2	g	<i>d</i> + 1	h
i	1	j	k

6 In a magic square the sum of each row, column and diagonal is the same. Find the value of the unknown variables to make the following into magic squares. Confirm your answer by writing out the magic square as a grid of numbers.

b

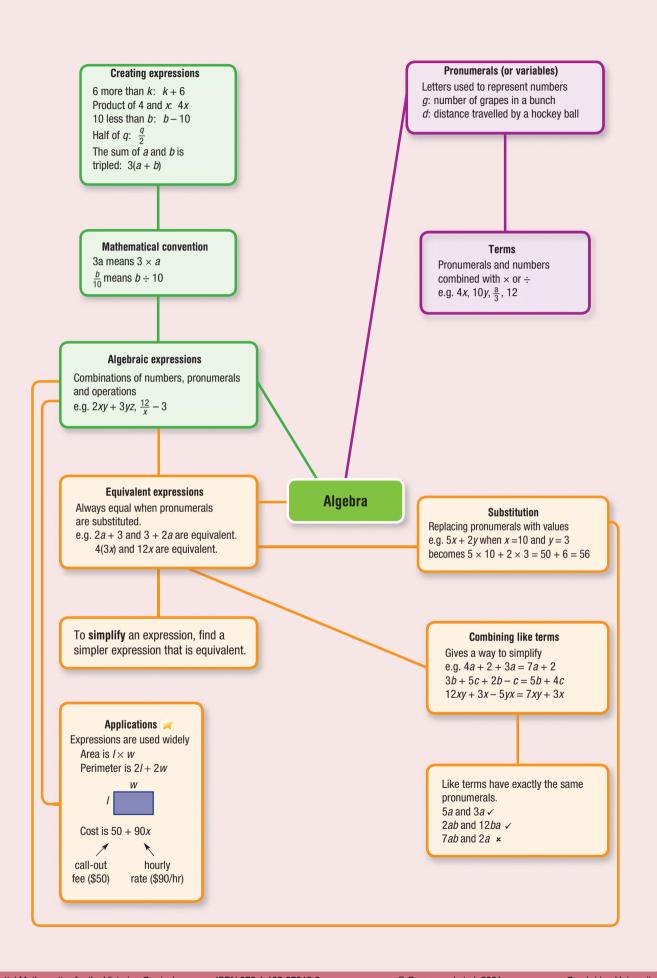
5	12	A				
В	С	6				
D	E	F				
(Magi	(Magic sum is 24.)					

A	В	С		
<i>A</i> – 1	<i>A</i> + 1	B - C		
<i>B</i> – 1	<i>C</i> – 1	A + C		
(Magic sum is 15.)				

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a

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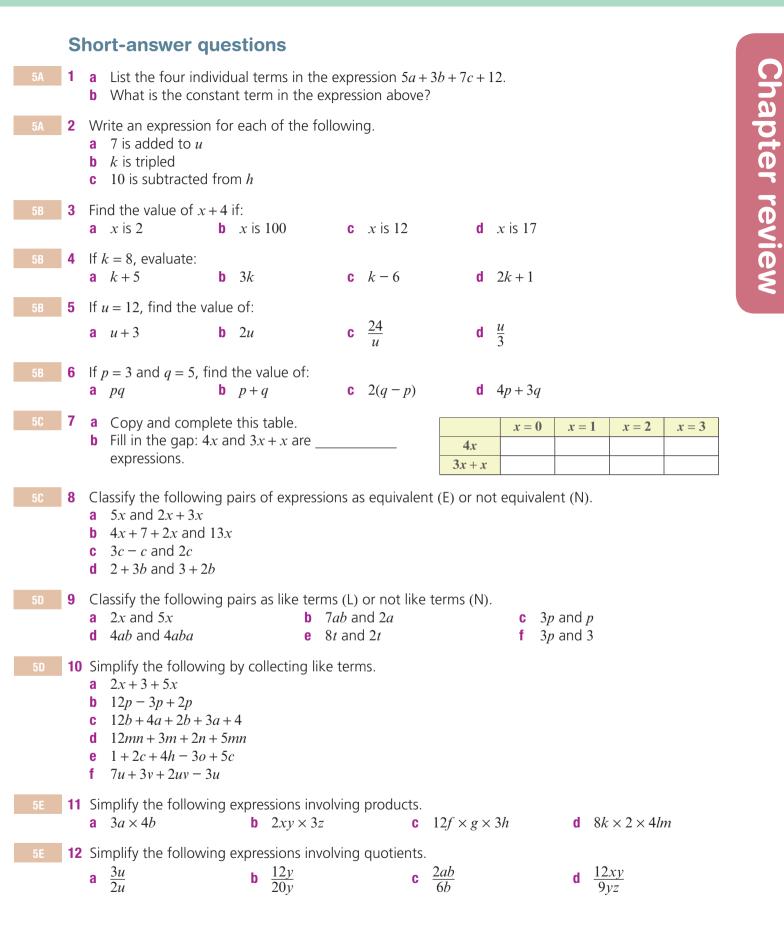
Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

V

Chapter checklist <

1	I can list terms within expressions. e.g. List the terms in $3a + b + 13c$.
2	
3	I can write algebraic expressions from word descriptions. e.g. Write an expression for "the sum of <i>a</i> and <i>b</i> ".
4	I can substitute a number for a pronumeral and evaluate. e.g. Given that $t = 5$, evaluate 8t.
5	I can substitute multiple numbers for multiple pronumerals and evaluate. e.g. Substitute $x = 4$ and $y = 7$ to evaluate $5x + y + 8$.
6	I can decide whether two expressions are equivalent. e.g. Fill in a table to help decide if $3a + 6$ and $(a + 2) \times 3$ are equivalent. Use $a = 0$, $a = 1$, $a = 2$ and $a = 3$.
7	I can decide whether two terms are like terms. e.g. Decide whether 2 <i>ab</i> and 5 <i>ba</i> are like terms, giving reasons.
8	I can simplify using like terms. e.g. Simplify $7b + 2 + 3b$ by collecting like terms.
9	I can simplify expressions involving multiplication. e.g. Simplify $4a \times 2b \times 3c$, giving your final answer without multiplication signs.
10	I can simplify expressions involving division. e.g. Simplify the expression $\frac{8ab}{12b}$.
11	I can apply an expression in a modelling problem. e.g. Given the perimeter of a rectangle is $2w + 2l$, find the perimeter of a rectangle with length 7 cm and width 5 cm.
12	I can construct an expression from a problem description. e.g. Write an expression for the total cost of hiring a plumber for <i>n</i> hours, if they charge \$30 call-out fee plus \$60 per hour.



13 If a tin of paint weighs 9 kg, write an expression for the weight of *t* tins of paint.

14 If there are g girls and b boys in a class, write an expression for the total number of children.



15 Analena owns *x* fiction books and twice as many non-fiction books. Write an expression for the total number of books that Analena owns.



Multiple-choice questions

5A	1	In the expression	3x + 2y + 7z	the coeffi	cient of y is:				
		A 3	B 2	C	4	D	7	Е	16
5B	2	If $b = 7$, then $b + $	5 is equal to	:					
		A 5	B 7	C	57	D	12	E	75
5B	3	If $t = 5$ and $u = 7$							
		A 17	B 32	C	24	D	257	E	70
5C	4	If two expression	s are always			the	5		
		A pronumerals			valent		C coefficie	ent	
	-	D variables			ant terms	Ι.			
5D	5	Which of the foll A $3x$ and $5x$	51		3 <i>ab</i> and 2 <i>ab</i>				3xy and xy
EA	G	How many terms	•	•				5	<i>3<i>xy</i> and <i>xy</i></i>
5A	0	A 1	B 2	che expre		ר <i>ככ</i> D		Е	6
5D	7	A fully simplified				_		7	0
00	1	A 4	•	•	10ab + 4			Е	11 <i>ab</i>
5E	8	The simplified fo							
	-	A 43 <i>xyz</i>	B 12 <i>xy</i>	·	12 <i>xyz</i>	D	12 <i>yz</i>	Е	4 <i>x</i> 3 <i>y</i> z
5E	9	The simplified fo	rm of $\frac{21ab}{3ac}$ is	5					
		A $\frac{7b}{c}$	B $\frac{7ab}{ac}$	C	$\frac{21b}{3c}$	D	7	E	$\frac{b}{7c}$
5F	10	A number is dou	bled and the	en 5 is add	ed. The result is	; tri	pled. The numb	ber i	S
-	-	represented by k	. An expressi						
		A $3(2k+5)$	B $6(k+5)$	C	2 <i>k</i> + 5	D	2 <i>k</i> + 15	E	30 <i>k</i>

Extended-response questions

- 1 To hire a tennis court, Cat must pay \$20 per hour. The total cost in dollars for *n* hours is 20*n*.
 - **a** How much would it cost in total to hire the court for 3 hours?
 - **b** If n = 3, state the value of 20n.
 - **c** If Cat wants to hire the court at night she must pay \$30 per hour to pay for the lights. How much would 3 hours at night cost?
 - **d** Write an expression for the total cost of hiring the court for *n* hours at night.
 - On one occasion, Cat hired the court for 2 hours during the day and then another 2 hours during the night. What was the total cost?



- 2 A taxi driver charges \$2 to pick up passengers and then \$1.50 per kilometre travelled.
 - a State the total cost if the trip length is: i 10 km ii 20 km
 - ii 20 km iii 100 km
 - **b** Write an expression for the total cost of travelling a distance of k kilometres.
 - **c** Use your expression to find the total cost of travelling 40 km.
 - **d** Another taxi driver charges \$6 to pick up passengers and then 1.20 per kilometre. Write an expression for the total cost of travelling k kilometres in this taxi.



Chapter Decimals

Essential mathematics: why skills with decimals are important

Decimal number calculations provide accurate results which are essential in sport, construction, food production, manufacturing, financial management, technology and scientific research.

- Many sports results include decimal places. Using modern technology, race times at the MotoGP, Phillip Island, are rounded to 3 decimal places; and at the Gold Coast 600, race times are rounded to 4 decimal places.
- Decimal numbers are multiplied when scoring individual or synchronised diving. A cricketer's batting average is found using division with decimal places. The highest Test cricket batting average in history is 99.94, held by Sir Donald Bradman.
- A car's engine capacity is the total volume of its cylinders. This is given in litres and rounded to the nearest tenth, e.g. 2.5 L or 1.8 L.
- Nurses calculate exact volumes to be injected for prescribed medications. To allow accurate measurements, syringe scales show tenths or hundredths of a millilitre.

Essential Mathematics for the Victorian Curriculum CORE Year 7



In this chapter

- 6A Decimals and place value (Consolidating)
- 6B Rounding decimals
- 6C Addition and subtraction of decimals (Consolidating)
- 6D Multiplying and dividing by powers of 10
- 6E Multiplication of decimals 🔶
- 6F Division of decimals 🔶
- 6G Decimals and fractions
- 6H Decimals and percentages

Victorian Curriculum

NUMBER AND ALGEBRA Real numbers

Multiply and divide fractions and decimals using efficient written strategies and digital technologies (VCMNA244)

Round decimals to a specified number of decimal places (VCMNA246)

Connect fractions, decimals and percentages and carry out simple conversions (VCMNA247)

Find percentages of quantities and express one quantity as a percentage of another, with and without digital technologies. (VCMNA248)

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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more. Warm-up quiz

1	Complete the following.			
	a $\frac{1}{10} = 0.$		b	$\frac{3}{10} = 0.$
	c $\frac{17}{10} = 1$		d	$\frac{1}{100} = 0.0$
	e $\frac{1}{1000} = 0.$		f	$\frac{47}{10} = $
2	Write the decimal for: a one-half b	one-quarter		c three-quarters
3	Write the following cents as dollaa 70 centsc 100 centse 105 cents	ſS.	b d f	85 cents 5 cents 3 cents
4	Find how many cents are in: a half a dollar c three-quarters of \$1		b d	one-quarter of \$1 half of \$5
5	Find the cost of: a two labels at 45 cents each c $1\frac{1}{2}$ boxes of mangoes at \$15 a		b d	10 pears at \$1.05 each three pens at 27 cents a pen

- 6 Tom paid \$20 for 200 photos to be printed. What was the cost of each print?
- **7** \$124 is shared between eight people. If each share is the same amount, how much does each person receive?
- 8 Complete:
 - **a** \$8.50 × 10 = _____
 - **b** \$6 \$5.90 = ___
 - **c** \$10 \$7.30 =
 - **d** \$70 ÷ 100 = ____
 - **e** \$6.90 + \$4.30 = ____
 - f \$20 \$19.76 =
- **9 a** Take \$5 away from \$12.
 - **b** Take \$2.10 away from \$5.
 - **c** Add \$1.70 and \$2.25.
 - **d** Add \$12.50 to \$17.25.
 - **e** Take \$2.50 away from \$10.

10 Calculate how much change from \$100 Calvin receives when he spends:

a \$12.50 **b** \$7.40 **c** \$79.10

11 Find the total of these amounts: \$7, \$5.50, \$4.90, \$12 and \$9.15.

12 Complete these problems (without decimals).

a 329	b 1024	c 104	d $5\overline{)6185}$
<u>+194</u>	<u>- 185</u>	<u>× 3</u>	,

6A Decimals and place value

CONSOLIDATING

Learning intentions

- To understand the meaning of a decimal point.
- To know what the place value is of digits after a decimal point.
- To be able to decide if one decimal is larger or smaller than another decimal.
- To be able to convert proper fractions and mixed numbers to decimals, when their denominators are powers of ten.

Key vocabulary: decimal, decimal point, place value, fraction part

Decimals are used in many aspects of everyday life. For example, Ian Thorpe swam the 400 metres freestyle in 3 minutes 40.08 seconds, which was a new world record at the time.

It's also very important to be able to use decimals, as our money works on a decimal system of dollars and cents.



Lesson starter: Decimals time trial

Work with a partner. You will need six cards:



How many different numbers can you make in 1 minute?

Key ideas

- A **decimal point** is used to separate the whole number from the **decimal** or **fraction part**.
- When dealing with decimal numbers, the place value table can be extended to involve tenths, hundredths, thousandths etc.

Hundreds	Tens	Ones	•	Tenths	Hundredths	Thousandths
4	2	8	•	3	5	7
4×100	2×10	8×1	1 1 1	$3 \times \frac{1}{10}$	$5 \times \frac{1}{100}$	$7 \times \frac{1}{1000}$
400	20	8	•	$\frac{3}{10}$	$\frac{5}{100}$	$\frac{7}{1000}$
whole	whole numbers		decimal point -	fractions		

We read the number 428.357 as four hundred and twenty-eight point three, five, seven.

Exercise 6A

Understanding 1-3 3 1 Match each decimal (a to e) with the correct wording (A to E). Hint: **a** 0.015 A Seventeen and three tenths **b** 10.835 **B** Five and thirteen hundredths ones . tenths hundredths thousandths **c** 5.13 **C** Zero point zero, one, six 0 1 T. 3 0 1 **d** 0.016 **D** Ten point eight, three, five $0.013 = \frac{13}{1000}$ = thirteen thousandths **e** 17.3 **E** Fifteen thousandths **2** For the number 58.237, give the value of the digit: Hint: **b** 3 **a** 2 **c** 7 Choose from: $\frac{7}{1000}, \frac{2}{10}, \frac{3}{100}$ **3** A stopwatch is stopped at 36.57 seconds. a What is the digit displayed in the tenths column? **b** What is the digit displayed in the ones column? c What is the digit displayed in the hundredths column? **d** Is this number closer to 36 or 37 seconds?

-	t 8 in the following numbers?
a 12.85	b 6.1287
Solution	Explanation
a The value of 8 is $\frac{8}{10}$.	The 8 is in the first column after the decimal point, which is the tenths column. (Think: First column, one zero in the denominator.)
b The value of 8 is $\frac{8}{1000}$.	The 8 is in the third column after the decimal point, which is the thousandths column. (Think: Third column, three zeros in the denominator.)
Now you try	
-	t 3 in the following numbers?
a 8.132	b 4.803

	Example 2 Changing to decimals						
Express each	of the following prope	r fractions and mixed	numbers as decimals.				
a $\frac{7}{10}$	b $\frac{5}{100}$	c $3\frac{1}{10}$	7_0				
Solution		Explanation					
a $\frac{7}{10} = 0.7$		$\frac{7}{10}$ means seven-tent	hs, so put the 7 in the tenths column.				
b $\frac{5}{100} = 0.0$	5	$\frac{5}{100}$ means five-hundredths, so put the 5 in the hundredths column.					
		Since there are no te	nths, put a zero in the tenths column.				
c $3\frac{17}{100} = 3$.	c $3\frac{17}{100} = 3.17$ $3\frac{17}{100}$ means 3 ones and 17 hundredths. 17 hundredths is one tenth and seven hundredths.						
Now you try							
	of the following prope	r fractions and mixed	numbers as decimals.				
a $\frac{2}{10}$	b $\frac{6}{1000}$	c 5 $\frac{4}{10}$					
5 Express ea a $\frac{3}{10}$	the following properties $\mathbf{b} = \frac{8}{10}$	per fractions as a decir c $\frac{15}{100}$	mal. d $\frac{23}{100}$				
e $\frac{9}{10}$	f $\frac{12}{100}$	g $\frac{121}{1000}$	h $\frac{174}{1000}$				
i $\frac{1}{10}$	j $\frac{11}{100}$	k $\frac{111}{1000}$	$1 \frac{3}{100}$				
6 Express ea	ach of the following mix	ed numbers as a decir	nal.				
	b $5\frac{7}{10}$		d $1\frac{16}{100}$				
a $6\frac{4}{10}$	10	10	100				
a $6\frac{4}{10}$	f $7\frac{51}{100}$	10					
 a 6⁴/₁₀ e 14⁸³/₁₀₀ 7 True (T) or 	f $7\frac{51}{100}$	g $5\frac{7}{100}$	h $18\frac{612}{1000}$				
 a 6⁴/₁₀ e 14⁸³/₁₀₀ 7 True (T) or 	f $7\frac{51}{100}$	g $5\frac{7}{100}$	h $18\frac{612}{1000}$				

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Problem-solving and reasoni	ng	8–10	9–12	
Example 3 Arranging decimal num	nbers in order			
Arrange the following decimal numbers in 3.72, 7.23, 2.73, 2.37, 7.32, 3.27	n ascending order (i.e. smallest	to largest):		
Solution	Explanation			
	The ones column has a higher column, and the tenths colum the hundredths column. 2.73 is bigger than 2.37 becaus is bigger than three tenths.	n has a higher v	value than	
Now you try				
Arrange the following decimal numbers in 8.34, 3.48, 4.83, 4.38, 3.84, 8.43	n ascending order (i.e. smallest	to largest):		
 8 Choose the larger decimal in each pair. a 6.1, 0.16 b 6.9, 9.6 d 25.8, 28.5 e 0.107, 0.17 	c 0.8, 0.08 1 f 0.032, 0.203	Hint: To compare		
	ending 0.6, 3.06, 3.6, 30.3 5.92, 29.26, 29.62, 22.96, 22.69	write them under other. Line up the points. 30.6 3.0	e decimal	
 10 The batting averages for five retired Augare: Adam Gilchrist 47.60, Steve Waugh Allan Border 50.56 and Kim Hughes 37.4 a List the five players in descending or b Ricky Ponting's test batting average retired Australian Test captains listed 	n 51.06, Mark Taylor 43.49, 41. Ider of batting averages (i.e. lar is 56.72. Where does this rank	5	30 t).	
 11 The depth of a river at 9 a.m. on six cord Day 1: 1.53 m Day 2: 1.58 m Day 3: 1.49 m Day 4: 1.47 m Day 5: 1.52 m Day 6: 1.61 m a On which day was the river level hig b On which day was the river level low c On which day was the water level at the second sec	hest? vest?			
12 Which is larger? a 0.7135 or $7 \times 1 + 1 \times \frac{1}{10} + 3 \times \frac{1}{100} + 5 \times \frac{1}{100} + \frac{1}{100$	$\times \frac{1}{1000}$ b 1.563 or $1 \times \frac{1}{10}$	$+5 \times \frac{1}{100}$		
Different decimal combinations			13	

- **13** For each of the following, write as many different decimal numbers as you can. (Each digit must be used only once, and all digits must be used.) How many different numbers did you get? Circle the largest number and the smallest number.
 - **a** Use the digits 0, 1 and a decimal point.
 - **c** Use the digits 0, 1, 2, 3 and a decimal point.
- **b** Use the digits 0, 1, 2 and a decimal point.

6B Rounding decimals

Learning intentions

- To understand that rounding involves approximating a decimal number to fewer decimal places.
- To know what the critical digit is for a rounding operation.
- To be able to round decimals to a given number of decimal places.

Key vocabulary: rounding, critical digit, round up, round down

Decimal numbers sometimes contain more decimal places than we need. It is important that we are able to round decimal numbers when working with money, measuring distance or writing answers to some division problems.

For example, the distance around the school oval might be 0.397 km, which rounded to 1 decimal place is 0.4 km or 400 m. The rounded figure, although not as precise, is accurate enough for most applications.



Lesson starter: Rounding brainstorm

In a group of four, brainstorm times when it may be useful to round or estimate decimal numbers. Aim to achieve more than 5 examples in each group.

Key ideas

- **Rounding** involves approximating a decimal number to fewer decimal places.
- To round a decimal, 'cut' the number after the required decimal place. For example, to round to 2 decimal places, imagine a cut after the second decimal place.
- To work out whether to round up or down, consider only the digit *immediately* to the right of the specified place. (We call this the **critical digit**.) Only the digit to the left of the 'cut' is changed (if necessary).
 - If the critical digit is 5 or more, **round up**.
 - If the critical digit is less than 5, round down.

Current critical digitRounding up:15.63 \$7becomes15.64Rounding down:21.35 \$48becomes21.35

Rounding *up* makes the decimal number *larger*, e.g. 15.64 > 15.6357 Rounding *down* makes the decimal number *smaller*, e.g. 21.35 < 21.3548

round down round up

Exercise 6B

	Understanding		1–4	4
1	How many decimal places do these decimals have a 0.73 b 0.1079 c 10		2.900 61	
2	The following decimals need to be rounded to	2 decimal places. [Draw a line where t	he number
	 must be cut and then circle the critical digit. a 12.6453 b 4.819 32 c 157.281 		Hint: Draw your line a 2nd decimal place ar next digit to the right.	d circle the
	 d 4001565.38471 e 0.06031 f 203.5791 g 66.6666 h 7.995123 			
3	 State the critical digit in each of the following ratio a 25.8174 rounded to 1 decimal place. b 25.8174 rounded to 2 decimal places. c 25.8174 rounded to 3 decimal places. d 25.8174 rounded to the nearest whole numbers. 		Critical digit Critical digit Critical digit Critical digit	=
4	For each of the following, select the closer alte a Is 8.2 closer to 8 or 9?	rnative.	· · · · · > 9	
	b Is 6.7 closer to 6 or 7?		• · · · · >	
	c Is 5.35 closer to 5 or 6?			
	Fluency		5–7(½), 8	5-7(1/2), 8, 9(1/2
Ε	xample 4 Rounding decimals to 1 deci	mal place		
R	25.682 b 13.5458			
R a	ound each of the following to 1 decimal place.	Explanation		
R a	cound each of the following to 1 decimal place. 25.682 b 13.5458 Solution	Explanation	t is 8, so round up.	
R a S	<pre>cound each of the following to 1 decimal place. 25.682 b 13.5458 colution 25.7</pre>	Explanation 25.682 The critical digi 13.5458	t is 8, so round up. t is 4, so round dow	/n.
R a s a b	25.682 b 13.5458 Solution 25.7	Explanation 25.6 8 2 The critical digi 13.5 4 58 The critical digit		/n.

Hint: Here, the critical digit is the

second decimal place.

5 Round each of the following to 1 decimal place.

а	14.82	b	7.38	C	15.62
d	0.87	е	6.85	f	9.94
g	55.55	h	7.98	i.	0.68
j	0.72	k	0.69	1	0.88

6 Write each of the following correct to 2 decimal places.

а	3.7823	b	11.8627	C	5.9156	d	0.93225
е	123.456	f	300.0549	g	3.1250	h	9.849
i	56.2893	j	7.121 999	k	29.9913	1	0.8971

a F	Round 18.347 28 t	03	decimal places.		b Rour	nd 0.439	917 to 2 de	cimal place	25.
Sol	ution				Explar	nation			
a 1	18.347				18.347 The cri	\sim	git is 2, so r	ound dow	n.
b ().44				0.439 The cri		git is 9, so re	ound up.	
Νοι	w you try								
a F	Round 0.0462 to 2	2 de	cimal places.		b Rour	nd 1.492	2 to 0 decim	nal places.	
d a		foll	owing to the sp	oecifie	d number of			decimal plac	nd $7.59(8)$ to 2 ces, think: 59 goes iswer = 7.60
	14.8992 (2) 6.954 32 (0) 29.999 731 (3)								
	ound each of the					er. This		e as zero d	ecimal places
а	27.612 22.26		9.458 117.555		12.299 2.6132	a h	123.72 10.7532		
-				Ŭ					
-									
e	roblem-solvi	ng	and reasor	ning				10, 11	11–13
e	roblem-solvi				ne nearest dol	lar.		10, 11	11–13
e	ound each of the \$12.85	foll b		s to th	ne nearest dol \$7.10 \$1.39	lar. d h	\$1566.80 \$36.19	10, 11	11–13

ISBN 978-1-108-87846-3 © Greenwood et al. 2021 Cambridge University Press Photocopying is restricted under law and this material must not be transferred to another party. 6**B**

11

- Petrol costs 149.9 cents per litre. Yannis put 48 litres in his car. He calculated that this would cost 7195.2 cents.
 - a What did Yannis type on his calculator to get this answer?
 - **b** How much should he pay correct to:
 - i the nearest cent?
 - ii the nearest dollar?



- 12 Lee rounded the decimal 74.74 63 to 2 decimal places. She wrote down 74.75. What could the missing digit be?
- **13** List all the decimal hundredths (such as 0.39) that would round to 0.4.

Rounding with technology

Most calculators are able to round numbers correct to a specified number of places. Find out how to do this on your calculator and check your answers to questions **6** and **7**.



14

6C Addition and subtraction of decimals CONSOLIDATING

Learning intentions

- To understand that to add or subtract decimals, additional zeros might need to be entered for some decimal places.
- To be able to add decimals.
- To be able to subtract decimals

Key vocabulary: decimal point, align, addition, subtraction

The techniques used for adding and subtracting decimals are similar to those used for whole numbers. Just as we vertically align digits in place value columns, we also align the decimal point.

Lesson starter: How fast can you calculate?

- Add 10 + 7 + 13 + 15 + 5.
 Now add 1 + 0.7 + 1.3 + 1.5 + 0.5.
- What about using money?
 Add \$1 + \$0.70 + \$1.30 + \$1.50 + \$0.50.
- Which calculation was the fastest?
- Now try 10 7.85 and \$10 less \$7.85.
 Counting with money often seems easier!



Key ideas

When adding or subtracting decimals, the decimal points and each of the matching decimal places must be written under one another.

1.56 Writing an +2.70 extra zero 4.26 will help. Line-up the decimal points underneath each other.

Ex Un	nderstanding]				1–3	3
1 If	7.12, 8.5 and 13.0 umbers ready for a	32 are to be	added togethe	r, which	of the follow	ing is the best	
A	-	В	7.12 8.5 13.032	C	7.120 8.500 +13.032	D	7.12 8.5 - <u>13.032</u>
	/hich of the follow	-	rrect way to pr		nd solve the su		olem 77.81
A	$ 77.81 \\ - 6.3 \\ \overline{84.11} $	-	77.81 6.30 71.51	С	$77.81 \\ -6.3 \\ \hline 14.81 \\ \hline$	D 	77.81 - 6.3 77.18
3 W	/rite down the ans	wer to these	sums by puttir	ng the d	ecimal point i	n the correct p	place.
а	5.16		b 3.047		C	15.7	
	$+ 3.41 \\ 857$		0.522 + 1.610			$\frac{+\ 0.056}{15\ 956}$	
E1.			5179			A ((1/)	6 7
	uency	docimala	5179			4–6(½)	5–7
Exa	uency Imple 6 Adding	decimals	5179			4–6(½)	5–7
Exa Find	uency Imple 6 Adding	decimals	5179	b 64.	8 + 3.012 + 5.9		5–7
Exa Find a 8.	uency Imple 6 Adding	decimals	5179		8 + 3.012 + 5.9 anation		5–7
Exa Find a 8. Solu a 1 +	uency mple 6 Adding I: 3.31 + 5.93	decimals	5179		anation	4	5–7
Exa Find a 8. Solu a 1 + 1 b 1 (+	uency mple 6 Adding 1: .31 + 5.93 ution 18.31 5.93	decimals	5179	Expl a Write Put c Fill m	e: 8.31 Th + 5.93 	4	other. ceros.

e	$ \frac{+5.6}{} $ 13.25 +14.72 Find each of the fo	$\begin{array}{c} \mathbf{b} & 12.61 \\ + 2.35 \\ \hline \\ \mathbf{f} & 7.23 \\ 16.31 \\ + 2.40 \\ \hline \end{array}$	g c 0.4	2.83 + 1.04 210.0 22.3 + 15.1 6 + 0.3 072 + 6.435	d 7.90 + 1.09 h 47.81 6.98 + 3.52 Hint: Rewrite the sums as shown in Example 6, lining up	
g	12.45 + 3.61	h 5.37 + 13.8		012 + 0.001	the decimal points.	
		acting decimals				
Fine	d: 5.83 – 3.12		h 146 3	35 - 79.5		
	lution		Explar			
а	$5.83 \\ -3.12 \\ \hline 2.71 \\ \hline$		Write:	5.83 Then su -3.12	btract.	
b	$\begin{array}{r} 1 & 13 \\ 4 & 6.35 \\ - & 7 & 9.50 \\ \hline & 6 & 6.85 \end{array}$		Fill mis			
	w you try					
Find a	d: 36.2 – 21.1		b 193.2	2 - 128.91		
e	$ \frac{-0.20}{-0.20} \\ \frac{-0.20}{-0.20}$	b 0.756 <u>-0.240</u> f 128.63 <u>- 14.50</u>	c 1.2 <u>-0.8</u> g 23.94 <u>-17.61</u>	d 1.99 <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.26</u> <u>-0.</u>		
7 F a c g j	23.7 - 2.5 14.8 - 2.5 25.9 - 3.67	d 0. f 2. h 3	.6 - 2.4 98 - 0.5 34.6 - 103.2 1.657 - 18.2 312.271 - 364.93		Hint: Rewrite the subtractions as shown in Example 7.	

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6C

Problem-solving and reasoning

- 8 Find the total of 0.808, 4.376 and 11.005.
- **9** Stuart wants to raise \$100 for the Rainbow Club charity. He already has three donations of \$30.20, \$10.50 and \$5.00.
 - **a** How much has Stuart already raised?
 - **b** How much does Stuart still need to raise?



8,9

9-11

10 Daily rainfalls for four days over Easter were 12.5 mm, 3.3 mm, 0.6 mm and 33 mm. What was the total rainfall over the four-day Easter holiday?



11 Bryce's normal body temperature is 36.9°C. During a fever, Bryce's temperature rose to 40.2°C. What is the difference in temperature?



Decimals magic square _____ 12

12 Complete these magic squares. First determine the magic sum.

b

0.6		0.2
0.1		
0.8		
	0.1	0.1

а

1.6	0.5		0.4
0.3		0.6	1.5
	1.1		
1.3		1.2	

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6D Multiplying and dividing by powers of 10

Learning intentions

- To understand that a power of ten is a number like 10, 100, 1000, etc.
- To be able to multiply a decimal by a power of ten.
- To be able to divide a decimal by a power of ten.

Key vocabulary: power of 10, decimal point, multiplication, division

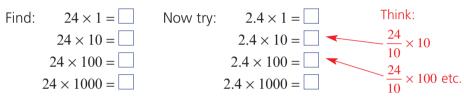
Powers of 10 include 10^1 , 10^2 , 10^3 , 10^4 , ..., which correspond to the numbers 10, 100, 1000, 10 000, ... Note that the number of zeros in the number is the same as the power of 10 for that number. $10^1 = 10$ (1 zero)

 $10^2 = 100 (1 \text{ zeros})$ $10^2 = 100 (2 \text{ zeros})$

 $10^3 = 1000 (3 \text{ zeros})$



Lesson starter: Multiplying by 'tens'



Where is the decimal point in the question?

Where is it in the answer?

How does the place value of the 2 and the 4 change when you multiply 24 by a power of 10?

Key ideas

- The decimal places are the number of digits on the right-hand side of the decimal point. For example: 7.8 has 1 decimal place and 12.407 has 3 decimal places.
- When multiplying by **powers of** 10:
 - the number of decimal places will decrease by the same number of places as there are zeros in the multiplier.

For example: to multiply by 1000, the decimal point should move 3 places to the right.

 $5.7839 \times 1000 = 5783.9$

- When dividing by powers of 10:
 - the number of decimal places will increase by the same number of places as there are zeros in the divisor.

For example: to divide by 100, the decimal point should move 2 places to the left.

$$2975.6 \div 100 = 29.756$$

Exercise 6D

Understanding

1 How many places does the decimal point move in each of these multiplications and divisions?

1-4

5-7(1/2)

5-8(1/2)

4

- **a** $278.71 \times 10 = 2787.1$
- **b** $15.389 \times 100 = 1538.9$
- **c** $15.98513 \times 10\,000 = 159\,851.3$
- **d** $48.9 \div 100 = 0.489$
- **e** $10.076 \div 10 = 1.0076$
- 2 Fill in the correct number of zeros in the multiplier to make the following product statements correct. The first one has been done for you.
 - **a** $56.321 \times 1 \ 0.0 = 5632.1$
 - **b** 27.9234×1 = 27 923.4
 - **c** 0.03572×1 = 3.572
 - **d** 3200×1 = $320\,000\,000$
- **3** Fill in the correct number of zeros in the divisor to make the following division statements correct. The first one has been done for you.
 - **a** $2345.1 \div 1 000 = 2.3451$
 - **b** 7238.4 \div 1 = 72.384
 - **c** $0.00367 \div 1$ = 0.000367
 - **d** 890 ÷ 1 = 0.0089
- **4** How many places, and in what direction, will the decimal point move if the following operations occur?

a × 100	b ÷ 10	c $\times 1000000$	d ÷ 1
e ÷ 1000	$f \times 1000$	$\mathbf{g} \times 10$	h $\div 10000000$

Fluency

Example 8 Multiplying by powers of 10	
Evaluate: a 36.532 × 100 Solution	b 4.31×10000 Explanation
 a 36.532 × 100 = 3653.2 b 4.31 × 10000 = 43100 	100 has two zeros, so the decimal point moves2 places to the right. 36.532The decimal point moves 4 places to the right and
Now you try Evaluate: a 1.43×10	additional zeros are needed. 4.3100 b 0.7721 × 1000

5	a e	lculate: 4.87 × 10 5.699 23 × 1000 0.34 × 10 000		35.283 × 10 1.259 63 × 100 213.2 × 10	g	422.27 × 10 12.7 × 1000 867.1 × 100 000		$\begin{array}{c} 14.304 \times 100 \\ 154.23 \times 1000 \\ 0.00516 \times 100000000 \end{array}$
E	xaı	mple 9 Dividing by	y po	owers of 10				
		late:						
		58.15 ÷ 10				82 ÷ 1000		
S	olu	tion			Exp	lanation		
а	26	$58.15 \div 10 = 26.815$				has one zero, so the lace to the left. 268.13		nal point moves
b	7.	82 ÷ 1000 = 0.007 82				decimal point moves additional zeros are	•	
N	ow	you try						
		uate: 213.1 ÷ 1000			b 3.	94 ÷ 100		
6	a d g	lculate: 42.7 ÷ 10 5689.3 ÷ 100 2.9 ÷ 100 36.7 ÷ 100	e h	$353.1 \div 10$ 12 135.18 ÷ 1000 13.62 ÷ 10 000 0.02 ÷ 10 000	f	$24.422 \div 10 \\93261.1 \div 10000 \\0.54 \div 1000 \\1000.04 \div 100000$		Write extra zeros when led. $1.6 \div 100 = 0.016$.
7	а	lculate: 22.913 × 100 22.2 ÷ 100		0.031 67 × 1000 6348.9 × 10 000		4.9 ÷ 10 1.0032 ÷ 1000		
E	xaı	mple 10 Working v	vitł	n 'the missing' d	lecim	al point		
		late:						
		57×10000		b 23 ÷ 1000	_			
S	olu	tion			Exp	lanation		
а	56	$57 \times 10000 = 5670000$)		it m ado invi	no decimal point is sl nust be at the very en litional zeros must be sible decimal point 4	nd of e put	the number. Four in to move the
b	23	$3 \div 1000 = 0.023$			The 0.02	decimal point moves	s 3 p	laces to the left.
N	ow	you try						
		iate: ↓×100			b 6	÷ 10 000		

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6D	8 Calculate:

a 156 × 100	b 43×1000	c 2251 × 10	d 16 × 1	000
e 2134 × 100	f 2134×1000	g 7×1000	h 99×1	00 000
i 34×10000	j 156 ÷ 10	k 156 ÷ 100	156 ÷	1000
m 87 ÷ 10	n 87 ÷ 100	o 87 ÷ 1000	p 16 ÷ 1	000
q 7 ÷ 1000	r $34 \div 10000$			
Problem-solvir	9, 10	10–12		

- 9 A service station charges \$1.37 per litre of petrol. How much will it cost Tanisha to fill her car with 100 litres of petrol?
- 10 Wendy is on a mobile phone plan that charges her 3 cents per text message. On average, Wendy sends 10 text messages per day. What will it cost Wendy for 100 days of sending text messages at this rate? Give your answer in cents and then convert it to dollars.



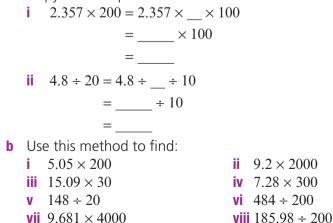
- **11** Darren wishes to purchase 10 000 shares at \$2.12 per share.
 - a What is the cost of the shares?
 - **b** There is an additional \$200 fee. How much will it cost Darren to buy the shares?
- 12 Choose 10, 100 or 1000 to complete the following.
 - **a** $5.67 \times 10 \div$ = 5.67
 - **b** $18.5 \div 100 \times \square = 1.85$ **d** 56 ÷ \rightarrow = 0.56 **e** 3.4 × \rightarrow 10 = 340

c 900 ÷ \times 1 = 9

13

Two-step calculations

13 a Copy and complete:



6E Multiplication of decimals 📩

- To be able to multiply decimals.
- To understand that it is helpful to estimate the answer first, in order to check the position of the decimal point in the final answer.

Key vocabulary: decimal places, decimal point, multiplication

Many real-life applications of mathematics involve the multiplication of decimal numbers. Examples include finding the area of a block of land that is 34.5 metres long and 5.2 metres wide, or pricing a 4.5-hour job at a rate of \$51.75 per hour.

You can use whole-number methods to multiply decimals, however, you must place the decimal point in the correct position in your answer.



Lesson starter: Multiplication musings

We can use what we know about multiplying fractions to multiply decimals. For example:

$$0.4 \times 1.6 = \frac{4}{10} \times \frac{16}{10} = \frac{64}{100} = 0.64$$

Now try these.

 0.7×0.3

• 0.07×0.03

 0.007×0.03

What do you notice about the decimal places in the question and the decimal places in the final answer?

Key ideas

When multiplying decimals, we use the following rule. The total number of **decimal places** in the answer is the same as the total number of decimal places in the question.

For example: $6.25 \times 4.5 = 28.125$ $2.41 \times 6 = 14.46$ (3 decimal places) (2 decimal places)

(2 decimal places)

- To multiply decimals:
 - Count the total number of decimal places in the question. For example:

 5.34×1.2 \checkmark 3 decimal places in the question

Now multiply, ignoring the decimal points.

534 Decimal points × 12 👞 ignored here. 1068 5340 6408

- Put the decimal point into your answer.
 - $5.34 \times 1.2 = 6.408$ \checkmark 3 decimal places in the answer

Exercise 6E

Understanding	1–4 3, 4
1 State the number of decimal places for each of the following. a 5.9 b 1.805 c 5.12 e 4.9 f 0.49 g 4.87	d 0.0072 h 5.29643
 Work out the total number of decimal places in each of the following a 4 × 6.3 b 3.52 × 76 c 42 × 5.123 e 5.283 × 6.02 f 2.7 × 10.3 g 4.87 × 3241.21 	d 8.71 × 11.2
	nultiplication is true. $0.64 \times 0.3 = 192$ $0.18 \times 0.42 = 00756$
4 Copy and complete the rule for multiplying decimal numbers (see the The total number of decimal places in the must equal in the answer.	
Fluency	5-7(1/2) 5-8(1/2)
Example 11 Multiplying decimals	
Calculate: a 0.56×3 b 4.13×0.3	
Solution Explanation	
XI	ecimal point. places in the question, so nal places in the answer.
	points. Multiply. aces in the question, so mal places in the answer.
Now you tryCalculate:a 2.7×6 b 3.19×0.2	
 5 Calculate: a 1.2 × 4 b 8.4 × 2 c 75 × 0.1 d 5.8 × e 9.8 × 2 f 9.8 × 0.2 g 0.6 × 4 h 0.6 × i 0.8 × 0.7 j 0.9 × 0.3 k 7.4 × 0.1 I 0.9 × 	0.4 write 5.60 as 5.6.
 6 Find: a 5.64 × 0.2 b 18.09 × 0.3 c 5.08 × 0.7 d 18.5 × 0.04 e 7.8 × 0.3 f 11.6 × 0.7 	Hint: If there are 3 decimal places in the question, there are 3 decimal places in the answer.

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Calculate:				
a 14 × 7.2	b 3×72.82	C	1.293×12	
d 3.4×6.8	e 5.4 × 2.3	f	0.34×16	
g 43.21 × 7.2	h 0.023×0.042	i	0.001 × 0.213	
Calculate and then round	d your answer to the nearest dollar			
a 5 × \$6.30	b $3 \times \$7.55$	C	$4 \times \$18.70$	
d $$5.64 \times 0.5$	e \$10.48 × 0.2	f	$$7.86 \times 1.5$	
Problem-solving a	nd reasoning		9(½), 10	9(1⁄2), 11, 12
	nd reasoning		9(½), 10	9(1⁄2), 11, 12
Calculate:			Hint:	
Calculate: a 2.52 × 40	b 6.9 × 70		Hint: 9.8 ×2	20 000
Calculate: a 2.52 × 40 c 31.75 × 800	b 6.9×70 d 1.4×7000		Hint: 9.8 ×2 = 9	20 000 9.8 × 2 × 10 000
Calculate: a 2.52 × 40	b 6.9 × 70		Hint: 9.8 ×2 = 9	20 000 9.8 × 2 ×10 000

- **10** Anita requires 4.21 m of material for each dress she is making. She is planning to make a total of seven dresses. How much material does she need?
- 11 The net weight of a can of spaghetti is 0.445 kg. Find the net weight of eight cans of spaghetti.
- **12** a If $68 \times 57 = 3876$, what is the answer to 6.8×5.7 ? Why?
 - **b** If $23 \times 32 = 736$, what is the answer to 2.3×32 ? Why?
 - **c** If $250 \times 300 = 75\,000$, what is the answer to 2.5×0.3 ? Why?
 - **d** What is 7×6 ? What is the answer to 0.7×0.6 ? Why?
 - e What about 0.07×0.6 ?

Using your calculator

13Yusef buys the following items at the supermarket.
He gives the checkout person \$80.

4 chocolate bars @ \$1.85 each 3 loaves of bread @ \$3.19 each newspaper @ \$1.40 2 × 2 litres of milk @ \$3.70 each washing powder @ \$8.95 toothpaste @ \$4.95 2 kg sausages @ \$5.99 per kg tomato sauce @ \$3.20 2 packets of chocolate biscuits @ \$3.55 each 5 × 1.25 litres of soft drink @ \$0.99 each

- a How much change does Yusef receive?
- **b** How could he be given this change if he receives at least one note?



13

Hint: Remember to count the

two decimal places.

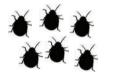
decimal places. 6.8×5.7 has

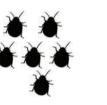
6F Division of decimals 🕇

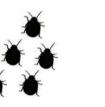
Learning intentions

- To be able to divide decimals by whole numbers.
- To be able to divide decimals by other decimals.
- Key vocabulary: decimal point, whole number, division

For multiplication, we treat decimals like whole numbers until the very end of the question. For division, however, we try to change the question so that we divide by a whole number instead of a decimal. First, let's review the terminology for division. Suppose we divide 24 by 4 to make groups of 6.







We can write this in several different ways.

 $24 \div 4 = 6$ or $\frac{24}{4} = 6$ or $4\frac{6}{24}$

- 24 is the dividend (the amount you have, or the number being divided).
- 4 is the divisor (the number doing the dividing).
- 6 is the quotient (the answer).

 $\frac{dividend}{divisor} = quotient$

Lesson starter: Division decisions

Use a calculator to find:

- $100 \div 2$ and $10 \div 0.2$
- $60 \div 3 \text{ and } 6 \div 0.3$
- 1.56 ÷ 0.02 and 156 ÷ 2

What do you notice about each pair? Can you think of an easy way to calculate $21.464 \div 0.02?$

Key ideas

- Division of decimal numbers by whole numbers:
 - Work out as you would any other division question.
 - The decimal point in the quotient (answer) goes directly above the decimal point in the dividend. For example: 60.524 ÷ 4

(15.131) $(4)6^{2}0.5^{1}24$

- Division of decimal numbers by other decimals:
 - Change the divisor (number after the ÷ sign) into a whole number.
 - Multiply the dividend and the divisor by the same power of 10 (10, 100, 1000, ...).
 - Then carry out the division by a whole number. For example: 24.562 ÷ 0.02

$$24.562 \div 0.02 = 2456.2 \div 2 = 1228.1$$

Exercise 6F					
Understanding				1–3	3
C 36.52 is the quotient,	5	1.3 is 1.3 is 91.3	the quotient. the quotient. is the divisor.		
 2 Rewrite each question so for you. a 1.2 ÷ 0.3 = 12 ÷ 3 c 15.2 ÷ 0.1 e 3.8 ÷ 0.1 	that you are dividing b	b d	vhole number. Th 1.8 ÷ 0.2 56.42 ÷ 0.02 3.8 ÷ 0.01	e first one has l	been done
3 For each of the following the second number becc					of places so th
a 3.2456 and 0.3c 0.00345 and 0.0001			120.432 and 0.1 1234.12 and 0.0		
					4–7(½)
c 0.00345 and 0.0001 Fluency	ecimals by whole ı	d	1234.12 and 0.0	04	4–7(½)
c 0.003 45 and 0.0001 Fluency Example 12 Dividing d Calculate:	ecimals by whole I	d numl	1234.12 and 0.0	04	4–7(½)
c 0.003 45 and 0.0001		d numl b 0	1234.12 and 0.0	04	4–7(½)
 c 0.003 45 and 0.0001 Fluency Example 12 Dividing d Calculate: a 42.837 ÷ 3 	Explanati Simply div	d numl b 0 on vide by oint in	1234.12 and 0.0 Ders $0234 \div 4$ If the whole num in the answer goe	04 4, 5, 6(½) ber. Remember	that the
 c 0.003 45 and 0.0001 Fluency Example 12 Dividing d Calculate: a 42.837 ÷ 3 Solution a 14.279 	Explanati Simply div decimal p point in th Remembe	d numl b 0 on vide by oint in ne div	1234.12 and 0.0 Ders $0234 \div 4$ If the whole num in the answer goe	04 4, 5, 6(½) ber. Remember s directly above	that the the decimal ime the

Calculate: **a** 26.196 ÷ 6

►

4 Calculate:

Ca	iculate.				
а	8.4 ÷ 2	b	30.5 ÷ 5	C	64.02 ÷ 3
d	$2.822 \div 4$	е	4.713 ÷ 3	f	2.156 ÷ 7
g	38.786 ÷ 2	h	1491.6 ÷ 4	i.	$0.0144 \div 6$
j –	234.21 ÷ 2	k	3.417 ÷ 5	1	$0.01025 \div 4$
m	1.56 ÷ 4	n	1.85 ÷ 5	0	$1.225 \div 7$
р	53.7 ÷ 6	q	28.08 ÷ 3	r	210.2 ÷ 2

Essential Mathematics for the Victorian Curriculum CORE Year 7

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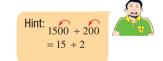
b 0.0142 ÷ 8

_
•

Evamn	1012	ind d	lecima	e h		cimal	
			ICCIIIIa	13 0	v uc	Gina	
		\sim			J		

Calculate:	
a 62.316 ÷ 0.03	b 0.031 52 ÷ 0.002
Solution	Explanation
a $62.316 \div 0.03$ = $6231.6 \div 3$ = 2077.2	We want to divide by a whole number, so we need to make the 0.03 into 3. Move each decimal point 2 places to the right.
20 7 7.2	$62.316 \div 0.03$
$3)62^{2}3^{2}1.6$	Carry out the division for $6231.6 \div 3$
b $0.03152 \div 0.002$ = $31.52 \div 2$	To change 0.002 into 2, move each decimal point 3 places to the right.
= 15.76	$0.03152 \div 0.002$
$\frac{15.76}{2}$	Carry out the division for $31.52 \div 2$.
$2)3^{1}1.5^{2}2$	Remember to line-up the decimal points.
Now you try	
Calculate: a 4.92 ÷ 0.4	b 0.0621 ÷ 0.09
5 Calculate:	

· ·	culculute.				
	a 6.14 ÷ 0.2	b	$23.25 \div 0.3$	C	$2.144 \div 0.08$
	d 5.1 ÷ 0.6	е	$0.3996 \div 0.009$	f	$45.171 \div 0.07$
	g 0.0032 ÷ 0.04	h	$0.04034 \div 0.8$	i	$10.78 \div 0.011$
	j 4.003 ÷ 0.005	k	0.948 ÷ 1.2	Т	$432.2 \div 0.0002$
6	Find:				
	a 1500 ÷ 200	b	$1500 \div 20$	C	1500 ÷ 2
	d 1500 ÷ 0.2	е	$1500 \div 0.02$	f	$1500 \div 0.002$
_			10 · · · · ·	-	1 1 I I



7 Calculate the following, rounding your answers to 2 decimal places.
 a 35.5 kg ÷ 3
 b \$213.25 ÷ 7
 c 182.6 m ÷ 0.6
 d 287 g ÷ 1.2
 e 482.523 L ÷ 0.5
 f \$5235.50 ÷ 9

Ρι	roblem-solving	8, 9	8, 10, 11	
a C	alculate: 236.14 ÷ 200 3.71244 ÷ 300 482.435 ÷ 5000	 b 413.35 ÷ 50 d 0.846 ÷ 200 f 0.0313 ÷ 40 	Hint: $2.6 \div 20$ = $2.6 \div$ = $1.3 \div$ = 0.13 Splitting 20 in makes the que	2 ÷ 10 10 to 2 and 10

- **9 a** A water bottle can hold 600 mL of water. How many water bottles can be filled from a large drink container that can hold 16 L?
 - **b** How many 400 mL bottles are needed for 16 L?



10 Rose paid \$12.72 to fill her lawnmower with 8 L of fuel. What was the price per litre of the fuel she purchased?

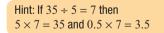


11 How many 20-cent pieces are needed to make:

а	\$0.80?	b	\$1.20?	C	\$5.40?
d	\$7.80?	е	\$15.20?	f	\$1000?



- **12** Given that $24.53 \times 1.97 = 48.3241$, write down the value of each of the following. Use a calculator to check your answers.
 - **a** 48.3241 ÷ 1.97
 - **b** 48.3241 ÷ 2.453
 - **c** 4832.41 ÷ 1.97
 - **d** 483.241 ÷ 245.3
 - **e** 0.483 241 ÷ 0.197
 - **f** 483 241 ÷ 2453



Progress quiz

6A	1 V a	What is the value of the digit 3 in the followi 26.37	ng b	numbers? 104.6732
6A	a b c	The formula for the formula formula formula formula for the formula f		
6A	3 (a c			7.9, 9.7 0.237, 0.271
<u>6</u> B	4 R a c	ound each of the following to 2 decimal pla 13.478 72.68099		8.043 45.3951
6B	5 R a c		ne b d	arest dollar. \$15.55 \$1099.50
6C	а	ind each of the following. 2.45 + 6.32 181.4 + 35.53 + 12.88	b d	15.23 + 41.62 5.123 + 25.8 + 32.08
60	7 F a c	41.054 10.41	b d	34.91 - 12.7 408.715 - 375.481
6D	a C			4.92 × 10 000 5.609 ÷ 1000 278 ÷ 100 000
6E		Calculate: 0.81×4 5.9×30	b d	5.23×0.6 4000×7.1
6F		Calculate: 52.842 ÷ 3 85.245 ÷ 0.05	b d	0.0064 ÷ 4 0.003 782 ÷ 0.02

11 A water bottle can hold 400 mL of water. How many water bottles can be filled from a large drink container that can hold 40 L?

6F

6G Decimals and fractions

Learning intentions

- To be able to convert decimals to fractions.
- To be able to convert fractions to decimals.
- To understand the symbols that indicate recurring decimals.

Key vocabulary: recurring decimal, convert, denominator, simplify

Sometimes we use decimals to show numbers that are not whole numbers, and sometimes we use fractions. It is important to be able to change a fraction to a decimal (for example, $\frac{1}{4} = 0.25$), and change a decimal

to a fraction (for example, $0.75 = \frac{3}{4}$).

Lesson starter: How many do you already know?

You probably know that the decimal 0.5 and the fraction $\frac{1}{2}$ are equivalent.

- List ten other decimal-fraction pairs you know.
- Could you use the decimal-fraction equivalences you know to work out some other pairs?



Key ideas

- Converting decimals to fractions
 - Using your knowledge of place value, express the decimal places as a fraction with a **denominator** that is a power of 10. Remember to **simplify** the fraction whenever possible.
- Converting fractions to decimals
 - When the denominator is a power of 10, we can simply change the fraction to a decimal through knowledge of place value.
 - When the denominator is *not* a power of 10, try to find an equivalent fraction with a denominator that has a power of 10, and then **convert** to a decimal.
 - A method that will always work for converting fractions to decimals is to divide the numerator by the denominator.
- **Recurring decimals** are decimals with a repeated pattern.
 - A dot, a bar or dots above a number indicates a repeated pattern.

For example:
$$\frac{1}{3} = 0.33333... = 0.3$$
 $\frac{13}{11} = 1.181818... = 1.18$ or $1.\overline{18}$

e.g.
$$0.25 = \frac{25}{100} = \frac{1}{4}$$

denominator

e.g.
$$\frac{37}{100} = 0.37$$

e.g.
$$\frac{2}{5} = \frac{4}{10} = 0.4$$

e.g.
$$\frac{5}{8} = 8 \frac{0.625}{5.50^20^40} = 0.625$$

Exercise 6G

Understanding	9		1–3	3
a $\frac{1}{2} = \frac{1}{10} = 0.5$ c $\frac{3}{4} = \frac{1}{100} = 0.5$ 2 Complete each of the function of the fun	hese statements, which cor hese statements, which cor	b $\frac{1}{4} = \frac{25}{10} = 0.25$ d $\frac{2}{10} = \frac{4}{10} = 0.$	ns, in simplest 1	orm.
a $0.2 = \frac{1}{10} = \frac{1}{5}$ c $0.8 = \frac{8}{10} = \frac{1}{5}$ 3 Write down the larce	ger number in each pair.	b $0.15 = \frac{1}{100} = \frac{3}{100}$ d $0.64 = \frac{64}{100} = \frac{1}{25}$		
a $\frac{1}{10}$, 0.3 d 1.5, $\frac{15}{100}$	b $\frac{1}{2}$, 0.4 e $\frac{3}{4}$, 0.9	c 0.8, $\frac{8}{100}$ f 0.05, $\frac{1}{2}$	Hint: Convert or numbers so tha compare two fr two decimals.	t you can
Fluency			4–7(½)	4–7(½), 8
Convert the following a 0.239 Solution a $\frac{239}{1000}$	denominato	b 10.35 decimal places. So use 1	3 zeros (1000) ir	n the
b $10\frac{35}{100} = 10\frac{7}{20}$	denominato 0.35 = 35 hu Simplify by d			or by the
Now you try Convert the following a 0.62	decimals to fractions in the	eir simplest form. b 1.037		
 4 Convert the followin a 0.4 f 5.5 k 0.001 	ng decimals to fractions in b 0.6 c 0.8 g 0.15 h 0.9 l 0.202 m 0.5	d 0.22 i 0.08	j	1.22 0.01 10.15

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	fractions to decimals.	_
a $\frac{17}{100}$	b $5\frac{3}{5}$	c <u>7</u> 12
Solution		Explanation
a $\frac{17}{100} = 0.17$		The denominator is a power of 10.
100		So write 17 hundredths as a decimal.
b $5\frac{3}{5} = 5\frac{6}{10} = 5.6$		The denominator (5) is not a power of 10.
5 10		So change $\frac{3}{5}$ to $\frac{6}{10}$ and write as a decimal.
		5 change 5 to 10 and write as a decimal.
c $\frac{7}{12} = 0.58333$ or	0.583	12 is not a factor of 10, 100 or 1000.
12		So divide the numerator (7) by the
		denominator (12). 0. 5 8 3 3 3
		$\frac{0.58333}{12)7.0^{10}0^{4}0^{4}0^{4}0}$
Convert the following a $\frac{6}{10}$		c $\frac{4}{15}$
Convert the following a $\frac{6}{10}$	fractions to decimals. b $2\frac{3}{4}$	c $\frac{4}{15}$
 a ⁶/₁₀ 5 Convert each of the 	b $2\frac{3}{4}$ ese fractions to decimals.	21
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$	c <u>31</u> 100
 a ⁶/₁₀ 5 Convert each of the 	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$	31
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$	c <u>31</u> 100
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$
 a ⁶/₁₀ 5 Convert each of the a ⁷/₁₀ d ⁷⁹/₁₀₀ g ¹²³/₁₀₀₀ 6 Convert the followi 	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ ng fractions to decimals H	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$ 6 Convert the followi a $\frac{4}{5} = \frac{1}{10}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ ng fractions to decimals B b $\frac{1}{2} = \frac{\Box}{10}$	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction c $\frac{7}{20} = \frac{\Box}{100}$
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$ 6 Convert the followi a $\frac{4}{5} = \frac{\square}{10}$ d $\frac{23}{50} = \frac{\square}{100}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ ng fractions to decimals B b $\frac{1}{2} = \frac{10}{10}$ e $5\frac{19}{20} = 3$	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction c $\frac{7}{20} = \frac{1}{100}$ f $3\frac{1}{4} = 3\frac{1}{100}$
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$ 6 Convert the followi a $\frac{4}{5} = \frac{1}{10}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ ng fractions to decimals B b $\frac{1}{2} = \frac{\Box}{10}$	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction c $\frac{7}{20} = \frac{1}{100}$ f $3\frac{1}{4} = 3\frac{1}{100}$
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$ 6 Convert the followi a $\frac{4}{5} = \frac{1}{10}$ d $\frac{23}{50} = \frac{1}{100}$ g $\frac{5}{2} = \frac{1}{10}$ 7 Convert the followi	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ ng fractions to decimals B b $\frac{1}{2} = \frac{1}{10}$ e $5\frac{19}{20} = 3$ h $\frac{3}{8} = \frac{1}{100}$ ng fractions to decimals B	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction c $\frac{7}{20} = \frac{1}{100}$ f $3\frac{1}{4} = 3\frac{1}{100}$ j $\frac{7}{25} = \frac{1}{100}$ by dividing the numerator by the denominator.
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$ 6 Convert the followi a $\frac{4}{5} = \frac{1}{10}$ d $\frac{23}{50} = \frac{1}{100}$ g $\frac{5}{2} = \frac{1}{10}$	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ Ing fractions to decimals B b $\frac{1}{2} = \frac{1}{10}$ e $5\frac{19}{20} = 3$ h $\frac{3}{8} = \frac{1}{100}$	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction c $\frac{7}{20} = \frac{1}{100}$ f $3\frac{1}{4} = 3\frac{1}{100}$ f $3\frac{1}{4} = 3\frac{1}{100}$ i $\frac{7}{25} = \frac{1}{100}$ by dividing the numerator by the denominator. c $\frac{3}{4}$ Hint: Use a dot to write recurring decimals: 0.333 = 0.3
a $\frac{6}{10}$ 5 Convert each of the a $\frac{7}{10}$ d $\frac{79}{100}$ g $\frac{123}{1000}$ 6 Convert the followi a $\frac{4}{5} = \frac{1}{10}$ d $\frac{23}{50} = \frac{1}{100}$ g $\frac{5}{2} = \frac{1}{10}$ 7 Convert the followi	b $2\frac{3}{4}$ ese fractions to decimals. b $\frac{9}{10}$ e $\frac{121}{100}$ h $\frac{3}{100}$ ng fractions to decimals B b $\frac{1}{2} = \frac{1}{10}$ e $5\frac{19}{20} = 3$ h $\frac{3}{8} = \frac{1}{100}$ ng fractions to decimals B	c $\frac{31}{100}$ f $3\frac{29}{100}$ i $\frac{7}{100}$ by first changing the fraction to an equivalent fraction c $\frac{7}{20} = \frac{1}{100}$ f $3\frac{1}{4} = 3\frac{1}{100}$ j $\frac{7}{25} = \frac{1}{100}$ by dividing the numerator by the denominator.

Essential Mathematics for the Victorian Curriculum CORE Year 7

- 6G
- 8 Copy and complete the following tables. Part **c** has already been done for you.
 - Try to memorise these fractions and their equivalent decimal values.
 - a halves

Fraction	$\frac{0}{2}$	$\frac{1}{2}$	$\frac{2}{2}$
Decimal			

b thirds

Fraction	$\frac{0}{3}$	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{3}{3}$
Decimal				

c quarters

Fraction	$\frac{0}{4}$	$\frac{1}{4}$	$\frac{2}{4}$	$\frac{3}{4}$	$\frac{4}{4}$
Decimal	0	0.25	0.5	0.75	1

d fifths

Fraction	$\frac{0}{5}$	$\frac{1}{5}$	$\frac{2}{5}$	$\frac{3}{5}$	$\frac{4}{5}$	<u>5</u> 5
Decimal						

Problem-solving and reasoning	9, 10	10–13

9 Arrange $\frac{1}{2}$, 0.75, $\frac{5}{8}$, 0.4, 0.99, $\frac{1}{4}$ from smallest to largest.

10 Copy and complete the following table.

Decimal amount	\$0.01	\$0.05	10 c	20 c		50 c		90 c	\$0.99
Fraction of \$1	$\frac{1}{100}$				$\frac{1}{4}$		$\frac{3}{4}$		

11 a Copy and complete the following fraction decimal table.

Fraction	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{4}$	$\frac{1}{5}$	$\frac{1}{6}$	$\frac{1}{7}$	$\frac{1}{8}$	$\frac{1}{9}$	$\frac{1}{10}$
Decimal									

Hint: You may need a calculator for questions **11** and **12**.



- **b** What happens to the decimals as the denominator increases?
- **c** Try to explain why this makes sense.

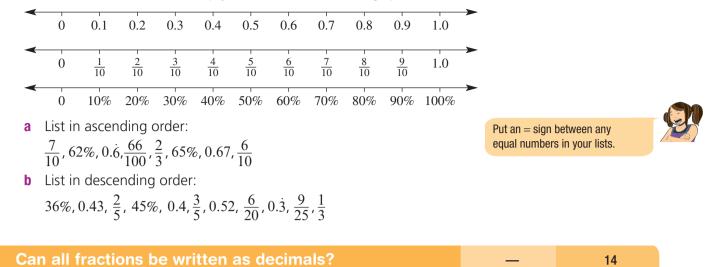
a Copy and complete the following decimal fraction table.

Decimal	0.1	0.2	0.25	0.4	0.5	0.6	0.75	0.8	0.9
Fraction									

b How many of the fractions can be expressed in simplest form using a denominator of 5?

c How many of the fractions can be expressed in simplest form using a denominator of 4?

13 Use these number lines to help you answer the following questions.



- 14 We know that $\frac{1}{3} = 0.333...$ and that $\frac{11}{7} = 1.\overline{571428}$. These are both infinite recurring decimals, where a pattern continues forever.
 - **a** Can you find a fraction that can be written as a decimal which continues indefinitely with no pattern?
 - **b** Now write the number $\sqrt{2}$ as a decimal. What do you notice?
 - **c** Do you think $\sqrt{2}$ can be written as a fraction?
 - d Research and write a brief summary of the discovery and existence of irrational numbers.



6H Decimals and percentages

Learning intentions

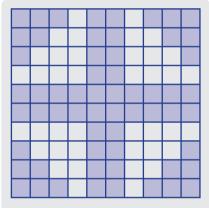
- To understand the relationship between a percentage and a decimal.
- To be able to convert between percentages and decimals.
- Key vocabulary: percentage, convert, decimal point

Percentages are used every day. We saw in chapter 4 that per cent means 'out of 100'. This makes it very easy to convert percentages into decimals, and vice versa. We need to do this when working with everyday percentages such as discounts and interest rates.



Lesson starter: Creative shading

- Draw a square of side length 10 cm and shade exactly 20% or 0.2 of this figure.
- Draw a square of side length 5 cm and shade exactly 60% or 0.6 of this figure.
- Draw another square of side length 10 cm and creatively shade an exact percentage of the figure. Ask your partner to work out the percentage you shaded. You may find it helpful to use grid paper.



What percentage is shaded?

×100 (and write %)

 $\div 100$ (drop the %)

percentage

decimal

Key ideas

The % symbol means per cent. It comes from the Latin words per centum, which mean 'out of 100'.

For example: 23% means 23 out of 100

$$23\% = \frac{23}{100}$$

- = 0.23
- To **convert** a percentage to a decimal, drop the % sign and divide by 100. That is, move the decimal point 2 places to the left.

For example: $42\% = 42 \div 100 = 0.42$

To convert a decimal to a percentage, multiply by 100 and write a % sign. That is, move the decimal point 2 places to the right.

For example: 0.654 = 65.4%

Exercise 6H

	Un	de	rs	ta	nd	lin	g														1-	5			Ĺ	4, 5	
1	Wł	nat	per	cer	ntag	ge o	of e	eacl	h so	qua	ire	nas been shade	ed?														
	а												b														
								-																			
													A		_			_									
	C												d		_			_	_								
																	_	_		_							
															_		-	_		_							
2	72	5%	is c	nn	iiva	len	t to		hic	h o	f tk	e following de	cimal											I			
2		72.		.qu	iiva	ICII		5 00		7.		e tonovning de		0.72	25						D	72	25.0)			
3	0.3	9 is	eq	uiv	aleı	nt t	to v	whi	ch (of t	the	following perce	entag	es?													
		399								3.		5.		0.39	9%						D	0.	003	39%			
4	Pru	ie a	nsv	ver	ed	hal	f th	ne c	que	stic	ons	correctly for a	test m	nark	ed	out	t of	10	0.								

- a What score did Prue get on the test?
- **b** What percentage did Prue get on the test?
- **c** Assuming Prue always gets half the answers correct, find her score if the test was out of: **i** 10
 - ii 200
 - iii 40
 - **iv** 2
- d Find Prue's percentage for each of the tests in part c.
- **5** Fill in the empty boxes.
 - **a** 58% = 58 out of
 - **b** 35% = out of 100
 - **c** 126% = 126 100
 - **d** % = 15 out of 100

6

	Fluency	6–7(½) 6–8(½)
	Example 16 Converting percentages to	decimals
	Express the following percentages as decimals.	
	a 30% b 240% c 12.5	
	Solution	Explanation
	a $30\% = 0.3$	$30 \div 100 = 0.3$
	b 240% = 2.4	$240 \div 100 = 240. = 2.4$
	c $12.5\% = 0.125$	$12.5 \div 100$
		Decimal point moves 2 places to the left.
	d $0.4\% = 0.004$	$0.4 \div 100$
		Decimal point moves 2 places to the left.
	Now you tryExpress the following percentages as decimals.a 67%b 460%c 82.4	% d 0.17%
	 6 Express the following percentages as decimals a 32% b 27% c 68% e 10% f 12% g 18% i 92% j 75% k 11% m 6% n 9% o 100% q 218% r 142% s 75% 	d 54% h 85% l 60% p 1% t 199% Hint: ×100 decimal percentage ÷100
	 7 Express the following percentages as decimals a 22.5% b 17.5% c 33 e 112.35% f 188.8% g 13 i 0.79% j 0.025% k 1. 	3.33% d 8.25% 50% h 520%
5	Example 17 Converting decimals to per	centages
	Express the following decimals as percentages. a 0.045	b 7.2
	Solution	Explanation
	a 0.045 = 4.5%	$0.045 \times 100 = 4.5$ Decimal point moves 2 places to the right.
	b $7.2 = 720\%$	$7.2 \times 100 = 720$.
	Now you try	
	Express the following decimals as percentages. a 0.941	b 2.37

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10-12

13

9,10

8 Express the following decimals as percentages.

	0.8	-	0.3			d	0.71
е	0.416	f	0.375	g	2.5	h	2.314
i	0.025	j	0.0014	k	12.7	1	1.004

Problem-solving and reasoning

9 At a hockey match, 65% of the crowd supports the home team. What percentage of the crowd supports the visiting team?



- **10** Sarah thinks that the chance of beating her brother, Tim, at tennis is 52%. What is this chance as a decimal?
- **11** Write the following as:
 - i percentages
 - ii decimals
 - a 50 cents in the dollar
 - **b** 25 cents in the dollar
 - c 90 cents in the dollar
 - d 10 cents in the dollar
 - e 100 cents in the dollar
- 12 a Explain why Yuang could not expect to get more than 100% for his Maths test.
 - **b** What does it mean to get 50% on a test out of 40?
 - c If a student received a mark of 0% for a test, how many questions were answered correctly?

AFL ladder

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Pos	Team	Р	W	L	D	F	Α	%	Pts
6	Brisbane Lions	22	13	8	1	2017	1890	106.72	54
0	Carlton	22	13	9	0	2270	2055	110.46	52
8	Essendon	22	10	11	1	2080	2127	97.79	42
9	Hawthorn	22	9	13	0	1962	2120	92.55	36
1	Port Adelaide	22	9	13	0	1990	2244	88.68	36

13 The Australian Rules football ladder has the following column headings.

- a Using a calculator, can you determine how the percentage column is calculated?
- **b** What do you think the 'F' and the 'A' column stand for?
- **c** In their next match, Essendon scores 123 points and has 76 points scored against them. What will be their new percentage?
- **d** Find out the current For and Against points for your favourite AFL team.

🔀 Maths@Work: Retail assistant

Retail assistants use many skills. They need to be confident, polite, pleasant people who like interacting with their customers. Also, they need to have good mathematical skills to quickly and accurately calculate the bill and give correct change.



1 Find the total of each of the following receipts.

a	600 mL lemonade	\$2.50
	half chicken	\$15.00
	burger	\$9.00
	chips	\$4.00
	ice-cream 2@	\$4.00 each
_	long black large	¢1 50

clong black large\$4.50baby chino\$2.50kids milkshake\$5.50small cappuccino\$3.50banana bread\$4.95

b	scarf	\$24.95
	4 cards @ \$1.00 each	\$4.00
	RFID card sleeve	\$16.95
	pencil case leather	\$39.95
	orbit key ring	\$52.95

In 1990 the Australian government removed all 1 and 2 cent coins. The total of all cash purchases was now rounded to the nearest 5 cents. For example, 71c or 72c rounded down to 70 cents, while 73c and 74c rounded up to 75 cents. 76c and 77c rounded down to 75 cents, and 78c and 79c rounded up to 80 cents. State the rounded price for each of the following cash amounts:

 a \$5.68
 b \$123.91
 c \$45.66
 d \$2.99

Hint: Remember that all cash amounts are rounded to the nearest 5 cents.



3 Customers often give a mixture of notes and coins to minimise the number of coins they receive in change. Complete the following table to find the change due to each customer.

Customer	Sub total	+ or - rounding amount in cents	Total due	Cash tendered	Change due
Adam	\$45.67			\$50.80	
Blake	\$123.03			\$130.00	
Christy	\$123.03			\$125.10	
Dion	\$56.92			\$57.00	
Eden	\$67.56			\$70.60	

4 Write the missing values in each of the following receipts. The question parts are shown in brackets beside each missing amount.

De	side each missing amount.			
а	cheese snack	\$1.80		
	cucumber 0.65 kg @ \$8.00/kg		_ (i)	
	capsicums red 0.45 kg @ \$7.00/kg		_ (ii)	
	Total of the 3 items		_(iii)	
	CASH TENDERED	\$10.50		
	CHANGE DUE		_(iv)	
b	honey beef 0.732 kg @ \$19.99	/kg		_ (i)
	lamb mince 1.317 kg @ \$17.99	/kg		_ (ii)
	kebabs 12 pack @ \$1.45 EACH keb	ab		_(iii)
	To	tal		<u>(iv)</u>
	Total due to roundi	ng		(v)
	CASH TENDER	ED \$5	5.80	
	CHANGE DI	JE		_(vi)

- **5** How much is saved by rounding when paying cash for the following?
 - a Sweet chilli red pepper thin sausages 0.236 kg @ \$15.99/kg
 - b Thin tasty beef sausages 0.354 kg @ \$15.99/kg
- 6 Complete the missing parts **i**–**iv** shown on the following receipt.

Description	\$
taco shells	2.20
potato chips 53 g	0.95
corn chips 150 g	1.50
frozen ⊠sh 375 g	5.60
chicken 400 g	5.00
frozen yoghurt 264 mL	6.79
chocolate 55 g 2 @ \$1.00	2.00
cherry tomatoes 200 g	3.00
donuts 12 pk	3.00
cucumber 1 each	1.00
spring onion 1 bunch	2.50
broccoli 0.217 kg @ \$5.90/kg	(i)
Total for the (ii) items	(iii)
Change from a \$50 note	(iv)



Using technology

Retail assistants help with stocktaking. This involves counting the items (called stock) in a store and calculating their total value for the company's financial records. It is usually done once a year in late June as the Australian Tax Office requires profits to be reported at the end of every financial year (June 30).

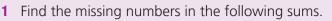


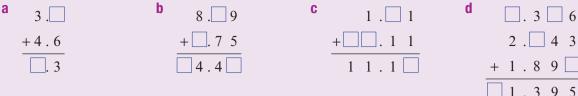
- 7 Barney and Noah have completed a stocktake of their hardware store.
 - a Set up the following spreadsheet for valuing some stock. Select all the value cells (in columns D and E), right click, select Format/Currency/0 d. p.
 - **b** Enter formulas in the shaded cells to calculate the total value of this stock.

Hint: In cell E10, add the cell values above =SUM(E3:E8)



	А	В	С	D	E		
1		Hardw	are store st	ocktake			
2	Assistant	Stock	Number	Value of 1 item	Total value		
3	Barney	Bathroom basin tap	25	\$82			
4	Barney	Shower mixer tap	34	\$119			
5	Barney	Bathroom mirror	8	\$77			
6	Noah	Cordless drill	5	\$139			
7	Noah	Mitre power saw	6	\$380			
8	Noah	Electric sander	12	\$48			
9							
10			Total stock value				





2 Find the missing digits in these questions involving division.



3 What room can nobody enter?

To find out, solve each problem. Then use your answers to unlock the code below.

- A Find the total of \$7.06, \$24.95, \$1.05 and \$3.50.
- **0** Calculate \$69.97 \$15.98.
- M Find $100 4 \times 16.05$.
- **S** Tracy bought five books at \$24.95 each. How much change did she receive from \$150?
- H Nensi spent \$216 on nine CDs. How much did each CD cost?
- **U** Find the cost of seven cans of cola if a dozen cans cost \$16.20.
- M Find the cost of six slices of cake at \$1.25 per slice.
- **0** Find the total cost of four books at \$4.95 each, three pens at 95 cents each, and one eraser at \$1.05.
- **R** Julie spent \$23.15 on items for school and another \$3.95 on chocolate. How much change did she get from \$30?

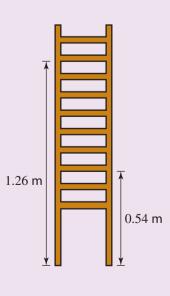
\$36.56	\$7.50	\$9.45	\$25.25	\$24	\$2.90	\$53.99	\$23.70	\$35.80

4 Take your age and double it.

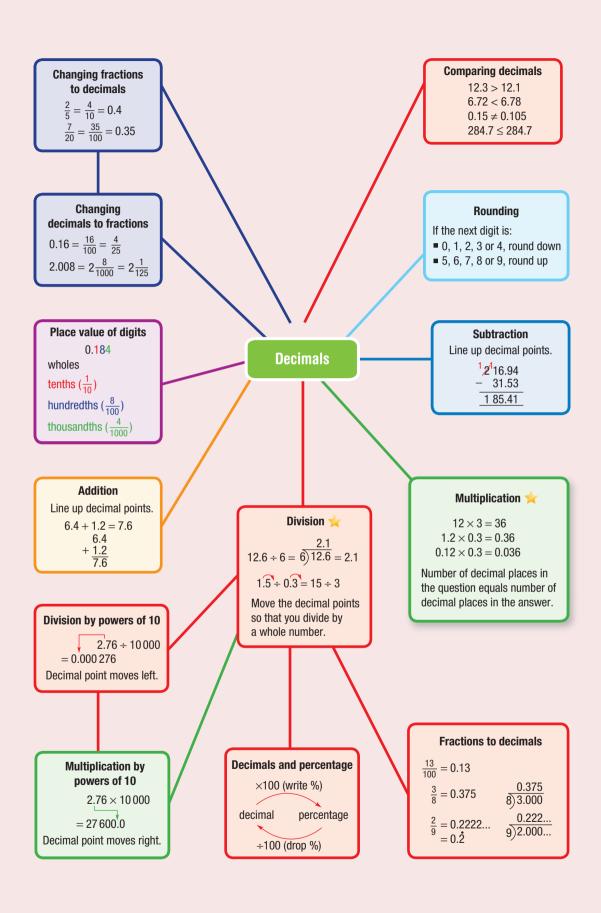
Add 5 to this number.

Multiply the answer by 50, then add your age. Now add 365 (the days in one year) to this value. Subtract 615 from your result. Now divide by 100 and put a dollar sign in front. What do you notice?

5 The rungs in this ladder are evenly spaced. The height above the ground is shown for two of the rungs. Find the height above the ground of each of the other rungs.



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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

			V
6A	1	I can state the value of a digit after the decimal point in a number. e.g. What is the value of the digit 8 in the number 6.1287?	
6A	2	I can convert fractions and mixed numbers to decimals (if the denominator is 10, 100, 1000 etc.). e.g. Convert $3\frac{7}{100}$ to a decimal.	
6A	3	I can compare two or more numbers written as decimals. e.g. Arrange the following decimal numbers in ascending order (i.e. smallest to largest): 3.72, 7.23, 2.73, 2.37, 7.32, 3.27.	
6B	4	I can determine the critical digit in a rounding operation. e.g. The number 23.5398 is to be rounded to two decimal places. Circle the critical digit.	
6B	5	I can round decimals to a given number of decimal places. e.g. Round 0.43917 to 2 decimal places.	
60	6	I can add decimals. e.g. Find 64.8 + 3.012 + 5.94.	
60	7	I can subtract decimals. e.g. Find 146.35 - 79.5.	
6D	8	I can multiply a decimal by a power of 10. e.g. Evaluate 4.31×10000 .	
6D	9	I can divide a decimal by a power of 10. e.g. Evaluate 7.82 ÷ 1000.	
6D	10	I can multiply and divide a whole number by a power of 10, introducing a decimal place if required. e.g. Evaluate 23 ÷ 1000.	
6E	11	I can multiply decimals. e.g. Calculate 0.56×3 and 4.13×0.3 .	
6F	12	I can divide decimals by whole numbers. e.g. Calculate 42.837 ÷ 3.	

			~
6F	13	I can divide decimals by decimals. e.g. Calculate 62.316 ÷ 0.03.	
6G	14	I can convert decimals to fractions or mixed numbers. e.g. Convert 10.35 to a mixed number in simplest form.	
6G	15	I can convert fractions and mixed numbers to decimals. e.g. Convert $5\frac{3}{5}$ to a decimal.	
6G	16	I can convert fractions to recurring decimals. e.g. Convert $\frac{7}{12}$ to a decimal.	
6H	17	I can convert a percentage to a decimal. e.g. Convert 12.5% to a decimal.	
6H	18	I can convert a decimal to a percentage. e.g. Convert 0.045 to a percentage.	

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Chapter review

Short-answer questions

6A	1	 Arrange each group in descending order, from largest to smallest. a 0.4, 0.04, 0.44 b 0.932, 0.98, 0.895 								
6A	2	Write each fraction as a decim	nal.	0.01		0.0.1				
		a $\frac{81}{10}$ b $\frac{81}{100}$		c $\frac{801}{100}$	d	$\frac{801}{1000}$				
6A	3	What is the place value of the a 12.835 b 6.1237	dig	it 3 in the follow c 13.5104	wing numb	oers?				
6A	4	Are the following statements a 8.34 < 8.28		or false? 4.668 > 4.67		С	8.2 > 8.18			
		d $3.08 \le \frac{308}{100}$		$\frac{62}{100} \ge 6.20$			$\frac{7}{10} = \frac{70}{100}$			
		g $0.6 = 0.60$	h	$1\% = \frac{1}{10}$		i	5% = 0.05			
6B	5	Write \$62.876 to the nearest: a cent	b	dollar		C	5 cents			
6B	6	Round each of the following t	:o 1	decimal place.						
		a 12.74 d 7.45	b e	8.36 0.08		C f	9.41 7.124			
6B	7	Round each of these to 2 deci					7.124			
UD	1	a 12.814	b	423.461		C	15.889			
_	_	d 7.2543	е	6.6666		f	3.3333			
6C	8	Evaluate: a 1.2 + 0.4	b	0.36 + 1.2		С	19.4 + 0.194			
		d $7.6 + 1.2 + 0.8$	e 6	20 + 1.9 200 - 156.5		f				
		g 47.06 - 1.12 j \$1.60 + \$5.40	h k	200 - 136.3 \$19.46 + \$10.34	4 - \$5		\$15 - \$7.24			
6E	9	How many decimal places will								
+		a A number with 2 decimal pb A number with 1 decimal p				-				
		c A number with 2 decimal p	blace	es × a number v	vith 2 deci	mal pl	aces			
CD 11	10	d A number with 2 decimal p	nace	es x a number v	vith 0 deci	mai pi	aces			
6D-H	IU	True (T) or false (F)? a $1.37 \times 100 = 137$		b	9.4 ÷ 10 =	= 940				
*		c $8.7 \div 10 = 0.87$		d	$18 \div 10 =$					
		e $5\% = 0.5$ g $12 \div 0.4 = 120 \div 4$		f	6% > 60% $10\% \times 6$		× 6			
		i $9.81 \times 10 \div 10 = 9.81$		j	$\frac{7}{100} = 709$					
		k 25% = 2.5		I.	100 56.1 ÷ 10		1			
6E/F	11	Calculate the following.								
		a 2.4×8	b	9×7.11		C	2.3×8.4			
\mathbf{X}		d 3.8 ÷ 4 g 4 ÷ 0.25	e h	$12.16 \div 8$ $1.2 \div 0.4$		f	$3 \div 0.5$ $3.42 \div 0.1$			
		-								

Chapter review

12 Copy and complete this table, stating fractions both with the denominator 100 and in their simplest form. Decimal Fraction Percentage Fraction Decimal Percentage 0.06 $\overline{100}$ $\frac{79}{100}$ 1 $\overline{10}$ 1.05 100 $\frac{?}{100} = \frac{7}{20}$ 100 0.45 65% $\frac{?}{100} = \frac{7}{10}$? $\frac{?}{1000} = \frac{1}{8}$ 32% **13** Complete these conversions. a Convert these percentages to decimals. 120% 70% **37%** iv 0.21% **b** Convert these decimals to percentages. i 0.4 1.65 iv 6.2 0.02 **Multiple-choice questions 1** The next number in the pattern 0.023, 0.025, 0.027, 0.029 is: **A** 0.0003 **B** 0.030 **C** 0.0031 **D** 0.031 **E** 0.033 **2** 0.05 is equivalent to: **A** $\frac{5}{10}$ **B** $\frac{5}{100}$ **C** $\frac{5}{1000}$ **D** $\frac{5}{500}$ E 5 **3** The smallest number out of 0.012, 10.2, 0.102, 0.0012 and 1.02 is: **C** 0.0012 **A** 0.012 **B** 0.102 **D** 1.02 **E** 10.2 **4** 0.36 ÷ 1000 is equal to: **A** 3.6 **B** 360 **C** 0.036 **D** 0.0036 E 0.00036 5 6.2×0.2 is equal to: **A** 1.24 **B** 12.4 **C** 0.124 **D** 124 **E** 0.0124 What is the answer to $0.08 \times 0.6?$ 6 **A** 0.48 **B** 4.8 **C** 0.0048 **D** 0.048 **E** 48 7 When rounded to 1 decimal place, 84.553 becomes: **A** 80 **B** 84 **C** 84.5 **D** 84.6 **E** 84.55 8 As a decimal, $\frac{3}{9}$ is equal to:

A 0.3

B $0.\dot{3}$

D 0.93

E 3.9

C 0.39

 6C
 10 Bread rolls at a bakery are 60 cents each or 6 for \$3.50. The lowest price of 8 bread rolls is:

 A \$3.60
 B \$4.80
 C \$4.70
 D \$4.10
 E \$21

Extended-response question

- 1 Find the answer in these practical situations.
 - **a** Jessica is paid \$125.70 for 10 hours of work and Jaczinda is paid \$79.86 for 6 hours of work. Who receives the higher rate of pay per hour, and by how much?
 - **b** Petrol is sold for 124.9 cents per litre. Jacob buys 10 L of petrol for his car. Find the total price he pays, to the nearest 5 cents.
 - **c** The cost of a ticket at the movies is \$14.50 for an adult and \$11.20 for a child. Find the cost for 1 adult and 2 children.
 - d A pie costs \$2.70 at the school canteen. Zara bought 2 pies and a drink. The total was \$8.60.
 - i How much change from \$10 did Zara receive?
 - ii How much was her drink?
 - e Jen buys one cappuccino every workday from different shops. Last week the prices were: \$2.70, \$3.30, \$3.50, \$4.50
 - i Find the total cost for the week.
 - ii Find the average cost by dividing the total cost by the number of coffees.
 - iii How much should Jen budget for the 200 days she works in a year?



	hole numbers ort-answer questions									
1	Write the missing number. a 0, 2,, 6, 8, 10 b 13, 9, 5, c 101, 202,, 404									
2	Write the number for: a seven thousand, three he b twelve thousand and nin			twen	ty-f	four				
3	Calculate: a $3712 + 1204 + 46$ c 49×3 e $525 \div 5$				d	1438 - 619 380×20 $411 \div 3$	9			
4	True or false? a $15 < 6 \times 2$	b 9>	< 6 >	> 45			C	23 = 40	÷ 2	+ 3
5	How much more than 9×1	1 is 11 $ imes$: 11?)						
6	Calculate: a $4 + 2 \times 3$ d $7 \times 6 - 4 \times 3$ g $9 \times (2 \times 4) - 10$	<pre>b 10 e 8 > h 24</pre>	< 8 -	- 16 ÷	- 2		f	20 - 15 $12 \times (6 - 56 - (7 - 56))$	- 2)	× 7
7	Are the following true or fa a $4 \times 25 \times 0 = 1000$ c $8 \div 0 = 0$ e $20 \div 4 = 20 \div 2 \div 2$	se?			d	$0 \div 10 = 0$ $8 \times 7 = 7 \times 2$ 8 + 5 + 4 = 2	× 8	9		
8	Put in brackets to make eac a $2+3 \times 4 = 20$	h of the b 10				ue.	C	4 × 6 - 2	2 ÷ 8	8 = 2
9	Round each number to the a 12	nearest b 35	ten.				C	137		
10	Round each number to the a 129	nearest b 87		dred.			C	1451		
M	ultiple-choice questions									
1	Five thousand, two hundred A 526 B 50 206			5260		D :	5026		E	5206
2	The place value of 8 in 4837 A 8 thousands B 8 hund		C	zero		D S	8 ten	S	E	8 ones
3	The remainder when 650 is A 0 B 4	divided I	by 4 C			D	2		E	3
4	$\begin{array}{c} 18 - 3 \times 4 \text{ simplifies to:} \\ \textbf{A} 12 \qquad \textbf{B} 81 \end{array}$		C	6		D	50		E	30
5	$(7 - 2 + 65) \div 10$ is equal to: A 7 B 10		C	11		D	70		E	32

Extended-response questions

- 1 Tom works as a labourer, earning \$25 an hour on weekdays and \$60 an hour on weekends.
 - **a** During a particular week, Tom works 7 a.m. to 2 p.m. Monday to Thursday. How many hours does he work that week?
 - **b** How much does Tom earn for this work?
 - **c** If Tom works 5 hours on Saturday in the same week, what is his total income for the week?
 - d How many hours on a Friday must Tom work to earn the same amount as working 5 hours on a Saturday? (Hint: work out how much he earns on Saturday.)



Geometry

Short-answer questions

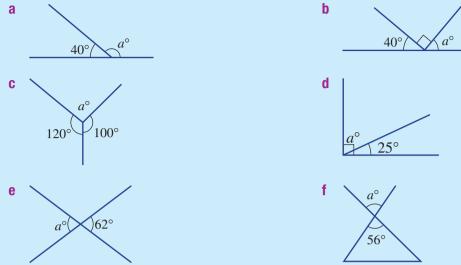
- 1 Give the name of the type of angle which is:
 - a between 0° and 90°
 - **b** exactly 90°
 - c between 90° and 180°
 - d exactly 180°
 - e between 180° and 360°
 - f exactly 360°

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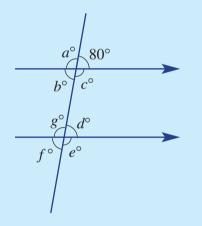
2 Measure these angles using a protractor.

С	
U	_

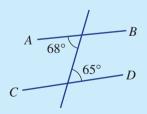
- **3** What is the complement of 65°?
- 4 What is the supplement of 102°?
- **5** Find the value of *a* in each of the following diagrams.



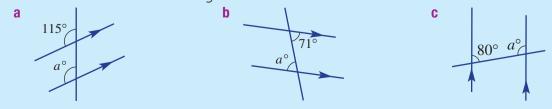
6 Find the value of each pronumeral when these two parallel lines are crossed by the transversal, as shown.



7 Explain why *AB* is not parallel to *CD*.



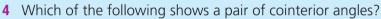
8 Find the value of *a* in these diagrams.

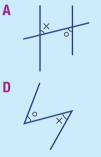


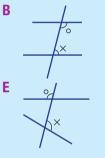
Multiple-choice questions

- 1 Which statement is correct?
 - **A** Line *m* is perpendicular to line *l*.
 - **B** Line *m* bisects line *l*.
 - **C** Line *m* is parallel to line *l*.
 - **D** Line *m* is shorter than line *l*.
 - **E** Line *m* is longer than line *l*.
- 2 An angle of 181° is classified as:
 - A acute

- B reflexE sharp
- D obtuse
- **3** Which two pronumerals are equal because of equal alternate angles in parallel lines?
 - **A** a and e
 - **B** d and f
 - **C** a and f
 - **D** g and b
 - **E** c and f

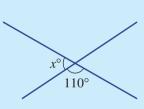






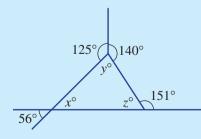
5 The value of *x* in this diagram is: **A** 140 **B** 110 **D** 70 **E** 65

C 220

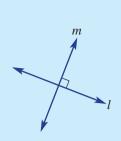


Extended-response questions

1 Consider the diagram shown.



- a Find the value of:
 - i x
 - ii y
- **b** What is the value of x + y + z?





С

Number properties and patterns Short-answer questions

 List the factors of: a 15 	b 30	c 100
2 List the first five multiples of: a 3	b 7	c 11

- **3** List all factors common to 30 and 36.
- **4** What is the highest factor common to 36 and 40?
- **5** Find the value of: **a** 11²

b $6^2 \times 2^2$ **c** $33 - 2^3$

- 6 Find:
 - **a** 7 to the power of 2
 - **b** 12 squared
 - c the square root of 81

7 Copy and complete each of these tables.

а	Index form	32		62]
	Value		25		64	
b	Square root f	form	$\sqrt{9}$		√36	
	Value			5		8

8 Which of the numbers 1080, 536, 135, 930, 316 are divisible by:

a 2? b 3? c 4? d 5? e 10?

9 A pattern of decorated squares is made with matchsticks.







a Copy and complete this table.

Number of squares	-			3	4	
Number of sticks	1	$1 + \square \times 1 = \square$	1 + 🗆 × 2 = 🗌	$1 + \square \times 3 = \square$	$1 + \checkmark 4 = \bigcirc$	

b Copy and complete the rule for this pattern.

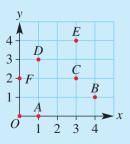
number of sticks = $1 + \square \times$ number of squares

- c How many sticks are needed to make 9 squares?
- d How many decorated squares could be made from 81 sticks?

10 Find the missing values in the table.

[input	4	5	6			100
	output	19	23		39	47	403

11 Write down the coordinates of each point, including the origin, O.



Multiple-choice questions

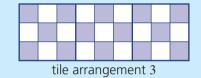
1	The first prime num	nber after 14 is: B 21	C	16	D	19	Е	17
2	0	on factor (HCF) of 12 B 12	2 ar C		D	2	Е	9
3	$2 \times 2 \times 2 \times 3$ is the A 6×3		C	8 ³	D	6 ³	E	4 ³
4	Evaluating $3^2 - \sqrt{25}$ A 8	5 + 3 gives: B 5	C	4	D	17	Е	7
5		prime factor form is: B $2 \times 3 \times 5$		$2^3 \times 3^2$	D	$2^4 \times 3$	Е	$2^3 \times 3$

Extended-response questions

1 Purple and white tiles are used to make a pattern for the border of a swimming pool.



tile arrangement (



tile arrangement 1

- **a** Draw tile arrangement 4 following this pattern.
- **b** How many purple tiles are in arrangement 4 of this pattern?
- c Which arrangement would use 41 purple tiles?
- **d** If each purple tile costs \$1 and each white tile costs 50 cents, what is the cost of an arrangement using 41 purple tiles?

Fractions and percentages

Short-answer questions

- 1 Arrange $\frac{1}{2}$, $\frac{2}{5}$ and $\frac{3}{10}$ in *ascending* order.
- 2 Express $5\frac{2}{3}$ as an improper fraction.
- **3** Find each of the following.
 - **a** $\frac{2}{3} + \frac{1}{4}$ **b** $4 - 1\frac{1}{3}$ **c** $2\frac{1}{2} + 3\frac{3}{4}$ **d** $\frac{2}{5} \times \frac{1}{2}$ **e** $\frac{2}{3} \div \frac{1}{6}$ **f** $1\frac{1}{5} \times \frac{5}{12}$
- 4 Write 15% as a simple fraction.
- **5** Find 25% of \$480.
- 6 Find 2% of \$400.
- 7 Are the following true or false?
 - a To find 25% of an amount, divide the amount by 4.
 - **b** 10% of an amount = amount \div 10
 - **c** 20% of $50 = 2 \times 10\%$ of 50
 - **d** 1% of x = 100x
- 8 Which is larger, $\frac{2}{3}$ or 60%?

Multiple-choice questions

1	Which of the follow	wing is equivalent to	$\frac{12}{7}?$		
	A $\frac{24}{7}$	B $1\frac{5}{7}$	C $1\frac{5}{12}$	D $\frac{112}{17}$	E $\frac{7}{12}$
2	$\frac{1}{2} + \frac{1}{3}$ is equal to:				
	A $\frac{2}{5}$	B $\frac{2}{6}$	C $\frac{5}{6}$	D $\frac{1}{5}$	E $\frac{7}{6}$
3	$\frac{350}{450}$ in simplest form	m is:			
	A $\frac{35}{45}$	B $\frac{4}{5}$	C $\frac{3}{4}$	D $\frac{3.5}{4.5}$	E $\frac{7}{9}$
4	What fraction of \$2		~	1	1
	A $\frac{1}{20}$	B $\frac{20}{1}$	C $\frac{5}{1}$	D $\frac{1}{5}$	E $\frac{1}{40}$
5	$2\frac{1}{2} \div \frac{3}{4}$ is the same	as:			
	A $\frac{5}{2} \times \frac{4}{3}$	$\mathbf{B} \frac{5}{2} \times \frac{3}{4}$	C $\frac{2}{5} \div \frac{3}{4}$	D $\frac{2}{5} \times \frac{4}{3}$	$\mathbf{E} \frac{3}{2} \times \frac{3}{4}$

Extended-response questions

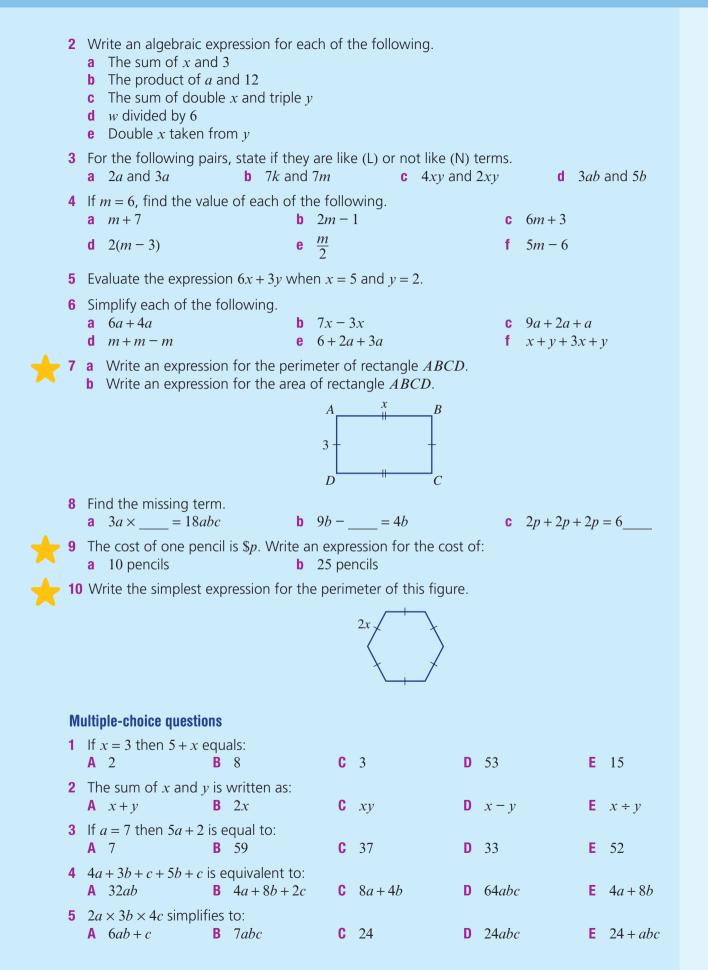
- 1 Caleb's cold and flu prescription states: 'Take two pills three times a day with food.' The bottle contains 54 pills.
 - a How many pills does Caleb take each day?
 - **b** What fraction of the bottle remains after Day 1?
 - c How many days will it take for the pills to run out?
 - **d** If Caleb takes his first dose Friday night before going to bed, on what day will he take his last dose?



Algebra

Short-answer questions

- 1 Consider the expression 5x + 7y + 3x.
 - a How many terms are in this expression?
 - **b** What is the coefficient of *y*?
 - **c** Simplify this expression by combining the like terms.



Extended-response questions

1 A bottle of soft drink costs \$3 and a pie costs \$2.

- **a** Find the cost of:
 - i 2 bottles of soft drink and 5 pies
 - ii x bottles of soft drink
 - iii x bottles of soft drink and 5 pies
- **b** Write an expression for the cost of buying *x* bottles of soft drink and *y* pies.
- **c** Substitute x = 2 and y = 5 into your expression from **b**.



Decimals

Short-answer questions

1 Write each of the following as a decimal.

	а	Two-tenths	b	$\frac{13}{100}$	C	$\frac{17}{10}$
2	а	the decimal 136.094: What is the value of the 6? What is the value of the 4?				
3	a b	ound 18.398 741 correct to: the nearest whole number 1 decimal place 2 decimal places				
4		valuate:		10.7 240 (0.02		20 0.00
		15 - 10.93		19.7 + 240.6 + 9.03		20 - 0.99
	d	0.6×0.4	е	0.3×0.3	📌 f	$\frac{12}{0.2}$
5	Fii	nd:				
	а	1.24 - 0.407	b	1.2 + 1.8 - 0.6	🔶 c	0.6×0.07
6		369 × 123 = 45 387, write down	n th			
	а	3.69×1.23	b	0.369×123	C	0.369×0.123
7		nd:				
		36.49×1000		$1.8 \div 100$	C	19.43×200
8		or each of the following, write	dov	vn the larger number.		2
	а	$\frac{4}{5}$, 0.79	b	1.1, 11%	С	$\frac{2}{3}$, 0.6
ę	St	ate if each of the following is t	rue	or false.		
	а	0.5 = 50%	b	$0.15 = \frac{5}{20}$	C	38% = 0.19
	d	126% = 1.26	е	$\frac{4}{5} = 0.08$	f	$1\frac{3}{4} = 1.75$

M	Multiple-choice questions										
1	$80 + \frac{6}{10} + \frac{7}{100}$ is the	same as:									
	A 8067	B 867	C	80.67	D	80.067	E	80.607			
2	Select the incorrect A $0.707 > 0.7$	statement.									
	B $0.770 = \frac{77}{100}$ C $0.07 \times 0.7 = 0.49$	9									
	D $0.7 \times \frac{1}{10} = 0.07$										
	E $0.7 \times 10 = 7$										
3	The best estimate f A 234	For 23.4 × 0.96 is: B 230	C	0.234	D	23	E	20			
4	$\frac{3}{8}$ is the same as:										
	A 0.375	B 3.8	C	0.38	D	2.6	E	38%			
5		ne as: B 680 ÷ 4	C	1.7	D	$\frac{4}{68}$	E	7 ÷ 0.05			

Extended-response questions

- **1** The cost of petrol is 116.5 cents per litre.
 - **a** Find the cost of 5 L of petrol, correct to the nearest cent.
 - **b** Mahir pays cash for 5 L of petrol for his motor bike. What is the amount that he pays, correct to the nearest 5 cents?
 - **c** How much change from \$10 does Mahir receive?

Super Li in
Super 19 Plus 199
Diesei 1209
Auto Gas 619

Chapter Negative numbers

Essential mathematics: why working with negative numbers is important

Negative numbers are an essential part of our numbering system.

- Temperature can be a positive or negative number or zero. Antarctic workers experience coastal temperatures from +10°C to -40°C, and inland temperatures from -30°C to -80°C.
- Accountants work with credit (positive amounts) and debit, i.e. debt, (negative amounts).
- Golf scores are positive and negative integers giving the number of strokes above or below par.
- Submarine operators and scuba divers can regard the sea surface as zero height, and measurements below sea level as negative heights.
- Places below sea level include Australia's Lake Eyre at –15 m, and the Dead Sea shore at –413 m, the lowest dry land on Earth.

In this chapter

- 7A Integers (Consolidating)
- 7B Adding or subtracting a positive integer
- 7C Adding a negative integer
- 7D Subtracting a negative integer
- 7E Substituting integers
- 7F Introducing the number plane

Victorian Curriculum

NUMBER AND ALGEBRA Number and place value

Compare, order, add and subtract integers (VCMNA241)

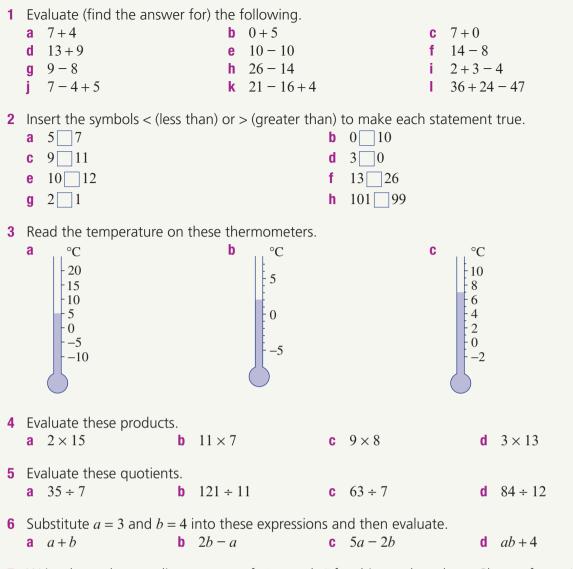
Linear and non-linear relationships

Given coordinates, plot points on the Cartesian plane, and find coordinates for a given point (VCMNA255)

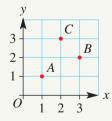
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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more. Warm-up quiz



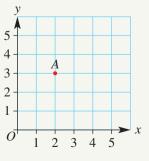
7 Write down the coordinates (*x*, *y*) of *A*, *B* and *C* for this number plane. Choose from (1, 1), (2, 3) and (3, 2).



8 Plot these points on the given number plane and join *A*, *B*, *C*, *D*, *E*, *F* and *A* to form a shape. Then find the perimeter of the shape you have formed. (Perimeter is the distance around the outside of the shape.) The first point is done for you.

а	<i>A</i> (2, 3)	b	<i>B</i> (2, 1)
C	<i>C</i> (5, 1)	d	D(5, 5)
е	E(3,5)	f	F(3, 3)

g The perimeter is _____ units.



7A Integers



Learning intentions

- To understand that integers can be negative, positive or zero.
- To be able to represent integers on a number line.
- To be able to compare two integers and decide which is greater.

Key vocabulary: negative number, positive number, integer, number line, opposite

Positive numbers are greater than zero. Negative numbers are less than zero. All the positive whole numbers (1, 2, 3, ...) and the negative whole numbers (-1, -2, -3, ...), together with zero (0), are called integers.

An English mathematician named John Wallis (1616–1703) invented the number line. He also invented the idea that numbers have a direction. This helped define our number system as an infinite set of numbers. This set extends infinitely in both the positive and negative directions.



Lesson starter: Do negative numbers exist?

Are negative numbers real?

- Can you think of any situations where negative numbers are used?
- How would you describe what a negative number is?

Key ideas

- Negative numbers are numbers less than zero.
- **Integers** are whole numbers that can be negative, zero or positive.

... - 10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, ...

positive

- A number line shows:
 - positive numbers to the right of zero
 - negative numbers to the left of zero.

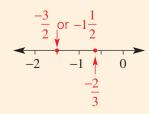
negative

-10-9 -8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8 9 10

• Each negative number has a positive opposite.

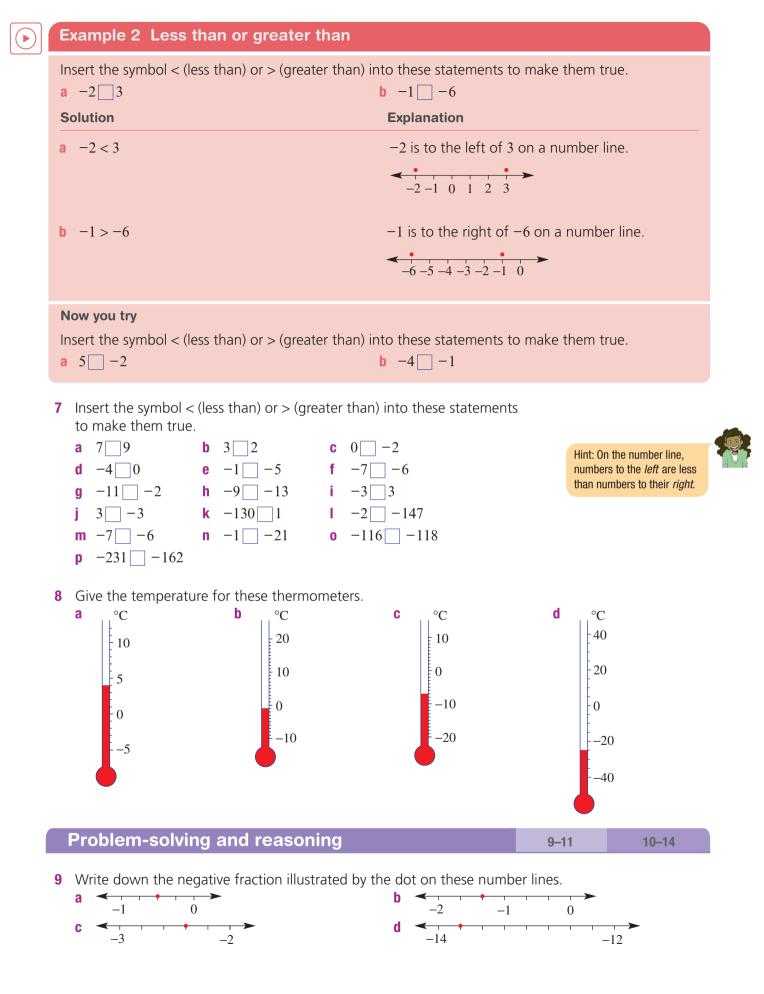
3 and -3 are examples of **opposite** numbers.

Negative fractions can also be located on the number line.



Exercise 7A

Understanding	1–3 3
 State the missing number. a -3, -2, -1, 0, , 2 c -6, -5, , -3, -2, -1, 0 e -21, -20, -19, , -17, -16 	b -1 , \Box , 1, 2, 3, 4 d -4 , -3 , -2 , \Box , 0, 1 f -37 , \Box , -35 , -34 , -33 , -32
2 What are the missing numbers on these numbers $a \xrightarrow{-3} -1 \ 0 \ 1 \ 3 \ 3 \ c \xrightarrow{-10-9-8} -6 \ c -$	umber lines? b $-2 -1$ 1 3 d -4 $-2 -1$ -1
3 Fill in each blank using the word greater of a 5 is than 0 b -3 is c 0 is than -6 d 0 is _ e -2 is than -3 f -6 is	than 0 Hint: On the number line, numbers to the right are greater than numbers to their left. than 1 than -2
Fluency	4, 5, 6–7(½) 4, 5–8(½)
Everable 1 Drewing a number line	
Example 1 Drawing a number line	
Durante a superior disconsistent and instances from	
Draw a number line showing all integers from	
Solution	Explanation
5 5	
Solution	Explanation Use equally spaced markings and put -4 on the left and 2 on the right.
Solution $-4 -3 -2 -1 \ 0 \ 1 \ 2$ Now you try	Explanation Use equally spaced markings and put -4 on the left and 2 on the right.
Solution -4 -3 -2 -1 0 1 2 Now you try Draw a number line showing all integers from 4 Draw a number line showing all integers: a from -2 to 2 c from -10 to -6	 Explanation Use equally spaced markings and put -4 on the left and 2 on the right. n -3 to 3. b from -5 to 1
Solution $-4 -3 -2 -1 \ 0 \ 1 \ 2$ Now you try Draw a number line showing all integers from 4 Draw a number line showing all integers: a from -2 to 2 c from -10 to -6 5 Add the word <i>right</i> or <i>left</i> to make the foll	Explanation Use equally spaced markings and put -4 on the left and 2 on the right. n -3 to 3. b from -5 to 1 d from -16 to -12 lowing statements true. Use this number line to help. eft right
Solution $-4 -3 -2 -1 \ 0 \ 1 \ 2$ Now you try Draw a number line showing all integers from 4 Draw a number line showing all integers: a from -2 to 2 c from -10 to -6 5 Add the word <i>right</i> or <i>left</i> to make the foll	Explanation Use equally spaced markings and put -4 on the left and 2 on the right. n -3 to 3. b from -5 to 1 d from -16 to -12 lowing statements true. Use this number line to help.
Solution $-4 -3 -2 -1 \ 0 \ 1 \ 2$ Now you try Draw a number line showing all integers from 4 Draw a number line showing all integers: a from -2 to 2 c from -10 to -6 5 Add the word <i>right</i> or <i>left</i> to make the foll a 2 is to the of 0 c -1 is to the of 2	Explanation Use equally spaced markings and put -4 on the left and 2 on the right. n -3 to 3. b from -5 to 1 d from -16 to -12 lowing statements true. Use this number line to help. eft right
Solution $\begin{array}{c} -4 \\ -3 \\ -2 \\ -4 \\ -3 \\ -2 \\ -1 \\ 0 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1$	Explanation Use equally spaced markings and put -4 on the left and 2 on the right. n -3 to 3. b from -5 to 1 d from -16 to -12 lowing statements true. Use this number line to help. lowing statements true. Use this number line to help. eft right 3-2-1 0 1 2 3 4 5 b 1 is to the of 3 d -4 is to the of -5
Solution $-4 - 3 - 2 - 1 \ 0 \ 1 \ 2$ Now you try Draw a number line showing all integers from 4 Draw a number line showing all integers: a from -2 to 2 c from -10 to -6 5 Add the word <i>right</i> or <i>left</i> to make the foll a 2 is to the of 0 c -1 is to the of 2 e -4 is to the of -1	ExplanationUse equally spaced markings and put -4 on the left and 2 on the right.n -3 to 3.b from -5 to 1 d from -16 to -12lowing statements true. Use this number line to help.eft righta -2 -1 0 1 2 3 4 5b 1 is to the of 3 d -4 is to the of -5 f 2 is to the of -4



Essential Mathematics for the Victorian Curriculum CORE Year 7



- True or false? 10
 - **a** -3 is the opposite of 6
 - **c** 0 is a positive number
 - **e** -8 is greater than -1
 - **q** -11 < -6

- **b** 0 is a negative number
- d -5 is less than -2
- f -2 is equal to 2
- **h** -7 > -2
- **11** List all the integers that fit the given description.
 - a from -2 up to 4
 - **c** greater than -3 and less than 2
 - e less than 4 and greater than -4
- 12 Arrange these numbers in *ascending* order.
 - **a** -3, -6, 0, 2, -10, 4, -1
 - **b** -304, 126, -142, -2, 1, 71, 0

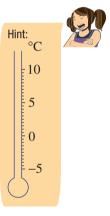
- **b** from -7 up to 0
- **d** greater than -5 and less than 1
- f less than -3 and greater than -10

Hint: Ascending means 'rising', so arrange numbers from lowest to highest (*left* to *right* on a number line).

13 Write the next three numbers in these simple patterns.

- **a** 3, 2, 1, ___, ___, ___, ___ **b** -8, -6, -4, ___, ___, ___ **c** 10, 5, 0, __, __, ___, **d** -38, -40, -42, ___, ___, ___ **e** -91, -87, -83, ___, ___, ___ **f** 199, 99, -1, ___, ___,
- 14 A thermometer shows a temperature of 10 degrees Celsius. What would be the new temperature if it drops by:
 - a 6 degrees?
- **b** 10 degrees?
- c 12 degrees?
- **d** 20 degrees?







15 For these sets of numbers, a positive number means to move right and a negative number means to move left. Start at zero each time and find the final position.

negative positive
-3 -2 -1 0 1 2 3
b Move 3, -5, -1, 4 d Move -10, 20, -7, -14, 8, -4

7B Adding or subtracting a positive integer

Learning intentions

- To understand the number line model for adding and subtracting positive integers.
- To be able to use a number line to add a positive integer to any integer.
- To be able to use a number line to subtract a positive integer from any number.

Key vocabulary: number line, left, right, positive number

When we add a positive number such as 3, we move 3 places to the right on the number line. So, 2 + 3 means start at 2 and move 3 to the right, and -5 + 3 means start at -5 and move 3 steps right.

To subtract the positive number 4, we move 4 places to the left on the number line. For 7 - 4, we start at 7 and move 4 steps left. For -2 - 4, we start at -2 and move 4 steps left.

So, to add or subtract a positive number, we need to pick a starting point and then move right for addition or left for subtraction.



Lesson starter: Walking the number line

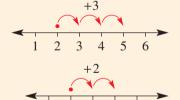
Imagine a number line running from one side of the room to the other, large enough to walk along. Decide which half is positive (the right) and which is negative (the left). Each step moves you one whole number along the line.

- Stand at zero and move to the right for addition and left for subtraction.
- Another student calls out a command such as 'add 3' or 'subtract 5'. Move the appropriate number of steps on the number line and tell the class your new position.
- If you make a mistake, let another student have a turn.

Key ideas

• If a **positive number** is added to an integer, you move **right** on a **number line**.

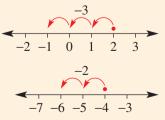
2 + 3 = 5Start here. Move right 3. -5 + 2 = -3Start here. Move right 2.



If a positive number is subtracted from an integer, you move left on a number line.

$$2-3 = -1$$

Start here. Move left 3.
 $-4-2 = -6$
Start here. Move left 2.



Exercise 7B

Understanding

- 1 Use the number line to help find the answer to each of the following.
 - **a** -2+3**b** -4+2

c
$$-10+1$$

d
$$3-4$$

e
$$-1-3$$

f $-6-2$
f $-6-2$

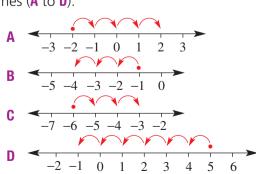
2 In which direction (i.e. right or left) on a number line do you move for the following calculations?

- a Start at -5, add 2
- **c** Start at 2, subtract 4

- **b** Start at -4, add 6
- d
- **d** Start at -4, subtract 3



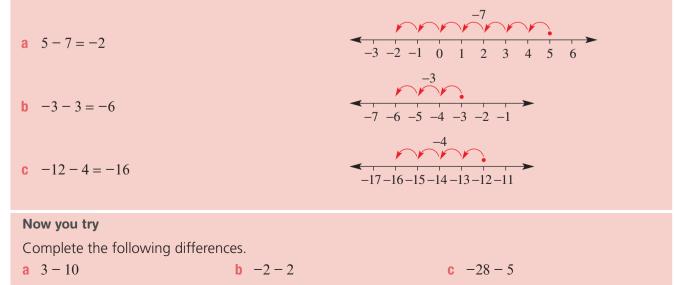
- 3 Match up the problems (a to d) with the number lines (A to D).
 - **a** 5-6=-1
 - **b** -2+4=2
 - **c** -1 3 = -4
 - **d** -6+3=-3



 $\begin{array}{c} +3 \\ -3 & -2 & -1 & 0 & 1 & 2 \\ +2 \\ -5 & -4 & -3 & -2 & -1 \\ +1 \\ -11 & -10 & -9 & -8 \\ -2 & -1 & 0 & 1 & 2 & 3 & 4 \\ \hline -2 & -1 & 0 & 1 & 2 & 3 & 4 \\ \hline -5 & -4 & -3 & -2 & -1 & 0 \\ -5 & -4 & -3 & -2 & -1 & 0 \\ \hline -2 & -2 & -2 & -1 & 0 \\ \hline \end{array}$

1–3

	Fluency	4-6(1/2) 4-7(1/2)
\mathbf{E}	Example 3 Adding a positive integer	
	Complete the following sums. a $-2+3$ b $-8+1$ Solution	c −11+4 Explanation
	a $-2 + 3 = 1$	+3 -3 -2 -1 0 1 $2+1$
	b $-8 + 1 = -7$ c $-11 + 4 = -7$	-9 -8 -7 -6 -5
	Now you try Complete the following sums. a $-5+7$ b $-13+2$	-12-11-10 -9 -8 -7 -6 c -22+5
	4 Complete the following sums. a $-1+2$ b $-1+4$ c $-3+5$ e $-7+2$ f $-10+7$ g $-13+$ i $-4+3$ j $-5+2$ k $-11+$ m $-4+0$ n $-8+0$ o $-30+$	9 I $-20 + 18$ a <i>positive</i> integer.
	Example 4 Subtracting a positive integer	
	Complete the following differences. a $5-7$ b $-3-3$	c -12 - 4
	Solution	Explanation



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5	Complete the fol	lowing differences.				
	a $4-6$ d $1-20$ g $-5-10$	b $7-8$ e $-1-2$ h $-11-2$	c $3-11$ f $-3-2$ i $-3-1$	4 I	Hint: Remember to move left on the number line when subtracting a positive integer.	
	j -5 - 5 m -37 - 4	k $-2 - 13$ n $39 - 51$	-7 - (0) 0 62 - 8			
6	Evaluate: a -130 + 132 e -100 - 200	b $-181 + 1$ f $100 - 200$		c $-57 + 63$ g $328 - 421$	d $-99 + 68$ h $-496 - 138$	
	G 100 200	100 20	0	y 520 4 21	H 4 70 138	

Example 5 Combining addition and subtraction

Evaluate the following, working from left to right. a $2-6+3$	b $-6+3-5$
Solution	Explanation
a $2-6+3=-4+3$ = -1	First work out $2 - 6 = -4$, then add 3
b $-6+3-5=-3-5$ = -8	First work out $-6 + 3 = -3$, then subtract 5

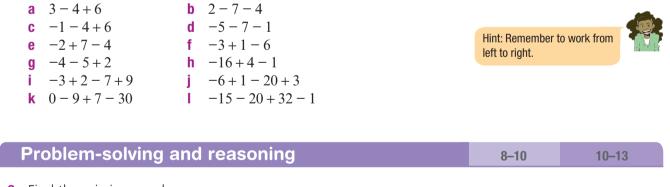
Now you try

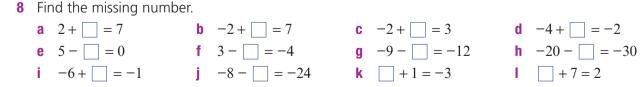
Evaluate the following, working from left to right.

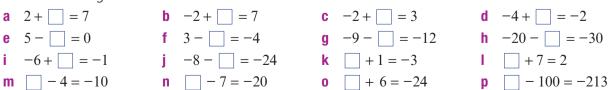
a -2 + 7 - 11

7 Evaluate the following.

b -10 - 32 + 28





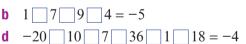


- 9 Determine how much debt remains in these bank accounts.
 - a Owes \$300 and pays back \$155
 - **b** Owes \$20 and borrows another \$35
 - **c** Owes \$21 500 and pays back \$16 250
- **10** a The reading on a thermometer rises 18° C from -15° C. What is the final temperature?
 - **b** The reading on a thermometer falls 7°C from 4°C. What is the final temperature?
 - **c** The reading on a thermometer falls 32° C from -14° C. What is the final temperature?
- **11** For an experiment, a chemical solution starts at a temperature of 25° C. It falls to -3° C, rises to 15° C and then falls again to -8° C. What is the total change in temperature? (Hint: it might be helpful to combine all three changes.)
- **12** An ocean sensor is raised and lowered to different depths in the sea. Note that -100 m means 100 m below sea level.
 - a If the sensor is initially at -100 m and then raised to -41 m, how far does the sensor rise?
 - **b** If the sensor is initially at -37 m and then lowered to -93 m, how far is the sensor lowered?



13 Insert + or – signs into these statements to make them true.

- **a** 3 4 5 = 4
- **c** -4 2 1 3 4 = 0



14

Positive and negative possibilities

- **14** Decide if it is possible to find an example of the following. If so, give a specific example. It might help to draw a number line.
 - **a** A positive number added to a positive number gives a positive number.
 - **b** A positive number added to a positive number gives a negative number.
 - c A positive number added to a negative number gives a positive number.
 - **d** A positive number added to a negative number gives a negative number.
 - e A positive number subtracted from a positive number gives a positive number.
 - **f** A positive number subtracted from a positive number gives a negative number.
 - **g** A positive number subtracted from a negative number gives a positive number.
 - **h** A positive number subtracted from a negative number gives a negative number.

7C Adding a negative integer

Learning intentions

- To understand that adding a negative integer is the same as subtracting a positive integer.
- To be able to use a number line to add negative integers.

Key vocabulary: opposite, sign, negative integer, number line

So far, we have added or subtracted positive integers to other integers. For example: -2 + 4 or -3 - 5.

We will now look at the case where we add negative integers to other integers. For example: 3 + (-4) or -6 + (-2).

As an example, think of a debt of \$40 as a negative amount (-40). Suppose an account has a balance of \$100. If you add the \$40 debt, you would have a total balance of \$60. So 100 + (-40) = 60.

But we know that 100 - 40 = 60. This suggests that to add -40 we should subtract 40.



Lesson starter: What does the pattern tell us?

Look at this addition pattern.

2+3=5 -1 2+2=4 -1 2+1=3 -1 2+0=2 -1 2+(-1)=1 -1 2+(-2)=0 -12+(-3)=-1

- Describe the vertical patterns that you see.
- What do the patterns tell you about adding a negative integer?

Key ideas

■ The **opposite** of 3 is −3, and the opposite of −2 is 2.

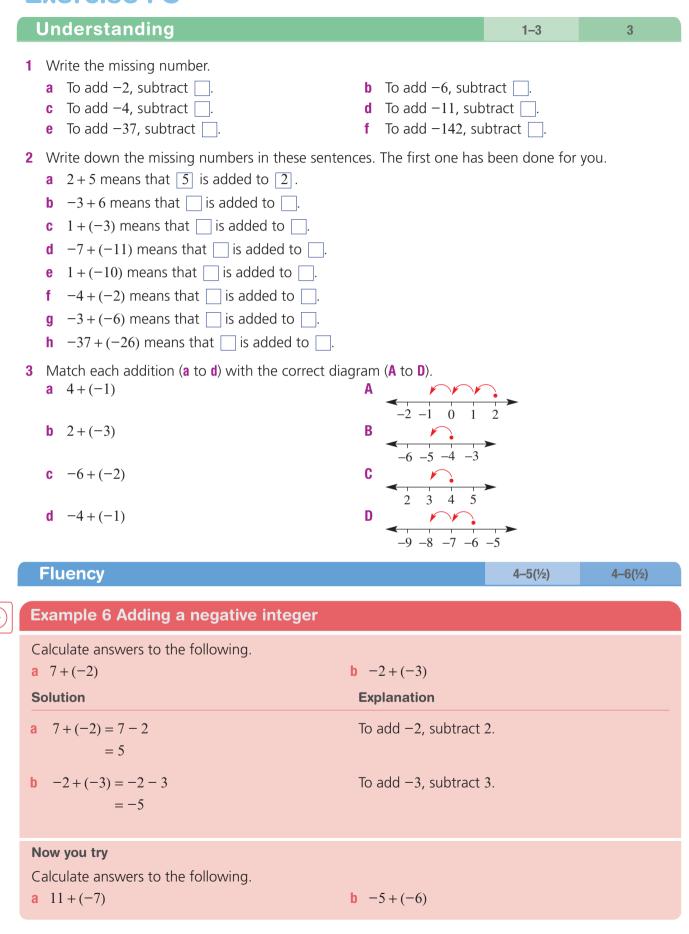
• To add a negative number, subtract its opposite. a + (-b) = a - b

$$2 + (-3) = 2 - 3 = -1$$

$$-4 + (-2) = -4 - 2 = -6$$

$$-7 - 6 - 5 - 4 - 3$$
To add -3, subtract 3.
To add -2, subtract 2.

Exercise 7C



7C

Calculate: **a** 3 + (-2)**b** 8 + (-3)**c** 12 + (-6)**d** 9 + (-7)f 6 + (-11)e 1 + (-4)**g** 20 + (-22) **h** 0 + (-4)i -2 + (-1)-7 + (-15)k -5 + (-30)-28 + (-52)**m** -7 + (-3)**n** -20 + (-9)**o** -31 + (-19)**q** -99 + (-10) **r** -12 + (-101)p -103 + (-9)

Hint: To add a negative integer, subtract its opposite. -3 + (-2) = -3 - 2

To add -2, subtract 2, then add 5 to finish.

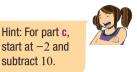
Starting at -2, add -3 by subtracting 3.

Then add -4 by subtracting 4.



5 Find the answer if:

a -2 is added to 7 **b** -3 is added to 10 **c** -10 is added to -2 **d** -1 is added to -6 **e** -13 is added to -2**f** -31 is added to -11



Example 7 Combining additions with integers	
Calculate the answers to these problems. a $3 + (-2) + 5$ b $-2 + (-3) + (-4)$	
Solution	Explanation

a	3 + (-2) + 5 = 3 - 2 + 5
	= 1 + 5
	= 6

b
$$-2 + (-3) + (-4) = -2 - 3 - 4$$

= $-5 - 4$
= -9

Now you try

Calculate the answers to these problems.

a 6 + (-5) + 2

b -12 + (-3) + (-10)

6 Calculate the answers to these problems.

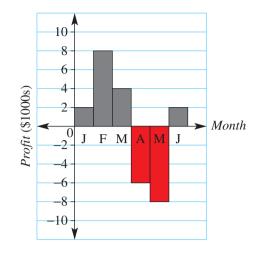
а	3 + (-1) + 2	b $7 + (-2) + 4$
C	2 + (-3) + 1	d $-1 + (-3) + (-4)$
е	-4 + (-2) + (-1)	f $-6 + (-3) + (-1)$
g	3 + (-10) + 6	h $-15+2+(-4)$
i.	-13 + (-17) + (-3)	

Problem-solving and	d reasoning	7–9 8–11
7 Find the missing number.		
a 2 + = -1	b $3 + \square = -7$	c $-2 + \square = -6$
d $-+(-3) = 1$	e -11 + (-10) = -11	f $[-4] + (-4) = 0$
g $-+(-3) = 2$	h $-+(-6) = -1$	i $-2 + \square = -3$
j -5 + = -7	k $-10 + \square = -12$	-37 + = -51

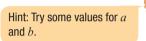
Essential Mathematics for the Victorian Curriculum CORE Year 7

- 8 A person has \$120 of debt. If \$70 of debt is added to this, how much debt is now owed by the person?
- **9** Here is a profit graph showing the profit for each month of the first half of the year for a bakery shop.
 - **a** What is the profit for:
 - i February?
 - ii April?
 - **b** What is the overall profit for the 6 months?





- **10** If *a* is a positive number and *b* is a negative number, are the following true or false?
 - **a** a+b is *always* positive.
 - **b** b + a is *always* negative.



12

X

- **11** If *a* is a negative number and *b* is a negative number, are the following true or false?
 - **a** a + b is *always* positive.
 - **b** b + a is *always* negative.

Negative magic squares

12 Complete these magic squares, using addition. The sum of each row, column and diagonal should be the same.a

а	-2		5	
		1		
			4	

	-6
-3	-17
	7

7D Subtracting a negative integer

Learning intentions

- To understand that subtracting a negative integer is the same as adding a positive integer.
- To be able to use a number line to subtract negative integers.

Key vocabulary: opposite, sign, negative integer, number line

Imagine that you have \$100 worth of debt and you subtract (pay back) \$30 of that debt. You still owe \$70. This can be written as -100 - (-30) = -70.

But to pay back \$30 of your debt, you must *add* \$30 to your account. Also, to move from -100 to -70 on a number line, we *add* 30. So -100 - (-30) = -100 + 30.

This suggests that to subtract (-30) we should add 30.

Lesson starter: Patterns reveal the trick

Look at this subtraction pattern.

- 2 3 = -1 + 1 2 2 = 0 + 1 2 1 = 1 + 1 2 0 = 2 + 1 2 (-1) = 3 + 1 2 (-2) = 4 + 1 2 (-3) = 5
- Describe the vertical patterns that you see.
- What do the patterns tell you about subtracting a negative integer?

Key ideas

To subtract a negative number, add its **opposite**.

a - (-b) = a + b5 - (-2) = 5 + 2 = 7

-2-(-3)=-2+3=1

$$-(-2) = + 2$$

$$-(-3) = + 3$$

$$-(-3) = + 3$$

$$-(-3) = + 3$$

To subtract -2, add 2.

To subtract -3, add 3.

Exercise 7D

Understanding	1–3 3
1 Write the missing number.	
a To subtract -3, add .	b To subtract -6, add .
c To subtract -4, add .	d To subtract -11, add .
e To subtract -15, add .	f To subtract -312, add .



4-5(1/2)

4-6(1/2)

- 2 Write down the missing numbers in these sentences. Parts a and c have been started for you.
 - **a** 5-3 means that 3 is subtracted from .
 - **b** -2-6 means that is subtracted from .
 - **c** 7 (-3) means that -3 is subtracted from .
 - **d** -7 (-11) means that \square is subtracted from \square .
 - e -2 (-4) means that is subtracted from .
 - **f** -6 (-1) means that \square is subtracted from \square .
 - **g** -11 (-7) means that \square is subtracted from \square .
 - **h** 27 (-12) means that \square is subtracted from \square .

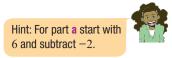
3 Match each subtraction (a to d) with the correct diagram (A to D).

Fluency

Example 8 Subtraction	ng a negative inte	ger	
Calculate: a $1 - (-3)$		b -6 - (-2)	
Solution a $1 - (-3) = 1 + 3$ = 4		Explanation To subtract -3, add 3.	
b $-6 - (-2) = -6 + 2$ = -4		To subtract −2, add 2.	
Now you try Calculate: a $4 - (-3)$		b -18 - (-12)	
4 Calculate: a 2 - (-3) d 29 - (-61) g -11 - (-6) j -9 - (-10) m 5 - (-23)	b $5 - (-6)$ e $-5 - (-1)$ h $-41 - (-7)$ k $-20 - (-20)$ n $28 - (-6)$		Hint: To subtract a negative integer, add its opposite $2 - (-3) = 2 + 3$

- **5** Find the answer if:

 - a -2 is subtracted from 6
 b -1 is subtracted from 10
 c -4 is subtracted from -1
 d -7 is subtracted from -3
 e -2 is subtracted from -7
 f -8 is subtracted from -13



	1 -8 is subtracted from -1	
Example 9 Combining sub	tractions	
Evaluate the following. a $7 - 9 - (-3)$ Solution	b $-2 - (-5)$ Explanation	
a $7 - 9 - (-3) = -2 - (-3)$ = $-2 + 3$ = 1	First work o To subtract −2 plus 3 is	-3, add 3.
b $-2 - (-5) - 9 = -2 + 5 - 9$ = $3 - 9$ = -6	To subtract -5 , add 5. -2 plus $5 = 3$. 3 minus 9 is -6 .	
Now you try Evaluate the following. a $4 - 8 - (-6)$	b -13 - (-2) – 7
6 Evaluate the following. a $6-9-(-1)$ d $-3-(-1)-4$ g $2-(-1)-(-3)$	b $2-4-(-3)$ e $-4-(-2)-5$ h $-10-(-4)-(-3)$	c $-1 - 3 - (-2)$ f $-10 - (-2) - 6$ i $-16 - (-10) - (-7)$
Problem-solving and r 7 Find the missing number. a $5 - \Box = 6$ d $\Box - (-3) = 7$ g $5 - \Box = 11$ j $\Box - (-5) = -1$	b $2 - \square = 7$ e $\square - (-10) = 12$	c $-1 - \square = 3$ f $\square - (-4) = -20$ i $-2 - \square = -4$ l $\square - (-2) = -4$
 8 Calculate the answer, working a 3+(-2)+(-1) c 3-(-1)-(-4) 	g from left to right. b $2 + (-1)$ d $10 - (-1)$)+(-6)

- **e** -7 (-1) (-4)
- **g** -9 (-19) + (-16)
- i -13 (-19) + (-21)
- **k** -18 (-16) (-19)

f 10 - (-6) + (-4)**f** -20 - (-10) - (-15)

- **h** -15 (-20) + (-96)j = -2 - (-3) - (-5)
- 5 + (-20) (-26)

Essential Mathematics for the Victorian Curriculum CORE Year 7

9 A diver is at a height of -19 m from the surface of the sea. During a diving exercise, the diver rises 10 m, falls 18 m and then rises once again by 15 m. What is the diver's final height from sea level?



- 10 A small business has a bank balance of -\$50 000. An amount of \$20 000 of extra debt is added to the balance and, later, \$35 000 is paid back. What is the final balance?
- **11** \$100 of debt is added to an existing balance of \$50 of debt. Later, \$120 of debt is removed from the balance. What is the final balance?



- **12** If *a* is a positive number and *b* is a negative number, are the following true?
 - **a** a b is *always* positive.
 - **b** b a is *always* negative.

Hint: Try some values for *a* and *b*.

14

- **13** If *a* is a negative number and *b* is a negative number, are the following true?
 - **a** a b is always positive. **b** b a is always negative.

Make it true

14 Insert + or – signs to make each statement true.

a
$$-2$$
 6 $(-2) = 2$

b
$$-3$$
 (-3) $2 = -8$

- **c** -2 (-5) 3 = 0
- **d** -4 (-3) (-1) = -6
- **e** 4 (-10) (-2) = 12
- **f** -3 (-16) (-2) = -17

Make up your own and try it on a friend!

1 Insert the symbol < (less than) or > (greater than) into these statements to make them true. 7A Progress guiz **a** -3 1 **b** -1 -6**c** 4 - 5**d** -3 -2**2** Write the next three numbers in these patterns. 7A **b** -12, -9, -6, ___, __, __ **c** 4, -1, -6, ___, ___, ___ d -77, -66, -55, ___, ___, **3** Evaluate the following. 7B **a** -4+6**b** -7+3d -15 + 40**c** -24 + 177B 4 Evaluate the following. **a** 8 – 11 **b** -4-5**c** 1 – 78 **d** -32 - 29 7B **5** Evaluate the following. **b** -3 - 6 - 4**a** 4 - 7 + 11 d -8 + 25 - 17 - 9**c** 6 - 13 - 5 + 26 Find the missing number. 7B **a** $6 - \square = -3$ **b** $-8 - \Box = -19$ **c** +7 = -34**d** -81 = -167C **7** Calculate answers to the following. **b** 12 + (-16)**a** 8 + (-5)**c** -4 + (-3)**d** -31 + (-31)8 Work from left to right to evaluate the following. 7C **a** 4 + (-3) + 7**b** 11 + (-21) + 5**c** -13 + (-10) + 45**d** -83 + 100 + (-27)**9** Calculate answers to the following. 7D **a** 3 - (-5)**b** 14 - (-13)**c** -27 - (-9)**d** -15 - (-38)7D **10** Work from left to right to evaluate the following. **a** 7 - 12 - (-5)**b** -14 - 21 - (-11)**c** -1 + (-5) - (-9)**d** 14 - (-15) + (-13)11 \$75 of debt is added to an existing balance of \$50 of debt. Later, \$100 of debt is removed 7D from the balance. What is the final balance?

7E Substituting integers

Learning intentions

- To understand that substitution involves replacing a pronumeral (letter) with a number.
- To be able to substitute positive or negative integers into an expression and evaluate.
- To know the convention for determining order of operations in an expression involving more than one operation.

Key vocabulary: pronumeral, substitute, evaluate, operation, brackets

Expressions with pronumerals or variables are used to describe many real-world situations. For example, the speed of an accelerating rocket could be shown by 100 + 20t metres per second, where t is the time in seconds.

To work out the speed after 5 seconds, we would substitute t = 5 into 100 + 20t to give $100 + 20 \times 5 = 200$ metres per second.

In this section, we will look at the process of substitution using both positive and negative integers.



Lesson starter: Order matters

Two students substitute the values a = -2, b = 5 and c = -7 into the expression ac - bc. Some of the different answers received are 21, -49, -21 and 49.

• Which answer is correct and what errors were made in the calculation of the other three incorrect answers?

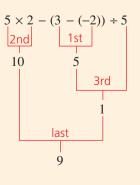
Key ideas

Substitute into an expression by replacing **pronumerals** (the letters) with numbers.

If a = -2 and b = 5, then:

$$b - a = 5 - (-2) = 5 + 2 = 7 = 8 2b + a = 2 \times 5 + (-2) = 10 - 2 = 8$$

- Use **brackets** around negative numbers to avoid confusion with other symbols.
- When working with more than one **operation** and with positive and/or negative numbers:
 - Deal with brackets first.
 - Do multiplication and division next, working from left to right.
 - Do addition and subtraction last, working from left to right.



Exercise 7E

Understanding 1–3 3 1 Find the value of each expression if a = 3. **a** a + 3**b** 2-ac $2 \times a$ **d** $4 \times a - 10$ **e** -2 + af -3 - a**q** $6 \div a$ **h** -4 - a2 Which of the following shows the correct substitution of a = -2 into the expression a - 5? **A** 2-5**B** -2+5C -2 - 5**D** 2+53 Which of the following shows the correct substitution of x = -3 into the expression 2 - x? **A** -2 - (-3)**B** 2 - (-3)**C** -2+3**D** -3+2Fluency 4-5(1/2) 4-6(1/2) **Example 10 Substituting integers** Evaluate the following expressions using a = 3 and b = -5. **a** 2 + 4a**b** a-b**c** 2a + bSolution **Explanation** $2 + 4a = 2 + 4 \times 3$ Replace *a* with 3 and evaluate the multiplication before doing the addition. = 2 + 12= 14**b** a-b=3-(-5)Replace *a* with 3 and *b* with -5. To subtract -5, add 5. = 3 + 5= 8 $2a + b = 2 \times 3 + (-5)$ Replace a with 3 and b with -5, and evaluate the С multiplication before the addition. = 6 - 5To add -5, subtract 5. = 1 Now you try Evaluate the following expressions using a = 2 and b = -6. **a** 3a - 10**b** 2a - b**c** 7a + b4 Evaluate the following expressions using a = 3 and b = -2. **a** 2a + 1**b** 4a - 3**c** a - 6Hint: Substitute a = 3d 3a - 20**e** 2 - af 4 - 3aand/or b = -2, then work **h** -2 - 2ab - 4**g** -1 - aout the answer.

 $\mathbf{k} \quad b-a$

 $\mathbf{n} \quad a-b$

q $9 \div a - b$

b + 8

m b + 7a

p 3a + b

b+2a

o 2a - b**r** $b - 12 \div a$

Evaluate the following using x a $3 \times (10 - y)$ Solution	= -2 and $y = 7$. b $(y - x) \div 3$ Explanation		
a $3 \times (10 - y) = 3 \times (10 - 7)$ = 3×3 = 9	Substitute $y = 7$. Deal with bracke	ts before oth	er operations.
b $(y - x) \div 3 = (7 - (-2)) \div 3$ = 9 ÷ 3 = 3	Substitute $x = -2$ Evaluate the brace	•	- (-2) = 7 + 2.
Now you try Evaluate the following using x a $2 \times (y - x)$	= -4 and $y = 9$. b $(x - y) - (-2)$		
5 Evaluate the following exprese a $2 \times (7 - x)$ c $(2 + x) \times 4$ e $3 \times (1 - y)$ g $(2 + y) \times 6$ i $(x + y) \times 4$ k $5 \times (x - y)$	ssions using $x = 5$ and $y = -3$. b $5 \times (8 - x)$ d $(-2 + x) \div 1$ f $4 \times (7 - y)$ h $(5 + y) \div 2$ j $(x + y) \div 1$ l $10 \div (x + y)$		Hint: Remember to deal with brackets first, before doing other operations.
6 Evaluate the following if $x = a x - y - 6$ c $3y - x + 7$ e $5y - x$ g $-4 + x - 2y$	-4 and $y = 3$. b $2y + x + 1$ d $2 - x - y$ f $2 - x + 3y$ h $-6 + x + 7y$		
Problem-solving and	reasoning	7–9	8–11
7 The volume of water runnin- minutes. Find the volume of a 2 minutes ($t = 2$) b 5 minutes ($t = 5$) c 20 minutes ($t = 20$)	g into a tank is given by the expression water after:	10 + 5 <i>t</i> litres,	, where <i>t</i> is the time ir

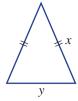
- **d** 2 a equals 6
- c 2a + 1 equals 7
 e 6 a equals 13
 - | -|
- **g** 3 + a equals -2
- **f** -1 a equals 0
- **h** -4 + a equals -3
- i -10 a equals -4
- **9** Albert substitutes c = -10 into 10 c and gets 0. Is he correct? If not, what is the correct answer?

substitute to see if you are

guess.

correct. If not, make a better

10 The formula for the perimeter, *P*, of this isosceles triangle is P = 2x + y.



a Use the formula to find *P* if: **i** x = 2 and y = 1

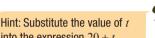
ii x = 4 and y = -2

- **b** What problems are there with part **a ii** above?
- 11 Write two different expressions involving x that give an answer of -10 if x = -5.

Negative time

- 12 A motorcycle's speed t seconds after passing a particular point on a racing track is given by the expression 20 + t metres per second.
 - a Find the motorcycle's speed after 4 seconds.
 - **b** Find the motorcycle's speed at t = -2 seconds (i.e. 2 seconds before passing the t = 0 point).
 - **c** Find the motorcycle's speed at t = -6 seconds.





12

into the expression 20 + t.

7F Introducing the number plane

Learning intentions

- To understand that the number plane can be extended to include negative numbers on both axes.
- To understand what a coordinate pair means if one or both numbers is negative.
- To be able to plot a point at a location expressed as *x* and *y* coordinates.

Key vocabulary: number plane, Cartesian plane, coordinates, x-axis, y-axis, origin

Street maps use a coordinate system, where a capital letter and a number, such as D7, are used to locate a square area on the map.

This kind of coordinate system is accurate enough to find a street name or park. In mathematics we need a more precise system so that we can locate points and draw graphs.

The number plane we use today is called the Cartesian plane, after the seventeenth century mathematician René Descartes, and this includes both positive and negative numbers.



Lesson starter: North, south, east and west

The units for this grid are in metres.

René starts at position O and moves:

- 3 m east 2 m south
- 4 m west
- 5 m north.

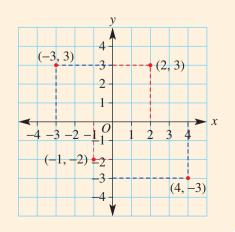
Pierre starts at position *O* and moves:

- 1 m west
- 3 m south
- 4 m east
- 5 m north.

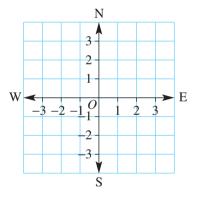
Using the number plane, how would you describe René and Pierre's final positions?

Key ideas

- The number plane (also called the Cartesian plane) uses two axes (x-axis and y-axis) at right angles.
- A point plotted on the plane has an *x*-coordinate and *y*-coordinate, which are written as (*x*, *y*). The *x*-coordinate is written before the *y*-coordinate, as in the alphabet.
- The point (0, 0) is called the **origin** and labelled *O*.
- To plot points, always start at the origin.
 - For (2, 3) move 2 right and 3 up.
 - For (4, -3) move 4 right and 3 down.
 - For (-3, 3) move 3 left and 3 up.
 - For (-1, -2) move 1 left and 2 down.



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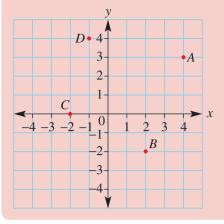


Exercise 7F

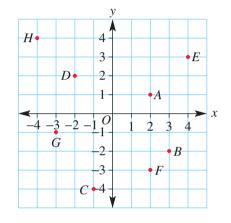
	nderstandi	ng			1, 2	2
1 P	Put the words <i>lef</i>	t or right and dou	<i>vn</i> or <i>up</i> into th	iese sentences.		
а					and 4 units	
b					and 1 unit	
C					and 2 units	
d					and 4 units	
	Match the points		G and H with t	he given coordina	bites. $D \bullet C$ $H \bullet$ -3 -2 -1 $G \bullet$	y $3 - E \cdot 2$ $1 - A \cdot 2$
	luency				3, 4	3–5
		ling coordinat		instant of the point	to labellad (P. C.	
For		ne shown, write o		inates of the poin	ts labelled <i>A</i> , <i>B</i> , <i>C</i> a	and D.
For	the number plan y $D \bullet \qquad 3$ $2 \bullet \qquad 1$ $1 \bullet \qquad 2$ $1 \bullet = 1$ $1 \bullet = 1$	ne shown, write o		inates of the poin	ts labelled <i>A</i> , <i>B</i> , <i>C</i> a	and <i>D</i> .

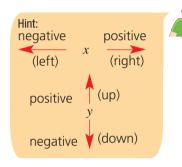
Now you try

For the number plane shown, write down the coordinates of the points labelled A, B, C and D.



3 For the number plane given, write down the coordinates of the points labelled *A*, *B*, *C*, *D*, *E*, *F*, *G* and *H*.





Example 13 Plotting points

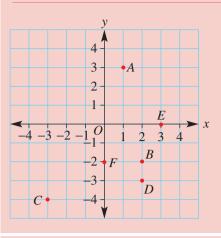
-4

Draw the number plane shown here and plot the following points. A(1, 3), B(2, -2), C(-3, -4), D(2, -3), E(3, 0), F(0, -2)

Continued on next page



Solution



Explanation

For each point, start at the origin (0, 0).

First move right (if x is positive) or left (if x is negative).

Then move up (if y is positive) or down (if y is negative).

Now you try

Draw a number plane and plot these points. *A*(2, 4), *B*(1, -3), *C*(-4, 1), *D*(-2, -2), *E*(-1, 0), *F*(0, 3)

- 4 a Draw a set of axes like those in the example above. (You can use grid paper to help.)b Now plot these points.
 - i A(-3, 2)v E(2, 2)
 - ix I(3, -2)
 - 3,-2)

- iii C(2, -1)vii G(-3, -1)xi K(-1, -1)
- iv D(-2, -4)viii H(1, -2)xii L(1, 2)

Hint: For each point, either the *x*-coordinate or *y*-coordinate

will be zero.

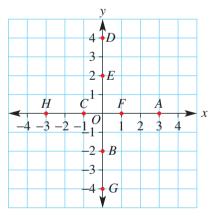
6-8

5 For the number plane given, write down the coordinates of the points labelled *A*, *B*, *C*, *D*, *E*, *F*, *G* and *H*.

B(1,4)

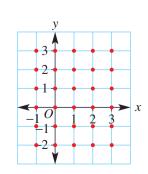
vi F(-1, 4)

x J(-2,1)



Problem-solving and reasoning

- 6 Count the number of points (red dots) on this plane that have:
 - a both x- and y-coordinates as positive numbers
 - **b** an *x*-coordinate as a positive number
 - **c** a *y*-coordinate as a positive number
 - **d** an *x*-coordinate as a negative number
 - e a *y*-coordinate as a negative number
 - f both x- and y-coordinates as negative numbers
 - g neither x- nor y-coordinate as positive or negative numbers

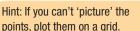


7–10

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- 7 When plotted on the number plane, what shape does each set of points form?
 - **a** A(-2, 0), B(0, 3), C(2, 0)
 - **b** A(-3, -1), B(-3, 2), C(1, 2), D(1, -1)
 - **c** A(-4, -2), B(3, -2), C(1, 2), D(-1, 2)
 - **d** A(-3, 1), B(-1, 3), C(4, 1), D(-1, -1)
- 8 Karen's bushwalk starts at a point (2, 2) on a grid map. Each square on the map represents 1 km.
 If Karen walks to the points (2, -7), then (-4, -7), then (-4, 0) and then

(2, 0), how far has she walked in total?







11

9 Seven points have the following *x*- and *y*-coordinates.

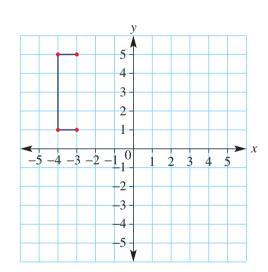
x	-3	-2	-1	0	1	2	3
У	-2	-1	0	1	2	3	4

- **a** Plot the seven points on a number plane. Use -3 to 3 on the x-axis and -2 to 4 on the y-axis.
- **b** What do you notice about these points on the number plane?
- **10** The points A(-2, 0), B(-1, ?) and C(0, 4) all lie on a straight line. Find the y-coordinate of point B.

The secret message

11 Plot these points to decode a secret message. Join points with a line segment if there is a + sign between coordinate pairs. The first one has been done for you.

(-3, 5) + (-4, 5) + (-4, 1) + (-3, 1)(-2, 2) + (-2, 4) + (-3, 4) + (-3, 2) + (-2, 2)(0, 2) + (0, 4) + (-1, 4) + (-1, 2) + (0, 2)(0, 5) + (1, 5) + (1, 1) + (0, 1)(2, 2) + (2, 4)(3, 2) + (4, 2) + (4, 3) + (3, 3) + (3, 4) + (4, 4)(-1, -2) + (-1, 0)(-2, 0) + (0, 0)(1, 0) + (1, -2)(1, -1) + (2, -1)(2, 0) + (2, -2)(4, 0) + (3, 0) + (3, -2) + (4, -2)(3, -1) + (4, -1)(-4, -3) + (-4, -5) + (-3, -5) + (-3, -3) + (-4, -3)(-2, -5) + (-2, -3) + (-1, -3) + (-1, -4) + (-2, -4) + (-1, -5)(0, -3) + (0, -5) $(2, -3) + (1, -3) + (1, -5) + (2, -5) + (2, -4) + (1\frac{1}{2}, -4)$ (3, -3) + (3, -5)(4, -5) + (4, -3) + (5, -5) + (5, -3)



🔀 Maths@Work: Golfer

Being a golf professional or a golf instructor can be a very exciting career. It is a physically demanding job needing stamina as well as a calculating mind. Distance, slope, angles, velocity of swings, wind speed and direction, as well as club type are all very important factors for success in golf.

Every golf course and each hole is assigned a number called a par. This is the number of shots an expert golfer should require to complete that golf course or hole. A player's score is the number of shots above or below the par value. Negative scores are better than positive scores. The person with the lowest score wins!



- 1 Different terms are used to describe a player's success at each hole. Write down the positive or negative number that best describes each of the following golfing terms.
 - a An Eagle, which is two under par
 - **b** A Birdie, which is one under par
 - c An Albatross, which is three under par
 - d A Bogey, which is one over par
 - e A Double bogey
- 2 One way of calculating a golfer's handicap is to use the average of their best 8 scores from the last 20 games. A handicap of 12 means a person's total shots are adjusted by −12 to give their final score.
 - Final score = total shots handicap
 - Very good golfers play 'off scratch' which means they have a zero handicap.
 - Expert golfers have a positive handicap that is added to their total shots.

Write down how the final score will be adjusted for players with:

- **a** a handicap of 7
- **b** a handicap of 20
- **c** a handicap of 5
- **d** playing off scratch
- e a positive handicap of 3
- **f** a positive handicap of 2



3 The Lakes Golf Club in NSW, where the Australian Open has been held, is rated as a par 72 course. Complete this table for these rounds of golf at Lakes Golf Club.

	Total shots	Handicap	Final score	How much over or under the course par is this player's final score?
Chelsea	84	6		
Mitchell	98	16		
Adam	76	6		
Bella	74	+1		



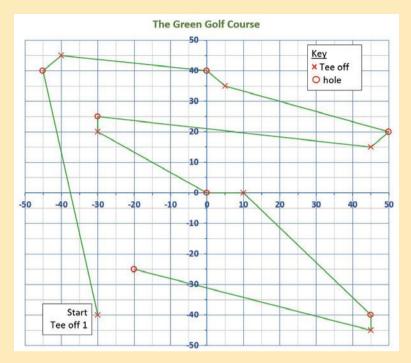
Abraham Ancer of Mexico hitting an iron shot on the 17th hole at the Lakes Golf Course during the 2018 Australian Open. He went on to win the tournament with a score of -16 over four rounds.

- 4 The next table has a summary of the scores for two players, Rick and Brad, at The Lakes.
 - a Complete the missing values in this scorecard.
 - **b** Calculate their final scores given Rick's handicap is +3 and Brad's handicap is 7.
 - **c** Who won and by how much?
 - **d** What was the average number of shots per hole for each of the players? Round your answers to 2 decimal places.
 - e How many Birdies did each player make on the course?

Hole	Par	Rick's score	under/over par for Rick	Brad's score	under/over par for Brad
1	4	4		5	
2	4	4		5	
3	4	4		5	
4	4	4		5	
5	4	6		4	
6	4	5		4	
7	3	5		4	
8	5	2		6	
9	3	3		4	
10	4	3		5	
11	5	4		5	
12	4	3		5	
13	4	3		3	
14	5	5		6	
15	3	3		4	
16	4	5		5	
17	5	4		6	
18	3	3		4	
TOTAL					

Using technology

5 The number plane below shows the layout for the first 7 holes of a golf course.



The Green Golf Course						
	x	У				
Tee off 1						
Hole 1						
Tee off 2						
Hole 2						
Tee off 3						
Hole 3						
Tee off 4						
Hole 4						
Tee off 5						
Hole 5						
Tee off 6						
Hole 6						
Tee off 7						
Hole 7						

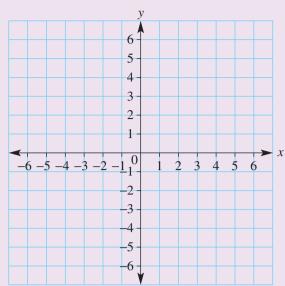
- **a** Complete the table above right for the (x, y) coordinates of each point plotted.
- **b** Using technology such as Excel or GeoGebra, plot and join the points on a number plane graph. (For example, for an Excel spreadsheet: select values/Insert chart/scatter/straight lines and markers. Choose a grid design.)
- c If you print your graph, you may wish to draw some water hazards and bunkers.



Aerial view of a golf course, with water hazards and bunkers clearly visible.

1 Plot the following points to find out what I am. Join points with a line segment if there is a + signbetween coordinate pairs.

(-3, 2) + (-3, -4) + (3, -4) + (3, 2)(-1, -4) + (-1, 0) + (1, 0) + (1, -4)(-5, 0) + (0, 5) + (5, 0)



C

- 2 Complete these magic squares. All rows, columns and diagonals have the same sum within a magic square.

b

	-5
-2	0
-6	-1

a

-9	5		-6
	-4		-1
		1	
3		-8	6

		-1	
-3			
-7	-5	-4	-10
-2		-13	1

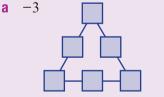
- 3 Insert brackets (if necessary) and symbols $(+, -, \times, \div)$ into these number sentences to make them true.
 - **a** -3 4 -2 = -6

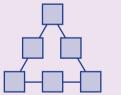
b
$$-2$$
 5 -1 $11 = 21$

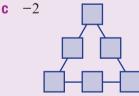
$$1 \boxed{30} - 6 \boxed{-2} = -3$$

Place the integers -3, -2, -1, 0, 1 and 2 into the triangle so that the sum of every side is: 4

> b 0



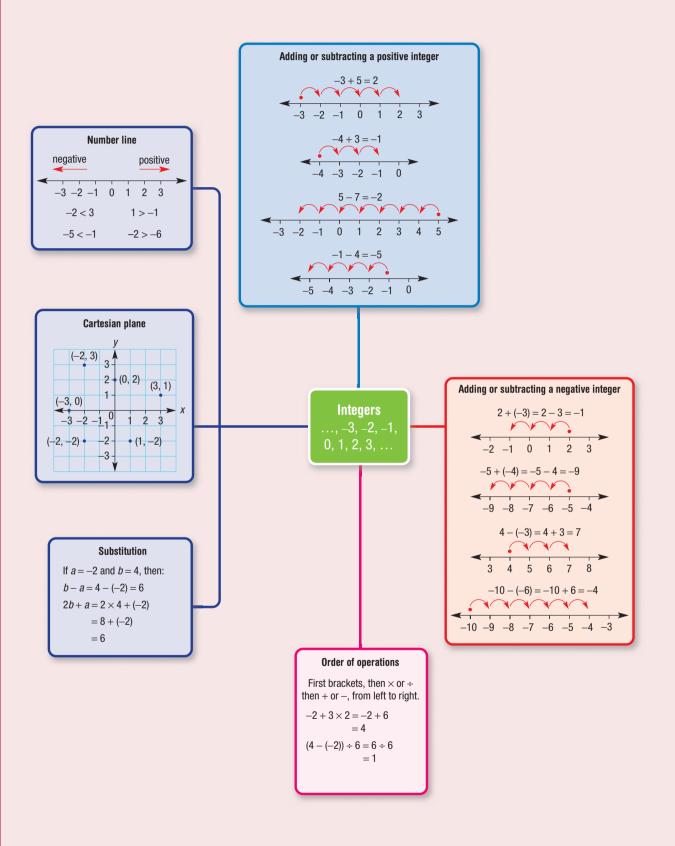




5 Find the next three numbers in these patterns.

- **b** -32, 16, -8, ___, ___, ___

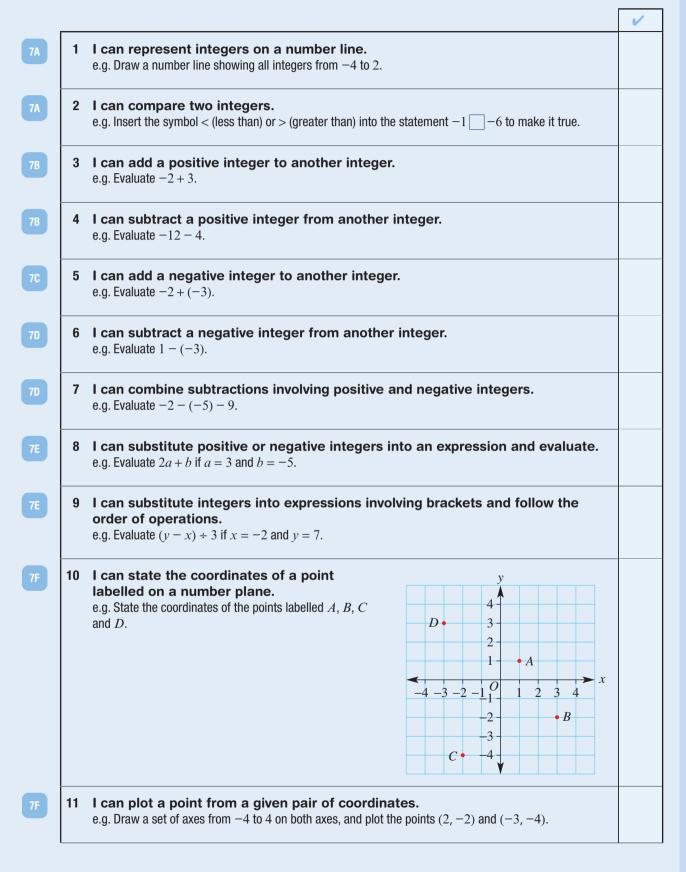
- 6 a The difference between two numbers is 14 and their sum is 8. What are the two numbers? **b** The difference between two numbers is 31 and their sum is 11. What are the two numbers?



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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.



Short-answer questions

7A	1	Write the missing nun					
		a -4,, -2, -1,			3, 2,, 0, -1,	1.6	
		c −10, −8,, −4, _	, 0	a	9, 4,, -6,, -	16	
7A	2	Insert the symbol < (le	ess than) or > (greater t	:han)) into each of these	sta	tements
		to make it true.	b 1 1 4	•	2 7	Ч	11 6
		a 0 7	b -1 4	C	3 77	u	-116
7B	3	Evaluate: a 2 – 7	b $-4+2$	•	0 - 15	d	-36 + 37
		e $-3+2$	f $-7+9$		-2-5		-30 + 37 -6 - 19
		i -4 - 7	j 4 – 11	-	-16 - 31		-126 - 5
7C/D	4	Evaluate:					
		a 2+(-1)		C	-1 + (-2)	d	-3 + (-4)
		e $5 + (-7)$	f $-1 + (-4)$		10 - (-2)		-21 - (-3)
		4 - (-3)	j -18 - (-1)	k	-2 - (-5)	1	-15 - (-18)
7C/D	5	Evaluate:					
			b $-3+7-(-1)$				
		e $-1 + (-2) - 3$	f $-4 - (-1) - 3$	g	-6 - (-4) + 7	h	-17 + (-14) - (-2)
7C/D	6	Find the missing num					
			b $-1 + \square = -10$				
		e $-1 - \square = 20$	f $-15 - \square = -13$	g	$7 + _ = -80$	h	$-15 + \square = 15$
7E	7	Evaluate using order o	-				
			b $-4 - 7 \div 7$				$25 \div 5 - (-2)$
		e $(3 - (-2)) \times 6$	f $2 \times (4 - (-1))$	g	$(7 + (-3)) \div 4$	n	$20 \times (-1 - (-3))$
7E	8	Evaluate the following					
		a $a+b$	b $b+c$ f $c-b$		$c + a \\ b - b$		b-a
		e $a - b$ i $c - 2a$	c - b b + 3a	-	b = b c = b = a		2a + c $2a - b + c$
			-		c o u	1	20 010
7F	9	For the Cartesian plan	ie shown, write down i ints labelled A, B, C, D,		nd F		<i>y</i>
		coordinates of the pol	$\prod_{i=1}^{n} abclicu A, B, C, D,$, L u			4
							3
						-0	
							1 A x
					-4 -3	-2 -	$-1 \stackrel{O}{1}$ 1 2 3 4

Multiple-choice questions

- 1 When the numbers -4, 0, -1, 7 and -6 are arranged from lowest to highest, the correct sequence is:
 - **A** 0, -1, -4, -6, 7 **D** -1, -4, -6, 0, 7 **B** 0, -4, **E** -6, -
- **B** 0, -4, -6, -1, 7 **E** -6, -1, 0, -4, 7
- **C** -6, -4, -1, 0, 7

3 + E

7B	2 The difference be	tween -3 and 4 is:			
	A -12	B −1	C 1	D -7	E 7
7D	3 The missing num	per in $2 - \square = 3$ is	5.		
	A 1	B −1	C 5	D -5	E 2
7A	4 Which of the follo	owing is true?			
	A 2 < -1	B $-4 > -3$	C 0 < −3	D -4 < -2	E 1 < −4
7B	5 The temperature	inside a mountain	hut is –5°C. After b	urning a fire for 2 hou	irs, the temperature
	rises to 17°C. Wh	at is the rise in tem	•		
	A −12°C	B 12°C	C 22°C	D -85°C	E −22°C
70	6 $-2 + (-3)$ is equal	to:			
	A -5	B 1	C -2	D -1	E 5
7D	7 5 - (-2) + (-7) is	equal to:			
	A -4	B 10	C 7	D 0	E 14
7E	8 Which operation	(i.e. addition, subti	raction, multiplicatio	on or division) is comp	leted <i>second</i> in the
	calculation of (-2				
	A addition		subtraction	C multi	plication
	D division	E	brackets		
7E	9 If $a = -2$ and $b =$				
	A -3	B 3	C 7	D 10	E -7
7F		3), $B(-3, -1)$, $C(1, $	-1) and $D(0, 3)$ are	joined on a number p	lane. What shape do
	they make?		Course	• Tree is a	
	A Triangle	В	Square	C Trape	210111

D Kite

E Parallelogram

Extended-response questions

- 1 A scientist is camped on the ice in Greenland. He records the following details in his notepad about the temperature over five days. Note that 'min' stands for minimum and 'max' stands for maximum.
 - Monday: min = -18° C, max = -2° C. •
 - Decreased 29°C from Monday's max to give Tuesday's min. •
 - Wednesday's min was -23° C.
 - Max was only -8°C on Thursday. •
 - Friday's min is 19°C colder than Thursday's max.



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Chapter review

Chapter review

- a What is the overall temperature increase on Monday?
- **b** What is Tuesday's minimum temperature?
- **c** What is the difference between the minimum temperatures for Tuesday and Wednesday?
- **d** What is the overall temperature drop from Thursday's maximum to Friday's minimum?
- e By how much will the temperature need to rise on Friday if its maximum is 0°C?
- 2 When joined, these points form a picture on the number plane. Use grid paper to draw a number plane from -5 to 5. What is the picture?

A(0, 5), B(1, 3), C(1, 1), D(2, 0), E(1, 0), F(1, -2), G(3, -5), H(-3, -5), I(-1, -2), J(-1, 0), I(-1, -2), I(-1, -2),K(-2, 0), L(-1, 1), M(-1, 3), N(0, 5)

Chapter 0

Statistics and probability

And all branching till branch will branch

Essential mathematics: why skills in statistics and probability are important

Statistical calculations and graphs are essential for interpreting data and are widely used, including by governments, sports clubs, TV rating agencies, farmers, insurance companies and other businesses.

- A nurse records a patient's temperature as continuous numerical data, and heart rate as discrete numerical data.
- Cricket batters are compared using their mean (average) runs per innings.
- Column graphs can compare TV and stadium spectator numbers for various sports, such as AFL (Australian Football League), NRL (National Rugby League), cricket, soccer and tennis.
- Businesses can use line graphs to display weekly expenses, sales and profits. A line graph makes it easy to visualise trends which can be used to make predictions.
- Daily weather forecasts generally include the chance, or probability, of rain.



In this chapter

- 8A Collecting and classifying data
- 8B Summarising data numerically
- 8C Dot plots and column graphs
- 8D Line graphs
- 8E Stem-and-leaf plots
- 8F Describing chance (Consolidating)
- **8G** Theoretical probability
- 8H Experimental probability 🔶

Victorian Curriculum

STATISTICS AND PROBABILITY Chance

Construct sample spaces for single-step experiments with equally likely outcomes (VCMSP266)

Assign probabilities to the outcomes of events and determine probabilities for events (VCMSP267)

Data representation and interpretation

Identify and investigate issues involving numerical data collected from primary and secondary sources (VCMSP268)

Construct and compare a range of data displays including stem-and-leaf plots and dot plots (VCMSP269)

Calculate mean, median, mode and range for sets of data. Interpret these statistics in the context of data (VCMSP270)

Describe and interpret data displays using median, mean and range (VCMSP271)

NUMBER AND ALGEBRA Linear and non-linear relationships

Investigate, interpret and analyse graphs from real life data, including consideration of domain and range (VCMNA257)

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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

- Warm-up quiz
- 1 Rosemary notes the temperature for a week.

Mon	Tue	Wed	Thu	Fri	Sat	Sun
21°C	24°C	22°C	19°C	20°C	21°C	15°C

- a What was the lowest temperature for the week?
- **b** What was the highest temperature recorded?
- c Which temperature(s) occurred on more than one day?
- 2 Write these fractions in simplest form.

а	$\frac{10}{20}$	b	$\frac{20}{30}$
C	$\frac{21}{28}$	d	$\frac{2}{8}$

- **3** Consider the set of numbers 4, 2, 6, 5, 9.
 - **a** What is 4 + 2 + 6 + 5 + 9?
 - **b** What is the difference between the smallest and highest number?
 - **c** Write the numbers from smallest to largest.
- 4 For each of the following axes, is the scale correct (C) or incorrect (I)?

a	0	1	2	3	4	
b	0	1	3	5	>	
C	0	5	10	15	>	
d	0	1	1 2	3	4	_

- **5 a** How many faces do dice have?
 - **b** How many flat sides do coins have?
- 6 Write the following values as decimals.
 - **a** 2 ÷ 4
 - **b** 20 ÷ 50
 - **c** 12 ÷ 60
 - **d** 11 ÷ 55

7 Order these events from least likely to most likely.

- A Rolling a die and it landing on the number 3.
- **B** Flipping a coin and it landing with 'tails' showing.
- **C** The Prime Minister of Australia being struck by lightning tomorrow.
- **D** The internet being used by somebody in the next 20 minutes.
- 8 Decide if you think these events have a low (L), medium (M) or high (H) chance of occurring.
 - a Rolling a 6 on a single toss of a die.
 - **b** It will rain at least once in the next month.
 - **c** Tossing a tail from flipping a coin once.

8A Collecting and classifying data

Learning intentions

- To be able to classify variables as numerical (discrete or continuous) or categorical.
- To understand that different methods are suitable for collecting different types of data, based on the size and nature of the data.

Key vocabulary: variable, numerical data, discrete numerical, continuous numerical, categorical data, primary source, secondary source, census, sample, observation

People collect or use data almost every day. Athletes and sports teams look at performance data, customers compare prices at different stores, investors look at daily interest rates, and students compare marks with other students in their class. Companies often collect and analyse data to help produce and promote their products to customers and to make predictions about the future.

Lesson starter: Collecting data

Consider, as a class, the following questions and discuss their implications.

- Have you or your family ever been surveyed by a telemarketer at home? What did they want? What time did they call?
- Do you think that telemarketers get accurate data? Why or why not?
- Why do you think companies collect data this way?
- If you wanted information about the most popular colour of car sold in NSW over the course of a year, how could you find out this information?

Key ideas

- In statistics, a variable is something that can be measured or observed. It is expected to change over time or between each observation. A variable (or data) can be numerical or categorical.
 - Numerical data is data that can be counted or measured. It can be labelled as discrete or continuous:
 - discrete numerical data that can only be whole number values, such as the number of televisions in a house (4 televisions) or the number of cars in a street (10 cars).
 - continuous numerical data that can take any number value, including decimals, such as heights, weights or temperatures. For example, the height of a person could be 172.2 cm, 172.4 cm or 172.215 cm.
 - **Categorical data** is data that can be placed into categories or types of objects, such as colours, genders, brands of car. In a survey, categorical data comes from answers that are given as words (e.g. yellow or female) or ratings (e.g. 1 = dislike, 2 = neutral, 3 = like).
- Data can be collected from primary or secondary sources.
 - Data from a **primary source** are firsthand information collected from the original source by the person or organisation needing the data. For example, a survey an individual student conducts, data collected as a scientist conducts an experiment, or census data collected and then used by an organisation like the Bureau of Statistics.
 - Data from a **secondary source** have been collected, published and possibly summarised by someone else before we use it. Data collected from newspaper articles, textbooks or internet blogs represent secondary source data.
- Samples and populations.
 - When an entire population (e.g. a maths class, all the cars in a parking lot, a company or a whole country) is surveyed, it is called a **census**.
 - When a subset of the population is surveyed, it is called a **sample**. Samples should be randomly selected and large enough to represent the views of the overall population.
 - When we cannot choose which members of the population to survey, and can record only those visible to us (e.g. people posting their political views on a news website), this is called an **observation**.

Exercise 8A

Understanding

- 1 Look at the following sets of data. Decide if the data set is numerical (N) or categorical (C).
 - **a** 5, 7, 7, 8, 10, 11, 11, 15
 - **b** red, blue, pink, red, yellow, black, black, blue
 - c high, medium, medium, high, low, medium, low, high
 - **d** 0.4, 0.6, -0.4, 0.1, 0.0, -1.3, 7.8, -2.3
- 2 Choose a word to complete the sentence.
 - **a** When an entire ______ is surveyed, it is called a census.
 - **b** When a subset of a population is surveyed, it is called a _____
 - **c** Data from a ______ source is firsthand information.
 - d Data from a ______ source has already been published.
- **3** Match each word on the left to its meaning on the right. Check the definitions in the **Key ideas** for help.

ii A complete set of data

- a Sample
- **b** Categorical
- c Discrete numerical
- **d** Primary source
- e Continuous numerical
- f Population
- V Data collected firsthand
- vi Can take on any number in a range

i Only takes on particular numbers within a range

iv Data grouped in categories like 'male' and 'female'

iii A smaller group taken from the population

Fluency

Example 1 Classifying variables

Classify the following variables as categorical, discrete numerical or continuous numerical.

- a The sex of a newborn baby
- **b** The length of a newborn baby
- **c** The number of TV sets in people's homes

Solution	Explanation
a Categorical	As the answer is 'male' or 'female' (a word, not a number) the data are categorical.
b Continuous numerical	Length is a measurement, so all numbers are theoretically possible.
c Discrete numerical	The number of TV sets can only be 0, 1, 2, 3, not 1.385, for example.

Now you try

Classify the following variables as categorical, discrete numerical or continuous numerical.

- a The type of language spoken at home
- **b** The number of mobile phones in a household
- **c** The volume of water taken from a tap



2.3

1 - 3

4-5(1/2), 6

4–5(½), 6, 7

- 4 Classify the following as categorical or numerical.
 - **a** The eye colour of each student in your class
 - **b** The date of the month each student was born, e.g. the 9th of the month
 - **c** The weight of each student when they were born
 - d The brands of aeroplanes landing at Sydney's international airport
 - e The temperature of each classroom
 - f The number of students in each classroom during period one on Tuesday
- **5** Classify the following variables as categorical, continuous numerical or discrete numerical data.
 - a The number of cars per household
 - b The weights of packages sent by Australia Post on the 20th of December
 - **c** The highest temperature of the ocean each day
 - d The favourite brand of chocolate of the teachers at your school
 - e The colours of the cars in the school car park
 - f The make of cars in the school car park
 - g The number of letters in different words on a page
 - h The number of advertisements in a time period over each of the free-to-air channels
 - i The length of time spent doing this exercise
 - j The arrival times of planes at Darwin Airport
 - **k** The daily pollution levels in the city of Melbourne.
 - I The number of text messages sent by an individual yesterday
 - **m** The times for the 100 m freestyle event at the world championships over the last 10 years
 - n The number of Blu-ray discs someone owns
 - The brands of cereals available at the supermarket
 - p Marks awarded on a maths test
 - **q** The star rating on a hotel or motel
 - r The censorship rating on a movie showing at the cinema

Example 2 Classifying a data source as primary or secondary

Decide if the following data sources are primary or secondary.

- a A scientist records the temperature of a chemical every minute for 10 minutes.
- **b** A buyer looking at house price data printed in the newspaper.

Solution	Explanation
a Primary data source	The data is collected firsthand from the experiment.
b Secondary data source	The data has already been collected and published.

Now you try

Decide if the following data sources are primary or secondary.

- a A person reads data in a magazine relating to rainfall patterns.
- **b** A farmer collects pH readings from soil on a farm.

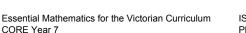


8A

- **6** Decide if the following data sources are primary or secondary.
 - **a** A scientist measures the mass of each mouse in a collection of 20 mice.
 - **b** A student records the colours of all the cars that pass by in 1 hour.
 - **c** Using the data from a website regarding maximum daily temperatures.
 - **d** Looking at a graph printed in the newspaper regarding crime rates.
- 7 Give an example of:
 - a discrete numerical data
 - b continuous numerical data
 - c categorical data

Problem-solving and reasoning

- 8 Is observation or a sample or a census the most appropriate way to collect data on each of the following?
 - a The arrival times of trains at a central station during a day
 - **b** The arrival times of trains at a central station over the year
 - **c** The heights of students in your class
 - d The heights of all Year 7 students in the school
 - e The heights of all Year 7 students in NSW
 - f The number of plastic water bottles sold in a year
 - g The religions of Australian families
 - **h** The number of people living in each household in your class
 - i The number of people living in each household in your school
 - j The number of people living in each household in Australia
 - **k** The number of native Australian birds found in a suburb
 - I The number of cars travelling past a school between 8 a.m. and 9 a.m. on a school day
 - ${\bf m}$ The money spent by students during a week at the canteen
 - **n** The ratings of TV shows
- **9** Give a reason why someone might have trouble obtaining reliable and representative data using a primary source to find the following.
 - **a** The temperature of the Indian Ocean over the course of a year
 - **b** The religions of Australian families
 - **c** The average income of someone in India
 - **d** Drug use by teenagers within a school
 - e The level of education of different cultural communities within Australia.



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8, 10-12

8-10



13

- **10** Secondary sources are already-published data that are then used by another party in their own research. Why is the use of this type of data not always reliable?
- 11 When obtaining primary source data you can survey the population or a sample.
 - a Explain the difference between a 'population' and a 'sample' when collecting data.
 - **b** Give an example of a situation where you should survey a population rather than a sample.
 - **c** Give an example of a situation where you should survey a sample rather than a population.
- 12 A Likert-type scale is for categorical data where items are assigned a number; for example, the answer to a question could be 1 = dislike, 2 = neutral, 3 = like.
 - a Explain why the data collected are categorical even though the answers are given as numbers.
 - **b** Give examples of a Likert-type scale for the following categorical data. You might need to reorder some of the options.
 - i strongly disagree, somewhat disagree, somewhat agree, strongly agree
 - ii excellent, satisfactory, poor, strong
 - iii never, always, rarely, usually, sometimes
 - iv strongly disagree, neutral, strongly agree, disagree, agree

Australian census

- **13** Australia's census surveys the entire population every five years.
 - a Why might Australia not conduct a census every year?
 - **b** Over 40% of all Australians were born overseas or had at least one of their parents born overseas. How does this impact the need to be culturally sensitive when designing and undertaking a census?
 - **c** The census can be filled out on a paper form or using the internet. Given that the data must be collated in a computer eventually, why does the government still allow paper forms to be used?
 - **d** Why might a country like India or China conduct their national census every 10 years?



8B Summarising data numerically

Learning intentions

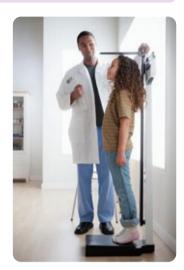
- To understand that numerical data can be summarised as a single number by finding its range, mean, median or mode.
- To be able to find the range of a set of data.
- To be able to find the mean, median and mode of a set of data.

Key vocabulary: range, data, mean, median, mode, frequency

Data sets may contain many numbers and therefore may need to be summarised so we can analyse and interpret the information in a meaningful way. For example, instead of listing the height of every Year 7 student in Australia, you could summarise this by finding the average height or the difference between the heights of the smallest and tallest people.

Lesson starter: Average height

- Write down your estimate of the average height (in cm) of students in your class.
- Going round the class, each student should state their height.
- Find the average by adding all the heights and dividing by the number of students in the class.
- What is the difference between the shortest and tallest students in the class?



Key ideas

The range of a set of data is given by: Range = highest number – lowest number

 $1 \quad 5 \quad 2 \quad 7 \quad 5 \rightarrow range = 6$

The mean of a set of data is given by: Mean = (sum of all the values) ÷ (total number of values)

 $1+5+2+7+5=20 \rightarrow 20 \div \text{total number of values} = 20 \div 5 \rightarrow \text{mean} = 4$

The median is the middle value if the values are sorted from lowest to highest. If there are two middle values, then add them together and divide by 2.

1 2 5 5 7 middle \rightarrow median = 5 3 4 4 6 9 10 middle = $\frac{4+6}{2} = 5$

The mode is the most common value. It is the value that occurs most frequently. We also say that it is the value with the highest frequency.

```
1 2 (5)(5) 7 \rightarrow mode = 5
```

3

1-3

Exercise 8B

Understanding

- 1 Write the numbers 1, 8, 3, 7, 2 from smallest to largest.
- **2** John finds that the ages of people in a room are 12, 35, 17, 8, 10 and 26 years.
 - a What is the age of the youngest person?
 - **b** How old is the oldest person?

3 Write the missing word.

- a The ______ is the middle value.
- **b** The _____ = (sum of all values) ÷ (total number of values).
- cThedTheis the most common value.

Fluency	4–7, 8–9(½) 5–11
Example 3 Finding the range, mean	n, median and mode
 Consider the ages of seven people who are a Find the range of values. c Find the median of this set of data. Solution 	 surveyed in a shop: 15, 31, 12, 47, 21, 65, 12 b Find the mean of this set of data. d Find the mode of this set of data. Explanation
a Range = $65 - 12$ = 53	Largest number = 65 Smallest number = 12
b Mean = $203 \div 7$ = 29	Sum of values = $15 + 31 + 12 + 47 + 21 + 65 + 12$ = 203 Number of values = 7
c Values: 12, 12, 15, 21 , 31, 47, 65 Median = 21	Place the numbers in ascending order. The middle value is 21.
d Mode = 12	The most common value is 12.
 Now you try Consider the number of pages of a book real a Find the range of values. c Find the median of this set of data. 	 b ad by Ned each night for a week: 26, 13, 9, 16, 20, 36, 13 b Find the mean of this set of data. d Find the mode of this set of data.
4 Consider the set of numbers 1, 5, 2, 10, 3.a Write the numbers from smallest to la	

c State the smallest number.

- **d** What is the range?

8B

5

- Consider the numbers 5, 6, 1, 10, 8.
- a What is the sum of these numbers?
- **b** How many numbers are there?
- **c** Find the mean of the numbers.
- 6 Consider the data 2, 5, 6, 9, 10, 12, 20.
 - a Copy and complete: When the numbers are listed in order, the middle number is called the
 - **b** State the median of the numbers.
- **7** The values in a set of data are 2, 8, 3, 5, 2, 7, 2.
 - a Copy and complete: The most common value is called the
 - **b** State the mode of the values.
- State the range of the following sets of numbers. 8
 - **a** 2, 10, 1, 3, 9 **b** 6, 8, 13, 7, 1
 - **c** 0, 6, 3, 9, 1 **d** 3, 10, 7, 5, 10
- **9** State the median for each of the following sets of data.
 - **a** 2, 5, 10, 12, 15
 - **c** 3, 1, 5, 2, 9
 - e 12, 18, 31, 15, 19, 10, 12 f 17, 63, 4, 13, 97, 82, 56
- **b** 1, 7, 8, 10, 11

d 12, 5, 7, 10, 2

Hint: Range = largest - smallest.



Hint: First list the numbers in ascending order. The median is the middle value.



Example 4 Finding the median with an even number of values

Find the median of 2, 7, 10, 12, 15, 23.

Solution	Explanation
10 and 12 are in the middle. Median = 11	Once the numbers are in ascending order, the two middle values are 10 and 12.
	The median is $(10 + 12) \div 2 = 11$

Now you try

Find the median of 14, 11, 2, 21, 18, 6, 21, 30.

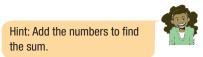
- **10** Find the median of:
 - **a** 3, 8, 10, 14, 16, 19
 - **c** 1, 5, 2, 9, 13, 17
- **b** 2, 7, 8, 10, 13, 18 **d** 5, 2, 3, 11, 7, 15

11	For each of the following sets of	data, calculate the
	mean and the mode.	
	a 1, 7, 1, 2, 4	b 2, 2, 10, 8, 13

- **c** 3, 11, 11, 14, 21
- **e** 1, 22, 10, 20, 33, 10
- d 25, 25, 20, 37, 25, 24 **f** 55, 24, 55, 19, 15, 36

Hint: The mode is the most common value. The mean is the sum of all values divided by the number of values.





12-14

12, 13

Problem-solving and reasoning

12 Brent and Ali make a table to show their test marks for a number of topics in Maths.

Test	1	2	3	4	5	6	7	8	9	10
Brent	58	91	91	75	96	60	94	100	96	89
Ali	90	84	82	50	76	67	68	71	85	57

- **a** Which student has the higher mean?
- **b** Which student has the higher median?
- c Which student has the smaller range?
- d Which student do you think is better at tests? Explain why.

13 The number of aces that a tennis player serves per match is recorded over eight matches.

Match	1	2	3	4	5	6	7	8
Number of aces	11	18	11	17	19	22	23	12

- **a** What is the mean number of aces the player serves per match? Round your answer to 1 decimal place.
- **b** What is the median number of aces the player serves per match?
- c What is the range of this set of data?



- **14** The children playing in a room are aged 3, 7, 8 and 10 years.
 - **a** What is the mean of these ages?
 - **b** An adult enters the room and the mean age is doubled. How old is the adult?

Hint: You could guess the adult's age and find the mean. Keep adjusting your guess until you get the correct mean.

15



Statistical socce

15 A soccer goalkeeper records the number of saves he makes per game during a season. He presents his records in a table.

Number of saves	0	1	2	3	4	5
Number of games	4	3	0	1	2	2

- a In how many games did the keeper make 5 saves?
- **b** How many games did he play this season?
- c How many saves in total did he make this season?
- **d** What is the mean number of saves per game this goalkeeper made?
- What is the most common number of saves that he had to make during a game?
- **f** Do these statistics tell you whether the goalkeeper's team was good or bad? Why?

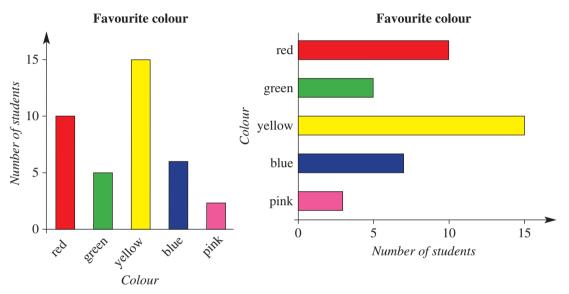


8C Dot plots and column graphs

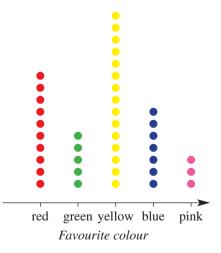
Learning intentions

- To understand that graphs should include titles and labelled axes which should be drawn to scale if they represent numeric data.
- To know what an outlier is.
- To be able to interpret a column graph and dot plot.
- To be able to construct a column graph and dot plot.
- Key vocabulary: dot plot, datum, column graph, axis, outlier

Graphs are a good way to illustrate data and highlight special information. For example, if students were surveyed on their favourite colours, the results could be shown as a column graph. The 'columns' can be vertical (going up) or horizontal (going across).



The data could also be shown in a dot plot (below).



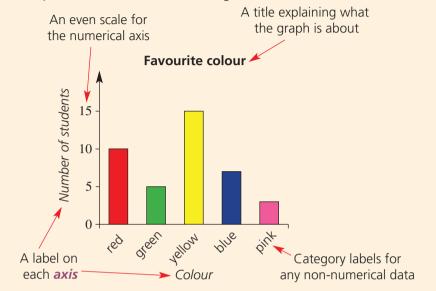
Lesson starter: Favourite colours

Survey the class to determine each student's favourite colour from the possibilities red, green, yellow, blue and pink.

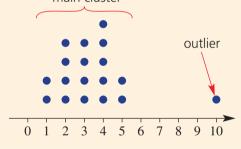
- Each student should draw a column graph or a dot plot to represent the results.
- Compare your graph with those of other students. Describe any differences you notice.



- A **dot plot** is a graph that can be used to display data, where each dot represents one **datum**.
- A column graph is a good way to show data in different categories, and is useful when more than a few items of data are present. Column graphs can be drawn vertically (going up) or horizontally (going across).
- Graphs should have the following features:



An outlier is a value that is noticeably smaller or larger than the main cluster of points. main cluster



Exercise 8C

Understanding	1–3	2, 3

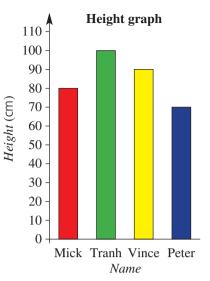
- 1 Fill in the blanks in the following sentences.
 - **a** A ______ is a graph which uses dots to represent data.
 - **b** A graph showing data in different categories as rectangles is called a _____
 - **c** An _____ is a value that is noticeably smaller or larger than the main cluster of points.

3C

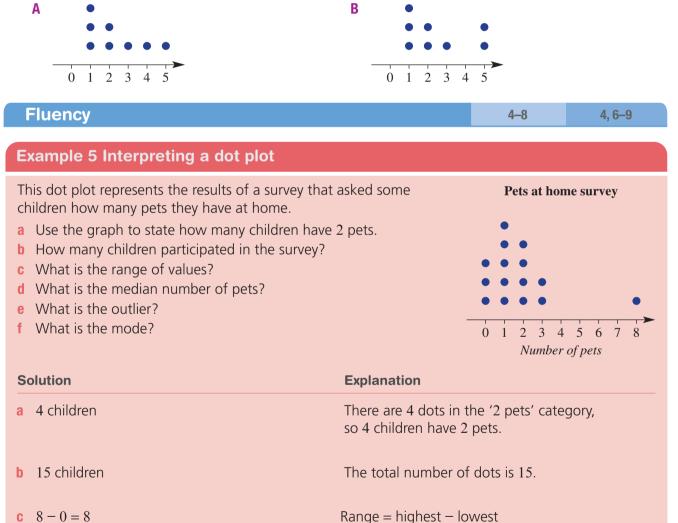
2

This column graph shows the height of four boys.

- Answer true or false to each of the following statements.
- a Mick is 80 cm tall.
- **b** Vince is taller than Tranh.
- **c** Peter is the shortest of the four boys.
- d Tranh is 100 cm tall.
- e Mick is the tallest of the four boys.



3 Which dot plot describes the data 1, 1, 1, 2, 2, 3, 5, 5?

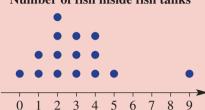


In this case, highest = 8, lowest = 0.

d 1 pet	Write the values in order:
	0, 0, 0, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 3, 3, 8
	Middle value = median = 1
e 8 pets	The main cluster of values is from 0 pets to 3 pets. The dot showing 8 pets is significantly outside this cluster.
f 1 pet	The most common number of pets is 1 pet.
Now you try	
This dot plot represents the number of fish insid	e a number of Number of fish inside fish tanks

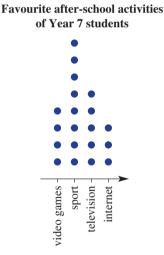
fish tanks in a shop.

- a How many tanks have 3 fish?
- **b** How many tanks in the shop were surveyed?
- **c** What is the range of values?
- **d** What is the median number of fish?
- е What is the outlier?
- What is the mode. f

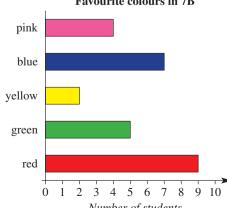


Number of fish

- 4 The favourite after-school activity of a number of Year 7 students is recorded in this dot plot.
 - a How many students have chosen television as their favourite activity?
 - **b** How many students have chosen surfing the internet as their favourite activity?
 - **c** What is the most popular after-school activity for this group of students?
 - **d** How many students participated in the survey?

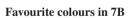


- **5** From a choice of pink, blue, yellow, green or red, each student of Year 7B chose their favourite colour. The results are graphed here.
 - a How many students chose yellow?
 - **b** How many students chose blue?
 - What is the most popular colour? С
 - **d** How many students participated in the class survey?



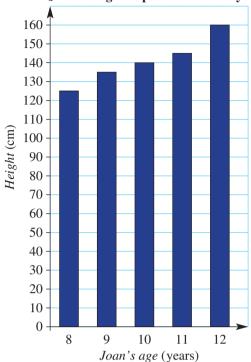
Number of students

Favourite colour



8C

6 Joan has graphed her height at each of her past five birthdays.

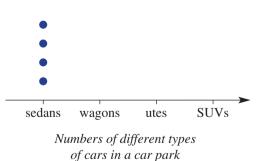


Joan's height at past five birthdays

- a How tall was Joan on her 9th birthday?
- **b** How much did she grow between her 8th birthday and 9th birthday?
- c How much did Joan grow between her 8th and 12th birthdays?
- d How old was Joan when she had her biggest growth spurt?
- 7 The types of cars parked in a small car park were:

Sedan	Wagon	Ute	SUV	
4	1	2	3	

- a How many utes were in the car park?
- **b** Copy and complete the dot plot.





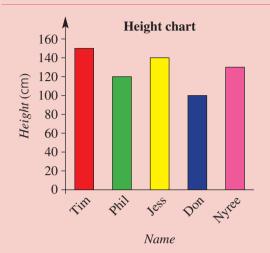
Hint: There should be 10 dots in total.

Example 6 Constructing a column graph

Draw a column graph to represent the following people's heights.

Name	Tim	Phil	Jess	Don	Nyree
Height (cm)	150	120	140	100	130

Solution



Explanation

First decide which scale goes on the vertical axis. Maximum height = 150 cm, so axis goes from 0 cm to 160 cm (to allow a bit above the highest value).

Remember to include all the features required, including labels on each axis and a graph title.

Now you try

Draw a column graph to represent the following test scores.

Name	Jack	Hugh	Cameron	Juliane
Score	90	84	62	78

- 8 Draw a column graph to represent each of these boys' heights at their birthdays.
 - a Mitchell

Age (years)	Height (cm)
8	120
9	125
10	135
11	140
12	145

b Fatu

Age (years)	Height (cm)
8	125
9	132
10	140
11	147
12	150

- **9** The ages (in years) of children at a party were: 7, 10, 8, 11, 8, 7, 9, 10, 12, 8.
 - **a** Represent this as a dot plot.
 - **b** What is the range of the ages?

Hint: The scale on your vertical axis could go 0, 10, 20 ... 150.





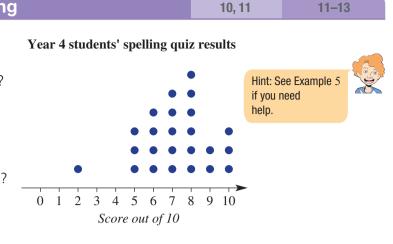
Hint: Range = largest - smallest.



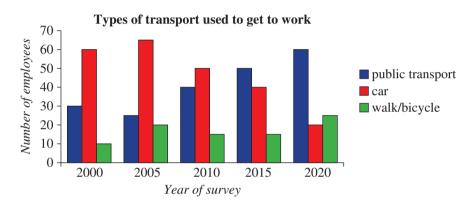
8C

Problem-solving and reasoning

- **10** The results of a Year 4 spelling quiz are shown as a dot plot.
 - a How many students got a score of 6?
 - **b** What is the most common score in the class?
 - **c** How many students participated in the quiz?
 - d What is the range of scores achieved?
 - e What is the median score?
 - f Identify the outlier.



11 Every five years, a company in the city conducts a transport survey of the way people get to work in the mornings. The results are graphed below.



- a Copy and complete this table to show the data in the graph.
- **b** In which year(s) was public transport the most popular option?

	2000	2005	2010	2015	2020
Use public transport	30				
Drive a car	60				
Walk or cycle	10				

- **c** In which year(s) were more people walking or cycling to work than driving?
- **d** Suggest one reason why the number of people driving to work has decreased.
- e What is one other trend that you can see from looking at this graph?

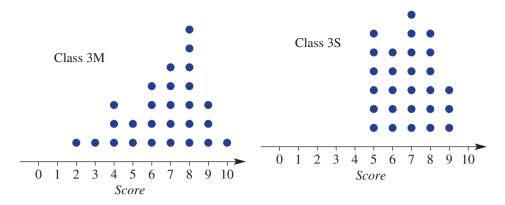


12 a Draw a column graph to show the results of the following survey of the number of boys and girls born at a certain hospital. Put the years on the horizontal axis.

	2012	2013	2014	2015	2016	2017
Number of boys born	40	42	58	45	30	42
Number of girls born	50	40	53	41	26	35

- **b** During which year(s) were more girls born than boys?
- c Which year had the smallest number of births?
- d Which year had the greatest number of births?
- e During the time of the survey, were more boys or girls born?

13 Mr Martin and Mrs Stevensson are the two Year 3 teachers at a school. For the latest arithmetic test, they plotted their students' scores on dot plots.



- a What is the median score for class 3M?
- **b** What is the median score for class 3S?
- c State the range of scores for each class.
- d Based on this test, which class has a greater spread of arithmetic abilities?
- e If the two classes competed in an arithmetic competition where each class is allowed only one representative, which class is more likely to win? Why?



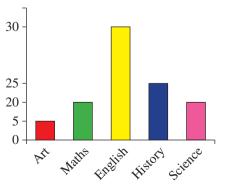
Misleading graphs

- **14** A survey is conducted of students' favourite subjects. Someone has tried to show the results in a column graph.
 - a What is wrong with the scale on the vertical axis?
 - **b** Give at least two other problems with this graph.
 - c Redraw the graph with an even scale and appropriate labels.
 - **d** The original graph makes Maths look twice as popular as Art, based on the column size. According to the survey, how many times more popular is Maths?
 - e The original graph makes English look three times more popular than Maths. From the survey, how many times more popular is English?
 - **f** Look in a newspaper or magazine for a graph with an uneven scale that makes the graph misleading.

Hint: Check the **Key ideas** to see what features graphs should show.

14





8D Line graphs

Learning intentions

- To understand that a line graph can be created with continuous numerical data.
- To be able to draw a line graph.
- To be able to use a line graph to estimate values.
- To be able to interpret a travel graph.

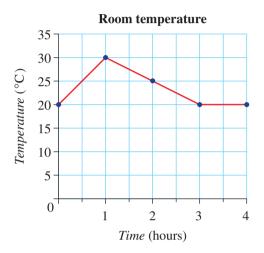
Key vocabulary: line graph, travel graph, continuous numerical

Line graphs can be used to show how quantities change over time. They clearly show trends in data over time.

Lesson starter: Room temperature

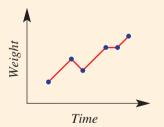
In an experiment, the temperature in a room is measured hourly over 4 hours. The results are shown in this line graph.

- Describe the temperature changes over the four hours.
- An air conditioner was turned on at some stage. When do you think this happened? Why?
- What was the approximate temperature 90 minutes (1.5 hours) after the experiment started?

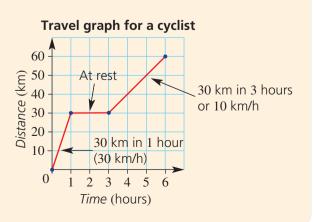


Key ideas

- A line graph is a graph that consists of a series of points joined by line segments.
- Time is often shown on the horizontal axis. For example:



- A common type of line graph is a **travel graph**.
 - Time is shown on the horizontal axis.
 - Distance is shown on the vertical axis.
 - The slope of the line shows the rate at which the distance is changing over time. This rate is called speed.

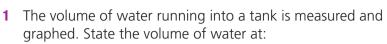


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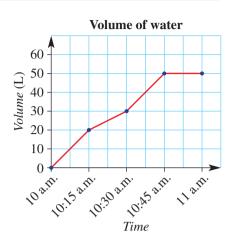
2.3

Exercise 8D

Understanding

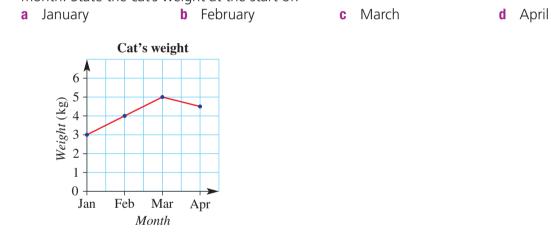


- **a** 10:15 a.m.
- **b** 10:30 a.m.
- **c** 10:45 a.m.
- **d** 11 a.m.



1-3

2 This line graph shows the weight of a cat over a 3-month period. The cat is weighed at the start of each month. State the cat's weight at the start of:



- **3** State the missing words.
 - a On a travel graph, distance is usually on the _____ axis.
 - **b** On a travel graph, time is usually on the _____ axis.

Fluency

Example 7 Drawing a line graph

The temperature in a room is noted at hourly intervals.

Time	9 a.m.	10 a.m.	11 a.m.	midday	1 p.m.
Temperature (°C)	10	15	20	23	18

a Draw a line graph of the temperature from 9 a.m. until 1 p.m.

b Use your graph to estimate the room temperature at 12:30 p.m.

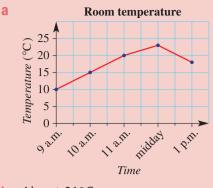
Continued on next page

4–8

4-8

8D

Solution



Explanation

- The vertical axis is from 0 to 25. The scale is even (i.e. increasing by 5 each time).
- Dots are placed for each measurement and joined with straight-line segments.

Look at the graph halfway between midday and

1 p.m. and form an estimate.

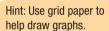
b About 21°C

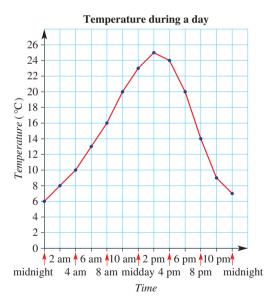
Now you try

The volume of water in a pond is noted at hourly intervals.

Time	1 p.m.	2 p.m.	3 p.m.	4 p.m.	5 p.m.	6 p.m.
Volume (L)	200	180	120	100	150	240

- a Draw a line graph of the volume from 1 p.m. to 6 p.m.
- **b** Use your graph to estimate the volume at 4:30 p.m.
- 4 A dog is weighed over a period of 3 months. Draw a line graph of its weight. January: 5 kg, February: 6 kg, March: 8 kg, April: 7 kg.
- **5** This graph shows the outside temperature over a 24-hour period that starts at midnight.
 - a What was the temperature at midday?
 - **b** When was the hottest time of the day?
 - **c** When was the coolest time of the day?
 - **d** Use the graph to estimate the temperature at these times of the day.
 - i 4 a.m.
 - **ii** 9 a.m.
 - iii 1 p.m.
 - iv 5 p.m.





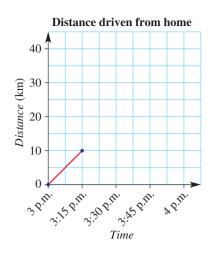
6 Oliver measures his pet dog's weight over the course of a year. He gets the following results.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Weight (kg)	7	7.5	8.5	9	9.5	9	9.2	7.8	7.8	7.5	8.3	8.5

- a Draw a line graph showing this information, making sure the vertical axis has an equal scale from 0 kg to 10 kg.
- **b** Describe any trends or patterns that you see.
- **c** Oliver put his dog on a weight-loss diet for a period of 3 months. When do you think the dog started the diet? Justify your answer.

7 This table shows how far Aisha has driven over the course of an hour. Copy and complete the travel graph.

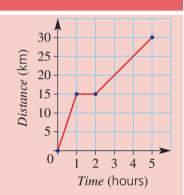
Time	Distance (km) from home
3 p.m.	0
3:15 p.m.	10
3:30 p.m.	15
3:45 p.m.	25
4 p.m.	30



Example 8 Interpreting a travel graph

This travel graph shows the distance travelled by a cyclist over 5 hours.

- a How far did the cyclist travel in total?
- **b** How far did the cyclist travel in the first hour?
- **c** What is happening in the second hour?
- d When is the cyclist travelling the fastest?
- e In the fifth hour, how far does the cyclist travel?

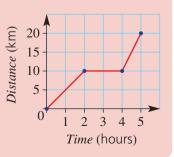


Solution	Explanation
a 30 km	The point at the right-hand end of the graph is (5, 30).
b 15 km	At time = 1 hour, the distance covered is 15 km.
c At rest	The distance travelled does not increase in the second hour.
d In the first hour	This is the steepest part of the graph.
e 5 km	In the last 3 hours, the distance travelled is 15 km, so in 1 hour, 5 km is travelled.

Now you try

This travel graph shows the distance travelled by a cyclist over 5 hours.

- a How far did the cyclist ride in total?
- **b** How far did the cyclist ride in the second hour?
- c During which hour did the cyclist ride the fastest?
- d For how long did the cyclist rest?



- **8D**
- 8 This travel graph shows the distance travelled by a van over 6 hours.
 - a How far did the van travel in total?
 - **b** How far did the van travel in the first hour?
 - c What is happening in the fourth hour?
 - **d** When is the van travelling the fastest?
 - e In the sixth hour, how far does the van travel?

Problem-solving and reasoning

- **9** The graph shows water storage levels for a certain city.
 - a What was the water level at the start of:
 - i January?
 - ii May?
 - iii December?
 - b Which month do you think had the highest rainfall? Why?
 - c What was the maximum water level?
 - d When did the water storage get to its lowest point?

b

10 Draw travel graphs to illustrate the following journeys.

a A car travels:

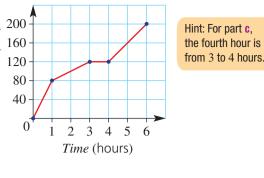
•

- 120 km in the first 2 hours
 - 0 km in the third hour
- 60 km in the fourth hour
- 120 km in the fifth hour
- 12 km in the first hour

A jogger runs:

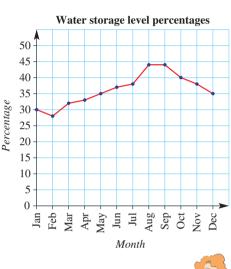
Distance (km)

- 6 km in the second hour
- 0 km in the third hour
- at a rate of 6 km per hour for 2 hours

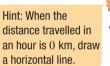




9,10



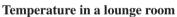
9

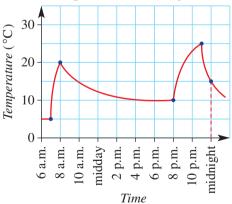


11

Heating and cooling

- **11** The temperature in a lounge room is measured several times on a particular day. The results are shown in a line graph.
 - a State the room's temperature at:
 - **i** 6 a.m. **ii** 8 a.m. **iii** 10 a.m. **iv** 8 p.m.
 - **b** Twice during the day the heating was switched on. At what times do you think this happened? Explain your reasoning.
 - **c** When was the heating switched off? Explain your reasoning.
 - **d** The house has a single occupant who works during the day. Describe when you think that person is:
 - i waking up
- ii going to work
- iii coming home iv going to bed
- e These temperatures were recorded during a cold winter month. Draw a graph that shows what the lounge room temperature might look like during a hot summer month. Assume that the room has an air conditioner which the person is happy to use when at home.





tentago

8E Stem-and-leaf plots

Learning intentions

- To be able to interpret a stem-and-leaf plot.
- To be able to represent data in a stem-and-leaf plot.

Key vocabulary: stem-and-leaf plot, stem, leaf, key

A stem-and-leaf plot is a useful way of presenting numerical data.		Stem	Leaf
It allows trends to be spotted easily. Each number is split into a stem	53 is	5	3
(the first digit or digits) and a leaf (the last digit).	78 is	7	8
	125 is	12	5

Lesson starter: Test score analysis

In a class, students' results on two recent tests out of 50 are recorded.

Test 1 results
43, 47, 50, 26, 38, 20, 25, 20, 50, 44,
33, 47, 47, 50, 37, 28, 28, 22, 21, 29

Test 2 results									
Stem									
1	8								
2	78								
3	2 2 4 5 5 7 9								
4	0 1 2 3 3 6 8 8								
5	8 7 8 2 2 4 5 5 7 9 0 1 2 3 3 6 8 8 0 0								

- For each test, try to find how many students:
 - achieved a perfect score (i.e. 50)
 - failed the test (i.e. scored less than 25)
 - achieved a mark in the 40s.
- If there are 100 test results to analyse, would you prefer a list of results or a stem-and-leaf plot? Why?

Key ideas

- A **stem-and-leaf** plot is a way to display numerical data. It lists numbers in order, grouped in rows.
- Each number is split into a stem (the first digit or digits) and a leaf (the last digit). For example:

	Stem	Leaf
The number 7 is	0	7
The number 31 is	3	1
The number 152 is	15	2
	Key 3	11 means 31

9

- A **key** is added to the **plot** to show the value of the stem and leaf. For example: 3 | 1 means 31 or 2 | 7 means 2.7.
- Leaves are aligned vertically, getting bigger as you move away from the stem.
- A space is used to separate each leaf value. Commas are not used between leaves. E.g.

Exercise 8E

	Understanding	1–4	4
--	---------------	-----	---

- 1 Copy and complete: In a stem-and-leaf plot the first digit(s) of a data value is called the ______ and the last digit is called the _____.
- 2 The number 52 is entered into a stem-and-leaf plot.
 - **a** Which digit is the stem?
 - **b** Which digit is the leaf?
- What number is represented by the following combinations if the digit on the right represents ones?
 a 3|9
 b 2|7
 c 13|4
- 4 In this stem-and-leaf plot, the smallest number is 35. What is the largest number?

Stem	Le	eaf		
3	5	7	7	9
4	2	8		
5	1	7		

Fluency		5–9	5–9
Example 9 Interpreting a stem-and-leaf p	olot		
 Average daily temperatures are shown for some different countries. a Write out the temperatures as a list. b How many countries' temperatures are represent c What are the maximum and minimum temperat d What is the range of temperatures recorded? e What is the median temperature recorded? 	ted? 3	Leaf 3 6 6 0 0 1 2 5 0 2 5 means 25°C	5 6 8 9
Solution	Explanation		
a 13, 16, 16, 20, 20, 21, 22, 25, 25, 26, 28, 29, 30, 32	Each number is conv leaf to a single numl For example, 1 3 is o	per.	
b 14	The easiest way is to leaves – each leaf co		
c Minimum = 13°C Maximum = 32°C	The first stem and le The last stem and lea	•	

d Range = 19° C

e Median = 23.5° C

Range = maximum - minimum = 32 - 13 = 19

The middle value is halfway between the numbers 2 | 2 and 2 | 5, so median = $\frac{1}{2}(22+25) = 23.5$

Now you try

The length of holidays, in days, was recorded from a number of people	Stem	Leaf
who had recently been away.	0	2 4 5 7 8
a How many people were surveyed?		0 1 2 5 9
b What are the maximum and minimum holiday lengths?		2
c What was the range of holiday length?		3 means 23 days
d What was the median holiday length?	2	5 means 25 days

- **5** This stem-and-leaf plot shows the ages of people in a group.
 - **a** Write out the ages as a list.
 - **b** How many ages are shown?
 - **c** Answer true or false to each of the following.
 - i The youngest person is aged 10.
 - ii Someone in the group is 17 years old.
 - iii Nobody listed is aged 20.
 - iv The oldest person is aged 4.

- Stem
 Leaf

 0
 8 9

 1
 0 1 3 5 7 8

 2
 1 4

 1|5 means 15 years old
- 6 For each of the stem-and-leaf plots below, state the range and the median. (See Example 10 parts d and e.)

а	Stem	Leaf	b	Stem	Leaf	C	Stem	Leaf
	0	9		1	1 4 8	-	3	1 1 2 3 4 4 8 8 9
	1	3567789		2	124468		4	0 1 1 2 3 5 7 8
	2	019		3	03479		5	0 0 0
	1 8	means 18		4	2		4 7	means 47
				3 4	means 34			

7 Copy and complete the stem-and-leaf plot for this set of data. 25, 27, 29, 30, 32, 39, 41, 42, 45, 51

Stem	Leaf		
2			1
3		Hint: Remember to list the	
4		leaves in increasing order	
5		across each row.	

8E

Example 10 Creating a stem-and-leaf plot

Represent this set of data as a stem-and-leaf plot: 23, 10, 36, 25, 31, 34, 34, 27, 36, 37, 16, 33

Solution	Explanation
Sorted list: 10, 16, 23, 25, 27, 31, 33, 34, 34, 36, 36, 37	Sort the list in increasing order so that it can be put directly into a stem-and-leaf plot.
Stem Leaf 1 0.6 2 3.5 7 3 1.3 4 4 6 6 7	Split each number into a stem and a leaf. Stems are listed in increasing order. Leaves are written vertically, listed in increasing order across each row.
2 5 means 25	A key is included as an example of how to combine a stem and a leaf.

Now you try

Represent this set of data as a stem-and-leaf plot: 43, 13, 18, 22, 37, 54, 49, 42, 27, 25, 15, 32

- 8 Show each of the following sets of data as a stem-and-leaf plot.
 - **a** 11, 12, 13, 14, 14, 15, 17, 20, 24, 28, 29, 31, 32, 33, 35
 - **b** 32, 27, 38, 60, 29, 78, 87, 60, 37, 81, 38, 11, 73, 12, 14

Show each of the following sets of data as a stem-and-leaf plot. 9

- **a** 80, 84, 85, 86, 90, 96, 101, 104, 105, 110, 113, 114, 114, 115, 119
- **b** 401, 420, 406, 415, 416, 406, 412, 402, 409, 418, 404, 405, 391, 411, 413, 413, 408, 395, 396, 417

Problem-solving and reasoning

10 A company recorded the duration (in seconds) that visitors spent on its website's home page.

> 00128 2 279 3 4 5 8 2 | 7 means 27 seconds

Leaf

24689

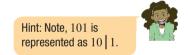
a How many visitors spent less than 20 seconds on the home page?

Stem

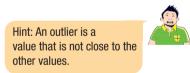
0

1

- **b** How many visitors spent more than half a minute?
- **c** How many visitors spent between 9 and 30 seconds?
- d What is the outlier for this stem-and-leaf plot?



10, 11



10

11 A teacher has compiled test scores out of 50 as a stem-and-leaf plot. However, some values are missing, as represented by the letters *a*, *b*, *c* and *d*.

Stem	Leaf
1	5
2	45 <i>a</i> 679
3	<i>b</i> 0 1 5
4	28 c
5	d
3 5	5 means 35

a How many students took the test?

7655441

9320

- **b** How many students passed the test (i.e. achieved a mark of 25 or higher)?
- **c** State the possible values for each of the missing digits *a* to *d*.

Back-to-back stem-and-leaf plots 12 **12** Two radio stations poll their audience to determine their ages. Hint: The leaves for Station 1 Stem Station 2 station 1 are read in reverse 0 1 23345689 8 7 2 means 27 and 28. 8 7 2 00124588 975433 3 112



- **a** Find the age difference between the oldest and youngest listener polled for:
 - i station 1 ii station 2

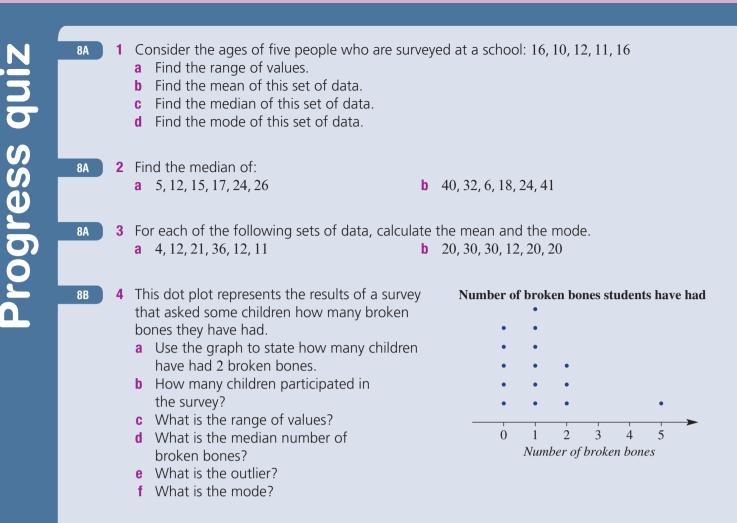
8

4

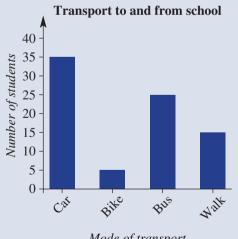
5

- **b** One radio station plays modern music that appeals to teenagers. The other plays classical music and broadcasts the news. Which radio station is most likely to be the one that plays classical music and news?
- **c** Advertisers want to know the age of the stations' audiences. This lets them target their advertisements more effectively (e.g. to 38 to 58 year olds). Give a 20-year age range for the audience majority who listen to:
 - i station 1 ii station 2





5 A survey was conducted of all the Year 7 students at Brimbrook Secondary College in regards to how they generally commuted to and from school. The answers to the survey are shown in the following column graph.



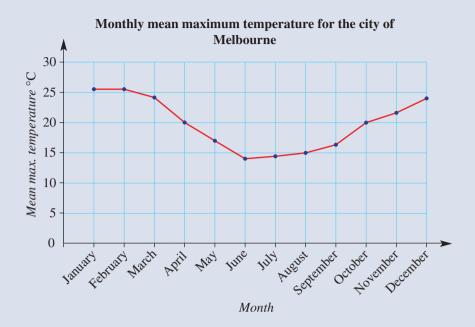
Mode of transport

- a How many students were surveyed?
- **b** Write the four modes of transport in order from most common to least common.
- c How many more students travelled by bus rather than walked?

Essential Mathematics for the Victorian Curriculum CORE Year 7

8B

6 The line graph shows the monthly mean maximum temperature, rounded to the nearest whole number, for the city of Melbourne.



- Which months have a mean maximum temperature above 25°C? а
- What is the range of monthly mean maximum temperatures? b
- How much cooler is the mean maximum temperature in May than October? C
- What is the average mean maximum temperature for the year? Give your answer rounded to d the nearest whole number.
- 7 The amount of time (in minutes) students spent completing Maths homework on a particular night is represented in the following stem-and-leaf plot.

Stem	Leaf
1	257
2	11245788
3	0036
2 4	means 24 minutes

- Write out the times as a list. а
- How many students were surveyed? b
- What are the maximum and minimum times spent completing Maths homework? C
- What is the range of times spent completing Maths homework? d
- What is the median time spent completing Maths homework? e
- 8 Show the following set of data as a stem-and-leaf plot: 57, 63, 60, 71, 78, 60, 54, 59, 74, 69, 68, 65, 66, 60, 73, 86

8D

8D

80

Essential Mathematics for the Victorian Curriculum CORE Year 7

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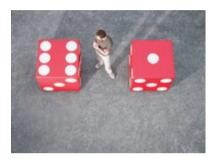
8F Describing chance

CONSOLIDATING

Learning intentions

- To understand that we can describe the likelihood of events using phrases such as 'even chance', 'unlikely' and 'certain'.
- To be able to describe the likelihood of an event.
- Key vocabulary: chance, 'even chance', equally likely

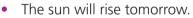
There may be times when you want to describe how likely it is that a certain event will occur. For example, how likely is your sporting team to win this year's premiership? Or how likely is it that you will receive a total of 12 from rolling two dice? Probability is the study of chance.



Lesson starter: Likely or unlikely?

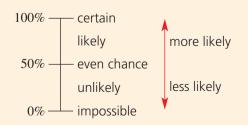
Try to rank these events from least likely to most likely. Compare your answers with other students in the class.

- It will rain tomorrow.
- Australia will win the soccer World Cup.
- Tails will land on top when a 20-cent coin is tossed.
- The king of spades is at the top of a shuffled deck of 52 playing cards.
- A diamond card is at the bottom of a shuffled deck of 52 playing cards.



Key ideas

- Chance is the likelihood of an event happening.
- There are a number of words and phrases we can use to describe chance.



If two events have the same chance of occurring, we say they are **equally likely**.



Exercise 8F

Exercise or			
Understanding		1, 2	2
 Fill in each blank with the word <i>likely</i> or a A fair coin is flipped 100 times. It is A page of this book is picked at rando C The television is switched on at 5 p.m be shown at some stage. d It is that the next Austral 	that there will be om. It is that the . and left on for 3 hours. It is	e letter 'e' will k t	
 2 Match each of the events (a to d) with a c a A tossed coin landing heads up b Selecting an ace first try from a fair de c Obtaining a number other than 6 if a d Obtaining a number greater than 8 if 	eck of 52 playing cards fair 6-sided die is rolled	are to occur (A A Unlik B Likely C Impo D Even	ely / ssible
Fluency		3–6	3–7
Example 11 Describing chance			
Say whether each of the following statement a It is likely that children will go to school of b It is an even chance for a fair coin to disp c Rolling a 3 on a 6-sided die and getting h d It is certain that two randomly chosen of	next year. blay tails. neads on a coin are equally lik	-	
Solution	Explanation		
a True	Although there is pe the laws might chan children will go to sc	ge, it is (very) l	ikely that
b True	There is a $50-50$ or e	even chance of	a fair coin

of the time.

a 6-sided die.

Now you try

c False

d True

Say whether each of the following statements is true or false.

- **a** It is unlikely that it will rain again this year.
- **b** There is an even chance of getting an odd number on a 6-sided die.
- **c** It is impossible to roll two 4's if tossing a 6-sided die twice.
- d Rolling a 2 and rolling a 6 on a 6-sided die are equally likely.

displaying tails. It will happen, on average, half

heads on a coin is more likely than rolling a 3 on

No matter what odd numbers are chosen, they

These events are not equally likely. Flipping

will always add to an even number.

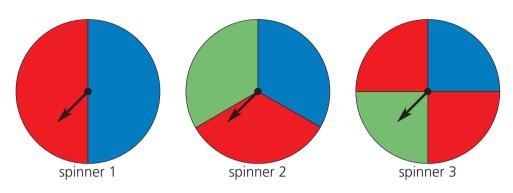
- Consider a fair 6-sided die with the numbers 1 to 6 on it. Say whether each of the following is true or false.
 - a Rolling a 3 is unlikely.
 - **b** Rolling a 5 is likely.
 - **c** Rolling a 4 and rolling a 5 are equally likely events.
 - d Rolling an even number is likely.
 - e There is an even chance of rolling an odd number.
 - **f** There is an even chance of rolling a multiple of 3.
- Copy and complete the following, using the special words that describe chance.
 - a If an event is guaranteed to occur, we say it is
 - b An event that is equally likely to occur or not occur has an
 - **c** A rare event is considered .
 - d An event that will never occur is called .
- 5 Match each of the events (a to d) with an equally likely event (A to D).
 - a Rolling a 2 on a 6-sided die
 - **b** Selecting a heart card from a fair deck of 52 playing cards

 - d Rolling a 1 or a 5 on a 6-sided die
- **A** Flipping a coin and heads landing face up
 - **B** Rolling a 5 or a 6 on a 6-sided die
- **c** Flipping a coin and tails landing face up **C** Selecting a diamond card from a fair deck of 52 playing cards
 - **D** Rolling a 4 on a 6-sided die
- **6** Give an example of:
 - **a** an event that is unlikely
 - c an event that has an even chance of occurring
- **b** an event that is likely
- **d** two events that are equally likely
- 7 This spinner could land with the arrow pointing to any of the three colours.
 - **a** State whether each of the following is true or false.
 - i There is an even chance that the spinner will point to green.
 - ii It is likely that the spinner will point to red.
 - iii It is certain that the spinner will point to purple.
 - iv It is equally likely that the spinner will point to red or blue.
 - **b** Use the spinner to give an example of:
 - i an impossible event
 - ii a likely event
 - **iii** a certain event
 - iv two events that are equally likely

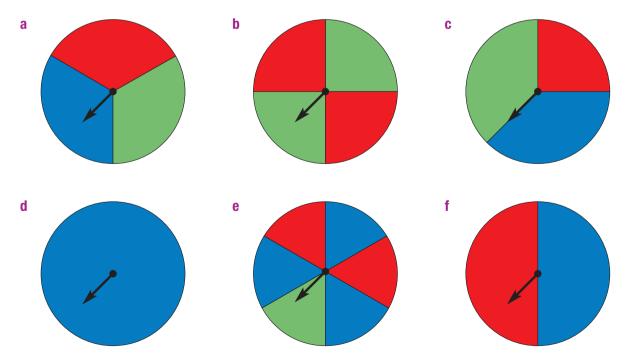


Hint: Choose from the words even chance, impossible, certain, unlikely





- a Has an even chance of red, but blue is unlikely.
- **b** Blue and green are equally likely, but red is unlikely.
- c Has an even chance of blue, and green is impossible.
- **9** Draw spinners to match each of the following descriptions.
 - **a** Blue is likely, red is unlikely and green is impossible.
 - **b** Red is certain.
 - c Blue has an even chance, red and green are equally likely.
 - d Blue, red and green are all equally likely.
- **10** For each of the following, describe the chances involved so that someone else could draw the spinner. Use colour names and the language of chance (e.g. *likely*, *impossible*) in your descriptions.



Essential Mathematics for the Victorian Curriculum CORE Year 7

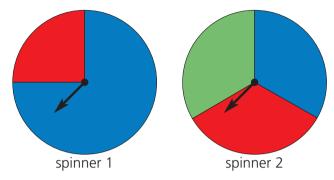
Hint: Blue, red and green are the only possible colours.

8F

Spinner fractions

11 The language of chance is a bit vague. For example, for both of the following spinners it is 'unlikely' that you will spin red, but in each case the chance of spinning red is different.

11



Rather than describing chance in words, we could consider the fraction of the spinner for a certain colour.

- a What fraction of spinner 1 is red?
- **b** What fraction of spinner 2 is red?
- c What fraction of a spinner would be red if red had an even chance?
- **d** Draw spinners for which red makes up:
 - i 100% of the spinner
 - ii 0% of the spinner
- **e** For the sentences below, fill each gap with an appropriate fraction or percentage value.
 - i You have an even chance of spinning a certain colour if it makes up ______ of the total spinner.
 - ii It is impossible to spin a certain colour if it makes up _____% of the total spinner.
 - iii You are unlikely to spin a certain colour if it makes up more than ______ but less than ______ of the total area.
 - iv You are likely to spin a certain colour if it makes up more than ______ of the total area.
- f How can the fractions help determine if two events are equally likely?



8G Theoretical probability

Learning intentions

- To understand that the probability of an event is a number between 0 and 1 inclusive, representing the chance the event will occur.
- To be able to calculate the probability of simple events.

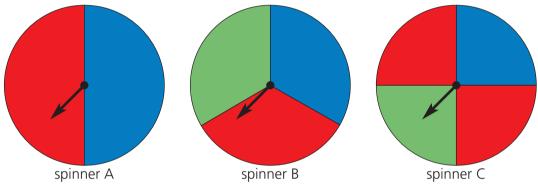
Key vocabulary: experiment, trial, outcome, event, probability, sample space, fraction, decimal, percentage

The theoretical probability of an event is the chance that it will happen. This chance is worked out mathematically.

Probabilities are numbers from 0 (impossible) to 1 (certain). They can be written as fractions, decimals or percentages. The larger the probability, the more likely the event will occur.

Lesson starter: Spinner probabilities

Consider these three spinners.



- Describe the differences between the spinners.
- What is the probability of spinning blue for each of these spinners?
- What is the probability of spinning red for each of these spinners?

Key ideas

- A random **experiment** is a chance activity that produces varying results.
- A trial is a single component of an experiment, such as tossing a coin, rolling a die or spinning a spinner.
- An **outcome** is a possible result of an experiment, like rolling a 5 or a coin showing tails.
- An event is either a single outcome (e.g. rolling a 3) or a collection of outcomes (e.g. rolling a 3, 4 or 5).
- The probability of an outcome occurring, if all the outcomes are equally likely, is:

number of ways the outcome can occur total number of possible outcomes

• Probability is often written as a fraction, but it can be written as a decimal or as a percentage. For example: $\frac{1}{2}$ or 0.5 or 50%

- The **sample space** is the set of all possible outcomes of a trial.
- We write Pr(green) to mean 'the probability that a spinner shows green'.



Exercise 8G

Understanding		1–3	3
 1 Complete the following sentences. a The is the set of possible b An impossible event has a probability of c If an event has a probability of 1, then it is d The higher its probability, the likely the e Rolling a 7 on a standard die is f An event with a lower probability than another is 	 e event will oc		s, sample,
2 A fair coin is flipped. The probability of flipping tails is	. Write this pr	obability as:	
a a decimal b a percentage			
 3 Match up each event (a to d) with a set of possible oute a Tossing a coin b Rolling a die c Selecting a suit from a fair deck of 52 playing cards d Selecting a letter from the word POWER 	 A 1, 2, B P, O, C Head 	3, 4, 5, 6 W, E, R	ubs, spades
Fluency		4–6	4–7
Example 12 Calculating probability			
 A fair 6-sided die is rolled. a List the sample space. b Find the probability of rolling a 3, giving your answer a c Find the probability of rolling an even number, giving y d Find the probability of rolling a number less than 3, giv one decimal place. 	our answer as		age correct to
a Sample space = {1, 2, 3, 4, 5, 6} For t	ne sample spa	ce, we list all the	e possible
even	s using set bra		1
b $Pr(3) = \frac{1}{6}$ The e	vent can occu	r in one way (rol	lling a 3) out

- **c** Pr(even) = $\frac{1}{2} = 0.5$
- **d** Pr(less than 3) = $\frac{1}{3}$ = 33.3%

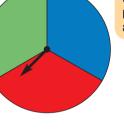
The event can occur in three ways (i.e. 2, 4 or 6). So the probability is $\frac{3}{6} = \frac{1}{2}$. As a decimal this is 0.5. The event can occur in two ways (1 or 2). So

the probability is $\frac{2}{6} = \frac{1}{3}$. As a percentage this is 33.3%, rounded to 1 decimal place.

Now you try

Consider a fair 6-sided die.

- a List the sample space.
- **b** List the odd numbers on the die.
- c State the probability of rolling an odd number.
- d State the probability of rolling a 5.
- 4 Consider the spinner shown.
 - a How many outcomes are there? List them.
 - **b** Find Pr(red). This means to find the probability of the spinner pointing to red.
 - **c** Find Pr(green).
 - d Find Pr(not red).
 - e Find Pr(yellow).
- 5 A spinner with the numbers 1 to 7 is spun. The numbers are evenly spaced.
 - a List the sample space.
 - **b** Find Pr(6) giving your answer as a fraction.
 - **c** Find Pr(8) giving your answer as a fraction.
 - **d** Find Pr(2 or 4) giving your answer as a fraction.
 - e Find Pr(even) giving your answer as a fraction.
 - f Find Pr(odd) giving your answer as a fraction.
 - **g** Give an example of an event having the probability of 1.
- 6 The letters in the word MATHS are written on 5 cards and then one is drawn from a hat.
 - a List the sample space.
 - **b** Find Pr(T), giving your answer as a decimal.
 - **c** Find Pr(A), giving your answer as a decimal.
 - **d** Find Pr(consonant is chosen), giving your answer as a decimal.
- 7 The letters in the word PROBABILITY are written on 11 cards and then one is drawn from a hat.
 - **a** Find Pr(P) giving your answer as a fraction.
 - **b** Find Pr(I) giving your answer as a fraction.
 - **c** Find Pr(letter chosen is in the word BIT) giving your answer as a fraction.
 - **d** Find Pr(not a B) giving your answer as a fraction.
 - e Find Pr(a vowel is chosen) giving your answer as a fraction.
 - **f** Give an example of an event with the probability of $\frac{3}{11}$.



Hint: Pr(not red) means the probability that the spinner's arrow does not point to red.



Hint: For part **b**, there are 2 cards out of 11 with the letter I.



CORE Year 7

8G

The whole numbers from 1 to 11 are written on 11 cards. If the cards are shuffled and one card is chosen

at random, which of the following outcomes is most likely?

Problem-solving and reasoning

- A Choosing a 5
- Choosing a two-digit number C
- 9 A bag of marbles contains 3 red marbles, 2 green marbles and 5 blue marbles. They are all equal in size and weight. A marble is chosen at random.
 - **a** What is the probability that a red marble is chosen?
 - **b** What is the probability that a blue marble is chosen?
 - **c** What is the probability that a green marble is *not* chosen?
- 10 A box contains different-coloured counters, with $Pr(purple) = \frac{1}{10}$, $Pr(yellow) = \frac{2}{3}$ and $Pr(orange) = \frac{1}{7}$.
 - **a** Is it possible to obtain a colour other than purple, yellow or orange? If so, state the probability.
 - **b** What is the minimum number of counters in the box?
 - c If the box cannot fit more than 1000 counters, what is the maximum number of counters in the box?
- Consider this spinner, numbered 2 to 9. 11
 - a List the sample space.
 - **b** Find the probability that a prime number will be spun, giving your answer as a decimal. (Remember that 2 is a prime number.)
 - **c** Giving your answers as decimals, state the probability of spinning a prime number if each number on the spinner is:
 - i increased by 1
 - i increased by 2
 - iii doubled
 - Design a new spinner for which Pr(prime) = 1. d



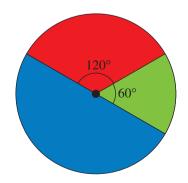
- **12** a State the probability of spinning green with this spinner.
 - For each of the following, design a spinner using only red, green and b blue sectors to obtain the desired probabilities. If it cannot be done, then explain why not.
 - $Pr(red) = \frac{1}{2}$, $Pr(green) = \frac{1}{4}$, $Pr(blue) = \frac{1}{4}$
 - ii $Pr(red) = \frac{1}{2}$, $Pr(green) = \frac{1}{2}$, $Pr(blue) = \frac{1}{2}$
 - iii $Pr(red) = \frac{1}{4}$, $Pr(green) = \frac{1}{4}$, $Pr(blue) = \frac{1}{4}$
 - iv Pr(red) = 0.1, Pr(qreen) = 0.6, Pr(blue) = 0.3

Hint: The probability of choosing red is not $\frac{1}{2}$ because the colours are not equally likely.

B Choosing an even number

D Choosing an odd number





12



8H Experimental probability 📩

Learning intentions

- To be able to find the experimental probability of an event given experimental results.
- To understand how experimental probability is related to the theoretical probability of an event for a large number of trials.
- To be able to find the expected number of occurrences.

Key vocabulary: experiment, expected number, trials, theoretical probability, experimental probability

If the probability of an event is unknown, experimental results can help to give you an idea of that probability. For example, when flipping a coin, the theoretical probability of it landing on heads is $\frac{1}{2}$. If you suspect

that the coin is not fair, you could run an experiment and use the results to estimate the experimental probability of heads.

The more trials (flips) you use in your experiment, the more likely you are to get a good estimate of the probability of heads.



Solution Lesson starter: Tossing coins

For this experiment, each class member needs a fair coin that they can toss.

- Each student should toss the coin 20 times and count how many times heads occurs.
- Tally the total number of heads obtained by the class.
- How close is this total number to the number you would expect that is based on the theoretical probability
 of ¹/₂? Discuss what this means.

Key ideas

The experimental probability of an event based on a particular experiment is:

number of times the event occurs total number of **trials** in the experiment

- The expected number of occurrences = probability × number of trials
- If the number of trials is large, then the experimental probability is likely to be close to the actual theoretical probability.

Exercise 8H

	Jnderstanding			1–2	2
	Which of the following experime A Flipping it once	B Flipping it twice		vas fair? Flipping it 20 t	imes
2	A coin is flipped and the results a	are:			
	00000)(2)(2)(2)(2)(
	a How many times did the coin		ALL DO		
	b How many times did the coinc How many times was the coi				
	Fluency			3–8	4–9
Ε	xample 13 Working with ex	perimental probability			
M	/hen using a spinner numbered 1	to 4, the following numbers	come up		
1,	4, 1, 3, 3, 1, 4, 3, 2, 3.	hility of actting 2.22			
a b	What is the experimental proba What is the experimental proba	, , ,	ber?		
S	olution	Explanatio	on		
а	$\frac{2}{5}$ or 0.4 or 40%	_number of	$\frac{1}{2} = \frac{4}{2}$	$\frac{1}{2} = \frac{2}{2}$	
	5	number of	f trials 1	0 5	
		number of	even resu	Ilts3_	
h	3	number of		$-\frac{-10}{10}$	
b	$\frac{3}{10}$	number of number	r of trials	10	
		number	r of trials	10	
N	ow you try				
N		es, the following numbers co			
N	ow you try /hen tossing an 8-sided die 8 time	es, the following numbers co bility of getting a 3?	ome up: 7,		
N V\ a b	ow you try /hen tossing an 8-sided die 8 time What is the experimental proba What is the experimental proba	es, the following numbers co bility of getting a 3? bility of getting an odd numb	ome up: 7, ber?	2, 1, 8, 3, 3, 6, 5	
N V\ a	ow you try /hen tossing an 8-sided die 8 time What is the experimental proba What is the experimental proba A 6-sided die is rolled 10 times a 1, 6, 4, 4, 3. Find the experimenta	es, the following numbers co bility of getting a 3? bility of getting an odd numb nd the following numbers co	ome up: 7, ber? ome up: 2	2, 1, 8, 3, 3, 6, 5 , 4, 6, 4, 5, Hint: For part c, count	: how many
N V\ a b	ow you try /hen tossing an 8-sided die 8 time What is the experimental proba What is the experimental proba A 6-sided die is rolled 10 times a 1, 6, 4, 4, 3. Find the experimenta a the number 3	es, the following numbers co bility of getting a 3? bility of getting an odd numb nd the following numbers co	ome up: 7, ber? ome up: 2	2, 1, 8, 3, 3, 6, 5 , 4, 6, 4, 5,	: how many
N V\ a b	ow you try /hen tossing an 8-sided die 8 time What is the experimental probal What is the experimental probal A 6-sided die is rolled 10 times a 1, 6, 4, 4, 3. Find the experimenta a the number 3	es, the following numbers co bility of getting a 3? bility of getting an odd numb nd the following numbers co	ome up: 7, ber? ome up: 2	2, 1, 8, 3, 3, 6, 5 , 4, 6, 4, 5, Hint: For part c, count	: how many
N W a b	ow you try /hen tossing an 8-sided die 8 time What is the experimental proba- What is the experimental proba- A 6-sided die is rolled 10 times a 1, 6, 4, 4, 3. Find the experimenta a the number 3 b the number 4 c an odd number When a coin is tossed 100 times,	es, the following numbers co bility of getting a 3? bility of getting an odd numb nd the following numbers co I probability of getting: , the results are 53 heads and	ome up: 7, ber? ome up: 2	2, 1, 8, 3, 3, 6, 5 , 4, 6, 4, 5, Hint: For part c, count	: how many
N W a b	ow you try /hen tossing an 8-sided die 8 time What is the experimental probal What is the experimental probal A 6-sided die is rolled 10 times a 1, 6, 4, 4, 3. Find the experimental a the number 3 b the number 4 c an odd number When a coin is tossed 100 times, a What is the experimental pro	es, the following numbers co bility of getting a 3? bility of getting an odd numb nd the following numbers co I probability of getting: , the results are 53 heads and bability of getting a head?	ome up: 7, ber? ome up: 2	2, 1, 8, 3, 3, 6, 5 , 4, 6, 4, 5, Hint: For part c, count	: how many
N M b	ow you try /hen tossing an 8-sided die 8 time What is the experimental proba- What is the experimental proba- A 6-sided die is rolled 10 times a 1, 6, 4, 4, 3. Find the experimenta a the number 3 b the number 4 c an odd number When a coin is tossed 100 times,	es, the following numbers co bility of getting a 3? bility of getting an odd numb nd the following numbers co I probability of getting: , the results are 53 heads and bability of getting a head? bability of getting a tail?	ome up: 7, ber? ome up: 2	2, 1, 8, 3, 3, 6, 5 , 4, 6, 4, 5, Hint: For part c, count	: how many

5 The table shows the results of spinning a spinner.

Colour	red	green	blue
Number of times	13	5	2

State the experimental probability of getting:

- a red b green c blue
- 6 A survey is conducted on people's television viewing habits.

Number of hours	0-5	5-10	10-20	20-30	30+
per week					
Number of people	20	10	15	5	0

- a How many people participated in the survey?
- **b** Find the probability that a randomly selected participant watches television for:
 - i less than 5 hours
 - ii 20–30 hours
 - iii between 5 and 20 hours

Example 14 Finding expected numbers

A spinner is found to land on red $\frac{1}{4}$ of the time. If it is spun 200 times, how many times would you expect it to land on red?

Solution	Explanation
50 times	Expected number = probability × number of trials = $\frac{1}{4} \times 200 = 50$

Now you try

A 4-sided die is rolled.

- a How many times would you expect it to show a 4 in 100 trials?
- **b** If it were rolled 20 times, explain how you could get an experimental probability of 0.4 for showing a 4.
- **c** If it were rolled 50 times, is it possible to roll 45 4s?

7 A fair coin is tossed.

- a How many times would you expect it to show tails in 1000 trials?
- **b** How many times would you expect it to show heads in 3500 trials?
- **c** You start by tossing the coin 10 times to find the probability of the coin showing tails.
 - i Explain how you could get an experimental probability of 0.7.
 - ii If you toss the coin 100 times, are you more or less likely to get an experimental probability close to 0.5?

8 A fair 6-sided die is rolled.

- a How many times would you expect to get a 3 in 600 trials?
- **b** How many times would you expect to get an even number in 600 trials?
- c If you roll the die 600 times, is it possible that you will get an even number 400 times?
- **d** Are you more likely to obtain an experimental probability of 100% from two rolls or to obtain an experimental probability of 100% from 10 rolls?

Hint: The theoretical probability of tails is $\frac{1}{2}$.



8H

9 The colour of the cars in a school car park is recorded.

Colour	red	silver	white	blue	purple	black
Number of cars	21	24	25	20	3	7

- **a** Based on this sample, find the probability that a randomly chosen car is:
 - i white
 - ii purple
 - iii silver or black
- **b** How many purple cars would you expect to see in a shopping centre car park with 2000 cars?

Problem-solving and reasoning

10 The number of children in some families is recorded in the table shown.

Number of children	0	1	2	3	4
Number of families	5	20	32	10	3

- a How many families have no children?
- **b** How many families have an even number of children?
- c How many families participated in the survey?
- **d** Based on this experiment, what is the probability that a randomly selected family has 1 or 2 children?
- e Based on this experiment, what is the probability that a randomly selected family has an even number of children?
- f What is the total number of *children* in this survey?
- 11 A handful of 10 marbles of different colours is placed into a bag. A marble is selected at random, its colour recorded and then returned to the bag.

Red marble	Green marble	Blue marble
chosen	chosen	chosen
21	32	47

- **a** Based on the results in the table, how many marbles of each colour do you think there are? Justify your answer in a sentence.
- b For each of the following, state whether or not they are possible colours for the 10 marbles in the bag.
 - i 3 red, 3 green, 4 blue
 - ii 2 red, 4 green, 4 blue
 - iii 1 red, 3 green, 6 blue
 - iv 2 red, 3 green, 4 blue, 1 purple
 - v 2 red, 0 green, 8 blue



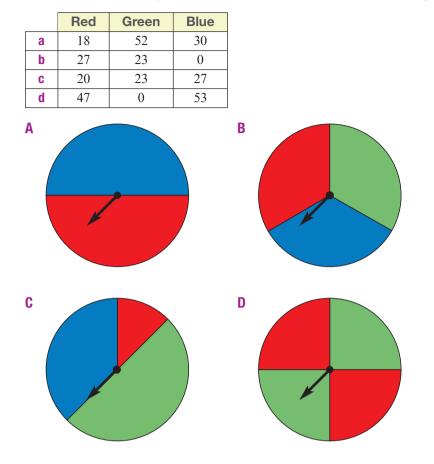
Hint: For part f, think: 3 families each with 4 children makes 12 children.

11-12

10, 11

13

12 Match each of the experiment results (a to d) with the most likely spinner that was used (A to D).



Dice-based basketball

- **13** Each time a certain basketball player takes a free throw there is a 4 in 6 chance that the shot will go in. This can be simulated by rolling a 6-sided die and using numbers 1 to 4 to mean 'shot goes in' and numbers 5 and 6 to mean 'shot misses'.
 - **a** Use a 6-sided die over 10 trials to find the experimental probability that the shot goes in.
 - **b** Use the die over 50 trials to find the experimental probability that the shot goes in.
 - **c** Working with a group, use the die over 100 trials to find the experimental probability that the shot goes in.
 - **d** Use the die over just one trial to find the experimental probability that the shot goes in. (Your answer should be either 0 or 1.)
 - e Which of the answers to parts a to d is closest to the theoretical probability of 66.67%? Why?
 - f How could you simulate a basketballer who has a 1 in 2 chance of getting a free throw in?



Maths@Work: Teachers

Teachers across all areas of education have many skills. They need to be enthusiastic and good communicators as well as having an in-depth knowledge of their course work. Keeping informed about educational research and the latest technology helps teachers to offer students a variety of learning experiences.

Teachers across all key learning areas need to be able to generate and interpret statistics. From NAPLAN results to class results, skill with statistics is important in a teacher's career. Teachers can discover the level of their students' and classes' understanding of a concept by analysing test responses.



1 In a recent formal exam of multiple-choice questions, the number of times each answer was selected by Ms Sharma's students for questions 5, 6 and 7 are shown in the tables below:

Qu	estion 5	Qu	estion 6	Question 7		
Α	5	А	2	A	15	
В	2	В	17	В	8	
С	3	С	3	С	4	
D	20	D	7	D	3	

- a Which answer would you assume to be correct for each question?
- **b** How many students answered each question?
- c How many students are in Ms Sharma's class?

Given that the correct answers were:

Question 5 - D, Question 6 - B, Question 7 - A, complete the following questions.

- **d** What percentage of students in Ms Sharma's class answered each question correctly? Round answers to a whole number.
- e Draw a column graph showing the percentage of correct answers for each question.
- 2 Mr White's class sat the same exam as Ms Sharma's class (in question 1 above). The responses to question 7 in Mr White's class were:

Α	В	А	В	А	А	С	D	D	D	Α	Α
Α	Α	Α	А	В	А	В	Α	С	D	Α	D

- a Show these results in a table with the number for each response: A, B, C and D.
- **b** What percentage of students in Mr White's class answered question 7 correctly?
- c Which class achieved a better result for question 7?



3 A teacher will often pre-test and post-test a topic to determine the understanding gained and to improve future teaching methods.

Results for fractions tests. Girls' marks are in red, boys' in black.

															20
Marks out of 50															
POST-TEST	23	38	34	35	44	32	18	42	27	46	39	34	47	22	22
Marks out of 50	31	36	19	32	21	45	29	25	44	28	29	46	34	43	38

- a Display the pre-test results for the entire class as a stem-and-leaf plot.
- **b** Display two separate stem-and-leaf plots for the girls' results, one for their pre-test results and another for their post-test results.
- **c** Have the girls' results improved from pre-test to post-test? Give at least one observation about their marks to support your conclusion.
- **d** The plot below is called a back-to-back stem-and-leaf plot. It shows the boys' pre-test results on the left and their post-test results on the right.

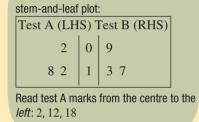
pre-test results	post-test results	
8	0	
8	1 9	Кеу
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 1 5 8 9 9 3 1 2 4 6 8	LHS:7 2 = 27 RHS:2 8 = 28
1 0	4 3 4 5 6	1113.2 0 - 20

- i List the boys' pre-test results that are less than 20.
- ii How many boys got marks in the 20s on each test?
- iii List the boys' marks from each test that are 40 or above.
- iv Have the boys' results improved from pre-test to post-test? Give at least one observation about their marks to support your conclusion.

Using technology

- 4 Teachers make good use of the calculation power of spreadsheets. Spreadsheet formulas will convert a result out of any total to a percent. Comparing percentages helps teachers to follow each student's progress.
 - **a** Set up the following spreadsheet.
 - b Select all the cells that will have percentage results, right click and select Format/percentage/0 d. p. The spreadsheet will convert decimal answers to a percentage and automatically insert a % symbol.
 - c Format average test mark cells to Number/1 d. p.
 - **d** Enter formulas into the shaded cells to calculate percentages and averages.

1	A	8	c	D	E	F.	G	н	1	1	ĸ	L
1					Mrs B	est's year	7 maths cl	ass				
2	Test	Ter	m 1	Ter	m 2	Mental A	rithmetic	Ter	m 3	Ter	m 4	Averages
3	Total marks	22	%	19	%	10	*	34	*	26	%	
4	Oscar	20		18		10		32		23		
5	Molly	17		16	-	9		29		22		
6	Blake	14		12		5		16		16		
7	Angus	19		19		8		33		23		
8	Bhavin	17		14	1	7		26		18	1	
9	Scarlett	14		11		6		24		19		
10	Vedika	18		16		8		31		24		
11	5.2/	200		080268	1	2.55	· · · · · · · · ·	y 2820.0		1.00210		
12	Class averages											



Hint: This is a back-to-back

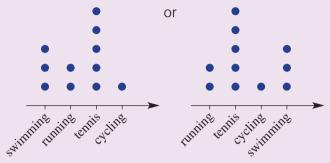
Hint: In each percentage cell, calculate a decimal, e.g. = $\frac{B4}{\Im D^{\Im 3}}$



Hint: Average formula example = Average(B4:B10)

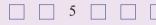


- Three brothers are asked about their ages. The youngest, Andrew, says, 'The range of our ages is 5'. The middle, Brett, says, 'The median age is 15'. The oldest, Chris, says, 'But the mean age is 14'. Assuming the brothers are telling the truth, how old are they?
- **2** The results of a survey are to be shown in a dot plot with four categories: swimming, running, tennis, cycling. Two ways the graph could be shown are:



How many ways in total are there to draw this dot plot?

3 Six numbers are listed in ascending order and then some are removed.



The mean and median are both 6, the mode is 2 and the range is 10. Find the missing numbers.

4 In a class of 20 students, a poll was taken of the number of cars owned by each family. The median number of cars owned is 1.5 and the mean number is 1.4 cars. Complete the following table of the results.

Number of cars	0	1	2	3
Number of students	4			

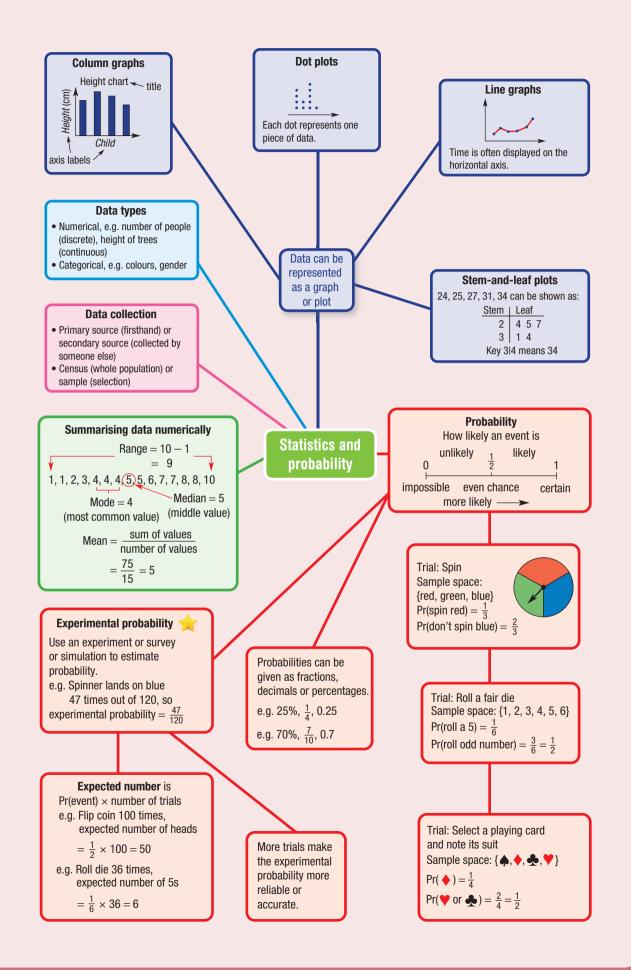


- 5 When one coin is flipped, Pr(heads) = $\frac{1}{2}$. For two coins, the probability that both are heads is
 - $\frac{1}{4}$. For three coins, Pr(all heads) = $\frac{1}{8}$. How many coins are flipped if the probability of getting all heads is $\frac{1}{64}$?
- 6 Five people are surveyed. They are asked if they prefer bottled water, tap water or mineral water. Two possible results are shown. How many more possible results are there?

Bottled	Тар	Mineral
3	1	1
2	3	0

7 A bag of 24 marbles contains blue, green and red marbles. If you pick one marble at random (without looking), there is an even chance that it will be blue. Given that there are twice as many green marbles as red marbles, how many of each colour are there?





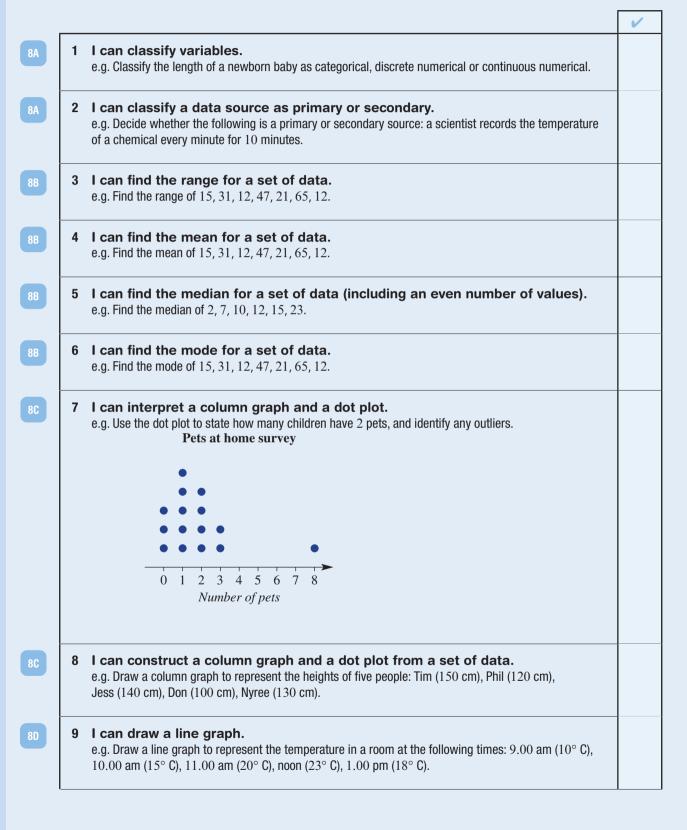
Essential Mathematics for the Victorian Curriculum CORE Year 7

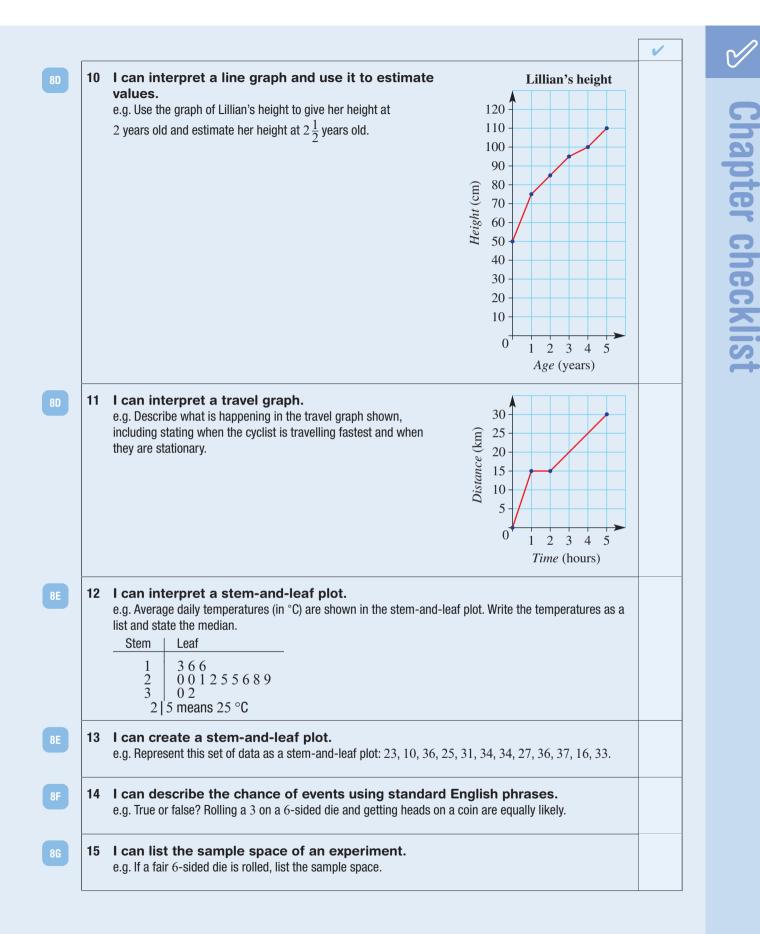
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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

Chapter checklist





\sim		
	8G	16 I can calculate the probability of a simple event, giving an answer as a
list		fraction, decimal or percentage. e.g. If a fair 6-sided die is rolled, find the probability of getting a number less than 3. Answer as a percentage correct to one decimal place.
apter checklist	8H	17 I can calculate the experimental probability of an event. e.g. When playing with a spinner the following numbers come up: 1, 4, 1, 3, 3, 1, 4, 3, 2, 3. Find the experimental probability of getting an even number.
3	8H	18 I can find the expected number of occurrences of an event.
		e.g. A spinner lands on red $\frac{1}{4}$ of the time. If it is spun 200 times, how many times would you expect it to
ote		land on red?
3		

1

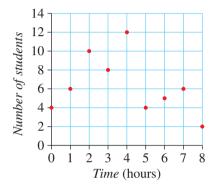
Short-answer questions

1 Draw a column graph to represent the following people's ages.

Name	Sven	Dane	Kelly	Hugo	Frankie
Age (years)	20	12	15	22	25

- **2** A Year 7 group was asked how many hours of television they watch in a week. The results are given in the table.
 - a How many students participated in the survey?
 - **b** How many students watched 11 or 12 hours of television?
 - **c** What was the most common amount of television watched?
 - **d** Show this information in a column graph.
- 3 The number of students in the library is recorded hourly, as displayed in the graph.
 - a How many students entered the library when it first opened?
 - **b** How many students were in the library at 8 hours after opening?
 - **c** If the library opens at 9 a.m., at what time are there the most number of students in the library?
 - d How many students were in the library at 4 p.m.?
 - e Why do you think these points have not been joined to make a line graph?

TV watched	No. of
(hours)	students
8	5
9	8
10	14
11	8
12	5





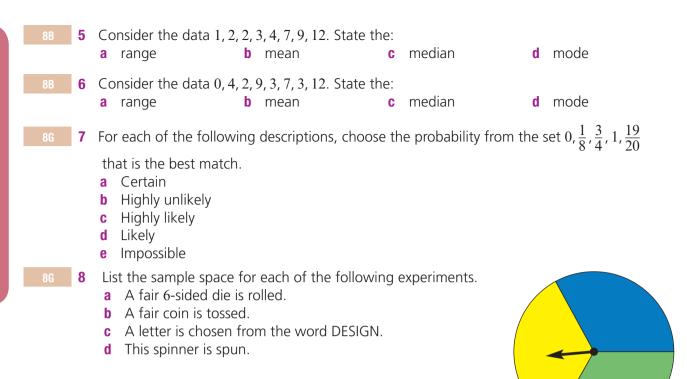
The weight in grams of various meat patties at a local burger shop are measured. The results are shown in this stem-and-leaf plot.
 Stem | Leaf

stem	Le	eaf				
10	5	8				
11	2	6	6	8	9	
12	0	2	4	5		
13	1					

12 4 means 124 grams

- a What is the weight of the pattie represented as 11 | 8?
- **b** What is the weight of the lightest pattie?
- c What is the weight of the heaviest pattie?
- **d** Find the range of the weights of the patties.



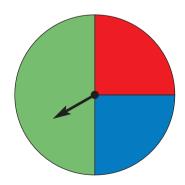


9 Vin spins a spinner with nine equal sectors, which are numbered 1 to 9.

- a How many outcomes are there?
- **b** Find the probability of spinning:
 - i an odd number
 - ii a multiple of 3
 - iii a number greater than 10
 - iv an even number

10 A coin is tossed 100 times, with the outcome 42 heads and 58 tails.

- **a** What is the experimental probability of getting heads? Give your answer as a percentage.
- **b** What is the actual probability of getting heads if the coin is fair? Give your answer as a percentage.
- **11** Consider this spinner.
 - **a** State the probability that the spinner lands in the green section.
 - **b** State the probability that the spinner lands in the blue section.
 - **c** Tanya spins the spinner 100 times. What is the expected number of times it would land in the red section?
 - **d** She spins the spinner 500 times. What is the expected number of times it would land in the green section?



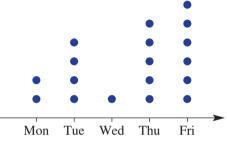
Multiple-choice questions

- 1 Which one of the following variables is continuous numerical?
 - A The gender (male or female) of newborn babies.
 - В The number of babies born in a given year.
 - The number of hairs on a baby's head. С
 - D The weight (in kg) of newborn babies.
 - The length (in number of letters) of a baby's E first name.



E Victoria

Students are asked their favourite day of the weekday. The results are shown in this dot plot. 2

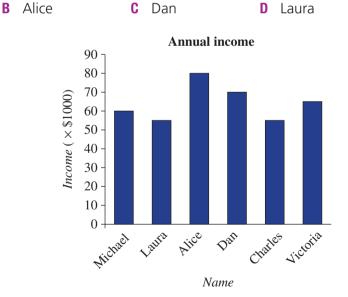


The total number of students asked was:



In the following column graph, the highest income is earned by: 3

A Michael



	Questions 4 and A stem-and-leaf Stem Leaf 1 7 9 2 3 4 3 2 7 2 4 means	olot shows	s the ages o					
8E 4	The youngest per	rson's age	is:					
	A 1	B 17	C	7	D	2	E	39
8E 5	The number of p	eople repr	esented is:					
	A 8	B 11	C	39	D	3	Ε	26
8B 6	The median of th	e number	s 2, 4, 7, 9, 1	1 is:				
	A 7	B 7.5	C	9	D	8	Ε	11
In a	stions 7 and 8 relations 7 and 8 relations 7 and 8 relations 7 and 7 relations 7 and 7 relations 7 and 7 relations 7 and 7 relations 7 and 8 relations 8 relations 7 and 8 relations 8 relat		0		: Wa	is absent over a	ter	m is recorded.
8B 7	The mode is:							
	A 0	B 1	C	2	D	3	E	4
8B 8	The mean numbe	er of days	a student w	as absent is:				
	A 1	B 2	C	4	D	1.8	E	18
9 Each of the five letters of the word APPLE is written on a separate card. One card is then chosen at random. Pr(letter P) is:								
	A 0	B 0.2	C	0.4	D	0.5	Ε	1
10 Michelle scores a goal in netball $\frac{1}{3}$ of the time. The expected number of goals out of 600								
*	shots is: A 100	B 200	3 C	300	D	400	Ε	600

Extended-response questions

1 This table shows the number of rainy days in a certain town over one year.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
No. of rainy days	10	11	3	7	2	0	1	5	6	9	7	5

- **a** Show this information in a line graph.
- **b** On how many days of the year did it rain in this town?
- c What is the probability that it rained on any day during June, July or August?



2 At a school camp, a survey was conducted to establish each student's favourite dessert.

Ice-cream	Yoghurt	Danish pastry	Jelly	Pudding	Cheesecake
10	5	2	7	4	12

- a How many students participated in the survey?
- **b** What is the most popular dessert?
- c If a student is picked at random, what is the probability that jelly is their favourite dessert?
- **d** For each of the following graphs and plots, state whether it would be a reasonable way of presenting the survey's results.
 - i Column graph
 - iii Dot plot

- ii Line graph
- iv Stem-and-leaf plot
- e If the campers attend a school with 800 students, how many students from the entire school would you expect to choose pudding as their preferred dessert?



Chapter C

Shapes/and transformations

Essential mathematics: why understanding shapes and transformations is important

Geometry has been applied for thousands of years and is essential knowledge for architects, engineers, construction workers, graphic designers, quilters, animators and urban planners.

- Civil engineers use shapes such as isosceles and equilateral triangles for stable and strong structural supports. These triangles can often be seen in bridges, power pylons and sports stadiums.
- House blocks usually have four straight sides, forming a quadrilateral. Surveyors can check their measurements knowing that angles in a quadrilateral add to 360°.
- Modern architectural design uses symmetry, reflection and rotation to create interesting visual effects.
- Virtual reality computer programmers apply geometry to construct digital scenery, and move virtual objects using transformations such as translations, reflections and rotations.



In this chapter

- 9A Triangles
- 9B Angle sum of a triangle
- 9C Quadrilaterals
- 9D Angle sum of a quadrilateral
- 9E Symmetry
- **9F** Reflection
- 9G Rotation
- 9H Translation
- 91 Drawing solids

Victorian Curriculum

MEASUREMENT AND GEOMETRY

Location and transformation

Describe translations, reflections in an axis, and rotations of multiples of 90° on the Cartesian plane using coordinates. Identify line and rotational symmetries (VCMMG261)

Geometric reasoning

Classify triangles according to their side and angle properties and describe quadrilaterals (VCMMG262)

Demonstrate that the angle sum of a triangle is 180° and use this to find the angle sum of a quadrilateral (VCMMG263)

Shape

Draw different views of prisms and solids formed from combinations of prisms (VCMMG260)

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Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

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Cambridge Univer

- 1 a How many sides does a triangle have?
 - What adds to 110 to give 180? C
 - e 180 subtract 99 gives what number?
- **b** How many angles are there inside a triangle?
- **d** What adds to 285 to give 360?
- f 360 subtract 212 gives what number?
- 2 a How many sides are there on a square?
 - **b** What is the size of the interior (inside) angles in a rectangle?

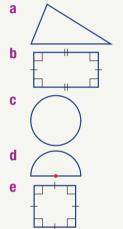
b

e

- **c** An equilateral triangle has how many sides of equal length?
- **d** An isosceles triangle has how many sides of equal length?
- **3** Find the missing number.

а

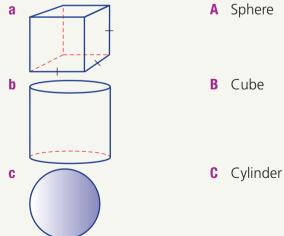
- +40 = 90**d** +124 = 360
- +125 = 180+32 + 109 = 180
- +30+70=180C f +95+135=360
- This square shows one mirror line. How many other mirror lines 4 could be drawn?
- 5 Match the names (A to E) with the given shapes (a to e).



B Square

A Rectangle

- Semicircle C
- **D** Triangle
- E Circle
- 6 Match the names (A to C) to the solids (a to c).



7 Complete this table.

Type of angle	acute	right	obtuse	straight	reflex	revolution
Angle size			90° - 180°			360°

9A Triangles

Learning intentions

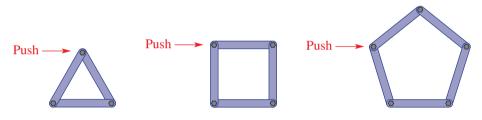
- To be able to classify triangles by their side lengths (scalene, isosceles, equilateral) or by their interior angles (acute, right, obtuse).
- To be able to draw triangles using a protractor and ruler.
- Key vocabulary: triangle, scalene, isosceles, equilateral, acute triangle, right triangle, obtuse triangle

The word triangle, meaning 'three angles', describes a shape with three sides. The triangle is an important building block in mathematical geometry. It's important in the practical world of building and construction because it is a rigid shape.



Lesson starter: Stable shapes

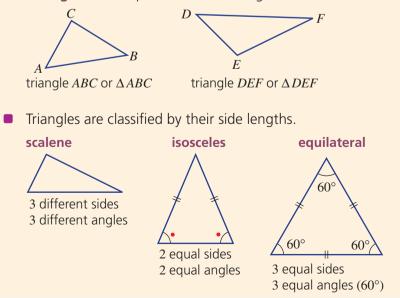
Consider these constructions, which are made from straight pieces of steel held together loosely with bolts. (That is, the bolts have not been tightened.)

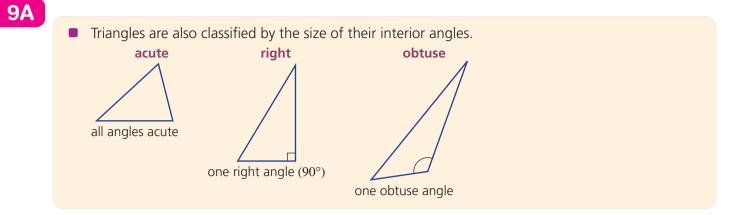


- Which of the constructions do you think could lose their shape if a vertex (corner) is pushed?
- Which of the constructions will not lose their shape when pushed? Why?
- For the constructions that might lose their shape, what could be done to make them rigid?

Key ideas

Triangles are shapes with three straight sides and can be named using their vertex labels.

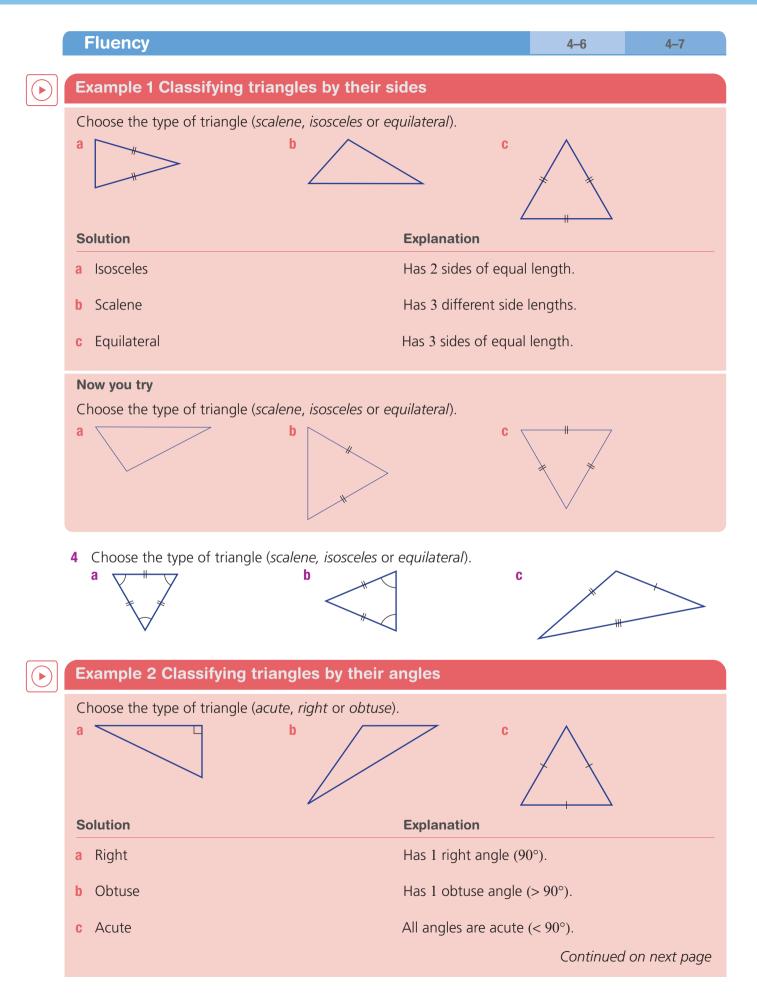




Exercise 9A

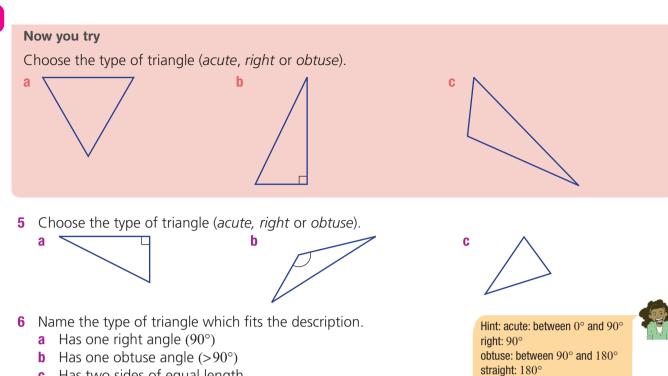
Understanding	1–3	3
 Match each type of triangle (a to c) with a diagram (A to C). a Acute b Right c Obtuse A B C 		
 2 Match each type of triangle (a to c) with a diagram (A to C). a Scalene b Isosceles c Equilateral A B B C 		
 3 Draw an example of each of these triangles. a Scalene b Isosceles c Equilateral d Acute e Right f Obtuse 	Hint: Scalene: 3 different side: Isosceles: 2 equal sides Equilateral: 3 equal sides Acute: 3 acute angles Right: 1 right angle Obtuse: 1 obtuse angle	

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Essential Mathematics for the Victorian Curriculum CORE Year 7

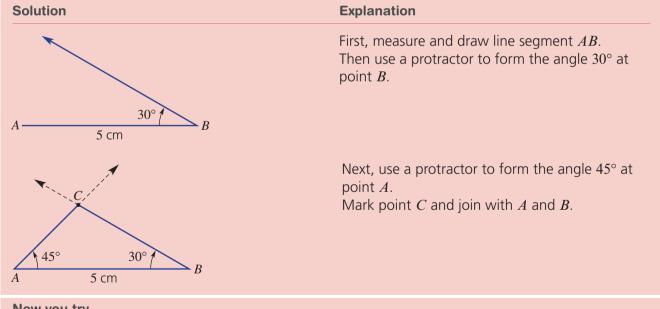
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- c Has two sides of equal length
- **d** Has three different side lengths
- e Has three sides of equal length
- Has three acute angles ($<90^{\circ}$) f

Example 3 Drawing triangles

Draw a triangle ABC with AB = 5 cm, $\angle ABC = 30^{\circ}$ and $\angle BAC = 45^{\circ}$.



Now you try

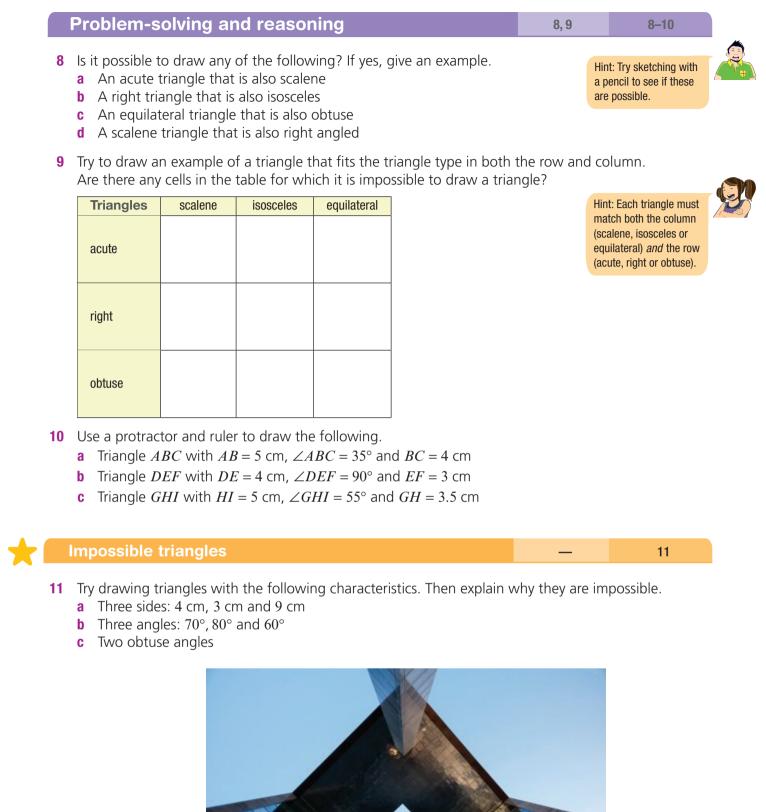
Draw a triangle XYZ with XY = 7 cm, $\angle YXZ = 30^{\circ}$ and $\angle XYZ = 60^{\circ}$.

7 Use a protractor and ruler to draw the following triangles.

- a Triangle ABC with AB = 5 cm, $\angle ABC = 40^{\circ}$ and $\angle BAC = 30^{\circ}$
- **b** Triangle *DEF* with DE = 6 cm, $\angle DEF = 50^{\circ}$ and $\angle EDF = 25^{\circ}$
- Triangle *GHI* with *GH* = 4 cm, $\angle GHI$ = 70° and $\angle HGI$ = 50° C

reflex: between 180° and 360°

revolution: 360°



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9B Angle sum of a triangle

Learning intentions

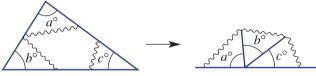
- To know that the sum of interior angles in a triangle is 180°.
- To know what an exterior angle is and how to find it using supplementary angles.
- To know that in an isosceles triangle, the angles opposite the apex are equal and the two sides (legs) adjacent to the apex are of equal length.
- To be able to find an unknown angle in a triangle if two other angles are given.
- Key vocabulary: angle sum, interior angle, exterior angle, isosceles

The three interior angles of a triangle have a very important property. No matter the shape of the triangle, the three angles always add to the same total.



Lesson starter: A visual perspective on the angle sum

Use a ruler to draw any triangle. Cut out the triangle and tear off the three corners. Then place the three corners together.



What do you notice and what does this tell you about the three angles in the triangle? Compare your results with those of others. Does this work for other triangles?

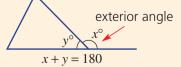
Key ideas

• The **angle sum** of the **interior angles** of a triangle is 180°.



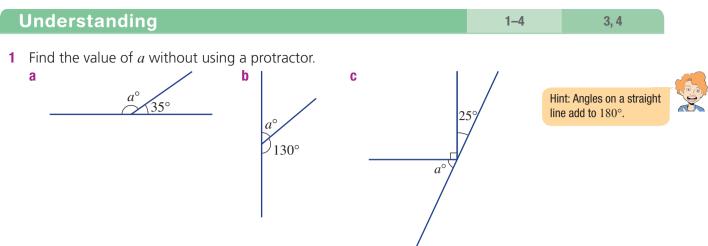
a+b+c=180

If one side of a triangle is extended, an exterior angle is formed.

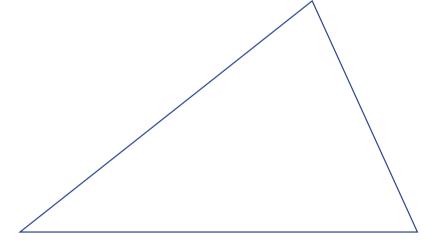


An isosceles triangle has one pair of equal angles.

Exercise 9B



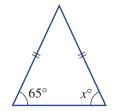
- 2 a Use a protractor to measure the three angles in this triangle.
 - **b** Add your three angles. What do you notice?



3 Copy and complete the working for this triangle.



4 State the value of *x* in these isosceles triangles.

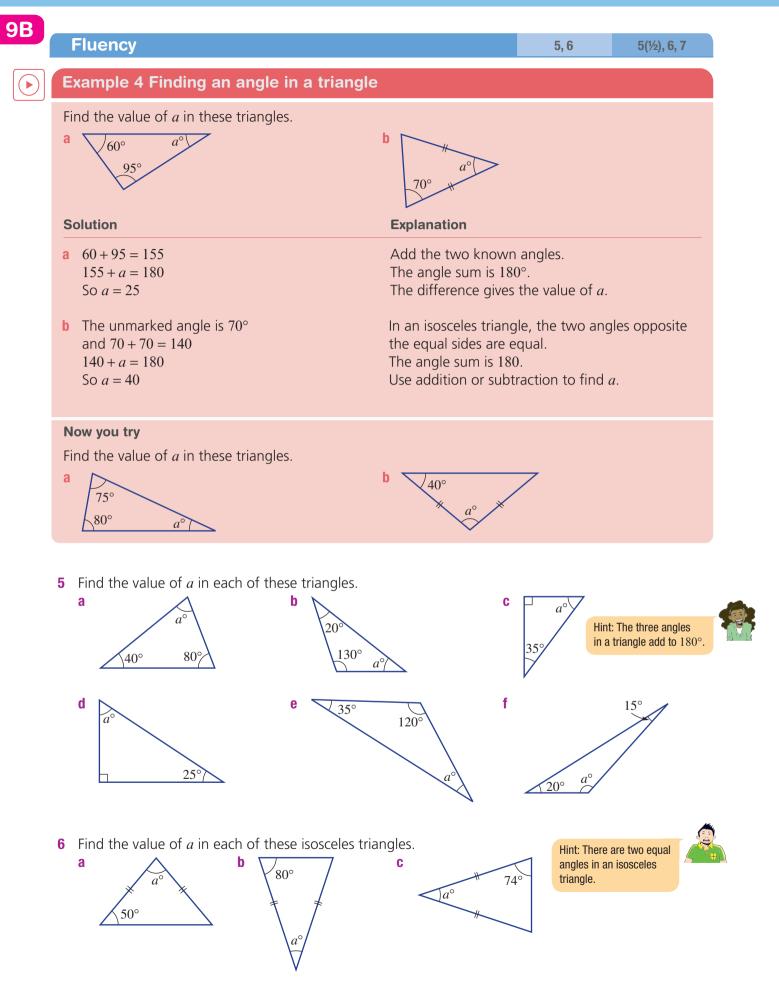


a

b 25° x°

Hint: Remember that an isosceles triangle has two equal angles.





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By first finding the value of *a*, find the value of *x*.

Solution

a + 62 + 90 = 18062 + 90 = 152So a = 28 Explanation

First use the angle sum to find *a*. (There are 90° in a right angle.) Think: 180 - 152 (or 152 + ? = 180).

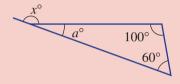
Angles x° and a° are supplementary (i.e. they add to 180°). Add or subtract to find x.

Now you try

x + 28 = 180

x = 152

By first finding the value of *a*, find the value of *x*.

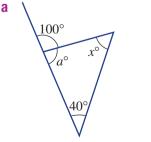


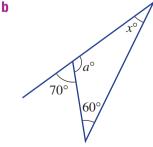
7 By first finding the value of a, find the value of x. a b x° 40° 85° a° x° x° x°

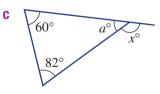


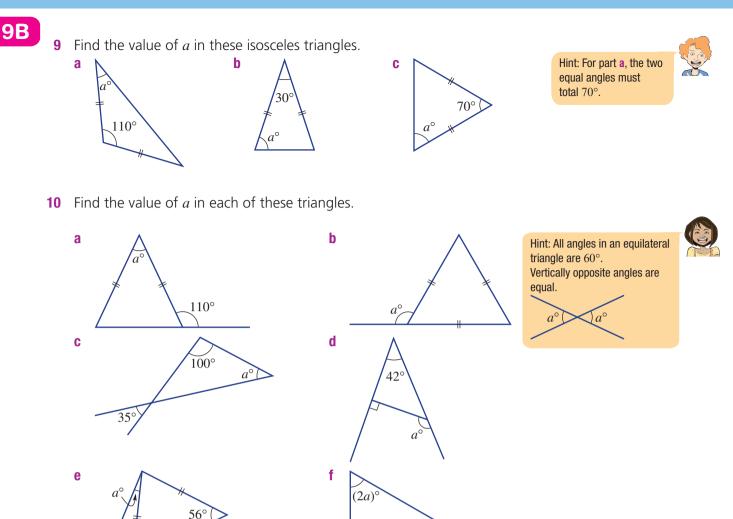
Problem-solving and reasoning8-109-12

8 The triangles below have exterior angles. Find the value of *x*.

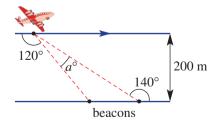








11 A plane flies horizontally 200 m above the ground. It detects two beacons on the ground. Some angles are known, and these are shown in the diagram. Find the value of *a* marked between the line of sight to the two beacons.

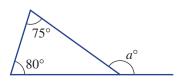


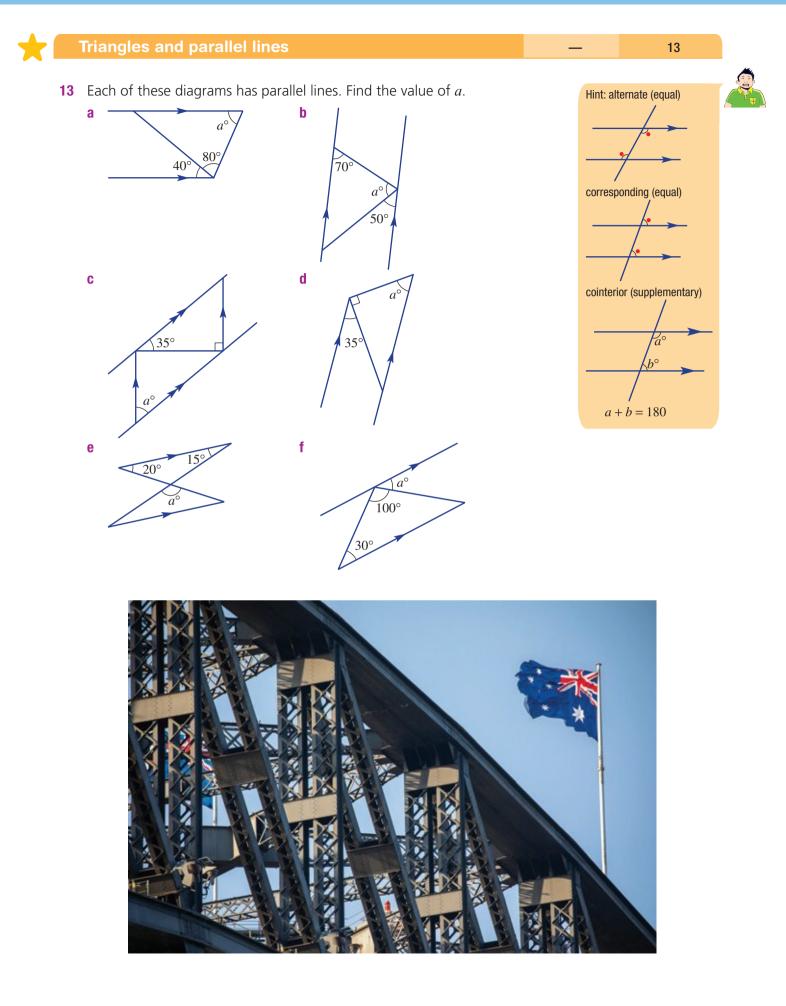


Hint: Draw a vertical line to create two right-angled triangles.



- **12 a** Work out $75^{\circ} + 80^{\circ}$.
 - **b** Find the value of *a* in the diagram.
 - **c** What do you notice about the answers to parts **a** and **b**?
 - **d** Do you think this would be true for other triangles with different angles? Explore.





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9C Quadrilaterals

Learning intentions

- To know what a quadrilateral is.
- To be able to classify a quadrilateral as convex or non-convex.
- To know from a diagram or description whether a quadrilateral is a parallelogram, rectangle, rhombus, trapezium or square.

Key vocabulary: quadrilateral, parallelogram, rectangle, rhombus, square, trapezium, kite, convex, non-convex

Quadrilaterals are shapes with four straight sides. Special types of quadrilaterals are identified by the number of equal side lengths and the number of pairs of parallel lines.

Lesson starter: Quadrilaterals that you know

You may already know the names and properties of some of the special quadrilaterals. Which quadrilaterals do you think have:

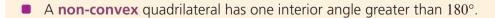
- 2 pairs of parallel sides?
- all sides of equal length?
- 2 pairs of sides of equal length?

Are there any types of quadrilaterals that you know which you have not yet listed?



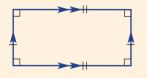
Key ideas

- A quadrilateral is a shape with four straight sides.
- A convex quadrilateral has all four interior angles less than 180°. All vertices point outward.

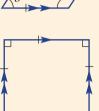


- Parallelograms are quadrilaterals with two pairs of parallel sides:
 - parallelogram2 pairs of parallel sides2 pairs of sides of equal lengthopposite angles equal
 - rectangle (a parallelogram with all angles 90°)
 2 pairs of parallel sides
 2 pairs of sides of equal length all angles 90°

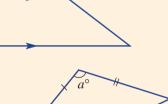




- **rhombus** (sometimes called a diamond) (a parallelogram with all sides equal) 2 pairs of parallel sides all sides of equal length opposite angles equal
- square (a rhombus with all angles 90°)
 2 pairs of parallel sides all sides of equal length all angles 90°



- Other special quadrilaterals include:
 - trapezium 1 pair of parallel sides



• kite

2 pairs of sides of equal length 1 pair of opposite angles that are equal

Exercise 9C

Understanding Draw an example of each of the quadrilaterals a to f. Mark any sides of equal length with single or double dashes. Mark parallel lines with single or double arrows.

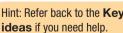
Mark equal angles using the letters a and b.

- a Square
- c Rhombus
- e Trapezium
- **2** a Draw two examples of a non-convex quadrilateral.
 - **b** For each of your drawings, state how many interior angles are greater than 180°.

b Rectangled Parallelogram

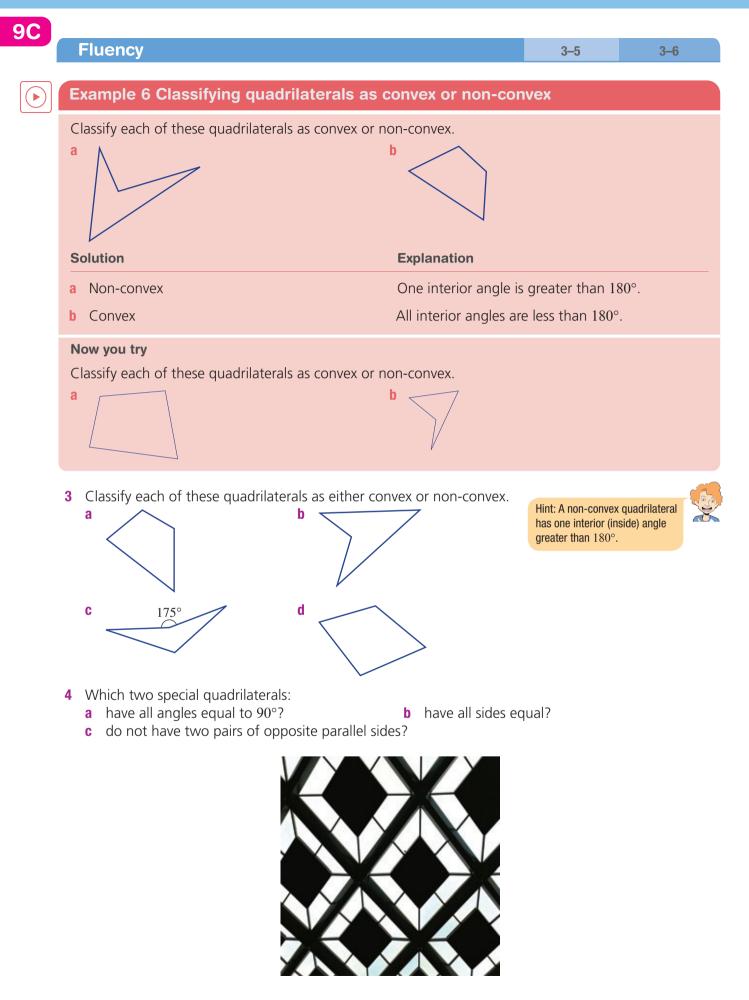
f Kite

1, 2



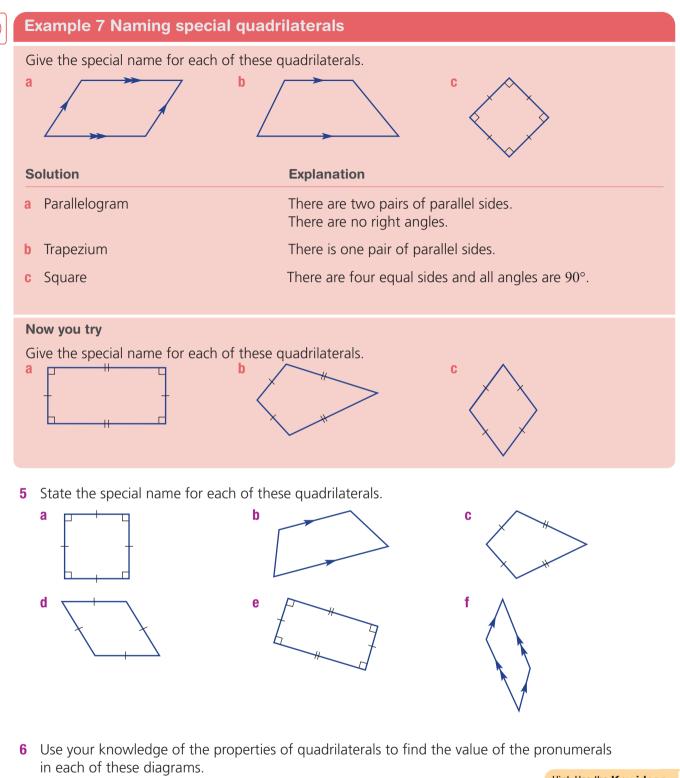
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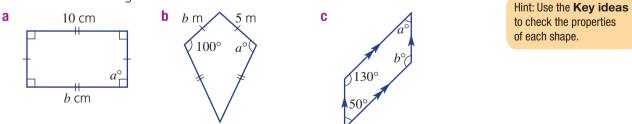




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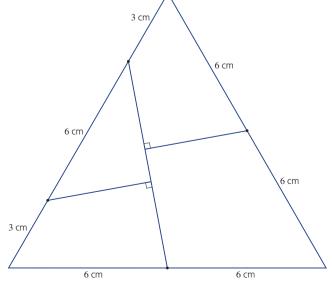
9C

Problem-solving and reasoning

- 7 Name all the quadrilaterals that have:
 - a 2 different pairs of sides of equal length
 - **b** 2 different pairs of opposite angles that are equal in size
 - c 2 different pairs of parallel sides
 - d only 1 pair of parallel sides
 - e only 1 pair of opposite angles that are equal in size
- 8 Consider this 4 × 4 grid. Using the dots as vertices, how many different shapes of each kind could be drawn? (Do not count shapes that are the same size.)
 - a Squares
 - **b** Rectangles (not including the squares from part **a**)
 - **c** Rhombuses (not including the squares)
 - d Parallelograms (not including the shapes from parts **a** to **c**)
- **9** The diagonals of a quadrilateral are line segments that join opposite vertices.
 - a Which quadrilaterals have diagonals of equal length?
 - **b** Which quadrilaterals have diagonals intersecting at 90°?
- **10 a** Are squares a type of rectangle or are rectangles a type of square? Give an explanation.
 - **b** Are rhombuses a type of parallelogram? Explain.
 - c Are parallelograms a type of trapezium? Explain.
 - d Is it possible to draw a non-convex trapezium? Give a reason.

A triangle makes a square!

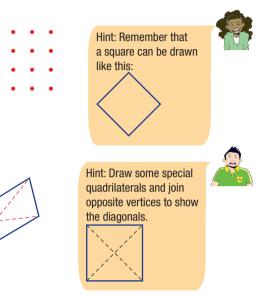
11 Using the given measurements, draw this equilateral triangle accurately on a piece of paper and cut it into the four pieces shown. Can you form a square with all four pieces? (If you're having trouble drawing it, you could photocopy or print it instead.)





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7.8

7–10

11

9D Angle sum of a quadrilateral

Learning intentions

- To know that the sum of interior angles in a quadrilateral is 360°.
- To know what an exterior angle is.
- To be able to find an unknown angle inside a quadrilateral given the other three angles.
- To be able to find the size of an exterior angle for a quadrilateral.

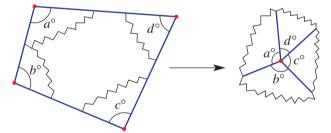
Key vocabulary: quadrilateral, sum, interior angle, exterior angle

We have seen that a triangle has an angle sum of 180°. A quadrilateral also has a special angle sum. We use this angle sum to help solve geometry problems that involve four-sided shapes.



Lesson starter: What do a circle and a quadrilateral have in common?

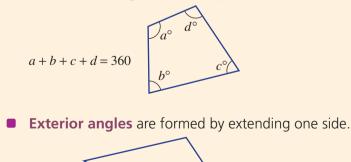
Use a ruler to draw any quadrilateral. Cut it out and tear off the corners. Arrange them to meet at a point.

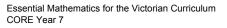


- What does the arrangement tell you about the angles inside a quadrilateral?
- Compare your results with those of others in the class.

Key ideas

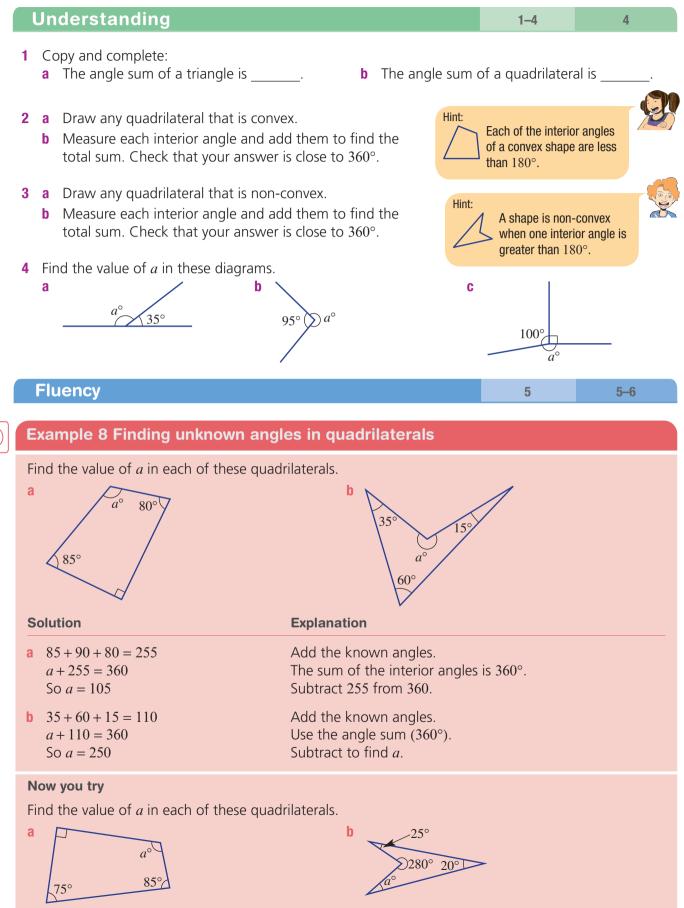
• The interior angle sum of a quadrilateral is 360°.





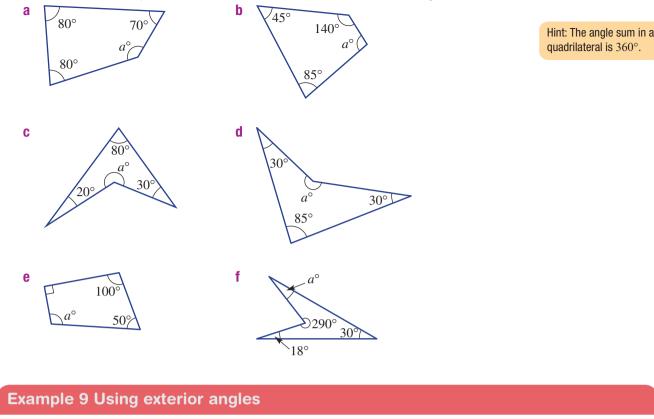
a + b = 180

Exercise 9D

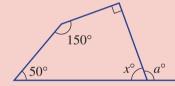


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5 For each of these quadrilaterals, find the size of the unknown angle marked *a*.



Find the value of *a* by first finding the value of *x*.



Solution

►

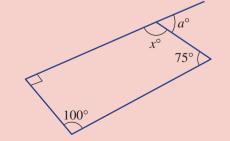
90 + 150 + 50 = 290 x + 290 = 360So x = 70 a + 70 = 180So a = 110 Explanation

First find the value of x using the angle sum (360°) .

Two angles on a straight line add to 180°.

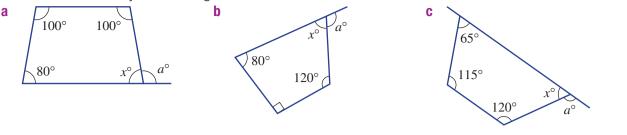
Now you try

Find the value of a by first finding the value of x.









Problem-solving and reasoning

7(1/2), 8 7(1/2), 8–10

 b°

а

70°

170°

120°

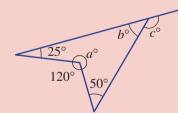
Example 10 Problem-solving with quadrilaterals

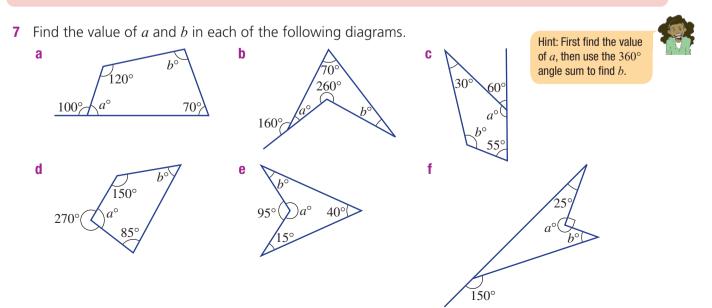
Find the value of a, b and c in this diagram.

Solution	Explanation
a = 180 - 120 = 60	<i>a</i> and 120° are supplementary.
b = 360 - 170 = 190	Angles at a point sum to 360°.
70 + 60 + 190 = 320	Add the known interior angles.
c + 320 = 360	The sum of the interior angles is 360°.
c = 40	Subtract to find <i>c</i> .

Now you try

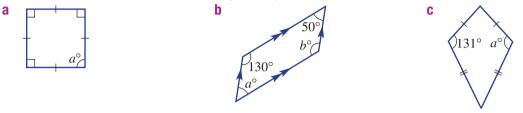
Find the value of *a*, *b* and *c* in this diagram.



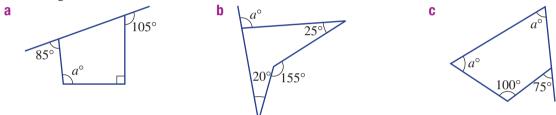


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- 8 Is it possible or impossible for a quadrilateral to have:
 - a each interior angle less than 100°?
 - **b** each interior angle less than 90°?
 - **c** more than one interior reflex angle?
 - d more than one interior obtuse angle?
 - e more than three interior acute angles?
- **9** Give the value of *a* (and *b*) in these special quadrilaterals.

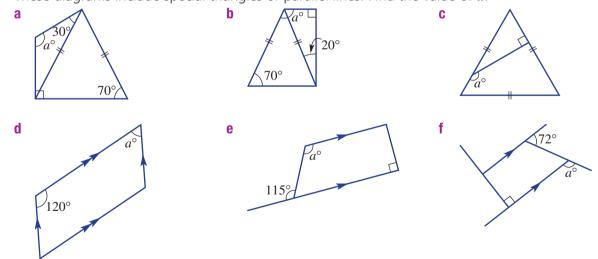


10 For each of these diagrams, find the size of the unknown angle marked *a*. You may need to find some other angles first.



Parallel lines and triangles

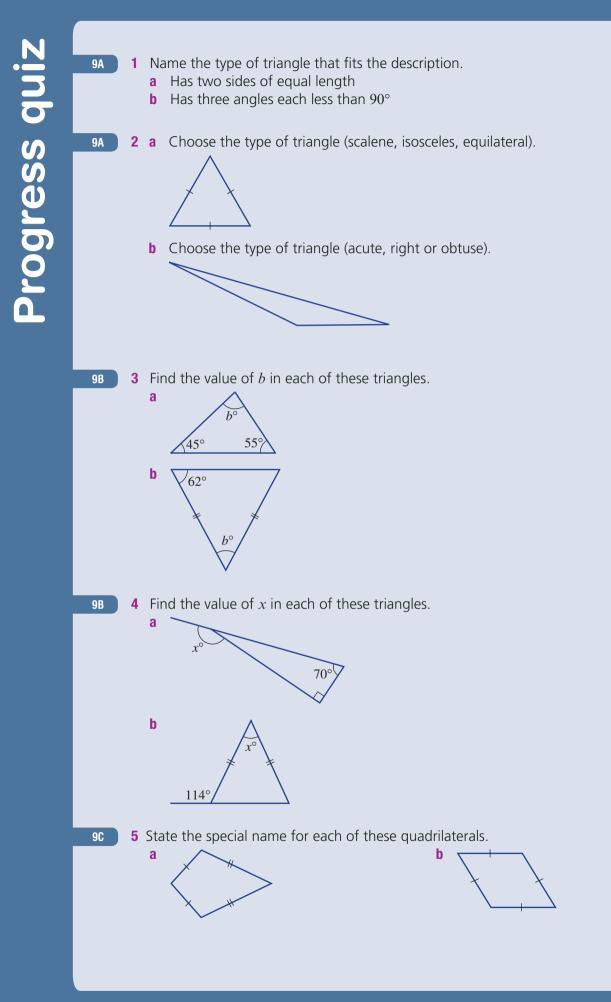
11 These diagrams include special triangles or parallel lines. Find the value of *a*.



Hint: Make drawings to explore these descriptions.

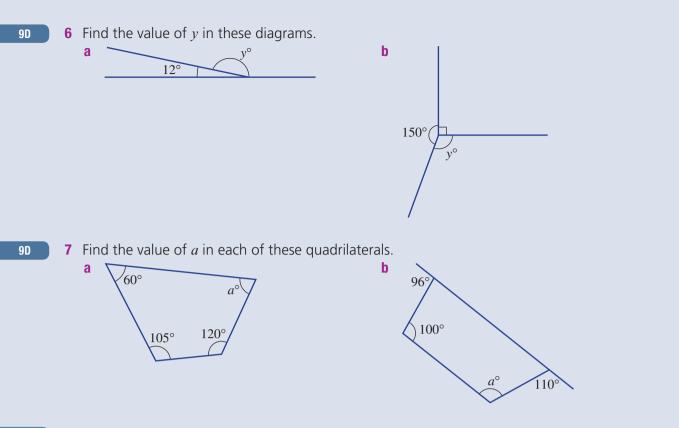
11



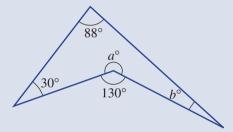


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Progress qui



8 Find the value of a and b in the following diagram.



9D

9E Symmetry

Learning intentions

- To understand what a line of symmetry is.
- To be able to determine the order of line symmetry for a shape.
- To understand what rotational symmetry is.
- To be able to determine the order of rotational symmetry for a shape.

Key vocabulary: line of symmetry, mirror line, rotational symmetry, order of rotational symmetry

The most familiar form of symmetry, called line symmetry, is connected to the idea of reflection. A flower, for example, might have one or more lines of reflection or mirror lines.

The flower might also have another form of symmetry called rotational symmetry, which will also be studied in this section.

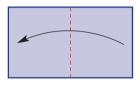


Lesson starter: Working with symmetry

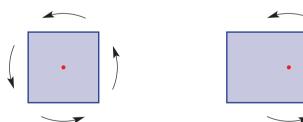
Cut out a paper square (with side lengths of about 10 cm) and a rectangle (with length of about 15 cm and width of about 10 cm).

• How many ways can you fold each shape in half so that the two halves match exactly? The number of creases formed will be the number of lines of symmetry.



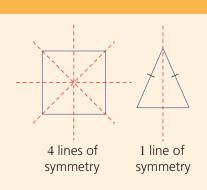


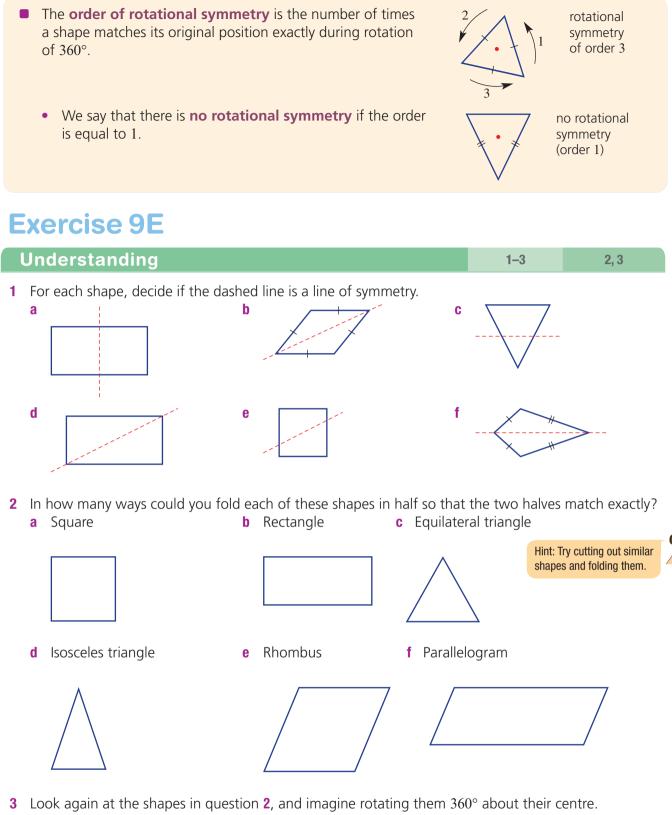
• Now locate the centre of each shape and place a sharp pencil on this point. Rotate the shape 360°. How many times does the shape match its original position exactly? This number describes the rotational symmetry.



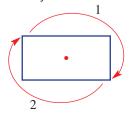
Key ideas

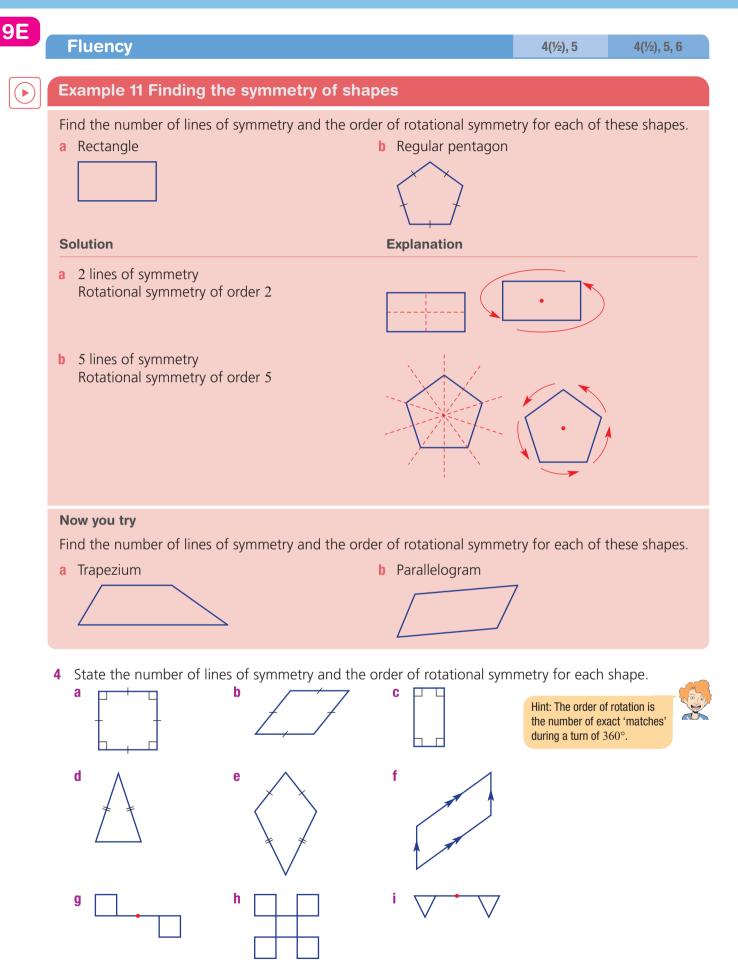
An axis or line of symmetry divides a shape into two equal parts. It acts as a mirror line, with each half of the shape being a reflection of the other.





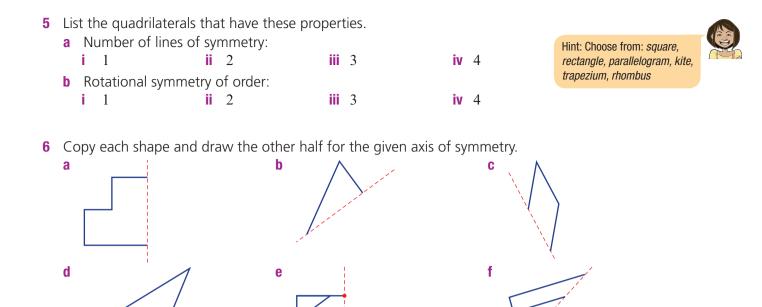
How many times would you get an exact match of the original position?





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Problem-solving and reasoning

7 State the number of lines of symmetry and the order of rotational symmetry for each of the following.

b



а

С



7, 8

8-10





8 Name a type of triangle that has:

- a 3 lines of symmetry and order of rotational symmetry 3
- **b** 1 line of symmetry and no rotational symmetry
- **c** no line or rotational symmetry

9E

9 Consider these capital letters in the font shown below.

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

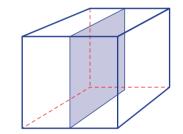
line of symmetry

List the letters that have:

- a 1 line of symmetry
- **b** 2 lines of symmetry
- c rotational symmetry of order 2
- **10** Many people think a rectangle has four lines of symmetry, including the diagonals.
 - **a** Complete the other half of this diagram to show that this is not true.
 - b Using the same method as that used in parta, show that the diagonals of a parallelogram are not lines of symmetry.

Symmetry in 3D

11 Some solid objects also have symmetry. Rather than line symmetry, they have plane symmetry. This cube shows one plane of symmetry, but there are more that could be drawn.



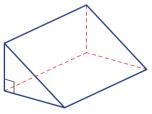
11

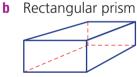
State the number of planes of symmetry for each of these solids.

a Cube

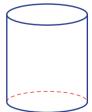


d Right triangular prism

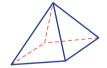




e Cylinder



c Right square pyramid



Sphere

f





Hint: The answer for

part a is not:

about K and Q.



9F Reflection

Learning intentions

- To understand that a shape can be reflected to give an image.
- To be able to draw the result of a point or shape being reflected in a mirror line.

Key vocabulary: reflection, transformation, image, mirror line

From our study of line symmetry, we already know that some shapes can be reflected in their own mirror lines.

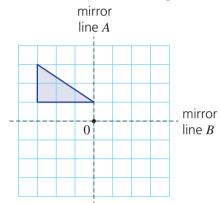
Now we will reflect shapes in mirror lines that are not positioned through the centre of the shape. Reflection is one type of transformation that results in an image of equal size and shape to the original.

Solution Lesson starter: Draw the image

Here is a shape on a grid.

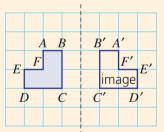
- Draw the image (result) after reflecting the shape in the mirror line *A*.
- Draw the image (result) after reflecting the shape in the mirror line *B*.

Discuss what method you used to draw each image and the relationship between the position of the shape and its image after each transformation.



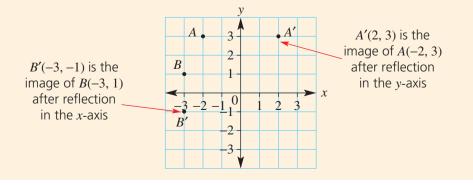
Key ideas

- Reflection is a transformation that gives an image of an object or shape without changing its shape and size.
 - A transformation is a change in position or size of a shape.
 - An image is the result of a shape after transformation.
 - Reflection involves a flip over a mirror line.
- The image of point A is denoted A'.
- A reflection involves a mirror line, as shown in the diagram.

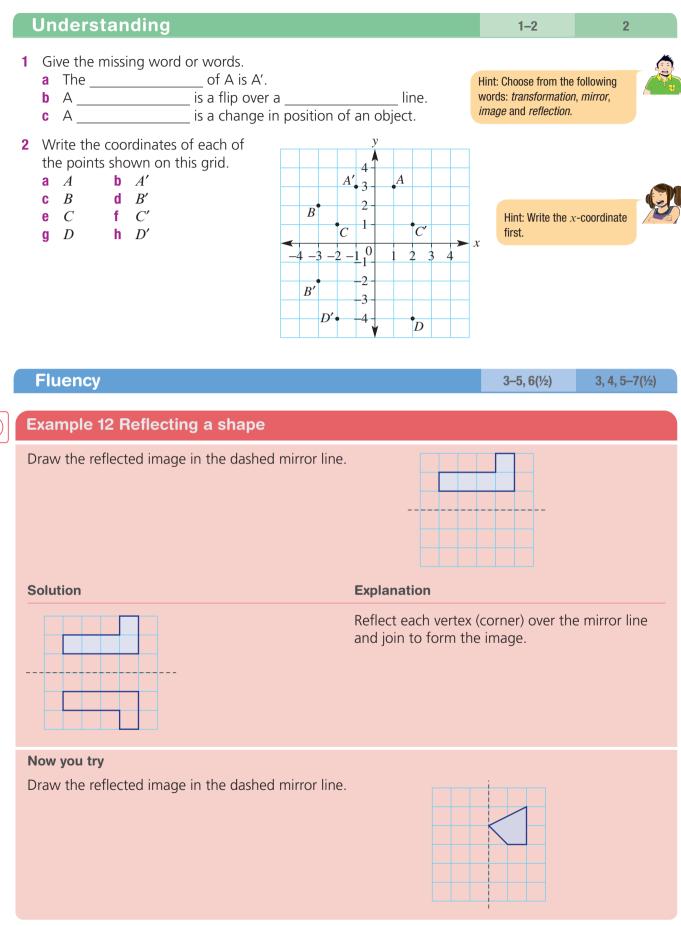


mirror line

We can use coordinates on the number plane to pinpoint an image after transformation.

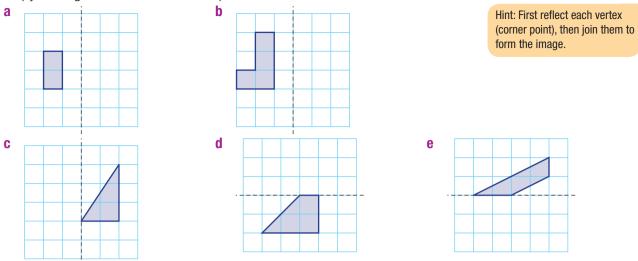


Exercise 9F



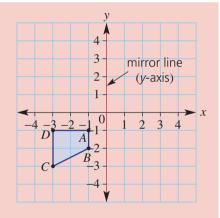
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ISBN 978-1-108-87846-3 © Greenwood et al. 2021 Cambridge University Press Photocopying is restricted under law and this material must not be transferred to another party. **3** Copy each grid and reflect the shape in the mirror line.

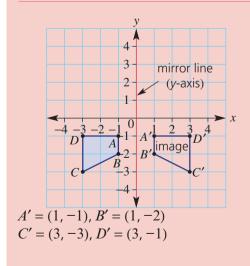


Example 13 Drawing reflections on a number plane

Draw the reflected image of this shape and give the coordinates of A', B', C' and D'. The y-axis is the mirror line.



Solution



Explanation

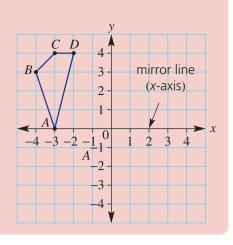
Reflect each vertex A, B, C and D about the mirror line. The line segment from each point to its image should be at 90° to the mirror line.

Continued on next page

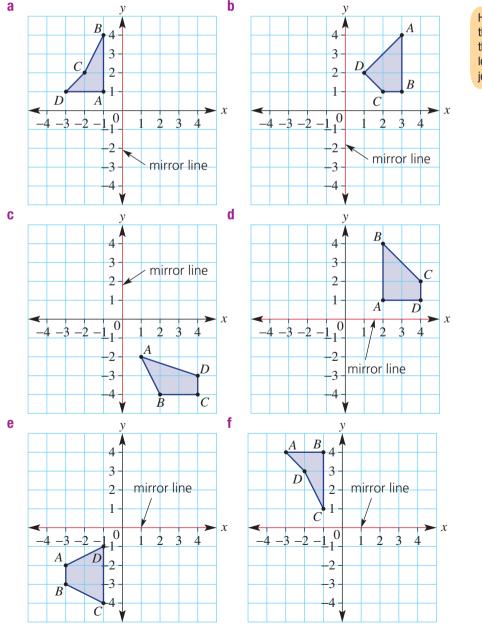
9**F**

Now you try

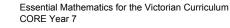
Draw the reflected image of this shape and give the coordinates of A', B', C' and D'. The x-axis is the mirror line.



- 4 Is the size and shape of an object changed after a reflection?
- **5** Draw the image of each shape and give the coordinates of A', B', C' and D'.



Hint: Reflect point A in the mirror line and label the image A'. Repeat to locate B', C' and D' then join the image points.

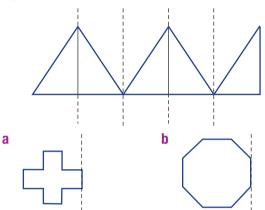


9–11

6	Write the coordin	ates of the followi	ng points after reflect	tion in the <i>x</i> -axis.	Hint: Reflection in the <i>x</i> -axis	
	a (2, 5)	b (4, 1)	c (-3, 2)	d (-3, 4)	is a vertical transformation.	
	e (0, -4)	f (3, 0)	g (-2,0)	h (-6, -10)		
7	Write the coordin	ates of the followi	ng points after reflect	tion in the <i>y</i> -axis.	Hint: Reflection in the <i>y</i> -axis	
	a (3, 2)	b (7, 1)	c (-2, 4)	d (-4, 6)	is a horizontal transformation.	
	e (0,7)	f (-4, 0)	g (-4, -6)	h (0, -3)		

Problem-solving and reasoning

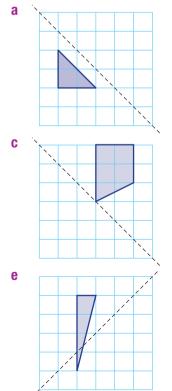
8 By repeatedly reflecting a shape over a moving mirror line, patterns can be formed. For example, the triangle below is reflected 4 times by placing the mirror line vertically and on the right side each time. Create a pattern using these starting shapes by repeatedly placing the vertical mirror line on the right side.

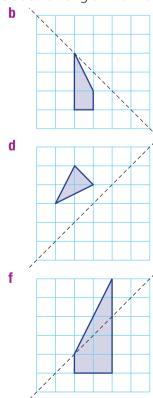


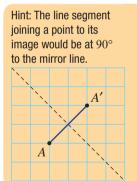
c Create your own pattern using reflection.

8,9

9 The mirror lines on these grids are at a 45° angle. Draw the reflected image.







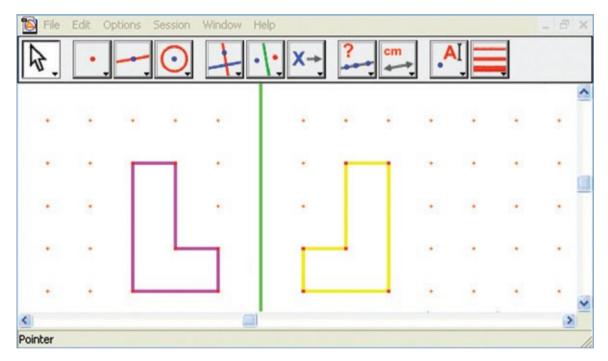
- 10 On the number plane, the point A(-2, 5) is reflected in the x-axis and this image point is then reflected in the y-axis. What are the coordinates of the final image?
- 11 What are the coordinates of the image of the point (2, 3) when it is reflected in the line which passes through these pairs of points?
 - **a** (0, -2) and (0, 4)
 - **b** (1, -3) and (1, 2)
 - **c** (−2, −4) and (−2, 1)
 - **d** (-2, 0) and (2, 0)
 - **e** (−3, 1) and (4, 1)
 - f (-1, -5) and (4, -5)

Dynamic geometry exploration

12 Try reflecting shapes using dynamic geometry software.

- a On a grid, create any shape using the polygon tool.
- **b** Construct a mirror line.
- **c** Use the reflection tool to create the reflected image about your mirror line.
- **d** Drag the vertices of your original shape and observe the changes in the image. Also try dragging the mirror line.

12



9F

9G Rotation

Learning intentions

- To understand that a shape can be rotated to give an image. •
- To be able to draw the result of a point or shape being rotated about a point. •

Key vocabulary: rotation, centre point, transformation, image, angle, clockwise, anticlockwise

We know that rotational symmetry involves turning a shape around its centre. Rotation can also involve moving a shape around a centre of rotation that is outside the shape. This type of transformation still results in an image that is the same size and shape as the original.

Lesson starter: Rotation on a grid

Look at the shape on the grid. Draw the image after rotating the shape about point O by:

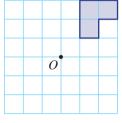
180° 90° clockwise 90° anticlockwise

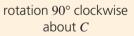
(Anticlockwise means going around a circle in the opposite direction from clockwise.)

Discuss what method you used to draw each image. What is the relationship between the position of the shape and its image after each rotation?

Key ideas

- Rotation is a transformation which involves a turn of every point on a shape about a given point.
- A rotation involves a **centre point** of rotation (*C*) and an **angle** of rotation, as shown.
 - A pair of compasses can be used to draw each circle, to help find the position of image points.





2

1,2

900

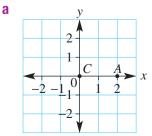
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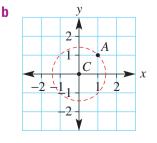
Exercise 9G

Understanding

1 Give the coordinates of the point A and its image A' after rotation about point C(0,0) by: ii 180° anticlockwise iii 90° clockwise iv 90° anticlockwise

180° clockwise i.





2 Is the size and shape of an object changed after a rotation?

9G Fluency 3, 4 3–5 **Example 14 Rotating a point** Give the coordinates of the image of the point (2, 3) after each of the following rotations about the origin (0, 0). a 90° clockwise **b** 90° anticlockwise **c** 180° Solution **Explanation** a (3, -2)Plot the point (2, 3). Use a pair of compasses to draw a circle through the point. 4 Draw a line interval from (2, 3) to the origin. (2, 3)3 Measure 90° clockwise from the interval. 2 Plot the image point. clockwise 0 Ż 2 (3', -2)-3 **b** (-3, 2)Use similar steps in the opposite direction. anticlockwise 4 (2, 3)3 (-3, 2)2 0 2 3 .3 Δ -2 -3 Rotating 180° in either direction gives the same **c** (-2, -3) image point. anticlockwise 4 (2, 3)3 2 1 X 3 2 3 4 clockwise

Now you try

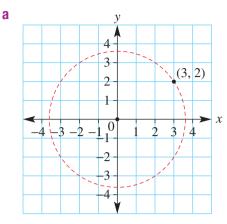
Give the coordinates of the image of the point (1, 4) after each of the following rotations about the origin (0, 0).

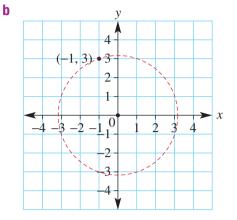
a 90° clockwise

b 90° anticlockwise

C 180°

- **3** Give the coordinates of each of the following points after rotation about the origin (0, 0) by:
 - i 90° clockwise
 - ii 90° anticlockwise
 - **iii** 180°

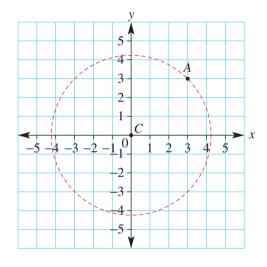




- 4 Give the new coordinates of the image point A' after point A has been rotated around point C(0, 0) by:
 - a 180° clockwise
 - **c** 90° anticlockwise
 - e 360° anticlockwise



- d 270° clockwise
- f 180° anticlockwise

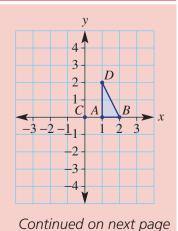


Example 15 Drawing rotations of shapes

Draw the image of this shape and give the coordinates of A', B' and D' after carrying out the following rotations.

- a 90° anticlockwise about C
- **b** 180° about C

Þ)



Essential Mathematics for the Victorian Curriculum CORE Year 7

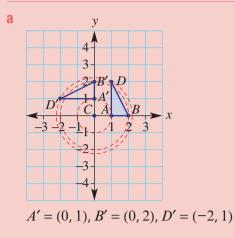
ISBN 978-1-108-87846-3 © Greenwood et al. 2021 Cambridge University Press Photocopying is restricted under law and this material must not be transferred to another party.

Hint: First draw a line interval between the point and (0, 0).



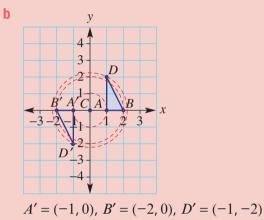
9**G**





Explanation

Rotate each point on a circular arc around point C by 90° anticlockwise.

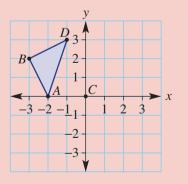


Rotate each point on a circular arc around point C by 180° in either direction.

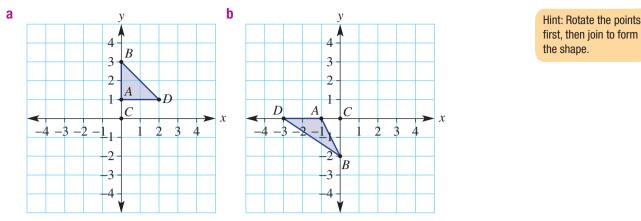
Now you try

Draw the image of this shape and give the coordinates of A', B' and D' after carrying out the following rotations.

- a 90° clockwise about C
- **b** 180° about C

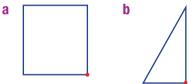


5 Draw the image of each shape and give the coordinates of A', B' and D' after the following rotations.
i 90° anticlockwise about C ii 180° about C iii 90° clockwise about C



Problem-solving and reasoning

6 By repeatedly rotating a shape about a point, patterns can be formed. This diagram shows a semicircle rotated by 90° three times about the given point. Use the shapes below and create a pattern using three 90° rotations about the given point.



- **c** Draw a shape and create your own pattern using rotation.
- 7 The point B(2, 3) is rotated about the point C(1, 1). State the coordinates of the image point B' for the following rotations.

С

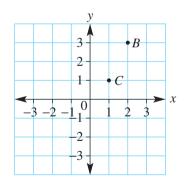
a 180°

- **b** 90° clockwise
- c 90° anticlockwise

d

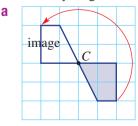
6,7

6–10

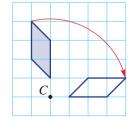


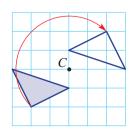
8 How many degrees has each shape been rotated, and in which direction?

b



	С		



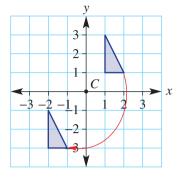


Hint: Pick a vertex and identify its image. Draw a line interval joining the vertex to point C, and another joining its image to point C. Then measure the angle between the two intervals.



9G

- **9** Write the missing number in these sentences.
 - **a** Rotating a point 90° clockwise is the same as rotating a point _____ anticlockwise.
 - **b** Rotating a point 38° anticlockwise is the same as rotating a point clockwise.
 - **c** A point is rotated 370° clockwise. This is the same as rotating the point _____ clockwise.
- **10** Explain what is wrong with this 180° rotation about C(0, 0).

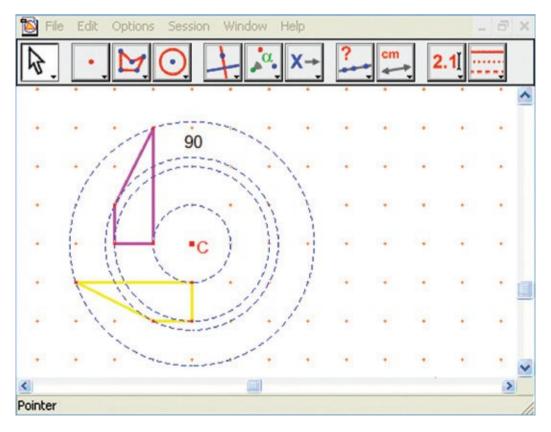


Dynamic geometry exploration

- **11** Try rotating shapes using dynamic geometry software.
 - **a** On a grid, create any shape using the polygon tool.
 - **b** Construct a centre of rotation point and a rotating angle (or number). In Cabri, use the Numerical Edit tool to create a dynamic number.

11

- **c** Use the rotation tool to create the rotated image that has your nominated centre of rotation and angle. You will need to click on the shape, the centre of rotation and your angle.
- **d** Drag the vertices of your original shape and observe the changes in the image. Also try changing the angle of rotation.



9H Translation

Learning intentions

- To understand that a shape can be translated left, right, up or down.
- To be able to draw the result of a point or shape being translated in a given direction.
- To be able to describe a translation given an original point and an image point.

Key vocabulary: translation, shift, transformation, image

Along with rotation and reflection, a third important transformation that does not change the shape or size of the image is called translation. Translation involves a shift in an object left, right, up or down. The orientation of a shape is also unchanged.

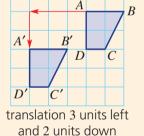
Lesson starter: City grid

Imagine that a point A on a simple city grid map is your starting point, and point B is your destination.

- Describe one simple way of travelling from A to B.
- Describe two other ways of travelling from A to B.
- How many different ways are there if no section can be travelled more than once?

Key ideas

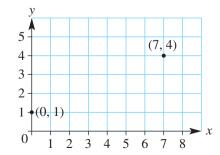
- Translation is a transformation involving a shift to the left, right, up or down.
 - Describing a translation involves saying how many units a shape is shifted left or right and/or up or down.



Exercise 9H

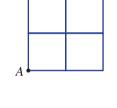
Understanding

- **1** The point (7, 4) is translated to the point (0, 1).
 - a How many units to the left has the point been translated?
 - **b** How many units down has the point been translated?
 - **c** If the point (0, 1) is translated to (7, 4):
 - i how many units to the right has the point been translated?
 - ii how many units up has the point been translated?



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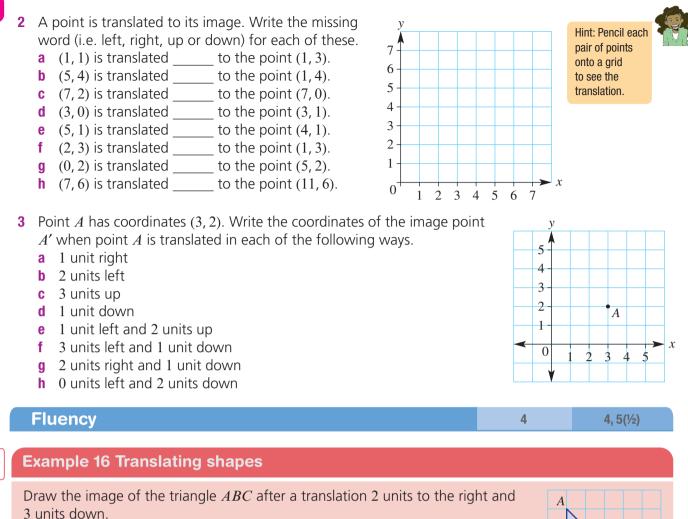


R



3





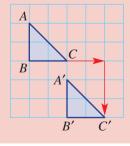


Explanation

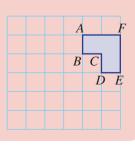
Shift each vertex 2 units to the right and 3 units down. Then join the vertices to form the image.

R

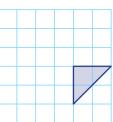
C



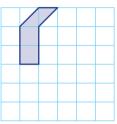
Now you try Draw the image of the shape *ABCDEF* after a translation 3 units left and 2 units down.



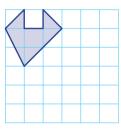
- 4 Draw the image of these shapes after each translation.
 - **a** 3 units left and 1 unit up



c 3 units right and 2 units down



e 2 units right and 3 units down



- 5 Point A has coordinates (-2, 3). Write the coordinates of the image point A' when point A is translated in each of the following ways.
 - a 3 units right
 - **b** 2 units left
 - **c** 2 units down
 - d 5 units down
 - e 2 units up
 - f 10 units right
 - **g** 3 units right and 1 unit up
 - **h** 4 units right and 2 units down
 - i 5 units right and 6 units down
 - j 1 unit left and 2 units down
 - **k** 3 units left and 1 unit up
 - 1 2 units left and 5 units down

Problem-solving and reasoning

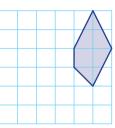
6 If only horizontal or vertical translations are allowed, how many different paths are there from points *A* to *B* on each grid below? No point can be visited more than once.



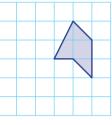
- **b** 1 unit right and 2 units up
- Hint: First translate each corner, then join the points to form the image.

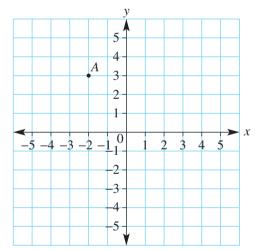


d 4 units left and 2 units down



f 3 units left and 1 unit down





6–9

6,7

9H

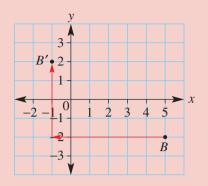
Example 17 Describing translations

A point B(5, -2) is translated to B'(-1, 2). Describe the translation.

Solution

Explanation

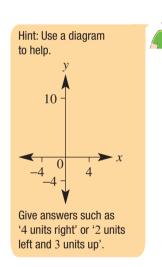
Translation is 6 units left and 4 units up.



Now you try

A point D(-4, 2) is translated to D'(1, -3). Describe the translation.

- 7 Describe the translation from each point to its image.
 - **a** A(1,3) is translated to A'(1,6).
 - **b** B(4,7) is translated to B'(4,0).
 - **c** C(-1, 3) is translated to C'(-1, -1).
 - **d** D(-2, 8) is translated to D'(-2, 10).
 - **e** E(4, 3) is translated to E'(-1, 3).
 - **f** F(2, -4) is translated to F'(4, -4).
 - **g** G(0, 0) is translated to G'(-1, 4).
 - **h** H(-1, -1) is translated to H'(2, 5).
 - i I(-3, 8) is translated to I'(0, 4).
 - **j** J(2, -5) is translated to J'(-1, 6).
 - **k** K(-10, 2) is translated to K'(2, -1).
 - L(6, 10) is translated to L'(-4, -3).



- 8 The point *A* is translated to its image, *A*'. Describe the translation that takes *A*' to *A* (i.e. the reverse translation), then do the same for *B*', *C*' and *D*'.
 - **a** A(2, 3) and A'(4, 1)
 - **b** B(0, 4) and B'(4, 0)
 - **c** C(0, -3) and C'(-1, 2)
 - **d** D(4, 6) and D'(-2, 8)
- **9** If only horizontal and vertical translations are allowed, how many different paths are there from point *A* to point *B*? No section can be used more than once in each path.



10



Combined transformations

- **10** Write the coordinates of the image point after each sequence of transformations. (Apply each transformation to the image of the previous transformation.)
 - **a** (2, 3)
 - reflection in the *x*-axis
 - reflection in the *y*-axis
 - translation 2 units left and 2 units up
 - **b** (-1, 6)
 - translation 5 units right and 3 units down
 - reflection in the *y*-axis
 - reflection in the *x*-axis
 - **c** (-4, 2)
 - rotation 180° about (0, 0)
 - reflection in the *y*-axis
 - translation 3 units left and 4 units up



9I Drawing solids

Learning intentions

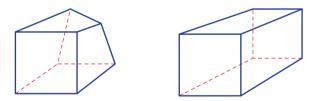
- To be able to draw pyramids, cylinders and cones.
- To be able to use square or isometric dot paper to accurately draw solids.
- Key vocabulary: cube, prism, pyramid, cylinder, cone, square dot paper, isometric dot paper

Three-dimensional solids can be represented as a drawing on a two-dimensional surface (such as paper or a computer screen), provided some basic rules are followed.



Lesson starter: Can you draw a cube?

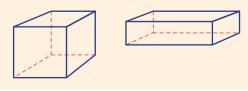
Try to draw a cube. Here are some bad examples.



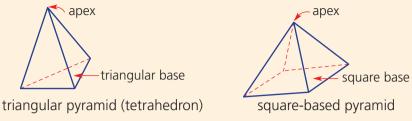
- What is wrong with these drawings?
- What basic rules do you need to follow when drawing a cube?

Key ideas

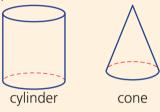
- A **cube** is a solid (3D shape) with six square faces that are congruent (the same size and shape), and a **prism** is a solid with two parallel congruent faces, joined by parallelograms (often rectangles).
- Draw cubes and rectangular prisms by keeping:
 - parallel edges pointing in the same direction
 - parallel edges the same length.



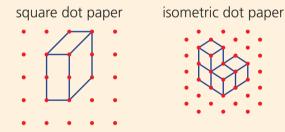
- A pyramid is a solid where the base has straight sides and the other faces are triangles meeting at a vertex (the apex).
 - Draw pyramids by joining the apex with the vertices on the base.



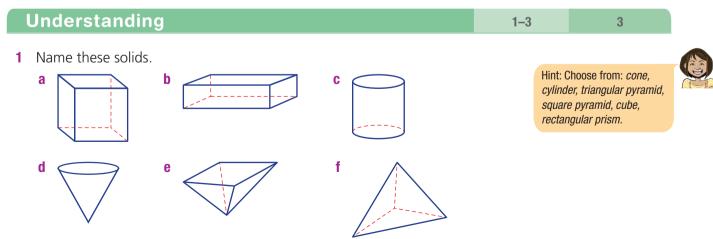
- Draw **cylinders** and **cones** by starting with an oval shape.
 - A cylinder is a solid with two circular faces joined by a curved surface.
 - A cone is a solid with a circular base and a slanting curved surface that tapers to a point called the apex.



• **Square and isometric dot paper** can help you to draw solids accurately. Drawings made on isometric dot paper clearly show the cubes that make up the solid.



Exercise 91



91







3 Cubes are stacked to form these solids. How many cubes are there in each solid?



Fluency

а

4–6

4, 5



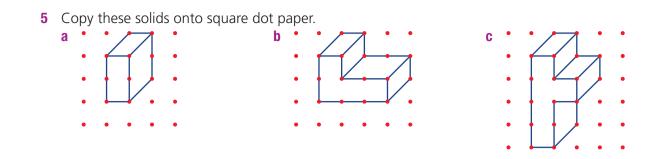
Draw these solids.

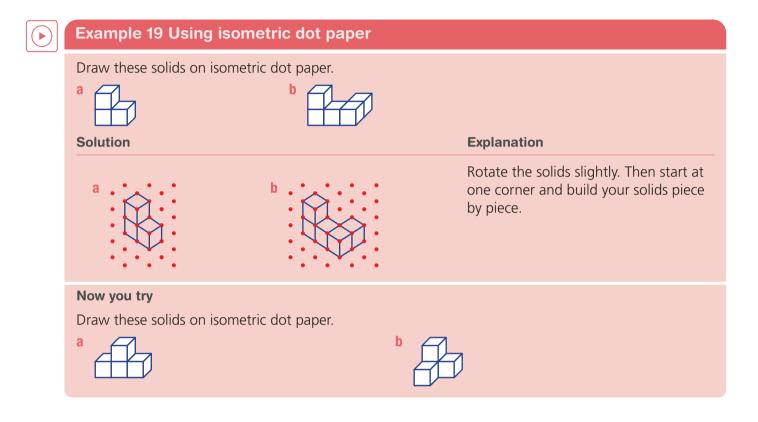
- a A cube
- b A cone
- c A square-based pyramid

Solution	Explanation		
a	Draw the square front. Draw edges parallel to the top and the right edge. Connect using dashed lines for hidden edges.		
b	Draw an oval shape for the base. Draw the apex point above the centre of the oval. Join the apex to the sides of the base and erase part of the oval to create a dashed (hidden) curve.		
c	Draw a rhombus for the base. Pick a central point above the base for the apex, then connect. Change hidden edges to dashed lines.		
Now you try			
Draw these solids. a Cylinder	b Rectangular prism		
 On plain paper, draw an example of these common solids. Cuba 			

- a Cube
- **c** Triangular-based pyramid
- e Rectangular prism

- **b** Cylinder
- d Cone
- f Square-based pyramid

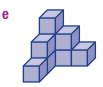




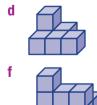
6 Draw these solids on isometric dot paper.



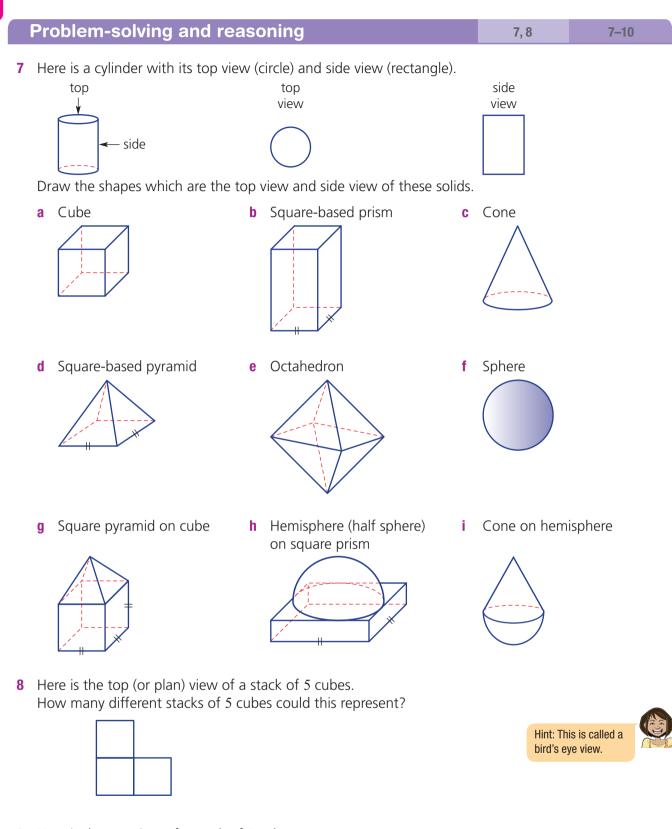




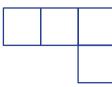






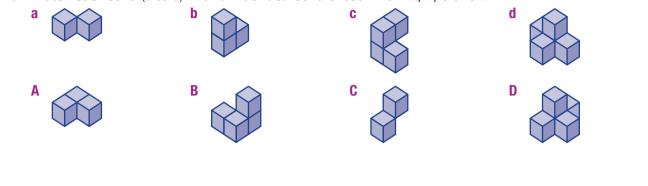


9 Here is the top view of a stack of 7 cubes. How many different stacks of 7 cubes could this represent?



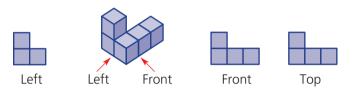
11

10 Match each solid (a to d) with an identical solid chosen from A, B, C and D.



3 view points

11 These diagrams show the front and left views of a solid.

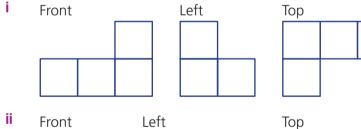


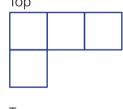
a Draw the front, left and top views of these solids.





b Draw the solid that has these views.





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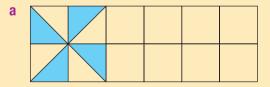
Maths@Work: Quilting

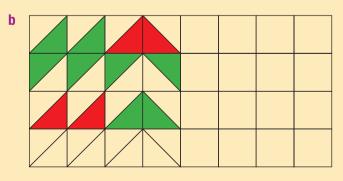
A home-based hobby can become a successful small business. Many communities run markets which are a great way for creative people to sell their handmade items.

Various crafts require an understanding of mathematics. The type of maths needed is dependent on the product created. Designing and making a quilt is a technical process which requires accurate measuring and an understanding of shapes and transformations. Also, an ability to select appealing colour combinations is useful.

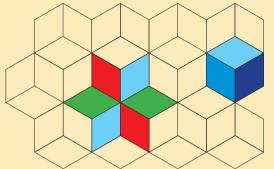


- 1 Understanding the properties of triangles and quadrilaterals is important in quilt design. Many standard quilt patterns use squares and triangles.
 - **a** State the properties of a right-angled isosceles triangle.
 - **b** List the names of the quadrilaterals that have at least one line of symmetry.
 - **c** Show three ways that a square can have exactly half of its area shaded. A rotation doesn't count as a different method.
- **2** Below are some quilting designs that have been started. Using grid paper, copy and complete each design.

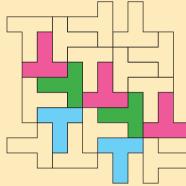




- **3** For each illustration, explain how the shapes are transformed.
 - a Rhombus shapes transformed:



- blue to the blue opposite (in the red/blue/green star) i.
- ii blue to green to red (in the red/blue/green star)
- iii light-blue to mid-blue to dark-blue (in the right side blue hexagon)
- **b** T shapes transformed:



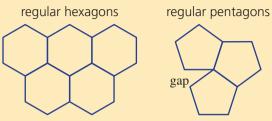
- pink to the next pink i.
- ii pink to green
- iii pink to blue
- 4 For each quilt design below:
 - i count how many lines of symmetry there are in the design
 - ii state the order of rotational symmetry
 - iii state the types of transformations applied to repeated shapes

b





- **5** Quilts are often designed using a tessellation pattern. A tessellation has polygons joined together on a flat surface without any gaps. Polygons that can tessellate have interior angles that divide evenly into a revolution (360°).
 - **a** Find the interior angles in regular hexagons and pentagons and show why one of these shapes can tessellate and why the other shape cannot tessellate.



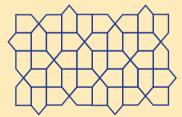
- **b** A popular design has a pinwheel pattern inside squares as shown in this photo of a quilt.
- i What type of triangle has been tessellated to make the pinwheel? Draw and label this triangle.

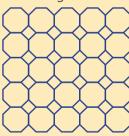


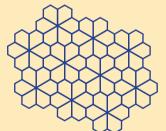
ii Describe the transformations of a triangle that are seen in the pinwheel design.

Using technology

6 Using a geometry application, design and colour your own quilt tessellation pattern. You may wish to use one of the following tessellations.







- 1 Use six matchsticks to create four equilateral triangles. Draw your creation.
- 2 How many equilateral triangles of any size are in this diagram?

- **3** A regular octahedron has its corners cut off. How many edges are there on the new shape?
- 4 A polygon's vertices are joined by diagonals. Without counting them, work out how many diagonals can be drawn in each of these polygons.
 - a Quadrilateral

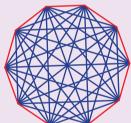
cubes were used?

- \bigoplus
- **b** Heptagon

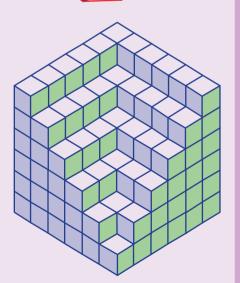
5 This solid was made from stacking 1 cm cubes. How many



c Decagon (10 sides)

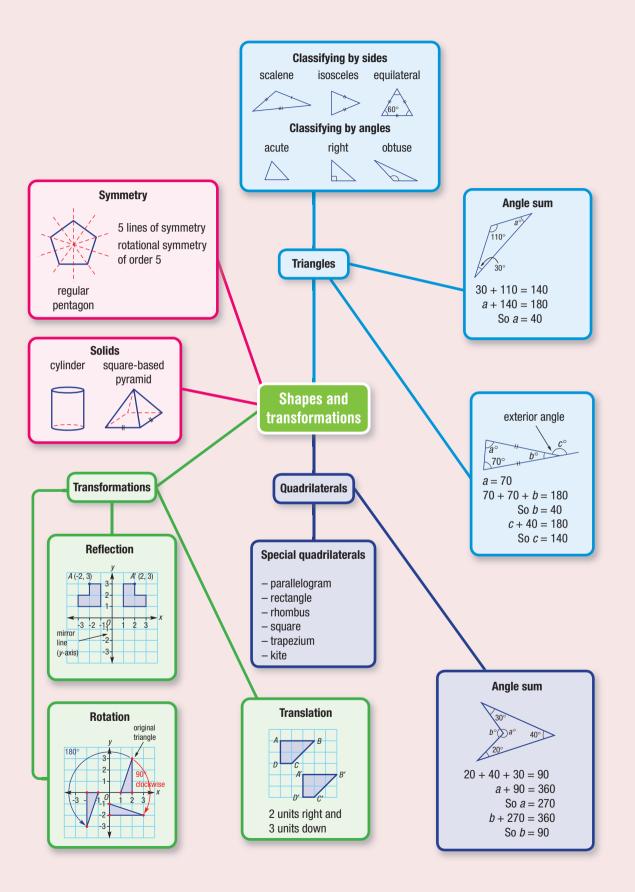


Hint: Use three dimensions.

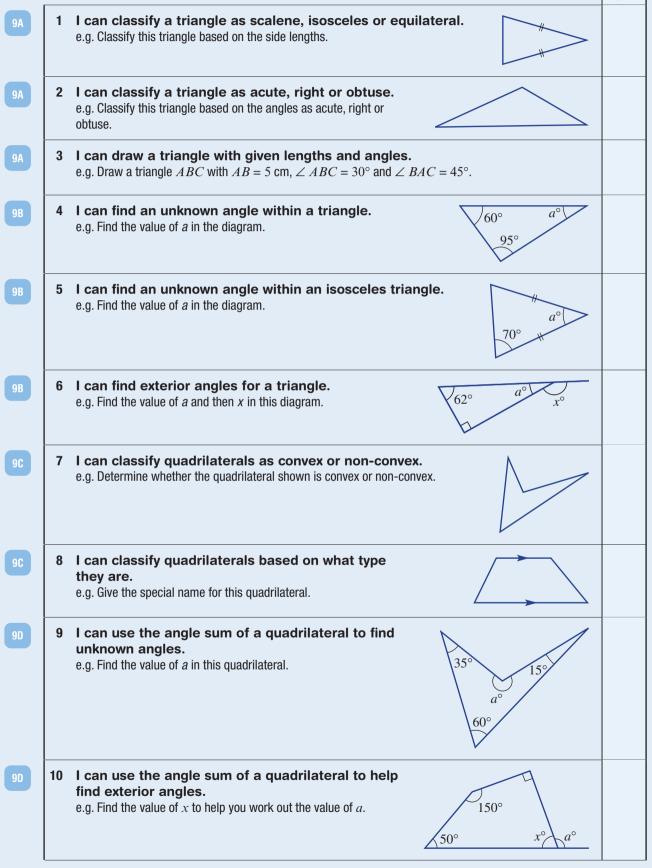


6 Make your own solid out of 1 cm cubes. Draw the solid on isometric dot paper. Add shading to enhance the 3D effect.

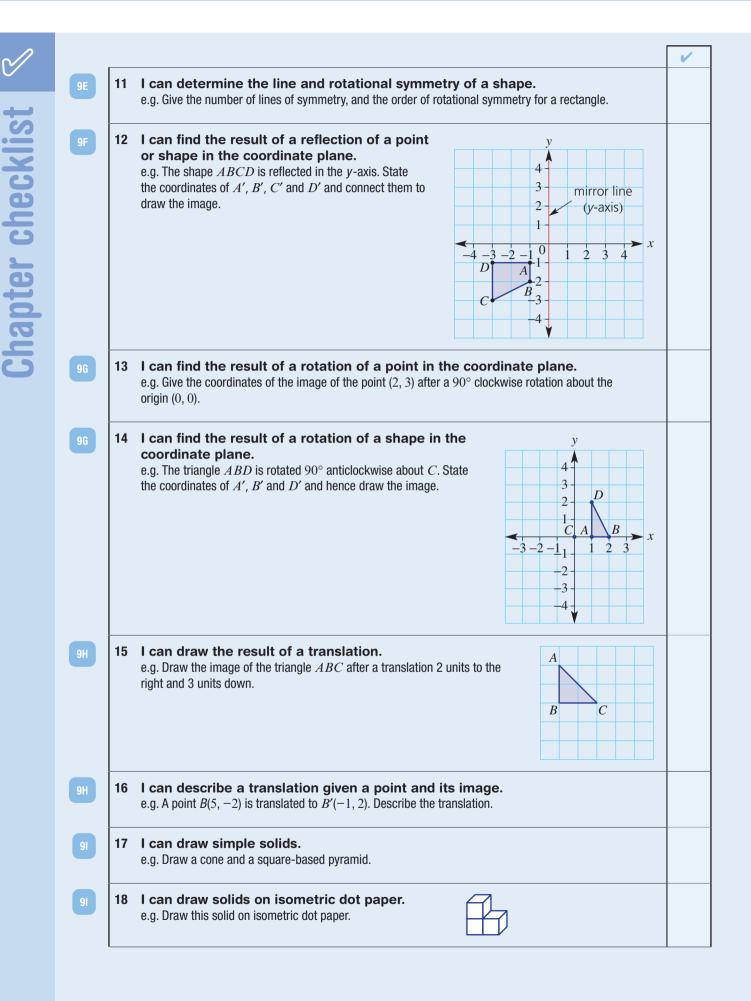




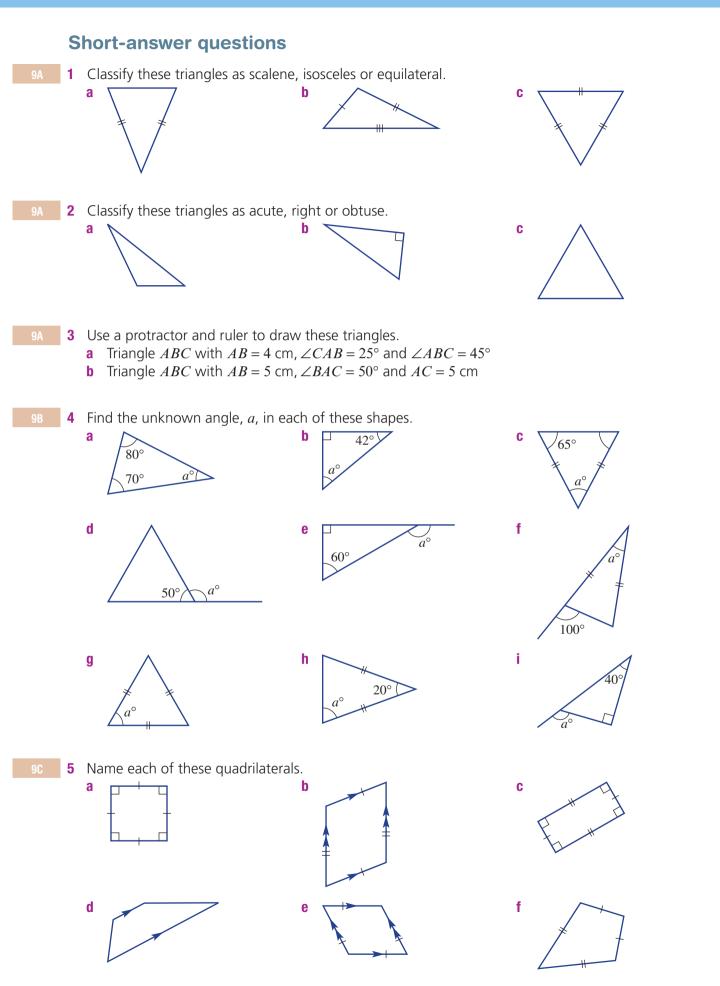
A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook. .



Chapter checklist

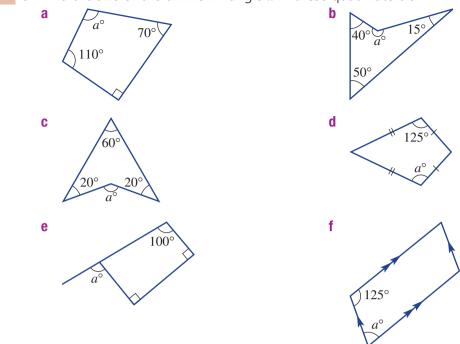




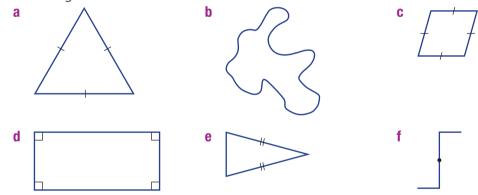


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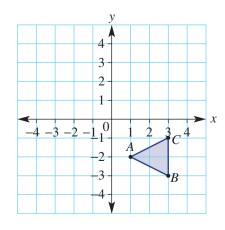
6 Find the size of the unknown angle *a* in these quadrilaterals.



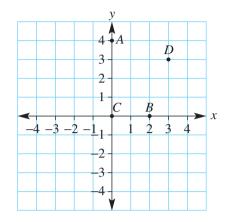
9 7 Give the number of lines of symmetry and the order of rotational symmetry for each of the following.



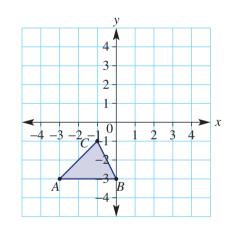
- **9F** 8 Write the coordinates of *A*', *B*' and *C*' when the triangle *ABC* is reflected in the following mirror lines.
 - a The y-axis
 - **b** The *x*-axis



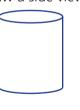
- Points A(0, 4), B(2, 0) and D(3, 3) are shown here. Write down the coordinates of the 9 image points A', B' and D' after each of the following rotations.
 - 180° about *C*(0, 0) а
 - 90° clockwise about C(0, 0)b
 - 90° anticlockwise about C(0, 0)С



- **10** Write the coordinates of the vertices A', B' and C' after each of these translations.
 - a 4 units right and 2 units up
 - **b** 1 unit left and 4 units up

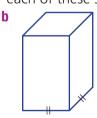


11 Draw a side view and top view for each of these solids.



a

CORE Year 7



12 Draw this solid on isometric dot paper.

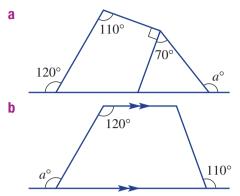


Chapter review

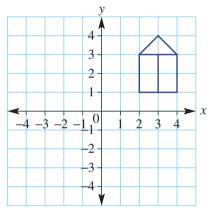
Multiple-choice questions 1 An equilateral triangle has: A each interior angle equal to 90° **B** a pair of equal sides **C** two pairs of equal opposite angles **D** one obtuse angle **E** each interior angle equal to 60° The three types of triangles all classified by their interior angles are: 2 A acute, isosceles and scalene B acute, right and obtuse **C** scalene, isosceles and right D right, obtuse and scalene E acute, equilateral and right Two angles inside an isosceles triangle are both 70°. The third angle is: 3 70^c 70° 30° **C** 40° Α В D 20° Е 180° 70° The angle sum of a triangle is always: 4 **A** 120° **B** 360° 180° **C** 270° D Ε 90° **5** For this triangle, which of the following is true? **A** a + 50 = 180**B** a + 6 = 36050° **C** a+b=180**D** b + 50 = 180**E** a+b+50 = 180The guadrilateral that has two pairs of equal sides and one pair of equal angles is called a: 6 A kite **C** rhombus **B** trapezium **D** triangle E square Three angles inside a quadrilateral add to 275°. The fourth angle is: 7 **A** 750° **B** 95° 285° **D** 125° C Е 85° How many lines of symmetry does a rhombus have? 8 **A** 0 **B** 1 C 2 **D** 3 Е 4 The point T(-3, 4) is reflected in the x-axis. The image point T' has coordinates: 9 **A** (3, 4) **B** (-3, 4)(0, 4)**D** (3, -4)E(-3, -4)**10** The translation that takes A(2, -3) to A'(-1, 1) could be described as: A 3 units left **B** 4 units up **C** 3 units left and 4 units up **D** 1 unit right and 2 units down

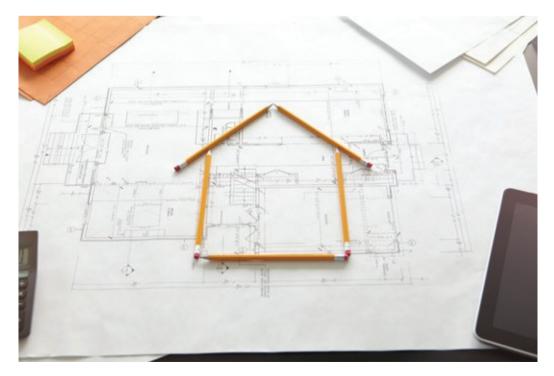
Extended-response questions

1 Here are two designs for a new city sculpture. Can you help the designers find the value of a?



- 2 Look at this drawing of a simple house. Draw the image of the house after these transformations: translation 5 units left and 4 units down
 - а
 - reflection in the *x*-axis b
 - rotation 90° anticlockwise about C(0, 0)C





Chapter Equations

A

Essential mathematics: why skills for solving equations are important

Solving equations is a skill underlying a range of occupations, including the trades, professions, manufacturing and business.

- Businesses solve equations to determine the number of sales needed to start making a profit. For example, finding the numbers of beef cattle sold, or kilograms of wool produced, or pizzas delivered, or new car sales, required to make a profit.
- Construction workers, such as engineers, builders, concreters and roofers, can solve equations to find the time a job will take, the cost of materials and possible profit.
- Advertising agents solve an equation to calculate the cost per click for running an online ad.
- Nurses use formulas to calculate medication amounts. For a child A years old, Young's formula

calculates the dose $C = \frac{A}{A+12} \times D$, where D is the adult dose.

10

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1. 2

18

A



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In this chapter

- **10A Introduction to equations**
- 10B Solving equations by inspection (Consolidating)
- 10C Using backtracking to solve equations
- 10D Using the balance method to solve equations
- 10E Equations with fractions 🔶
- 10F Formulas 🔶
- 10G Applications of equations 🔶

Victorian Curriculum

NUMBER AND ALGEBRA Linear and non-linear relationships

Solve simple linear equations (VCMNA256)

© Victorian Curriculum and Assessment Authority (VCAA)

Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

1	Fill in each missing number. a $7+5=$ c $2 \times 8=$		3 + 12 = 19 - 12 =
2	Fill in the missing numbers.		
	a $-+3 = 10$	b	50 = 30
	c $+3 = 19$	d	$100 \div \square = 20$
3	If $\Box = 5$, state whether each of these equations	s is	true or false.
	a $-2 = 5$	b	\sim 3 = 15
	c $20 \div 4 =$	d	7 × 🗌 = 42
4	If $a = 3$, find the value of:		
	a <i>a</i> + 4	b	8 - a
	$a \times 5$	d	<i>a</i> +21
5	If $n = 6$, state the value of: a $n \div 2$ c $8 - n$		$n \times 4 + 3$ $12 \div n + 4$

- 6 The expression *n* + 3 can be described as 'the sum of *n* and 3'. Match the descriptions (**a**–**c**) with the expressions (**A**–**C**):
 - a the sum of k and 5A 2pb double pB 7y
 - **c** 7 lots of y **C** k + 5
- 7 Copy and complete the tables.

а	n	1	2	3	4	5
	5 × <i>n</i>	5				
b	n	2	4	6	8	10
	<i>n</i> – 2					
C	n	1	2	5	8	9
	2 <i>n</i>					

- 8 Match each of the following operations (a–d), with its opposite operation (A–D).
 - a × A + b + B -
 - **c** ÷ **C** ×
 - d D ÷
- **9** Find each of the following.
 - **a** The sum of 15 and 12
 - **b** The product of 8 and 5
 - **c** Triple 6
 - d Double 8, then add 10
 - e 12 more than 5
 - f 20 divided by 5, then add 10
 - g Add 10 to 20, then divide that answer by 5
- 10 a If Mia is 12 years old and Oliver is 15 years old, what will their ages be in 5 years' time?b Ethan is paid \$7 per hour for mowing lawns. How much would he earn in 4 hours?

10A Introduction to equations

Learning intentions

- To understand what an equation is.
- To be able to determine if an equation is true or false, substituting for pronumerals if required.
- To be able to write an equation given a description in words.

Key vocabulary: equation, pronumeral, left-hand side (LHS), right-hand side (RHS)

An equation is a mathematical statement with an equals sign, such as 3 + 3 = 6 or $4 \times 2 = 8$.

When we are using pronumerals, some equations can be true or false, depending on the value of those pronumerals.

For example, 5 + x = 7 would be true if x = 2, but it would be false if x = 15.



Rearrange the following five symbols to make as many different true and false equations as possible.

5, 2, 3, +, =

- Which of them are true? Which are false?
- How many true equations could you form if a subtraction sign was included?

Key ideas

- An **equation** is a mathematical statement that tells us that two things are equal.
- Equations have a left-hand side (LHS) and a right-hand side (RHS), with an equals sign in between.

2x + 3 = 4y - 2LHS RHS equals sign

• Equations can be true (e.g. 2 + 3 = 5) or false (e.g. 5 + 7 = 21).

Exercise 10A

	Understanding			1–4	4
1	 a ls 7 + 4 = 11 true or f b ls 3 × 2 = 6 true or fa c ls 6 - 1 = 2 true or fa 	llse?			
2	Classify each of these each $2+3=5$	•	c $5-1=6$	d 2+4	= 6
3	Put a number in the box a $7+2 = \square$	to make a true equation b $5 \times 3 = \square$	c $8 + \square = 10$	d 2 × [] = 20
4	If k is 5, what is the value	le of $4 + k$?			



10A

Fluency		5, 6(1⁄2), 7, 8	5, 6(½), 7–9		
Example 1 Classi	fying equations involving a pronu	meral			
If k is 5, is $4 + k = 9$ t	rue or false?				
Solution	Explanation				
True	If k is 5, the equation become	s 4 + 5 = 9 which is true.			
Now you try					
If <i>a</i> is 7, is $a - 4 = 2$ t	If a is 7, is $a - 4 = 2$ true or false?				
 5 a If x is 2, is 10 + b If y is 10, is y + 	x = 12 true or false? 3 = 16 true or false?				
Example 2 Class	ifying equations by comparing sid	les			

State whether the following equations are true or false.

a $10 + 15 = 30 - 5$	b $2+5+6=10-3$
Solution	Explanation
a True	LHS (left-hand side) is 25. RHS is 25. So LHS = RHS therefore the equation is true.
b False	LHS = 13 and RHS = 7. They are different so the equation is false.

b $12 \div 4 + 2 = 20 \div 4$

Now you try

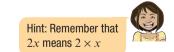
State whether the following equations are true or false.

a $6 \times 3 = 12 + 5$

6 For each of the following equations, state whether it is true or false.

a $3 \times 2 = 5 + 1$	b $100 - 90 = 2 \times 5$	c $30 \times 2 = 32 + 5$
d $12 - 4 = 4$	e $2(3-1) = 4+2$	f $5 - (2 + 1) = 7 - 4$
g $2 = 17 - 14 - 1$	h $10 + 2 = 12 - 4$	$2 \times 3 = 1 + 2 + 3$

7 If x = 3, state whether each of these equations is true or false. **a** 5+x=7 **b** x+1=4 **c** 13+x=10 **d** 6=2x



- 8 Consider the equation 4 + 3x = 2x + 9.
 - **a** If x = 5, state the value of the left-hand side (LHS).
 - **b** If x = 5, state the value of the right-hand side (RHS).
 - **c** Is the equation 4 + 3x = 2x + 9 true or false when x = 5?

9 If b = 4, state whether each of the following equations is true or false.

a
$$5b+2=22$$

b $10 \times (b-3) = b+b+2$
c $12-3b=5-b$
d $b \times (b+1) = 20$



13

Problem-solving and reasoning 10, 11 10-12 **Example 3 Writing equations from a description** Write equations for each of the following. a The sum of x and 5 is 22. **b** A deck of cards costs x. The cost of 7 decks is \$91. **c** Priya's age is currently *j*. In 5 years' time her age will equal 17. **Solution Explanation** a x + 5 = 22The sum of x and 5 is written x + 5. **b** 7x = 917x means $7 \times x$ and this number must equal the total cost. We don't include the \$ sign in an equation. In 5 years' time Priya's age will be 5 more than her current c i + 5 = 17age, so j + 5 must be 17. Now you try Write equations for each of the following. a The product of 3 and y is 36. **b** A packet of chips costs \$*d*. The cost of 4 packets is \$3.20 **c** I am currently x years old. Seven years ago I was 34. **10** Write equations for each of the following. Hint: sum: + **a** The sum of 3 and x is equal to 10. product: \times **b** When k is multiplied by 5, the result is 1005. doubled: $\times 2$ **c** The sum of *a* and *b* is 22. tripled: $\times 3$ **d** When *d* is doubled, the result is 78. e The product of 8 and x is 56. **f** When *p* is tripled, the result is 21. 11 Write true equations for each of these problems. You do not need to solve them. a Chairs cost \$*c* at a store. The cost of 6 chairs is \$546. **b** A plumber charges k per hour. The cost of 7 hours' work is \$567. **c** Pens cost a each and pencils cost b. Twelve pens and three pencils cost \$28 in total. **d** Amy is *f* years old. In 10 years' time her age will be 27. **12** a Find a value of *m* that would make this equation true: 10 = m + 7. Hint: For part b. there is more than one possible answer. **b** Find a possible value of k that would make this equation

Equation permutations

true: $k \times (8 - k) = 12$.

13 For each of the following, rearrange the symbols to make a true equation.

a 6, 2, 3, \times , = **b** 1, 4, 5, -, = **c** 2, 2, 7, 10, -, \div , = **d** 2, 4, 5, 10, -, \div , =

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10B Solving equations by inspection

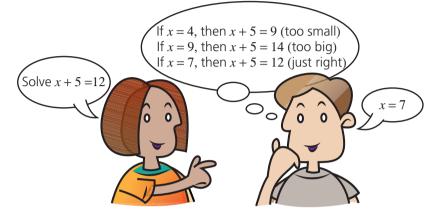


Learning intentions

- To understand that a solution to an equation is a value for the pronumeral that makes the equation true.
- To be able to use inspection (also called trial and error) to find a solution.

Key vocabulary: solving, solution, unknown, inspection, trial and error

Solving an equation involves finding the value of the variable that makes it true. Simple equations can be solved by trying different numbers until one works.



Lesson starter: Finding the missing value

- Find the missing values to make the following equations true. $16 - \square = 9$ $27 = 15 + 3 \times \square$ $2 \times \square + 4 = 17$
- Can you always find a value to put in the place of in any equation and make it true?

Key ideas

- **Solving** an equation means finding the values of any pronumerals to make the equation true.
- An unknown is a pronumeral (or variable) with a value that needs to be found in order to make an equation true.
- One method of solving equations is by inspection (also called trial and error), which involves inspecting (or trying) different values and seeing which ones make the equation true.

Exercise 10B

Understanding1-331 State whether each of the following equations is true or false.a 10+7=19b 5=12-7a 10+7=19b 5=12-7d $2+5\times3=17$ c $8\times2=3+11$ d $2+5\times3=17$ $2+5\times3=2+15$ 2 If the missing number is 5, classify each of the following equations as true or false.1-3

c $10 - \Box = 5$

a +3 = 8

- **b** $10 \times + 2 = 46$ **d** $12 = 6 + \times 2$
- **3** For the equation + 7 = 13:
 - **a** Find the value of the LHS (left-hand side) if $\Box = 5$.
 - **b** Find the value of the LHS if = 10.
 - **c** Find the value of the LHS if = 6.
 - **d** What value of would make the LHS equal to 13?

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Fluency	4-7(1/2) 4-7(1/2), 8
Example 4 Finding the missing	number
For each of these equations, find the v a $\square \times 7 = 35$ Solution	value of the missing number that would make it true. b $20 - \square = 14$ Explanation
a 5	Think: What number multiplied by 7 equals 35? $5 \times 7 = 35$ is a true equation.
b 6	Think: 20 minus what number equals 14? 20 - 6 = 14 is a true equation.
Now you try For each of these equations, find the v a $\square \div 9 = 4$	value of the missing number that would make it true. b $16 + \square = 31$
 4 Find the value of the missing number a 4+□=7 b 2×□= 5 What value should go in the box to a 12=3+□ b 5=8− 	= 12 c $\times 4 = 80$ d $- + 12 = 31$
Example 5 Solving equations b Solve each of the following equations	y inspection
a $c + 12 = 30$ b 5 Solution	b = 20 c $2x + 13 = 21Explanation$
a $c + 12 = 30$ c = 18	18 + 12 = 30 is a true equation.
b $5 \times b = 20$ b = 4	$5 \times 4 = 20$ is a true equation.
c $2x + 13 = 21$ x = 4	2x means $2 \times x$. Trying a few values: x = 10 makes LHS = $20 + 13 = 33$, which is too large. x = 3 makes LHS = $6 + 13 = 19$, which is too small. x = 4 makes LHS = 21 .
Now you try Solve each of the following equations	

Solve the following equations by inspection. 6

	5 1 5 1		
a $8 \times y = 64$	b $l \times 3 = 18$	c $4 - d = 2$	d
f $s + 7 = 19$	g $x \div 8 = 1$	h $12 = e + 4$	- i -

- **7** Solve the following equations by inspection. (See part **c** of Example 5.)
 - **a** 2p 1 = 5**b** 3p + 2 = 14**c** 4q - 4 = 8**d** 4v + 4 = 24**e** 2b - 1 = 1**q** 5g + 5 = 20**h** 3d - 5 = 13f 5u + 1 = 218 = 3m - 4
- 8 Solve the following equations by inspection. (All solutions are whole numbers between 1 and 10.)
 - **a** x = 6 x**b** $7 + x = 2 \times x$ Hint: An equation is true if its LHS and RHS are equal. **c** 10 - x = x + 2d 15 - 2x = x
 - **Problem-solving and reasoning**
- **9** Find the value of the number in each of these examples.
 - a A number is doubled and the result is 22.
 - **b** 3 less than a number is 9.
 - **c** Half of a number is 8.
 - **d** 7 more than a number is 40.
- **10** Justine is paid \$10 an hour for x hours. During a particular week, she earns \$180.
 - **a** Write an equation involving x to describe this situation.
 - **b** Solve the equation by inspection to find x.

- 11 Karim's weight is w kg and his brother is twice as heavy, weighing 70 kg.
 - **a** Write an equation involving w to describe this situation.
 - **b** Solve the equation by inspection to find w.
- 12 Yanni's current age is y years old. In 12 years' time he will be three times as old.
 - **a** Write an equation involving y to describe this situation.
 - **b** Solve the equation by inspection to find y.

Multiple variables

- 13 When multiple variables are involved, inspection can still be used to find a solution. For each of the following equations, use inspection to find one pair of values for x and y that make them true.
 - **a** x + y = 8
 - **b** x y = 2

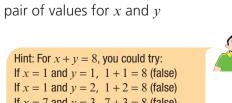
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- **c** $x \times y = 6$
- **d** $x + y = x \times y$

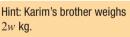
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9.10



If x = 7 and y = 3, 7 + 3 = 8 (false) Keep going until your equation is true.





13



10-12

l + 2 = 14

13 = 5 + s

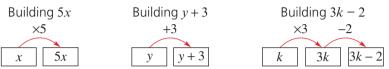
10C Using backtracking to solve equations

Learning intentions

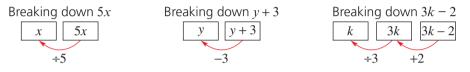
- To understand that expressions can be built from a single pronumeral by performing operations.
- To understand that an equation can be solved by performing operations in reverse.
- To be able to use backtracking to solve simple equations.

Key vocabulary: backtracking, pronumeral, expression, operation, opposite, solution

Flow charts give a systematic way to solve equations. Consider how an expression can be 'built' from a single pronumeral.

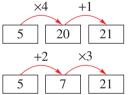


The arrows can be reversed to break down the expression and the label is changed to its opposite.



Lesson starter: 5 to 21

Starting with the number 5, you can get to the number 21 in many different ways. Two ways are shown here.



- Try to find other ways to get from 5 to 21. You can use more than two operations.
- What are some ways of getting from 21 to 5?

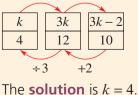
Key ideas

Expressions such as 3k - 2 can be built from a single **pronumeral**, k.



Equations can be solved by reversing the arrows in the flow chart and applying the **opposite operations** (i.e. – and +; ÷ and ×). This is called **backtracking**.

For example, to solve 3k - 2 = 10, put 10 at the right and follow the arrows to the left. ×3 -2



Exercise 10C

1 State the missing numbers in these flow charts. a $\frac{+4}{4}$ b $\frac{x^2}{1-1}$ c $\frac{+2}{4}$ c $\frac{x^3}{6}$ d $\frac{-1}{3}$ c $\frac{x^5}{5}$ 2 Copy and complete these flow charts. a $\frac{+4}{4}$ b $\frac{x^2}{6}$ for $\frac{x^2}{6}$ c $\frac{x^2}{6}$ c $\frac{x^2}{6}$ c $\frac{x^2}{6}$ c $\frac{x^2}{6}$ c $\frac{x^2}{6}$ 3 Write down the opposite of these operations. a Adding 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Multiplying by 2 b Adding 10 c Subtracting 5 d Subtracting 2 d Subtracti	Understanding	1–5	3–5
a $+4$ c -3 a $+4$ b k c -3 b k c -3 c k c -3 c k c -3 c k c	$a +4$ $3 - b \times 2$ $7 5$ $d -1 \times 5$		
a Adding 2 b Adding 10 c Subtracting 5 f Dividing by 2 b Adding 10 c Subtracting 5 f Dividing by 2 b Adding 10 c Subtracting 5 f Dividing by 2 b Multiplying by 4 f Dividing by 2 b Solution to the equation $p + 4 = 7$? Fluency 6-9 6-7(½), 8, 9 Example 6 Building an expression Use a flow chart starting with k to build the following. a $k + 12$ b 9k Solution Explanation a $+12$ Starting with k, add 12 to get $k + 12$.	a $+4$ c -3 b $\times 2$ k -3 d $\div 5$		t $k \times 2$ is
a $+3$ m m m m m m m m m m m m m m m m m m m	a Adding 2 b Adding 10 c Subtracting 5		
b What is the solution to the equation $p + 4 = 7$? c b What is the solution to the equation $p + 4 = 7$? c c e c c c c c c c c c c	a $+3$ b -2 c $\frac{k}{6}$	x 7x 21	
Example 6 Building an expressionUse a flow chart starting with k to build the following.a $k+12$ b $9k$ SolutionExplanationa $+12$ Starting with k , add 12 to get $k+12$.	$\begin{array}{c} +4 \\ \hline p \\ \hline p \\ \hline 7 \\ \hline -4 \end{array}$		
Use a flow chart starting with k to build the following. a $k + 12$ b $9k$ Solution Explanation a $+12$ Starting with k, add 12 to get $k + 12$.	Fluency	6–9	6-7(½), 8, 9
Use a flow chart starting with k to build the following. a $k + 12$ b $9k$ Solution Explanation a $+12$ Starting with k, add 12 to get $k + 12$.	Example 6 Building an expression		
SolutionExplanationa $+12$ Starting with k , add 12 to get $k + 12$.			
a $+12$ Starting with k , add 12 to get $k + 12$.	a k+12 b 9k		
	· · · · · · · · · · · · · · · · · · ·	1	
		κ + 12.	

k 9 k	Starting with k , multiply by 9 to get 9 k . Remember that 9 k means 9 × k .
Now you try	
Use a flow chart starting with y to build	d the following.
a 4 <i>y</i>	b y - 3

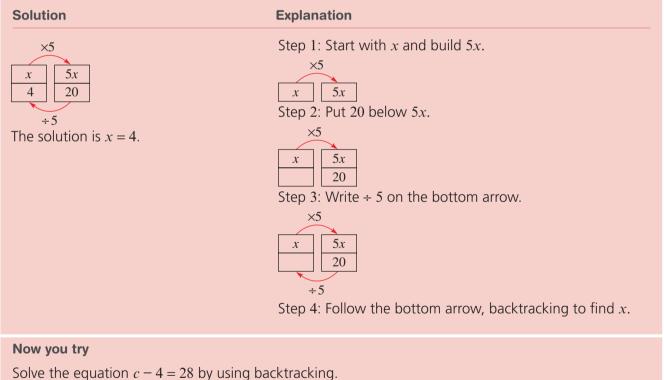
6 Use a flow chart starting with *k* to build the following.

- **a** *k*+4
- **b** 9k
- **c** k 7
- **d** k + 8

(\mathbf{b})

Example 7 Using backtracking to solve one-step equations

Solve the equation 5x = 20 by using backtracking.

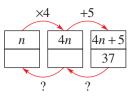


7 Solve the following equations by using backtracking.

а	5k = 30	b	2x = 20
C	a + 4 = 19	d	m - 3 = 12
е	$q \times 7 = 35$	f	p + 3 = 12

10C

- 8 a Copy and complete this flow chart for the equation 4n + 5 = 37. (Replace each question mark with the correct operation.)
 - **b** What is the solution to 4n + 5 = 37?



Example 8 Using backtracking to solve two-step equations					
Solve the equation $4x + 3$	= 23 by using backtracking.				
Solution	Explanation				
$\begin{array}{c c} x 4 & +3 \\ \hline x & 4x & 4x+3 \\ \hline 5 & 20 & 23 \\ \hline \div 4 & -3 \end{array}$ The solution is $x = 5$.	Step 1: Build $4x + 3$, starting with x . x + 3 x + 4x + 3 Step 2: Write 23 below $4x + 3$. x + 4x + 3 x + 4x + 4x + 3 Step 3: Write the opposite operations on the bottom arrows. Step 4: Follow the arrows back to x .				
Now you try					
Solve the equation $2x - 5 = 13$ by using backtracking.					

- 9 Solve the following equations by using backtracking.
 - **a** 4n + 5 = 21
 - **b** 2n + 7 = 29
 - **c** 3x 8 = 22
 - **d** 8a 4 = 60
 - **e** 2y 4 = 2
 - f 4m + 12 = 24

Problem-solving and reasoning

- **10** Ezekiel's current age is unknown. In 5 years' time he will be 18 years old.
 - **a** If *x* is Ezekiel's current age, which of the following equations can be used to describe this situation?
 - **A** x + 18 = 5
 - **B** x + 5 = 18
 - **C** $x \times 5 = 18$
 - **D** x 5 = 18
 - **b** Solve the equation above using a flow chart.
 - c How old is Ezekiel?
- **11 a** Solve the equation 4x + 192 = 340 using a flow chart.
 - **b** In what ways is using a flow chart easier than solving by inspection?



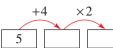
11, 12

10, 11

Hint: Solving by inspection is when you guess a sensible value for the variable and substitute to check if you were right.



- 12 Sophie thinks that it does not matter what order the arrows go in a flow chart.
 - a Prove that she is wrong by filling out these two flow charts.





b Give an example of two flow charts where the operations on the arrows are swapped but the result is the same.



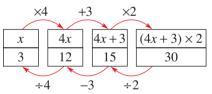
Hint: Try making a flow chart which involves addition and subtraction only.

13



Three-step equations

13 Equations with three steps can also be solved using flow charts. For example, $(4x + 3) \times 2 = 30$ can be solved as follows.

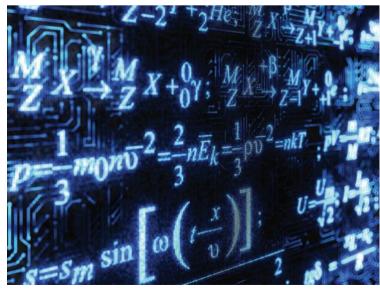


Solve the following three-step equations using flow charts.

a $(2x+5) \times 3 = 33$

b $(3m-1) \times 2 = 28$

c $(10p - 3) \times 5 = 35$



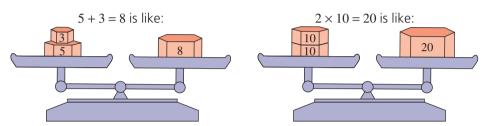
10D Using the balance method to solve equations

Learning intentions

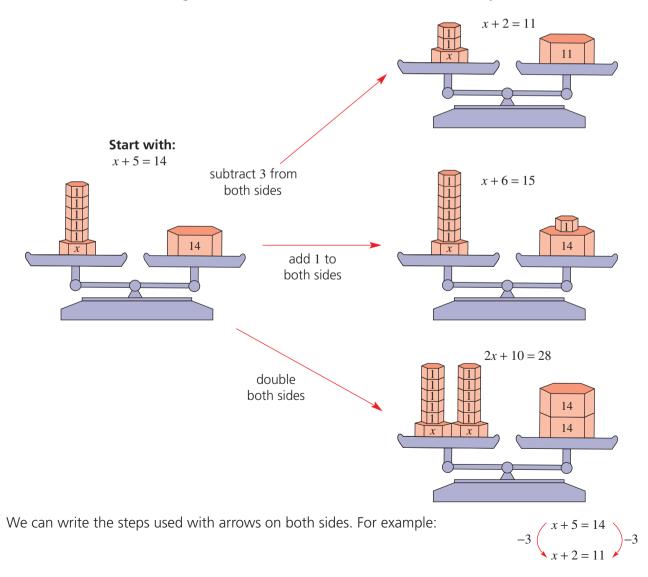
- To understand that it is possible to apply the same operation to both sides of an equation to keep it in balance.
- To understand that we can find simpler equations by using opposite operations (e.g. dividing by 3 when the pronumeral was multiplied by 3).
- To be able to solve one-step equations using the balance method.
- To be able to solve two-step equations using the balance method.

Key vocabulary: balance method, opposite operation, solution

We can think of an equation as a balanced scale, with two sides that weigh the same.



We can do the same thing to both sides of a balanced scale, and it will stay balanced.



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Lesson starter: Equations as scales

These scales show 2 + 3x = 8.

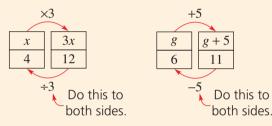
- What would the scales look like if two moved from both sides?
- What would the scales look like if the two T were removed just from the left-hand side? (Try to show whether they would be level.)
- Use scales to illustrate 2x = 12. Then show what would happen if both sides were halved.

Key ideas

To solve an equation using the **balance method**, do the same thing to both sides to find a simpler equation. For example:

$$\div 3 \begin{pmatrix} 3x = 12 \\ x = 4 \end{pmatrix} \div 3 \qquad -5 \begin{pmatrix} g + 5 = 11 \\ g = 6 \end{pmatrix} - 5$$

• Each step to be performed is like backtracking on a flow chart.



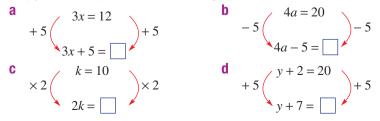
• To check a **solution**, substitute the value and see if the equation is true. e.g. LHS = $3 \times 4 = 12$ \checkmark

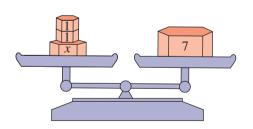
Exercise 10D

Understanding

- 1 Which one of the following equations do the scales represent?
 - **A** x + 7 = 2
 - **B** *x* = 7
 - **C** x + 2 = 7
 - **D** x 2 = 7

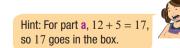
2 Copy and complete the following.





5,6

1-6



ed

10D

State whether each of the following equations is true or false. 3

a x + 4 = 7, if x = 3

- **b** b-2=7, if b=5
- **c** g + 5 = 3g, if g = 2
- **d** $f \times 4 = 20$, if f = 3
- 4 Consider the equation 7x = 42.
 - a Copy and complete the following.

$$\div 7$$
 $7x = 42$ $\div 7$

- **b** What is the solution to the equation 7x = 42?
- **5** Copy and complete the following, showing which operation was used.

a
$$\begin{pmatrix} 5+a=30\\ 2\\ a=25 \end{pmatrix}$$
?
b $\begin{pmatrix} 10b=72\\ b=7.2 \end{pmatrix}$?
c $\begin{pmatrix} 12=4c\\ 2\\ a=c \end{pmatrix}$?
d $\begin{pmatrix} 8=c-12\\ 20=c \end{pmatrix}$?

- 6 For the equation 2x = 18, write the new equation you get if:
 - **a** 2 is added to both sides
 - **b** 2 is subtracted from both sides
 - **c** both sides are doubled
 - **d** both sides are halved

Fluency

Example 9 Solving one-step equations

Solve each of the following equations using the balance method.

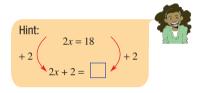
a 5x = 30**b** 17 = y - 21**Solution Explanation** The opposite of \times 5 is \div 5. 5x = 30÷5 By dividing both sides by 5, we get an equivalent equation. Recall that $5x \div 5$ simplifies to x. So the solution is x = 6. b The opposite of -21 is +21. +21 +21 +21So the solution is y = 38. Write the pronumeral on the LHS. Now you try

b 77 = 11x

Solve each of the following equations using the balance method.

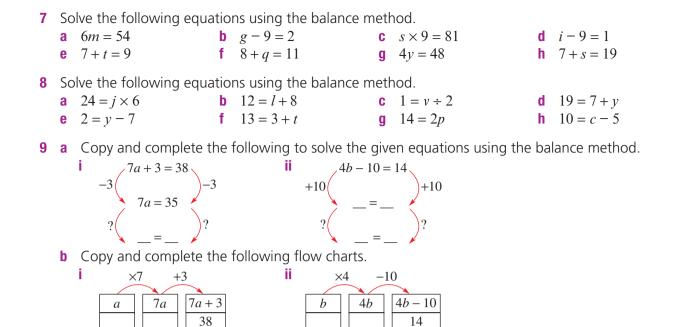
Hint: For part **a**, substitute x = 3in x + 4 = 7. Does LHS = RHS?

Hint: Remember that the same operation must be used for both



sides.

?



- **c** How are your answers to parts **a** and **b** related?
- 10 If you were solving these equations, what is the first operation you would apply to both sides? **b** 4x - 7 = 33**c** 3p + 8 = 38
 - **a** 2x + 3 = 9

Example 10 Solving two-step equations

Solve 4a + 7 = 23 using the balance method and check the solution.

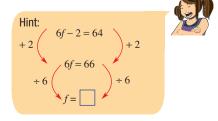
Solution	Explanation
-7(4a+7=23) -7	At each step, try to make the equation simpler by applying an operation to both sides.
$-7 \begin{pmatrix} -7 \\ 4a = 16 \\ \div 4 \\ a = 4 \end{pmatrix} \div 4$	Choose the opposite operations based on $4a + 7$: a + 7 + 4a + 7 Opposite operations: -7, then ÷ 4.
Check: $4a + 7 = 4 \times 4 + 7$ = 16 + 7 = 23	Check that your solution is correct by substituting $a = 4$ back into the equation.

Now you try

Solve 5b - 1 = 34 using the balance method and check the solution.

- **11** For each of the following equations:
 - Solve the equation using the balance method. i.
 - ii Check your solution.

а	6f - 2 = 64	b	5x - 4 = 41	C	5k - 9 = 31
d	2n - 8 = 14	е	2g - 7 = 1	f	3q - 3 = 30
g	3z - 4 = 26	h	9 + 8p = 17	i	10d + 7 = 47
j –	6t - 10 = 38	k	9u + 2 = 47	- I	10c - 3 = 7

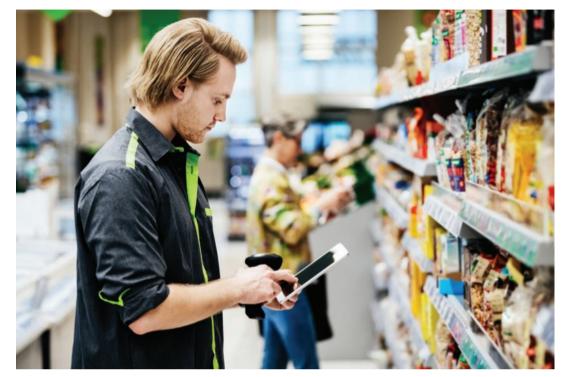


Hint: The opposite of +3 is -3

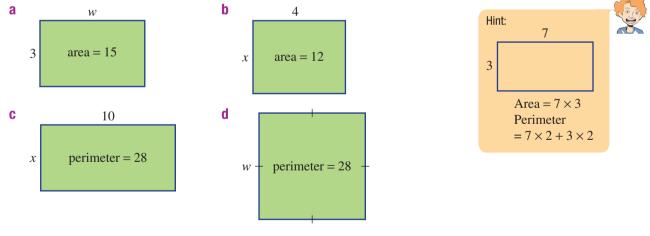
Problem-solving and reasoning

- 12 Danny gets paid \$12 per hour, plus a bonus of \$50 for each week. In one week he earned \$410.a Write an equation to describe this, using *n* for the number of hours worked.

 - **b** Solve the equation and state the number of hours worked.



13 Write equations and solve them using the balance method to find the unknown value in each of the following diagrams.

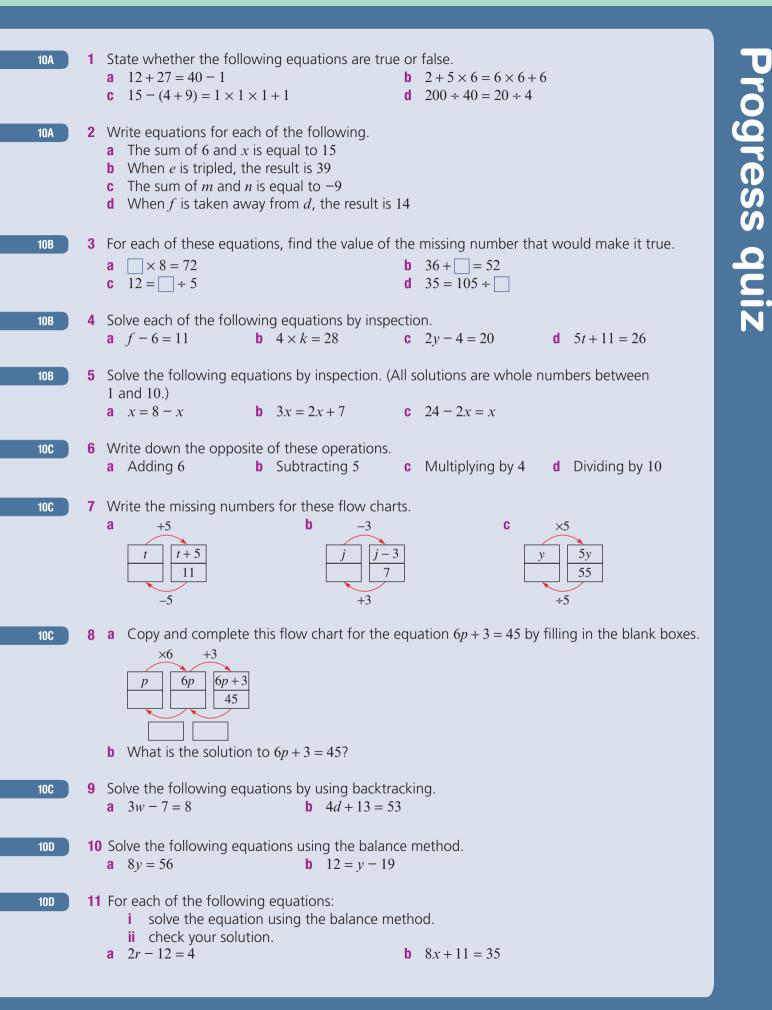


From solutions to equations

- **14 a** The equations 2x = 12 and x 4 = 2 each have the solution x = 6. Find four other equations with this solution.
 - **b** Find an equation with the solution $x = \frac{1}{2}$.
 - **c** Is there a limit to the number of equations with the solution x = 10? Why, or why not?

14

12



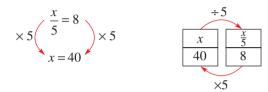
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10E Equations with fractions **†**

- To understand that to solve an equation with a fraction, it is helpful to multiply both sides by the denominator. •
- To be able to solve equations involving fractions using backtracking or the balance method. •
- Key vocabulary: denominator, balance method, backtracking, solution

Remember that $\frac{x}{5}$ means $x \div 5$.

This means we can solve equations such as $\frac{\chi}{5} = 8$ by using the balance method or backtracking.





Lesson starter: Fractional differences

Starting with the number 6, find the result for each of these flow charts.



- If you start with 10 instead of 6, what results do you get? •
- If you start with x, which of the two flow charts gives $\frac{x}{2}$ + 4 and which gives $\frac{x+4}{2}$? C

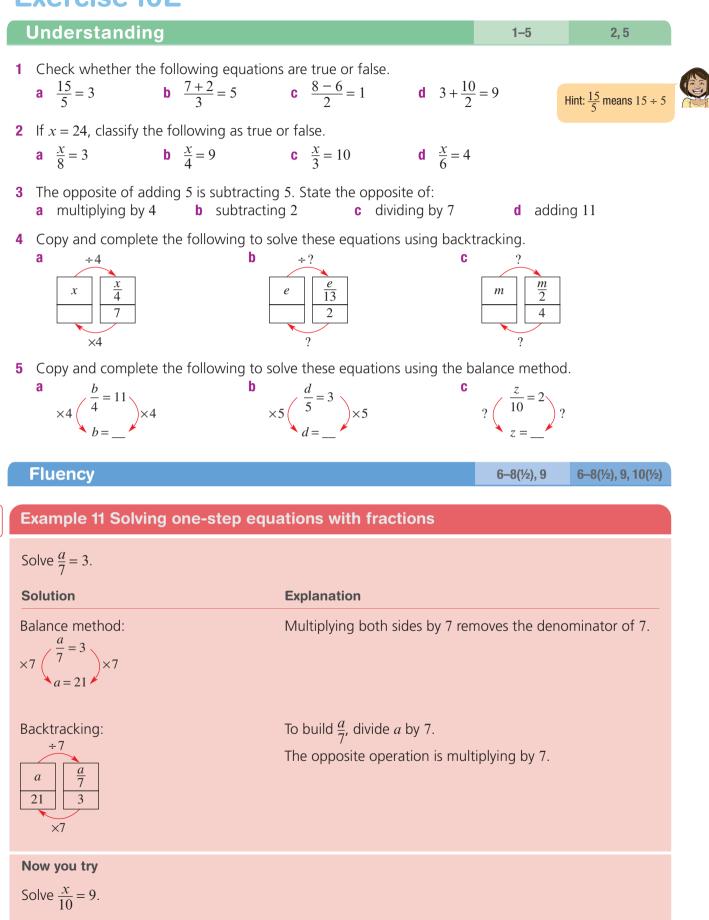
Key ideas

To solve an equation that has a fraction on one side, multiply both sides by the denominator. Alternatively, use **backtracking**.

Do not multiply by the denominator until the fraction is on its own on one side.

$$\times 3 \begin{pmatrix} \frac{x}{3} + 5 = 8 \\ \cdots \end{pmatrix} \times 3 \times \text{Do not do this!} -5 \begin{pmatrix} \frac{x}{3} + 5 = 8 \\ -5 \begin{pmatrix} \frac{x}{3} + 5 = 8 \\ x = 9 \end{pmatrix} \times 3 \text{Do this.}$$





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6 Solve the following equations using the balance method or backtracking.

а	$\frac{m}{6} = 2$	b	$\frac{c}{9} = 2$
C	$\frac{s}{8} = 2$	d	$\frac{r}{5} = 2$
е	$\frac{u}{2} = 6$	f	$\frac{y}{5} = 10$
g	$\frac{x}{2} = 1$	h	$\frac{a}{4} = 3$

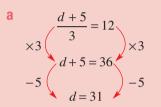
Example 12 Solving two-step equations with fractions

Solve each of the following.

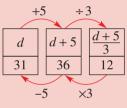
a
$$\frac{d+5}{3} = 12$$

$$\frac{m}{5} + 2 = 10$$

Solution



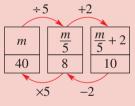
Multiply both sides by 3 to remove the denominator of 3. Then solve d + 5 = 36 in the usual way. Alternatively, use backtracking.



Explanation

b $-2\begin{pmatrix} \frac{m}{5} + 2 = 10\\ -2 & \frac{m}{5} = 8\\ \times 5 & m = 40 \end{pmatrix} -2$

First subtract 2 to get the fraction on its own on the LHS. Then multiply both sides by the denominator (5). Alternatively, use backtracking.



Now you try

Solve each of the following.

a
$$\frac{a-1}{3} = 3$$

$$\frac{b}{2} + 4 = 10$$

7 Solve the following equations.

a $\frac{d+15}{12} = 2$ **b** $\frac{y+5}{11} = 1$ **c** $\frac{j+8}{11} = 1$ **d** $\frac{b-2}{2} = 1$ **e** $\frac{w+2}{6} = 3$ **f** $\frac{s+2}{5} = 1$ **g** $\frac{v-4}{7} = 1$ **h** $\frac{f-2}{7} = 1$

8 Solve the following equations.

a $\frac{m}{2} + 7 = 12$ **b** $\frac{q}{3} - 2 = 1$ **c** $\frac{k}{4} - 3 = 7$ **d** $4 + \frac{x}{5} = 10$ **e** $\frac{a}{2} + 3 = 5$ **f** $\frac{x}{5} - 1 = 10$ **g** $\frac{y}{2} + 5 = 8$ **h** $\frac{a}{7} - 2 = 1$

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11 - 13

- **9** For each of the following equations, choose the appropriate first step (**A** to **D**) needed to solve it using the balance method.
 - a $\frac{x}{3} = 10$ AMultiply both sides by 2.b $\frac{x}{3} + 2 = 5$ BMultiply both sides by 3.c $\frac{x-3}{2} = 1$ CSubtract 2 from both sides.d $\frac{x}{2} 3 = 5$ DAdd 3 to both sides.
- **10** Solve the following equations.

a $\frac{x+5}{2} = 7$	b $\frac{x}{2} + 5 = 7$	c $\frac{p}{3} - 5 = 2$	d $\frac{p-5}{3} = 2$	Hint: Don't multiply until the fraction is on its own.	
e $\frac{q}{2} = 10$	f $\frac{r-3}{2} = 12$	g $\frac{r}{3} + 5 = 12$	h $\frac{x}{5} - 2 = 10$		

Problem-solving and reasoning

- 11 In each of the following cases, write an equation and solve it to find the number.
 - **a** A number, *t*, is halved and the result is 9.
 - **b** A number, x, is divided by 10 and the result is 8.
 - **c** 4 is subtracted from *q* and this is halved, giving a result of 3.
 - **d** 3 is added to x and the result is divided by 4, giving a result of 2.
 - **e** A number, *y*, is divided by 4 and then 3 is added, giving a result of 5.
- **12** A group of five people go out for dinner and split the bill evenly. They each pay \$22.
 - **a** If *b* represents the total cost of the bill, in dollars, write an equation to describe this situation.
 - **b** Solve this equation algebraically.
 - c What is the total cost of the bill?
- **13** a Explain, in one sentence, the difference between $\frac{x+3}{5}$ and $\frac{x}{5}+3$.
 - **b** Using the balance method, what is the first operation you would apply to both sides to solve:

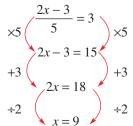
i
$$\frac{x+3}{5} = 7?$$

ii
$$\frac{x}{5} + 3 = 7?$$

c Are there any values of x for which $\frac{x+3}{5}$ and $\frac{x}{5}$ + 3 are equal to each other?

Three-step equations with fractions

14 Sometimes an equation involving fractions takes more than two steps to solve. For example:



Solve the following equations, showing all three steps.

$$\frac{3a-4}{2} = 1$$

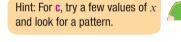
b $\frac{5k-3}{4} = 3$

c
$$\frac{2q+11}{3} = 7$$

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Hint: You can also use backtracking to solve these

equations.

14

11, 12

10F Formulas 🕇

Learning intentions

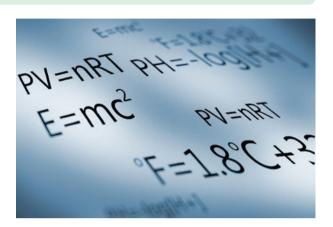
- To understand that formulas and rules are types of equations.
- To be able to apply a formula by substituting and evaluating.
- To be able to apply a formula by substituting and solving an equation.

Key vocabulary: formula, rule, substitution, LHS

A formula is a rule for finding the value of something. For example, the equation $E = mc^2$ is a formula that relates energy, mass and the speed of light.

Lesson starter: Different formulas

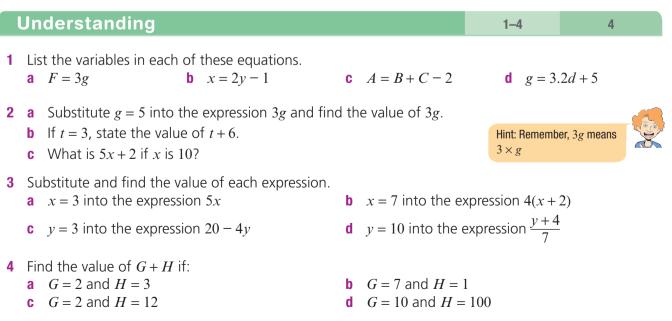
- List all the formulas you can think of.
- Using the internet or a library, find the longest and/or most complicated formula you can, and try to explain what it does.



Key ideas

- A formula or rule is an equation that shows the relationship between two or more variables. One of these variables is written by itself on the LHS of the equation.
- To use a formula, first substitute all the known values into the equation. Then solve the equation to find the unknown variable.

Exercise 10F



10F	Formulas	511
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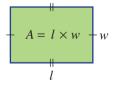
	formula
Consider the formula $k = 3b$. a $b = 5$	+ 2. Find the value of k if: b $b = 10$
Solution	Explanation
a $k = 3b + 2$ = 3 × 5 + 2 = 17	Copy the formula. Substitute $b = 5$ into the equation, then evaluate.
b $k = 3b + 2$ = 3 × 10 + 2 = 32	Copy the formula. Substitute $b = 10$ into the equation, then evaluate.
Now you try Consider the formula $a = 2b + a$ a $b = 4$	- 1. Find the value of a if: b $b = 22$
 5 Consider the formula d = t a t = 2 b 6 Consider the rule n = 2m + 	t = 10 c $t = 6$
	m = 4 c $m = 100$ Hint: If $m = 3$ the
7 Consider the formula $F = m$ a $m = 3$ and $a = 7$ b	<i>ma.</i> Find <i>F</i> if: m = 9 and $a = 2$ c $m = 1$ and $a = 30$
Example 14 Applying a 1	formula and solving to find the unknown
Consider the formula $k = 3b$	+ 2. Find the value of b if $k = 23$.
	Explanation
Solution	Substitute $k = 23$ into the equation. Now solve the equation to
Solution Solve $23 = 3b + 2$. -2 (23 = 3b + 2) - 2 -2 (21 = 3b) - 2 $\div 3 (7 = b) \div 3$ Therefore, $b = 7$.	find the value of <i>b</i> . Alternatively, use backtracking, starting with <i>b</i> . $\begin{array}{r} & & & \\ & & & \\ & & & \\ \hline & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & &$
Solve $23 = 3b + 2$. $-2 \begin{pmatrix} 23 = 3b + 2 \\ -2 \\ 21 = 3b \\ \div 3 \\ 7 = b \end{pmatrix} \div 3$	Alternatively, use backtracking, starting with <i>b</i> . $x_3 + 2$ b 3b 3b + 2 21 23

10F

9 You are given the formula A = 3b + 4. a If b = 2, what is A? b If A = 34, what is b? c Find b if A = 25. 10 Consider the formula y = 5 + 3x. Find: a y if x = 6 b x if y = 17 c x if y = 26Problem-solving and reasoning 11 11, 12 11 The perimeter, P, of a square is given by the formula P = 4w where w is the width.

a Find the perimeter if:

- **b** If the perimeter is 48, solve the equation 48 = 4w to find the width.
- **12** The formula for the area of a rectangle is $A = l \times w$, where *l* is the rectangle's length and *w* is the rectangle's width.

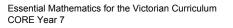


- **a** Find the value of A if l = 7 and w = 5.
- **b** Set up and solve an equation to find the length of a rectangle with A = 20 and w = 4.
- **c** A rectangle is drawn for which A = 25 and w = 5.
 - i Set up and solve an equation to find *l*.
 - ii What type of rectangle is this?

Converting temperatures

- **13** To convert between temperatures in degrees Celsius (°C) and degrees Fahrenheit (°F), the rule is F = 1.8C + 32.
 - **a** Find F if C = 20.
 - **b** Find C if F = 50.
 - c What is the temperature in degrees Fahrenheit if it is 23°C outside?
 - **d** In Florida, USA, last week, the temperature hit 97°F. What is this in degrees Celsius? Solve an appropriate equation and round your answer to the nearest degree.
 - e Marieko claims that the temperature in her city varies between 68°F and 95°F. What is the difference in degrees Celsius between these two temperatures?





13

Hint: For parts c and d, round to

the nearest whole degree.

10G Applications of equations **†**

Learning intentions

- To know that equations can be applied to real-world situations.
- To be able to solve problems using equations.

Key vocabulary: pronumeral, unknown, solution, units

Our methods for solving equations can be applied to many everyday situations.

Lesson starter: Stationery shopping

Sylvia bought 10 pencils and 2 pens for \$25. She knows that the pens cost \$3.50 each. How much did each pencil cost?

- Describe how you got your answer.
- Can you show your steps using equations?

Key ideas

To solve a problem, follow these steps.

Define pronumerals to stand for unknown numbers.

Write an equation to describe the problem.

Make sure that you answer the original question!



For example: Let p = the cost of a pencil.

For example: 6p = 12

You could use inspection, backtracking or the balance method.

Don't forget to include the correct units (e.g. dollars, years, cm).

Exercise 10G

Understanding	1–4	3, 4
1Match each of the descriptions (a to e) with the correct a a The sum of x and 3A $2x$ bTwice the value of xB $\frac{x}{2}$ c2 less than xC $5x$ dHalf of xD $x + e$ eThe product of 5 and xE $x - e$	+ 3	
2 Solve the following equations. a $5x = 30$ b $7a + 2 = 16$ c $2k$	- 3 = 15	
3 Alysha notices that buying 4 pens costs \$12. Which of the A \$4 B \$12 C \$1	e following is the cost of 1 p D \$3 E S	
 4 The product of k and 7 is 42. a Write an equation to describe this fact. b Solve the equation to find the value of k. 	Hint: The written 7k	product of <i>k</i> and 7 is

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10

B				
	Fluency		5–7	5–8
	Example 15 Solving a problem us	ing equations		
	The sum of Kate's age now and her age r Solution	next year is 19. How old is Kate? Explanation	,	
	Let $k = Kate's$ current age.	Define a variable to stand for t	he unknown n	umber.
	k + (k + 1) = 19	Write an equation to describe is Kate's age next year.	the situation. N	lote that $k+1$
	$-1 \begin{pmatrix} 2k+1 = 19 \\ -1 \\ 2k = 18 \\ \div 2 \\ k = 9 \end{pmatrix} \div 2$	Simplify the LHS and then solve balance method (left) or backter $x^2 + 1$ k $2k$ $2k + 19$ 18 $19\div 2 -1$	•	using the
	Kate is currently 9 years old.	Answer the original question ir	n a sentence.	

Now you try

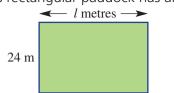
Norman gets paid \$30 per hour plus a bonus of \$100 each week. In one particular week he gets paid \$730.

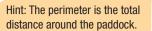
- a Define a variable for the number of hours worked in the week.
- **b** Write an equation to describe the problem.
- **c** Solve the equation.
- d How many hours did Norman work that week?

5 Millie buys 12 pens for a total cost of \$18.

- a Define a variable for the cost of one pen.
- **b** Write an equation to describe the problem.
- **c** Solve the equation.
- **d** What is the cost of one pen?
- 6 Launz buys four new tyres for his car. He also buys a smaller spare tyre for his trailer, which costs \$160. The total cost is \$1400.
 - **a** Define a variable for the cost of a car tyre.
 - **b** Write an equation to describe the problem.
 - **c** Solve the equation.
 - d What is the cost of a car tyre?
- 7 Jonas is paid \$17 per hour and gets paid a bonus of \$65 each week. One particular week he earned \$643.
 - a Define a variable for the number of hours Jonas worked.
 - **b** Write an equation to describe the problem.
 - **c** Solve the equation.
 - d How many hours did Jonas work in that week?

8 This rectangular paddock has an area of 720 m^2 .





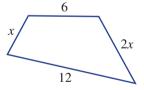


- Write an equation to describe the problem, using *l* for the paddock's length. a
- Solve the equation. b
- How long is the paddock? С
- **d** What is the paddock's perimeter?



Problem-solving and reasoning

- 9 A number is doubled, then 3 is added. This gives a final result of 31. Set up and solve an equation to find the original number, showing all the steps clearly.
- **10** Consider the shape below.



- The perimeter of this shape is 30. Find the value of x. а
- Is it possible for the perimeter to equal 15? Why, or why not? b
- 11 Marco and Sara's combined age is 30. Given that Sara is 2 years older than Marco, write an equation and find Marco's age.

Hint: If Marco's age is m, then Sara's age is m + 2.

3

12

6



Curious rectangles

- **12** The formulas for the area and perimeter of rectangles are $A = l \times w$ and P = 2l + 2w.
 - a Calculate the area and the perimeter of this rectangle (l = 6 and w = 3). What do you notice about the numbers you get?
 - **b** Find some other solutions to the equation $l \times w = 2l + 2w$ by inspection. (There are many solutions.)
 - **c** Are there any solutions when the rectangle is a square (that is, l = w)? Justify your answer.

9.10

9-11

🔀 Maths@Work: Uber fares

Taxis have competition from Uber and its drivers. Anyone aged 21 and over, with a car less than 10 years old, can apply to be an Uber driver. The Uber company is expanding and is in over 70 countries and 500 cities world-wide.

The cost of your trip is calculated before you even get in the Uber car. The formula usually used is:

Fare = Base fare + $/min \times time + /km \times distance$



1 UberX is the basic level of Uber transport. It has the following fee rates in Australia.

	Base fare	\$2.50
	Per minute	\$0.40
	Per kilometre	\$1.45
	Minimum fare	\$8.00
	Cancellation fee	\$10.00
Ш		

- **a** How much would the following journeys cost using the fee structure of UberX?
 - i A 6-minute trip covering 3 km.
 - ii A 10-minute trip of 12 km.
 - iii A 34-minute trip of 24 km.
- **b** How many kilometres was Sam's Uber trip if it lasted $\frac{3}{4}$ of an hour and cost her \$70?
- **c** How long did it take Tyrone to travel the 34 km from his home to the city centre if it cost \$71?
- **d** Write an equation that calculates the UberX fare for a ride of *n* kilometres taking *t* minutes.
- **2** UberSELECT is a more luxurious ride. It has a different fee structure, depending on the city of travel. The prices here are for up to 4 passengers in Brisbane, Queensland.

Base fare	\$4.00
Per minute	\$0.55
Per kilometre	\$1.80
Minimum fare	\$10.00
Cancellation fee	\$10.00

- **a** How much would a half-hour ride covering 40 km cost using UberSELECT?
- **b** What is the maximum distance you can travel in 5 minutes if you only pay the minimum fare?
- **c** Brisbane to the Sunshine Coast is 120.3 km and should take 1 hour 22 minutes. If these figures are used, what should an UberSELECT ride cost you between these two places?
- **d** From Brisbane airport to Australia Zoo is 75 km. If you can only afford \$180, how long do you hope the UberSELECT ride will take for a family of 4?
- **e** Write an equation that can be used to calculate the cost of UberSELECT for *n* kilometres, at a time of *t* minutes.
- **f** A person was charged \$10 for a 2-kilometre trip that took 2 minutes. Explain why the formula was not used.

3 UberBLACK operates in Western Australia:

Base fare	\$10.00
Per minute	\$0.68
Per kilometre	\$2.04
Minimum fare	\$8.00
Cancellation fee	\$10.00

- a How much does the 30-minute, 23-km trip from Perth CBD to Fremantle cost?
- **b** How much does the 14-minute, 8-km trip from Fremantle to Cottesloe beach cost?
- **c** How far can a person travel in 30 minutes for \$50 using UberBLACK in Western Australia?
- **d** Write an equation that can be used to calculate the cost of *n* kilometres at a time of *t* minutes.
- 4 a Research the levels of Uber rides available and their costs in two world cities outside of Australia.b Research the reasons why Uber fares can sometimes be a lot more expensive for the same route.
 - **c** Research the fares charged by the taxi companies operating in your area.

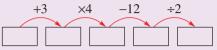


Using technology

- **5 a** Set up the following spreadsheet to calculate Uber fares. Select all the cost cells (in columns D, F, H and I) right click, select Format/Currency/2 d.p.
 - **b** Enter formulas in the shaded cells to calculate these Uber fares.

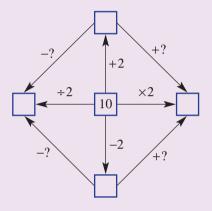
4	A	В	C	D	E	F	G	н	1
1			Uber	fare calculati	ons				
	Uber level	Pickup place	Destination	Base fare	Distance in km	Cost per km	Time in minutes	Cost per minute	Fare
	UberX	Burke and Wills Hotel, Toowoomba, Qld	Byron Bay, NSW	\$2.00	268	\$1.00	180	\$0.35	
	UberX	Melbourne Airport, Vic	Mornington Peninsula, Vic	\$2.00	109	\$1.00	90	\$0.32	
	UberXL	Brisbane Airport, Qld	Surfers Paradise, Gold Coast, Qld	\$3.10	87	\$1.60	70	\$0.50	
	UberXL	Perth Airport, WA	Margaret River, WA	\$4.50	274	\$1.70	185	\$0.50	
,	UberBLACK	Napier Street, Adelaide SA	Adelaide Airport, SA	\$8.00	9	\$2.05	17	\$0.45	
3	UberASSIST	Canberra Airport, ACT	Goulburn, NSW	\$2.35	94	\$1.35	65	\$0.45	

- 1 Find the unknown number in the following puzzles.
 - a A number is added to half of itself and the result is 39.
 - **b** A number is doubled, then tripled, then quadrupled. The result is 696.
 - **c** One-quarter of a number is subtracted from 100 and the result is 8.
 - **d** Half of a number is added to 47, and the result is the same as the original number doubled.
 - e A number is increased by 4, the result is doubled and then 4 is added again to give an answer of 84.
- 2 Find values of x and y that will make *both* these equations true: x + y = 20 and $x \times y = 91$
- **3** A flow chart is set up like this:



How could you get from the last box back to the start in just one operation?

4 Some numbers in this two-dimensional flow chart are unknown. Find the sum of the four numbers that are shown by question marks.



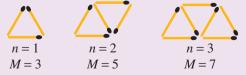
5 What did the student expect when she solved the puzzle? Find the answer by solving the following equations. If the solution is x = 1, the letter is A. If the solution is x = 2, the letter is B, and so on.

3x + 2 = 5	16 = 2x + 10	5x - 10 = 65	$\frac{x}{3} + 1 = 7$	$2 = \frac{x+2}{8}$	2x + 10 = 60	$\frac{x}{2} + 3 = 8$	3x + 2 = 47	20 - x = 9	4x - 3 = 17

6 In a farmer's paddock there are sheep and ducks. Farmer Jess says to her grandson, 'There are 41 animals in this paddock.' Grandson James says to his grandma, 'There are 134 animal legs in this paddock.'

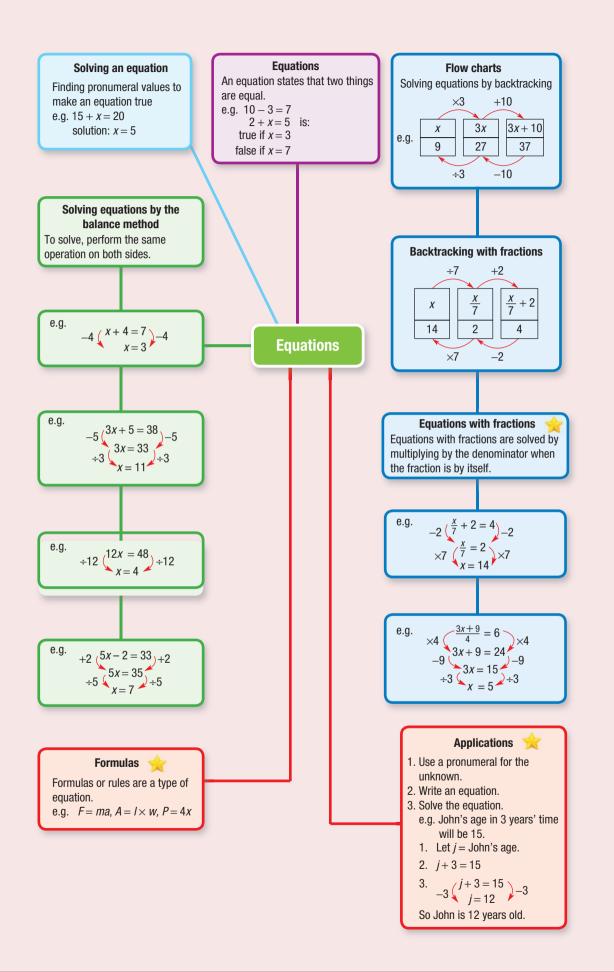
How many sheep and how many ducks are in the paddock?

7 Michelle looks at how many matchsticks are required to make a pattern of triangles.



a Find a formula relating M and n.

- **b** How many matchsticks would Michelle need to make 100 triangles?
- 8 Egan and Joel have ages that are 5 years apart. When their ages are added, the result is 21. How old is each boy?



Essential Mathematics for the Victorian Curriculum CORE Year 7

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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

1	I can classify an equation as true or false, given the value of any pronumerals. e.g. If k is 5, is $4 + k = 9$ true or false?
2	I can classify an equation as true or false by comparing both sides. e.g. ls $2 + 5 + 6 = 10 - 3$ true or false?
3	I can write an equation from a description written in words. e.g. Write an equation for "the sum of x and 5 is 22."
4	I can solve equations by inspection. e.g. Solve the equation $c + 12 = 30$ by inspection.
5	I can solve one-step equations using backtracking. e.g. Solve $5x = 20$ by using backtracking.
6	I can solve two-step equations using backtracking. e.g. Solve $4x + 3 = 23$ by using backtracking.
7	I can solve one-step equations using the balance method. e.g. Solve $5x = 30$ using the balance method.
8	I can solve two-step equations using the balance method. e.g. Solve $4a + 7 = 23$ using the balance method.
9	I can check solutions to equations. e.g. Check that $a = 4$ is a solution to $4a + 7 = 23$.
10	I can solve one-step equations involving fractions. e.g. Solve $\frac{a}{7} = 3$.
11	I can solve two-step equations involving fractions. e.g. Solve $\frac{m}{5}$ + 2 = 10.
12	I can apply formulas when the unknown is by itself. e.g. For the rule $k = 3b + 2$, find the value of k if $b = 10$.
13	I can apply formulas when an equation must be solved. e.g. For the rule $k = 3b + 2$, find the value of b if $k = 23$.
14	I can solve problems using equations. e.g. The sum of Kate's current age and her age next year is 19. Use an equation to determine how old Kate is.

2 Write an equation for each of the following situations. You do not need to solve the equations. a The sum of 2 and *u* is 22. **b** The product of k and 5 is 41. When z is tripled the result is 36. **d** The sum of *a* and 12 is 15. **3** Solve the following equations by inspection. **a** x + 1 = 4**b** x + 8 = 14**c** 9 + y = 10**d** y - 7 = 2 $a \div 5 = 2$ **e** 5a = 10f 4 Solve each of the following equations by using backtracking. **a** 4x = 20**b** 7q = 42**c** a + 4 = 25**d** k - 6 = 12**e** 2k + 3 = 23f 5w - 7 = 333b + 5 = 20h 10r - 12 = 8**5** Solve each of the following equations by using the balance method. **a** 5x = 15**b** r + 25 = 70**c** 5 = x - 4**d** 13 = 2r + 5**e** 10 = 4q + 28u + 2 = 666 Solve the following equations. **a** $\frac{u}{4} = 6$ **b** $\frac{p}{2} = 8$ **d** $\frac{y}{2} + 10 = 30$ **c** $3 = \frac{x+1}{3}$ **e** $4 = \frac{y+20}{7}$ f $\frac{x}{3} + 4 = 24$ 7 Consider the equation 4(x+3) = 2x + 14. **a** Is x = 2 a solution? (Check the LHS and RHS.) **b** Show that x = 1 is a solution. 8 The formula for the area of a rectangle is $A = w \times l$, where w is the width and l is the length. **a** Find the area if w = 10 and l = 45. **b** If A = 24 and w = 3, find the value of l. Give an example of the length and width of a rectangle that has an area of 40.

b 2(3+5) = 4(1+3)

f 4 = z + 2, if z = 3

d 2x + 5 = 12, if x = 4

9 Consider the rule F = 3a + 2b. Find: **a** F if a = 10 and b = 3**b** b if F = 27 and a = 5**c** *a* if F = 25 and b = 8

- **a** A number is multiplied by 4 and the result is 20. What is the number?
- **b** The sum of 5 and a number is 30. What is the number?
- c Juanita's mother is twice as old as Juanita. The sum of their ages is 60. How old is Juanita?
- **d** A square has a perimeter of 20. What is its length?

Short-answer questions

a 4+2=10-2

a

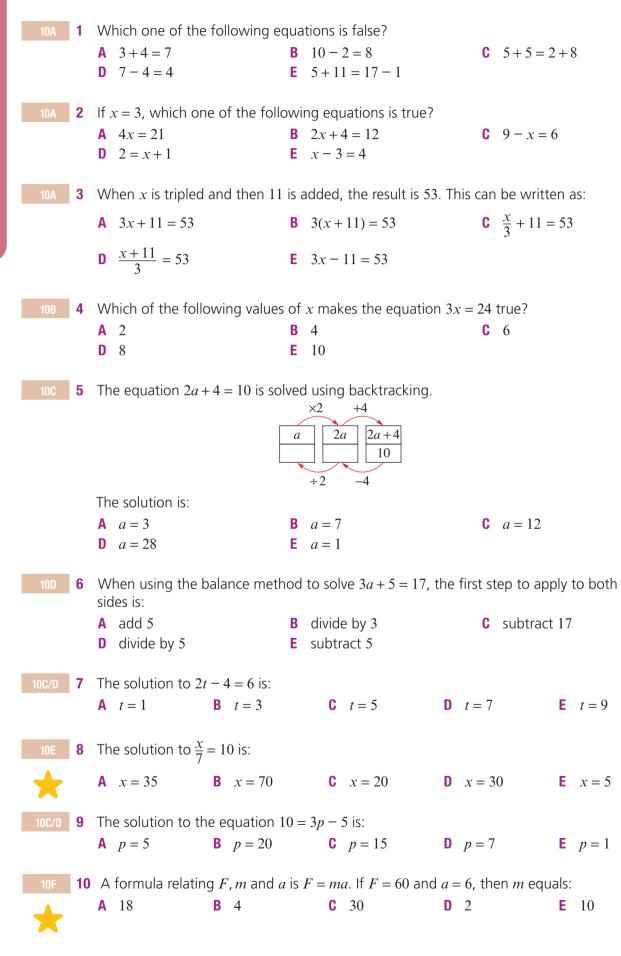
c 5w + 1 = 11, if w = 2

e y = 3y - 2, if y = 1

1 Classify each of the following equations as true or false.

Chapter review

Multiple-choice questions

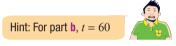


Chapter review

Extended-response questions

- 1 Mya is paid \$12 per hour at her workplace.
 - **a** How much is she paid if she works for 10 hours?
 - **b** Which of the following formulas correctly relates her total wage W (in dollars) and the number n of hours worked?
 - **A** W = 12
 - **B** W = 12n
 - **C** W = 12 + n
 - **D** W = n 12
 - **c** If n = 5, what is the value of her total wage, W?
 - d If her wage one day is \$84, for how long did she work?
 - e Write an equation (but do not solve it) for the following problem. One week, Mya worked *n* hours and earned \$252.
- **2** Udhav's satellite phone plan charges a 15-cent connection fee and then 2 cents per second for every call. The total cost is given by C = 15 + 2t if C is the cost in cents and t is the time in seconds.
 - a How much does a 30-second call cost?
 - **b** How much would a 1-minute call cost?
 - **c** Solve the equation 15 + 2t = 39.
 - d If a call cost 39 cents, how long did it last?
 - e If a call cost \$1.15, how long did it last?
 - **f** On a particular day, Udhav makes two calls. The first call lasted 20 seconds and the second lasted twice as long. What was the total cost of these two calls?





Chapter 11 Measurement

Essential mathematics: why measurement skills are important

Making accurate measurements, converting between units and calculating areas, volumes, capacities, masses, temperatures and times are all essential skills for practical occupations.

- Measurement skills are essential for trade workers including bakers, boilermakers, bricklayers, builders, carpenters, concreters, cooks, farmers, forestry workers, glaziers, hairdressers, house painters, machinists, mechanics, pipelayers, plumbers, plasterers, seamstresses, sheet metal workers, tilers and welders.
- Measurement skills are also essential for the practical professions, such as engineers, industrial designers, surveyors, architects and scientists.
- Boat designers and builders require measurement skills, for example, when building the Spirit of Tasmania ferry, which carries 500 vehicles, is 194.33 m long, has a capacity for 1,222,000 litres of fuel, and weighs 29,338 tonnes when loaded.

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Essential Mathematics for the Victorian Curriculum

In this chapter

- 11A Using and converting metric lengths (Consolidating)
- **11B** Perimeter (Consolidating)
- 11C Units of area and area of a rectangle
- 11D Area of a parallelogram
- 11E Area of a triangle
- 11F Volume of rectangular prisms
- 11G Capacity (Consolidating)
- 11H Mass and temperature (Consolidating)

Victorian Curriculum

MEASUREMENT AND GEOMETRY

Using units of measurement

Establish the formulas for areas of rectangles, triangles and parallelograms, and use these in problem-solving (VCMMG258)

Calculate volumes of rectangular prisms (VCMMG259)

Shape

Draw different views of prisms and solids formed from combinations of prisms (VCMMG260)

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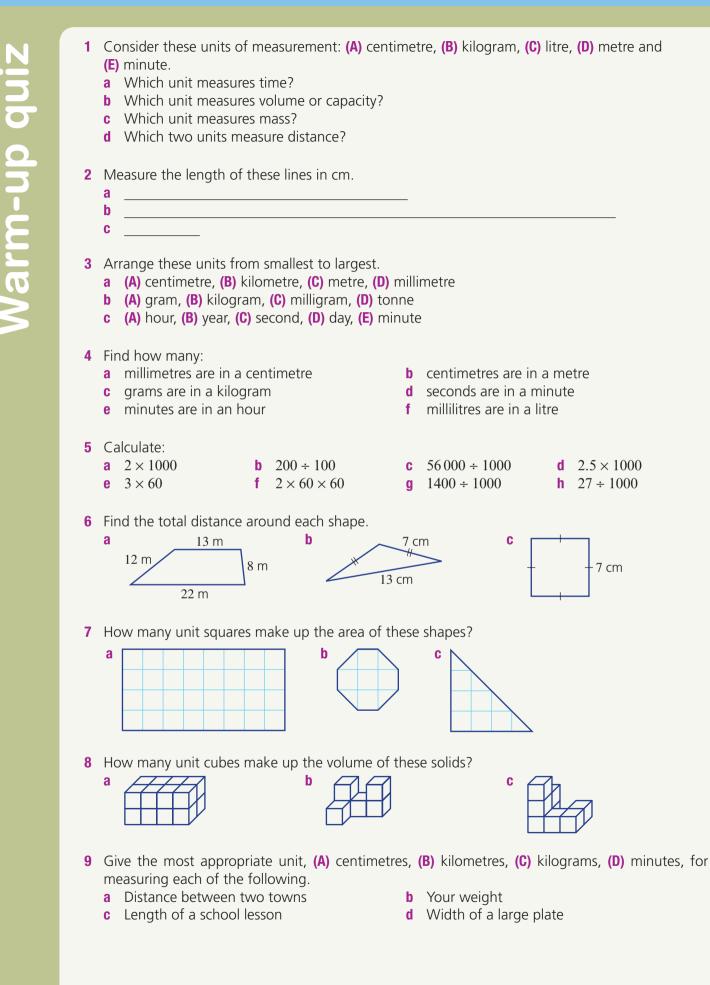
Online resources

A host of additional online resources are included as part of your Interactive Textbook, including HOTmaths content, video demonstrations of all worked examples, auto-marked quizzes and much more.

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11A Using and converting metric lengths CONSOLIDATING

Learning intentions

- To be able to choose an appropriate metric unit for measuring different lengths.
- To be able to convert between metric lengths (km, m, cm and mm).
- To be able to read a length shown on a ruler or tape measure.

Key vocabulary: metre, metric system, conversion, scale

The metric system for measurement was developed in France in the 1790s and is the universally accepted system today. The word *metric* comes from the Greek word *metron* meaning 'measure'. It is a decimal system where length measures are based on the unit called the *metre*.

The definition of the metre has changed over time. Originally it was proposed to be the length of a pendulum that beats at a rate of one per second. It was later defined as 1/10 000 000 of the distance from the North Pole to the Equator, on a line on the Earth's surface passing through Paris.



 $\times 1000$

 $\div 1000$

m

km

 $\times 100$

 $\div 100$

cm

 $\times 10$

 $\div 10$

mm

Lesson starter: How good is your estimate?

In less than 3 seconds, guess the length of your desk, in centimetres.

- Now use a ruler to find the actual length in centimetres.
- Convert your answer to millimetres and to metres.
- If you lined up all the class desks end to end, how many desks would be needed to reach 1 kilometre? Explain how you got your answer.

Key ideas

- The metre (m) is the basic metric unit of length in the metric system.
 - 1 centimetre (cm) = 10 millimetres (mm)
 - 1 metre (m) = 100 centimetres (cm)
 - 1 kilometre (km) = 1000 metres (m)

= 4.7 cm

Conversion

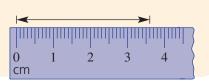
• When converting to a smaller unit, multiply by a power of 10 (i.e. 10, 100, 1000). Move any decimal point to the right. For example: $2.3 \text{ m} = (2.3 \times 100) \text{ cm}$ 28 cm = $(28 \times 10) \text{ mm}$

$$= 230 \text{ cm}$$
 $= 280 \text{ mm}$

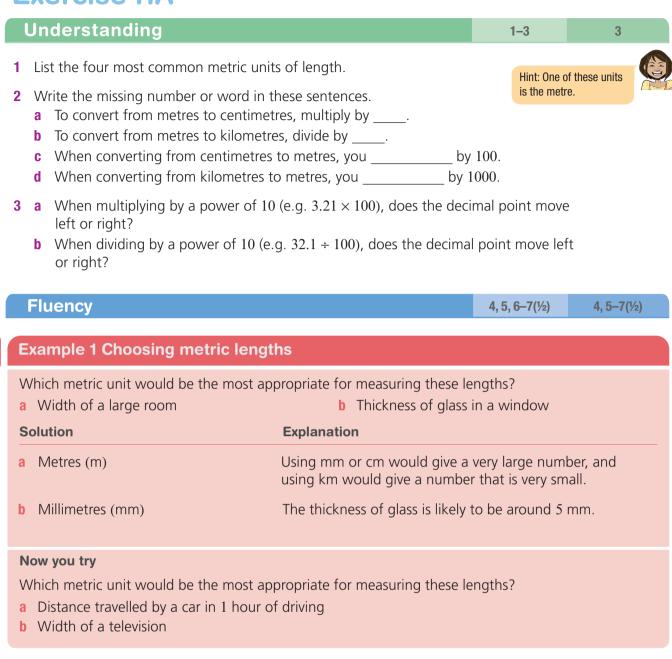
 When converting to a larger unit, divide by a power of 10 (i.e. 10, 100, 1000). Move any decimal point to the left. For example:

47 mm = $(47 \div 10)$ cm 4600 m = $(4600 \div 1000)$ km

When reading scales, be sure about what units are showing on the scale. This scale shows 36 mm or 3.6 cm.



Exercise 11A



4 Which metric unit would be the most appropriate for measuring the following?

- a Distance between two towns
- **c** Height of a flag pole
- e Width of a small desk

- **b** Width of a small drill bit
- d Length of a garden hose
- f Distance across a city

Example 2 Reading length scales Read the scales to measure the marked length. a 0 1 0 1 2 3

Solution	Explanation	
a 25 mm	2.5 cm is also accurate.	
b 70 cm	Each division is $\frac{1}{10}$ of a metre, which is 10 cm.	
Now you try		
Read the scales on these rulers to measure the marked length.		
	b	

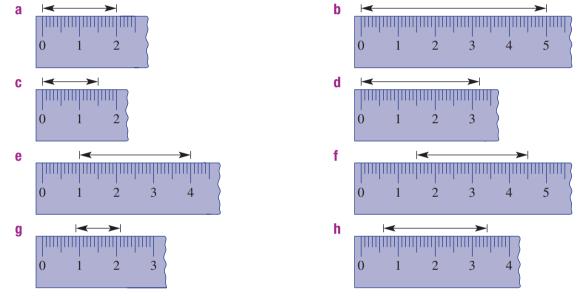
5 These rulers show centimetres with millimetre divisions. Read the scale to measure the marked length.

6 cm

7

8

9



Convert to the units given in brackets.	
a 3 m (cm)	b 2.8 km (m)
Solution	Explanation
a $3 \text{ m} = (3 \times 100) \text{ cm}$ = 300 cm	1 m = 100 cm Multiply, as you are converting to a smaller unit.
b $2.8 \text{ km} = (2.8 \times 1000) \text{ m}$ = 2800 m	There are 1000 m in 1 km, so multiply by 1000.
Now you try	
Convert to the units given in brackets.	
a 6 cm (mm)	b 4.1 m (cm)

0 mm

1

2

3

а

C

g i.

5 cm (mm)

3.5 km (m)

6.2 m (cm)

6.84 m (cm)

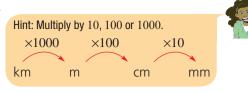
e 2.2 km (m)

k 38 m (cm)

11A

6 Convert these measurements to the units shown in brackets.

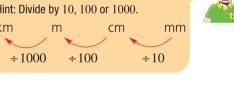
- **b** 2 m (cm)
 - 26.1 m (cm) d
 - 5.3 cm (mm) f
 - **h** 20 cm (mm)
 - 0.02 km (m) j.
 - Т 6.7 m (cm)



Example 4 Converting to larger units	of length
Convert to the units given in the brackets.	
a 39 mm (cm)	b 580 m (km)
Solution	Explanation
a 39 mm = (39 ÷ 10) cm = 3.9 cm	There are 10 mm in 1 cm so divide by 10.
b 580 m = (580 ÷ 1000) km = 0.58 km	There are 1000 m in 1 km so divide by 1000.
Now you try Convert to the units given in the brackets.	
a 46 cm (m)	b 4321 m (km)
7 Convert these measurements to the units sh	nown in the brackets.

a 40 mm (cm)	b 500 cm (m)	g)
c 4200 m (km)	d 472 mm (cm)	Hint: Divide by 10, 100 or 1000.
e 360 cm (m)	f 32 mm (cm)	km m cm mm
g 50000 m (km)	h 27 000 m (km)	$\div 1000 \div 100 \div 10$
i 362 mm (cm)	j 0.4 mm (cm)	÷1000 ÷100 ÷10
k 9261 mm (cm)	4230 m (km)	

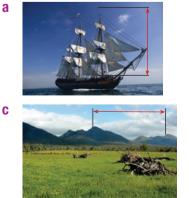
Problem-solving and reasoning



8–12

8 Choose which metric unit (mm, cm, m, km) would be the most suitable for measuring the length indicated in these photos.

b







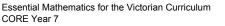
Hint: Choose the unit for the real-life length, not the length of the arrow in the photo!

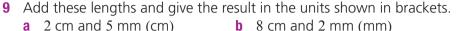


8, 13–16

d







c 2 m and 50 cm (m)

e 6 km and 200 m (m)

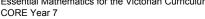
e

- **d** 7 m and 30 cm (cm)
- f 25 km and 732 m (km)
- 10 Use subtraction to find the difference between the measurements, and give your answer with the units shown in brackets.
 - **a** 9 km, 500 m (km)
- **b** 3.5 m, 40 cm (cm)
- **c** 0.2 m, 10 mm (cm)
- 11 Read the measurement on each of these scales. Be careful with the units shown!

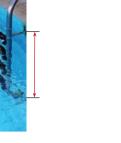
а	$\boldsymbol{\prec}$	\rightarrow	
	0 1	$\begin{array}{c} 1 \\ 2 \\ 3 \end{array}$	
	m		

- b 12 13 11 km
- **12** Arrange these measurements from smallest to largest.
 - a 38 cm, 540 mm, 0.5 m
 - **c** 0.003 km, 20 cm, 3.1 m, 142 mm
- **b** 0.02 km, 25 m, 160 cm, 2100 mm d 0.001 km, 0.1 m, 1000 cm, 10 mm
- **13** Joe widens a 1.2 m doorway by 50 mm. What is the new width of the doorway in centimetres?

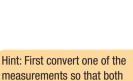
- 14 Steel chain costs \$8.20 per metre. How much does it cost to buy chain of the following lengths? **c** 500 mm **a** 1 km **b** 80 cm
- **15** Mount Everest is moving with the Indo-Australian plate at a rate of about 10 cm per year. How many years will it take to move 5 km?









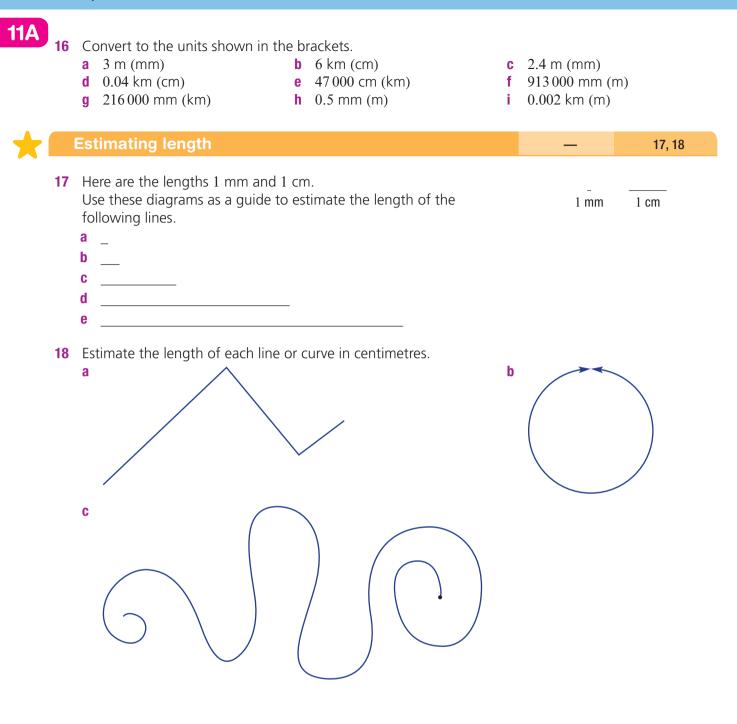


lengths have the same units

Hint: Make sure you identify the unit on each scale.

shown in brackets.





11B Perimeter



Learning intentions

- To understand that perimeter is the distance around the outside of a two-dimensional shape.
- To understand that marks can indicate two (or more) sides are of equal length.
- To be able to find the perimeter of a shape when the measurements are given.

Key vocabulary: perimeter, distance, rectangle, units

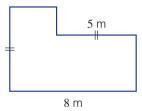
The distance around the outside of a two-dimensional shape is called the perimeter. The word *perimeter* comes from the Greek words *peri*, meaning 'around', and *metron*, meaning 'measure'.

We associate perimeter with the outside of all sorts of regions and objects, like the length of fencing around a block of land or the length of timber required to frame a picture.



Lesson starter: The L-shaped perimeter

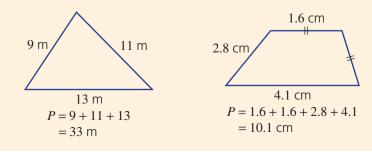
This L-shaped area has two given measurements. All angles are 90°.



- For each of the other sides, state whether it is possible to find their lengths. Give reasons for each answer.
- Is it possible to find the perimeter of the entire shape? Explain your answer.

Key ideas

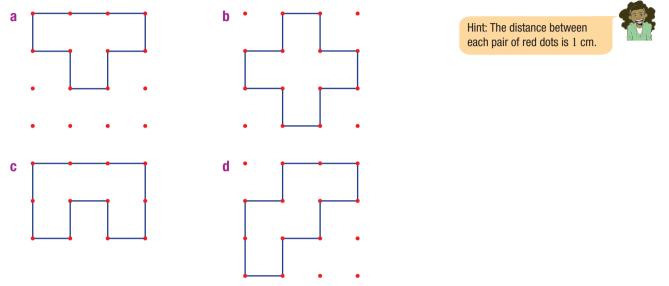
- **Perimeter**, often denoted as *P*, is the **distance** around the outside of a two-dimensional shape.
- Sides with the same markings are of equal length.



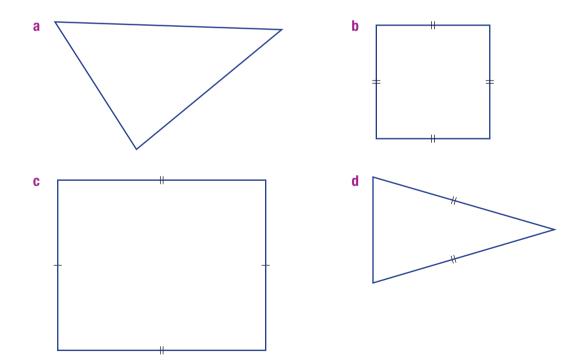
Exercise 11B

Understanding	1–3	3

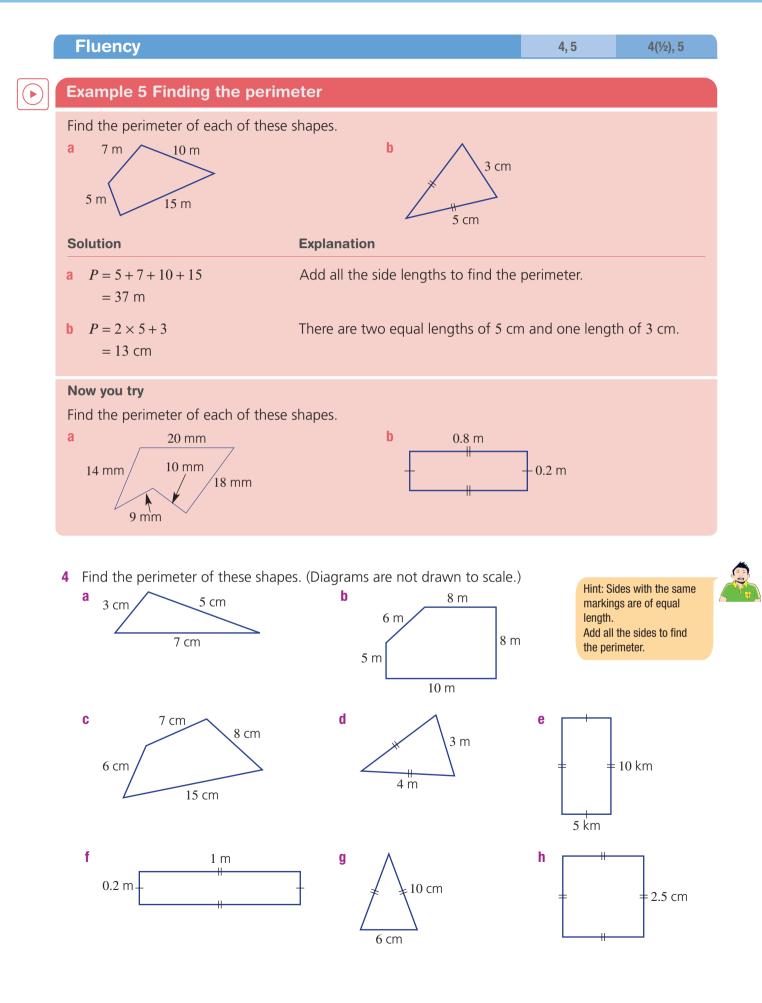
- 1 Choose a suitable word to complete each sentence.
 - a The distance around the outside of a shape is called the _____
 - **b** Sides with the same markings are of ______ length.
- 2 These shapes are drawn on 1-cm grids. Give the perimeter of each.



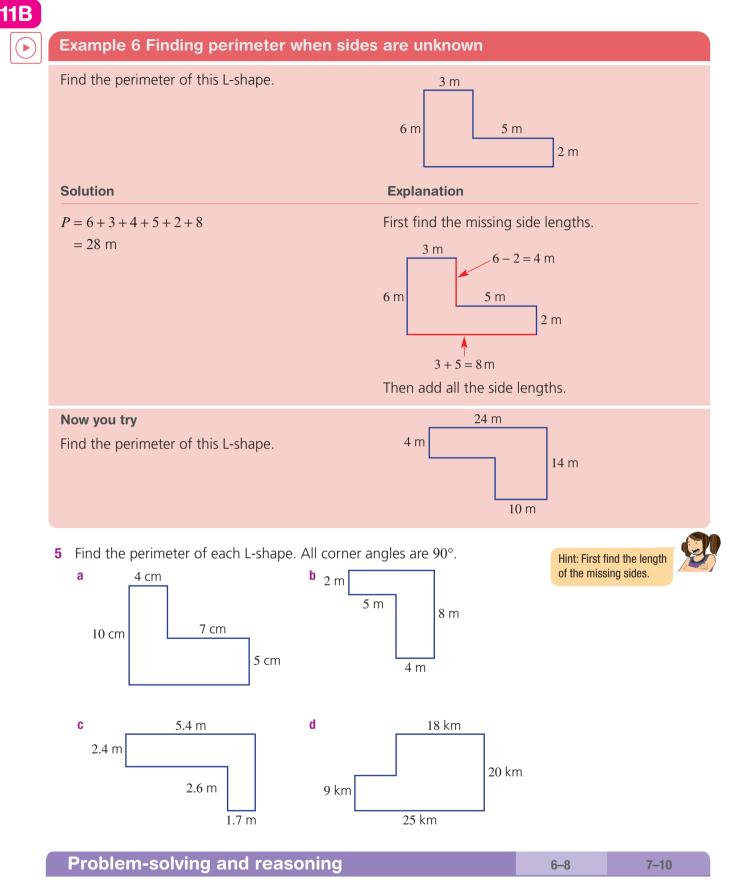
3 Use a ruler to measure the lengths of the sides of these shapes, and then find the perimeter in centimetres.



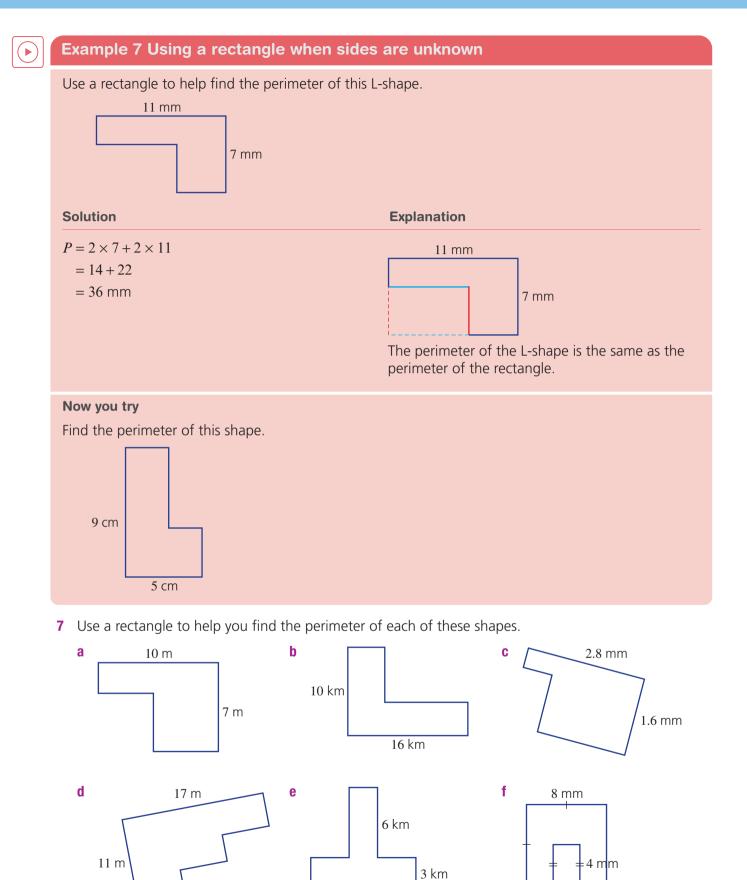




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- 6 a A square has a side length of 2.1 cm. Find its perimeter.
 - **b** A rectangle has a length of 4.8 m and a width of 2.2 m. Find its perimeter.
 - c An equilateral triangle has all sides the same length. If each side is 15.5 mm, find its perimeter.



9 km

3 mm

3 mm

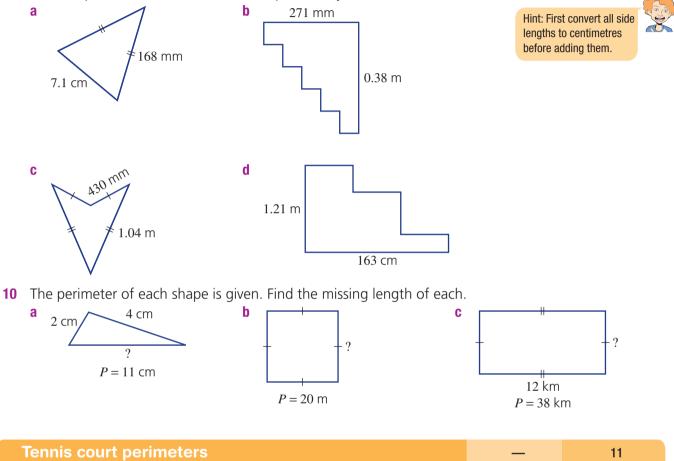
11B

H

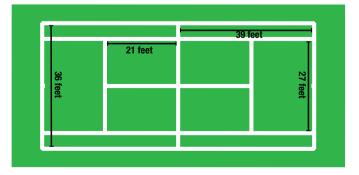
8 A horse paddock is to be fenced on all sides. It is rectangular in shape, with a length of 242 m and a width of 186 m. If fencing costs \$25 per metre, find the cost of fencing required.



9 Find the perimeter of each of these shapes. Give your answers in centimetres.



11 A grass tennis court has white chalk lines. All the measurements are shown in the diagram and given in feet.



- a Find the total number of feet of chalk required to mark all the lines of the tennis court.
- **b** There are 0.305 metres in 1 foot. Convert your answer to part **a** to metres.

11C Units of area and area of a rectangle

Learning intentions

- To understand what the area of a two-dimensional shape refers to.
- To be able to convert between metric areas (square millimetres, square centimetres, square metres, square kilometres, hectares).
- To be able to find the area of squares and other rectangles.

Key vocabulary: area, rectangle, square, hectare (ha), units

The number of square units inside the boundary of a closed shape gives the measurement called area.

The number of square centimetres inside this rectangle is 6, so the area of the rectangle is 6 cm^2 .

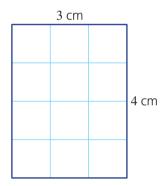


Other shapes may be measured in larger or smaller units. For example, the area of a coin might be 200 mm^2 and the area of a soccer field might be 8000 m^2 .

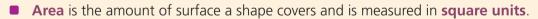
Solution Lesson starter: The 12 cm² rectangle

Consider an area of 12 square centimetres (12 cm²).

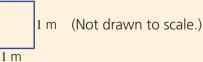
- Draw examples of rectangles that have this area, showing the length and width measurements. One example is shown here. You might find it helpful to draw on grid paper.
- How many different rectangles with whole-number dimensions are possible?
- How many different rectangles are possible if there is no restriction on the type of numbers used for length and width?



Key ideas



- The metric units of area include:
 - 1 square millimetre (1 mm²)
 1 mm
 1 mm
 - 1 square metre (1 m²)



1 cm

1 square centimetre (1 cm^2)

• 1 square kilometre (1 km²)

1 km

1 km (Not drawn to scale.)

• 1 hectare (1 ha) (10000 m²)

100 m (Not drawn to scale.)

100 m

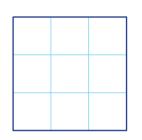
11C

- The area of a **rectangle** is given by: Area = length \times width or $A = l \times w$
- On a grid, you can count squares to find the area of a rectangle or multiply the number of rows by the number of columns.
- The area of a square is given by: $A = l \times l = l^2$

Exercise 11C

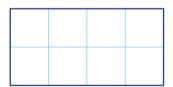
Understanding

- 1 Arrange the following from largest to smallest. 1 cm², 1 m², 1 ha, 1 km², 1 mm²
- 2 For this square drawn on a centimetre grid, find:
 - **a** the number of single 1 cm squares
 - **b** the length and the width
 - c length × width

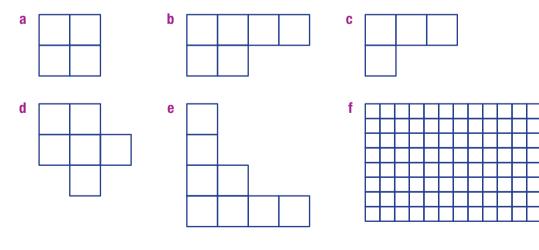


Hint: For part b, give the side lengths in cm.

 $A = l^2$



- **3** For this rectangle drawn on a 1-cm grid, find:
 - **a** the number of single 1-cm squares
 - **b** the length and the width
 - $\textbf{c} \quad \text{length} \times \text{width}$
- 4 Count the number of squares to find each area in square units.



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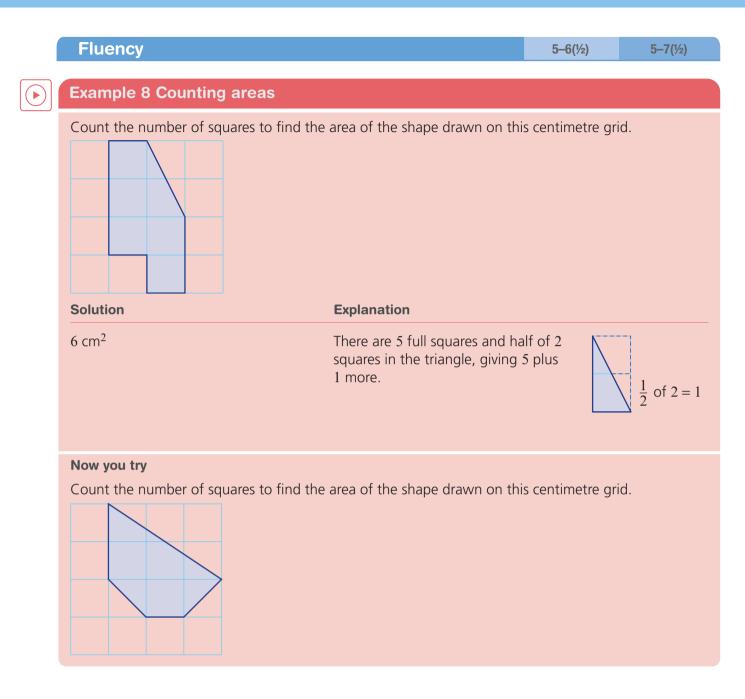
1–4 4 Hint: 1 ha is not as large

as 1 km².

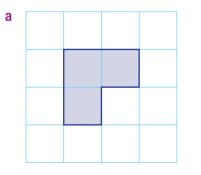
w

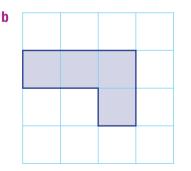
 $A = l \times w$





5 Count the number of squares to find the area of these shapes on centimetre grids.

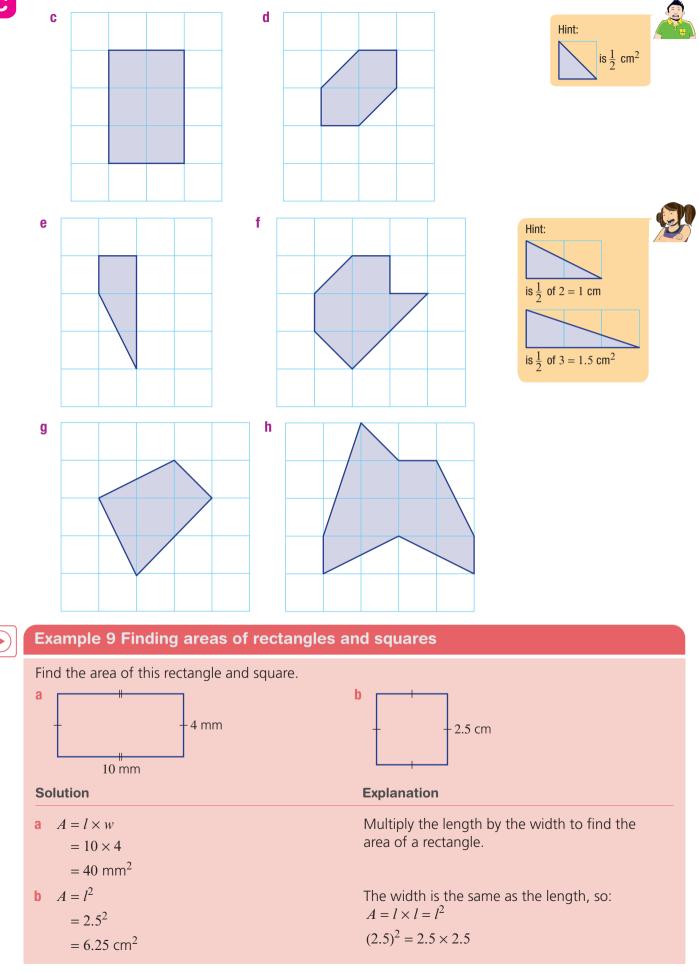




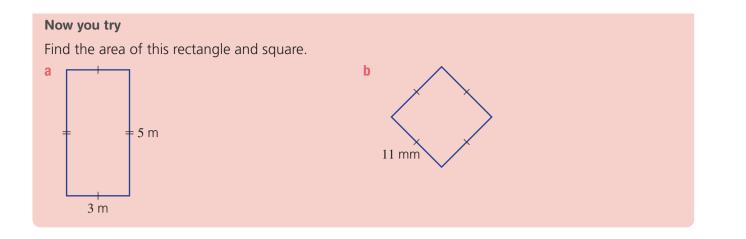








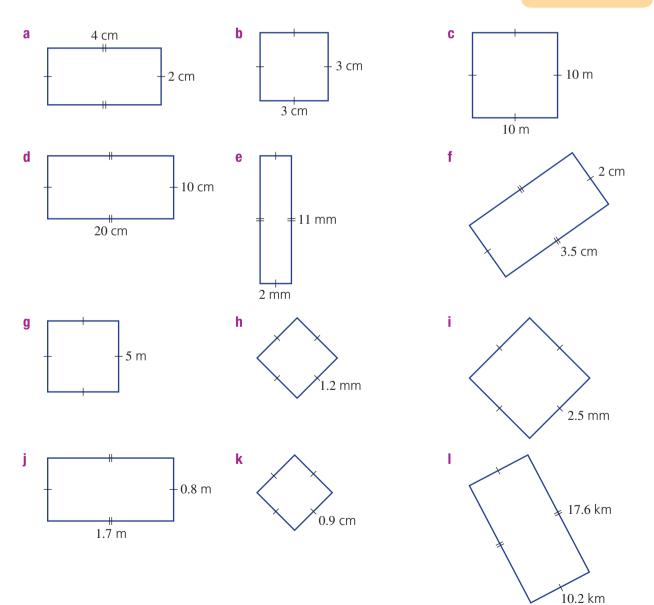
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6 Find the area of these rectangles and squares. Diagrams are not drawn to scale.

Hint: Multiply the length by the width to find the area.





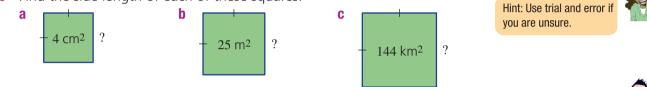
11(

- measure these areas? a Area of an A4 piece of paper
- c Area of a small farm
- e Area of a large football oval

Problem-solving and reasoning

Which unit of area $(mm^2, cm^2, m^2, ha or km^2)$ would you choose to

- 8 A rectangular soccer field is to be laid with new grass. The field is 100 m long and 50 m wide. Find the area of grass to be laid.
- **9** Glass is to be cut for a square window of side length 50 cm. Find the area of glass required for the window.
- **10** Find the side length of each of these squares.



- **11 a** A square has a perimeter of 20 cm. Find its area.
 - **b** A square has an area of 9 cm^2 . Find its perimeter.
 - c A square's area and perimeter are the same number. How many units is the side length?
- **12** a Find the missing length for each of these rectangles.



- **b** Explain the method that you used for finding the missing lengths of the rectangles above.
- **13** Explain why the area shaded here is exactly 2 cm².

Renovation work

- 14 Two hundred square tiles, each measuring 10 cm by 10 cm, are used to tile an open floor area. Find the area of flooring that is tiled.
- **15** The carpet chosen for a room costs \$70 per square metre. The room is rectangular and is 6 m long by 5 m wide. What is the cost of carpeting the room?
- **16** Tania wants to paint a house wall that is 11 m long and 3 m high. Two coats of paint are needed. The paint suitable to do the job can be purchased only in whole numbers of litres and covers an area of 15 m² per litre. How many litres of paint will Tania need to purchase?

- **b** Area of a wall of a house
- d Area of a large desert

8-10

Hint: First try to work out the side length of each square.

4 cm

14-16

f Area of a nail head

Hint: Remember, 1 km² is much larger than 1 ha.

10 - 13

1 cm

11D Area of a parallelogram

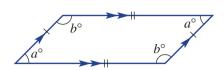
Learning intentions

- To understand that the area of a parallelogram is related to the area of a rectangle.
- To be able to find the area of a parallelogram given its base and height.

Key vocabulary: height, base, perpendicular, parallelogram, rectangle

Recall that a parallelogram is a quadrilateral with two pairs of parallel sides. Opposite sides are of the same length and opposite angles are equal.

Like a triangle, the area of a parallelogram is found by using the length of one side (called the base) and the height (which is perpendicular to the base.)



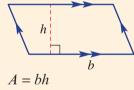
Lesson starter: How is a parallelogram like a rectangle?

Draw and then cut out a large parallelogram. (Make sure that the opposite sides are parallel.) Label one side as the base and label the height, as shown in the diagram.

- Cut along the dotted line.
- Now shift the triangle to the other end of the parallelogram to make a rectangle.
- Now explain how to find the area of a parallelogram.

Key ideas

- The height of a parallelogram is perpendicular (at 90°) to the base.
- Area of a parallelogram = base \times height or A = bh.





Exercise 11D

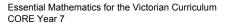
Understanding	1–3	3

1 Which of the following is the correct formula for the area of a parallelogram?

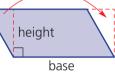
A
$$A = \frac{1}{2}bh$$
 B $A = \pi r^2$ **C** $A = bh$ **D** $A = b \div h$

2 Copy and complete the following, using the given values of *b* and *h*.

a $b = 5, h = 7$	b $b = 20, h = 3$	c $b = 8, h = 2.5$
A = bh	<i>A</i> =	A =
= ×	= 20 ×	= ×
= 35	=	=



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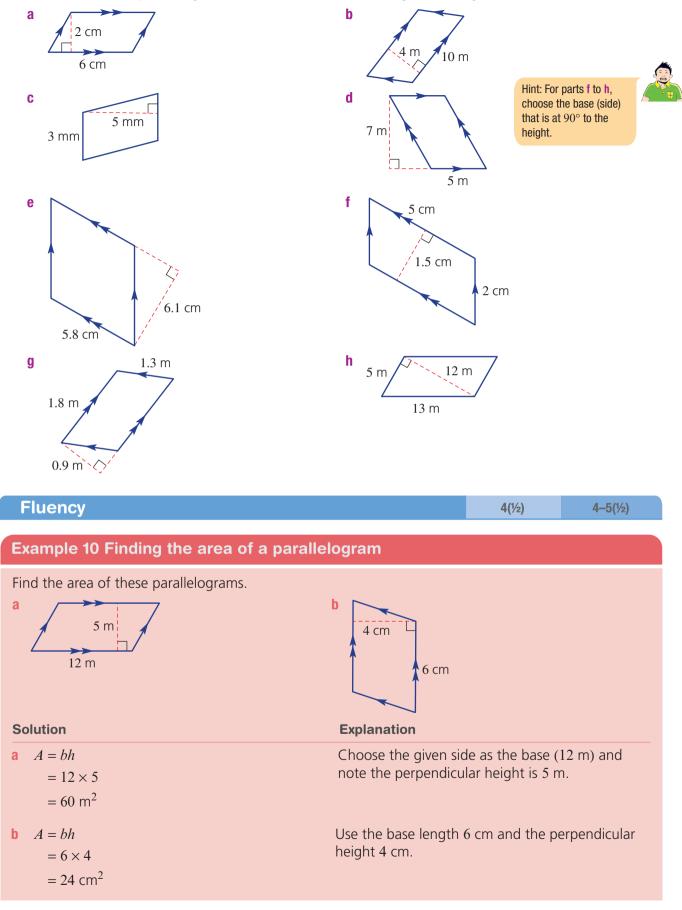
height

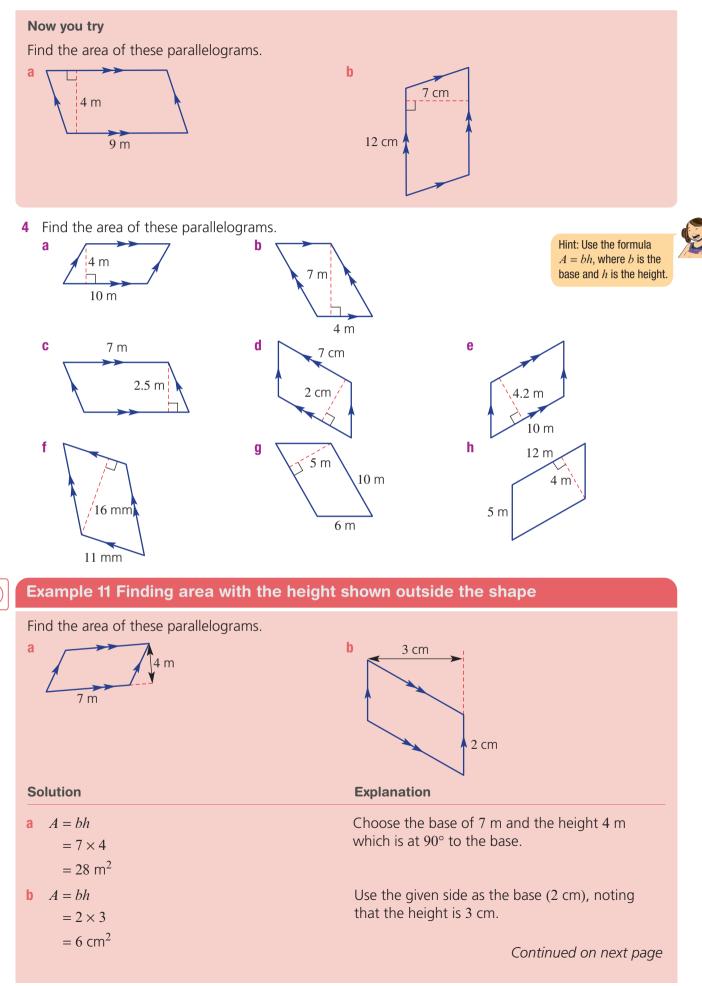
base

A = bh

11D

3 For each of these parallelograms, state the base and the height that might be used to find the area.



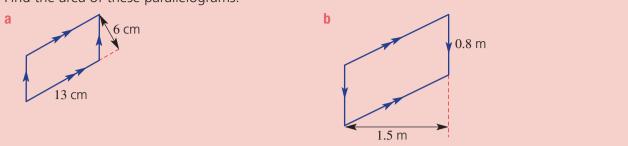


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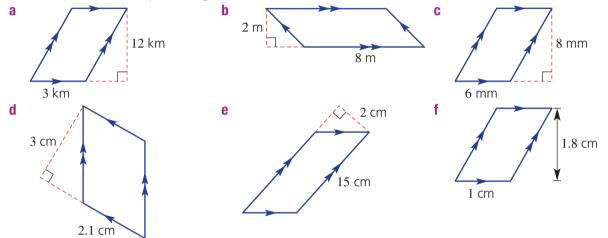
11D

Now you try

Find the area of these parallelograms.

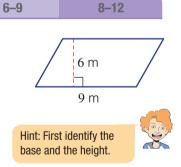


5 Find the area of these parallelograms.

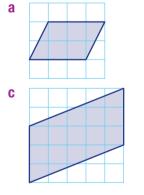


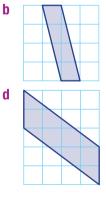
Problem-solving and reasoning

6 The floor of an office space is in the shape of a parallelogram. The longest sides are 9 m and the distance between them is 6 m. Find the area of the office floor.

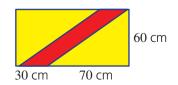


7 These parallelograms are on 1-cm grids (not to scale). Find each area.

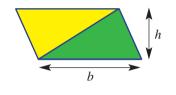




- 8 A proposed rectangular flag for a new country is yellow with a red stripe in the shape of a parallelogram, as shown. Find:
 - a the area of the red stripe.
 - **b** the yellow area.



- **9** Find the height of a parallelogram when its:
 - **a** area = 10 m^2 and base = 5 m
 - **b** area = 28 cm^2 and base = 4 cm
- **10** Find the base of a parallelogram when its:
 - **a** area = 40 cm^2 and height = 4 cm
 - **b** area = 150 m^2 and height = 30 m
- 11 A large wall in the shape of a parallelogram is to be painted with a special red paint, which costs \$20 per litre. Each litre of paint covers 5 m². The wall has a base length of 30 m and a height of 10 m. Find the cost of painting the wall.
- **12** A parallelogram includes a green triangular area, as shown. What fraction of the total area is the green area? Give reasons for your answer.



Glass facade

13 The Puerta de Europa (Gate of Europe) towers are twin office buildings in Madrid, Spain. They look like normal rectangular glass-covered skyscrapers but they lean towards each other at an angle of about 15° to the vertical.

For each building:

- The height of the building is 126 metres.
- The base is a square with 50 m sides.
- The two vertical walls (i.e. the front and the back) are parallelograms, as shown in the diagram.
- The two slanting walls are rectangles.
- All four walls are covered with glass.

Answer the following for one of the towers.

- a Find the area of one of the sloping (rectangular) walls.
- **b** Find the area of one of the sides that is vertical (a parallelogram).
- c Calculate the total area of all four sides of the tower.
- **d** If glass costs \$180 per square metre, find the cost of covering the tower with glass. (Assume that glass covers the entire surface, ignoring the beams.)



Hint: First work out the

area of the wall. Then

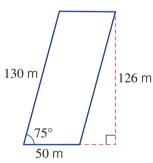
of paint needed.

find the number of litres

13

Hint: Use A = bh and substitute the given information.





11E Area of a triangle

Learning intentions

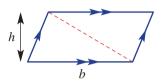
- To understand that two copies of a triangle can combine to form a parallelogram with the same base and height.
- To be able to identify the base and the (perpendicular) height of a triangle.
- To be able to find the area of a triangle.

Key vocabulary: height, base, perpendicular, parallelogram

A triangle can be considered to be half a parallelogram. This is why the formula for the area of a triangle looks very much like the formula

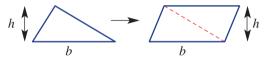
for the area of a parallelogram, but with a factor of $\frac{1}{2}$. One of the

sides of a triangle is called the base (*b*). The height (*h*) is the distance between the base and the opposite vertex, perpendicular (i.e. at 90°) to the base.



Lesson starter: Half a parallelogram

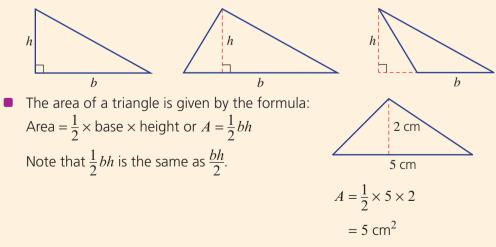
Consider a triangle which is duplicated, rotated and joined to the original triangle shown.



- What type of shape is the one on the right?
- What is the rule for the area of the shape on the right?
- What does this tell you about the rule for the area of the original triangle?

Key ideas

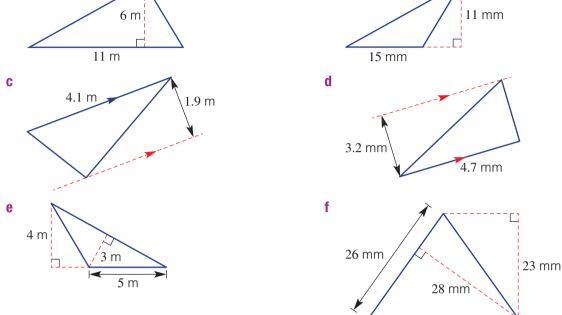
- One side of a triangle is called the **base**, *b*.
- The perpendicular distance from the base to the opposite vertex is called the height, h



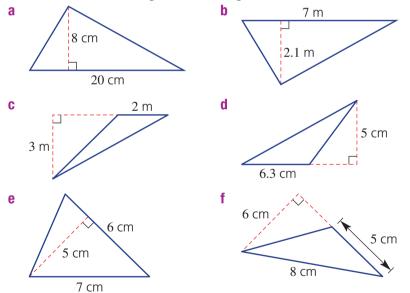
3

1–3

Exercise 11E Understanding 1 For each of these triangles, what length would be used as the height? a b



2 For each of these triangles, what length would be used as the base?



3 Using the formula $A = \frac{1}{2}bh$, find the value of A if: a b = 5 and h = 4

b b = 7 and h = 16

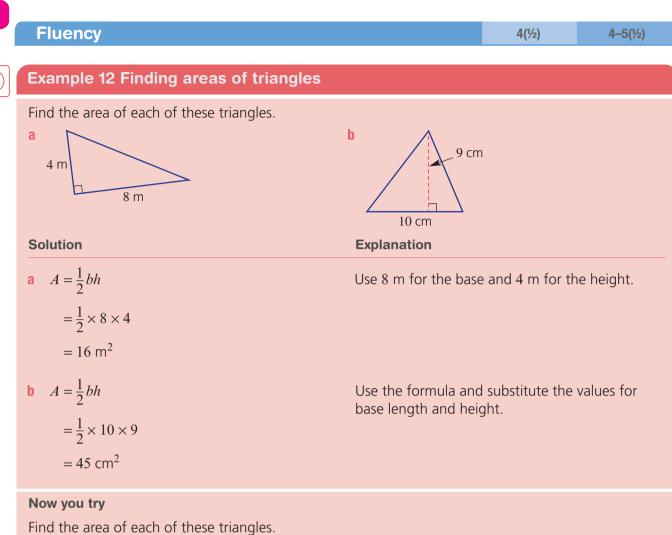
- **c** b = 2.5 and h = 10
- **d** b = 1.5 and h = 7

Hint: Substitute the values for b and h into the formula.

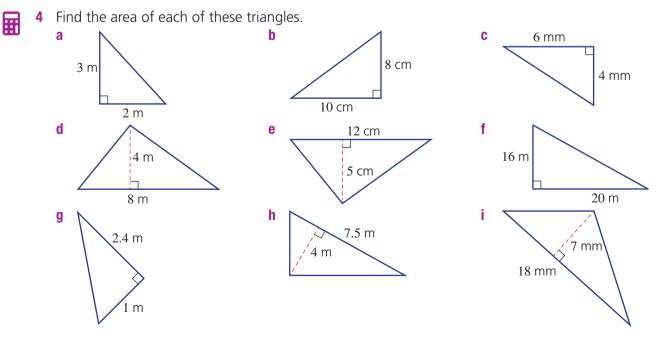


Hint: The base is one of the side lengths of the triangle.

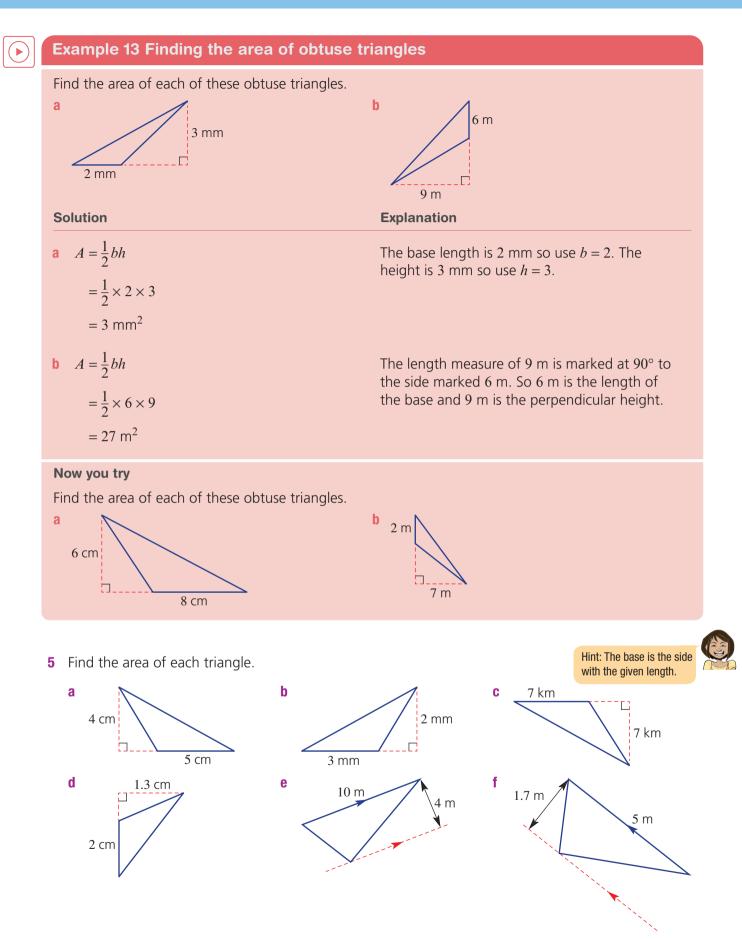
11E







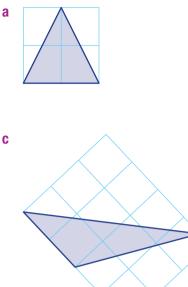
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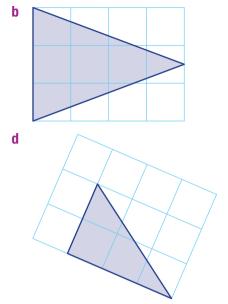


11E

Problem-solving and reasoning

6 Find the area of these triangles, which have been drawn on 1-cm grids. Give your answer in cm².

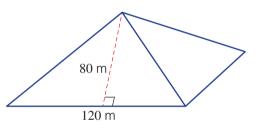




6-8

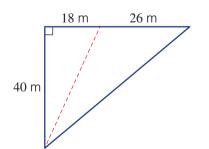
8–11

A square pyramid has a base length of 120 m and a triangular face of height 80 m. Find the area of one triangular face of the pyramid.





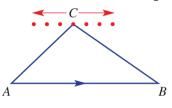
- **8** A rectangular block of land measuring 40 m long by 24 m wide is cut in half along a diagonal. Find the area of each triangular block of land.
- 9 A farmer uses fencing to divide a triangular piece of land into two smaller triangles, as shown.What is the difference in the two areas?

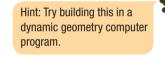


10 A yacht must have two of its sails replaced as they have been damaged by a recent storm. One sail has a base length of 2.5 m and a height of 8 m. The bigger sail has a base length of 4 m and a height of 16 m. If the cost of sail material is \$150 per square metre, find the total cost of replacing the yacht's damaged sails.



11 If the vertex *C* for this triangle moves left or right (to one of the red dots) will the area of the triangle change? Justify your answer.





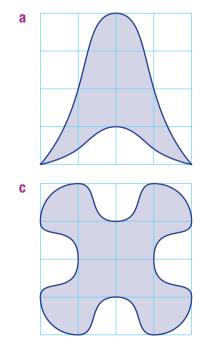
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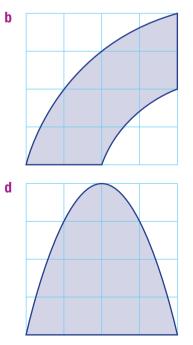
Estimating areas with curves

12 This diagram shows a shaded region that is $\frac{1}{2}$ of 3 cm² = 1.5 cm².

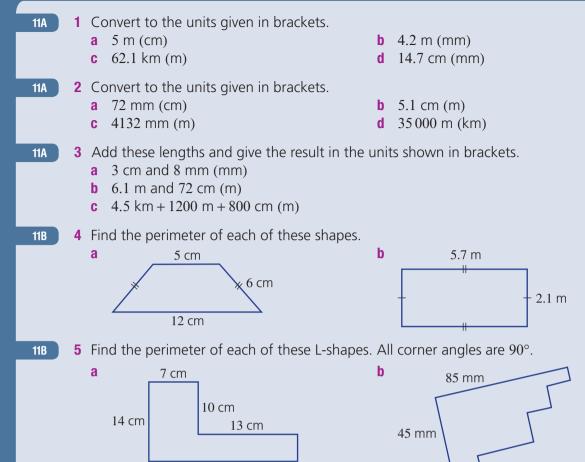


Using triangles like the one shown here, and by counting whole squares also, estimate the areas of these shapes below.





11B

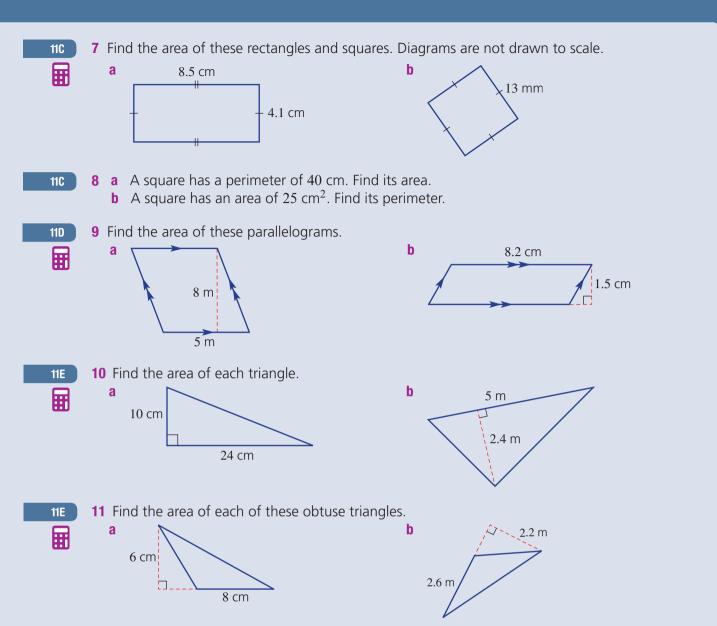


6 A playground is to be fenced on all sides. It is rectangular in shape, with a length of 35 m and a width of 19 m. If fencing costs \$120 per metre, find the cost of fencing required.



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Progress qui



11F Volume of rectangular prisms

Learning intentions

- To understand what the volume of a three-dimensional object refers to.
- To know that common metric units for volume include cubic millimetres, cubic centimetres, cubic metres and cubic kilometres.
- To be able to find the volume of a cube and other rectangular prisms. **Key vocabulary:** volume, cube, rectangular prism, cuboid

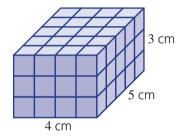
The amount of space inside a three-dimensional (3D) object is called volume. Volume is measured in cubic units such as the cubic centimetre, which is 1 cm long, 1 cm wide and 1 cm high. Just as with length and area, different units can be selected, depending on what is being measured. For example, the volume of a matchbox could be measured in cubic centimetres.



Lesson starter: The quick method

This rectangular prism is made up of small blocks (1 cm^3 cubes). The prism is 4 cm wide, 5 cm long and 3 cm high.

- How many 1 cm³ cubes are there in one horizontal layer? Explain how you worked this out.
- How many 1 cm³ cubes are there in total?
- What is the quickest way to find the total number of cubes (i.e. the volume)?



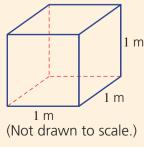
Key ideas

- Volume is the amount of three-dimensional space in (or occupied by) an object and is measured in cubic units.
- The common metric units for volume include:
 - cubic millimetres (mm³)

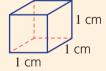


(Not drawn to scale.)

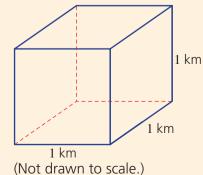
• cubic metres (m³)



• cubic centimetres (cm³)



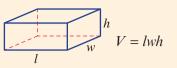
• cubic kilometres (km³)

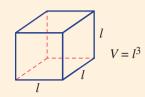


The volume of a rectangular prism is given by the formula:

Volume = length \times width \times height or V = lwh

- A rectangular prism is also called a cuboid.
- The volume of a **cube** is given by: $V = l \times l \times l$ $= l^3$



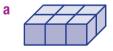


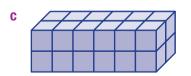
Exercise 11F

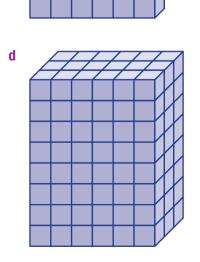
Understanding	1, 2	3–4

b

- 1 Which of the following is a unit of volume?
 - **A** 3 cm²
 - **B** 5 m³
 - **C** 2 mm
 - **D** 7.2 km
- 2 Which of the following is *not* a unit of volume?
 - **A** 7 mm^3
 - **B** 6 m³
 - **C** 5 cm^3
 - **D** 10 km^2
- 3 For each of these solids, count the number of cubic units to find the volume.

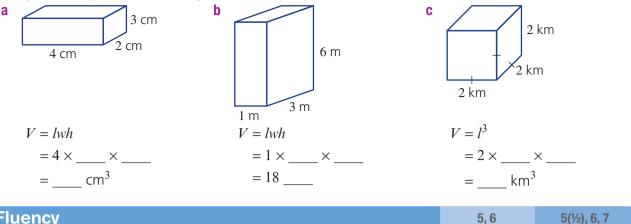






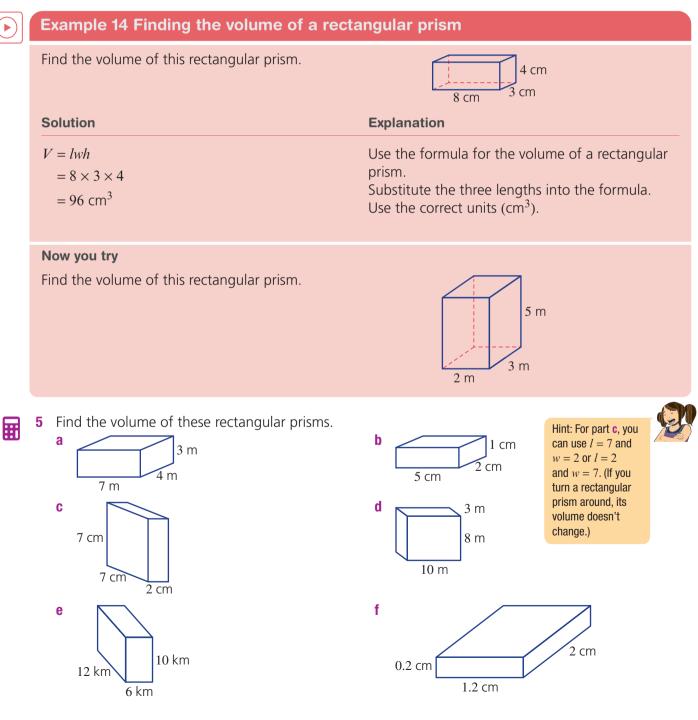
11F



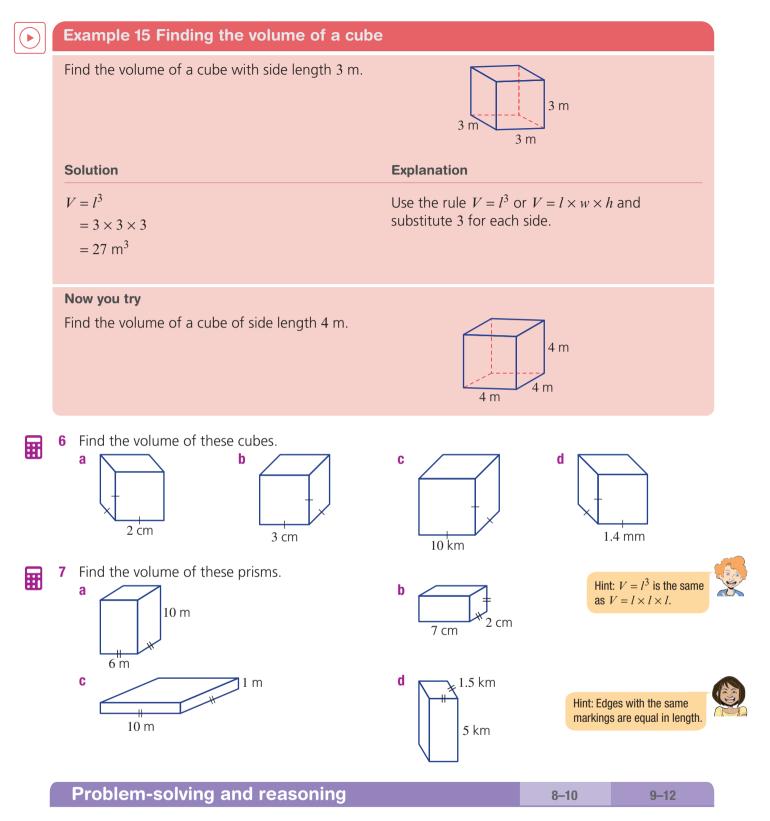


Fluency

5(1/2), 6, 7



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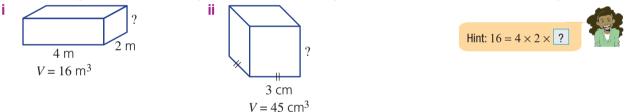
8 A shipping container is 3 m wide, 4 m high and 8 m long. Find its volume.



- **11F** 9 A fruit box is 40 cm long, 30 cm wide and 20 cm high. Find its volume.
 - **10** There is enough ice on Earth to fill a cube of side length 300 km. Find the approximate volume of ice on Earth.



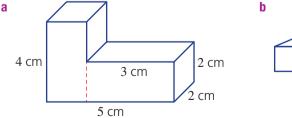
- 11 A box measuring 30 cm long, 20 cm high and 30 cm wide is packed with matchboxes, each 5 cm long, 2 cm high and 3 cm wide. How many matchboxes will fit in the box?
- **12** a Find the height of these rectangular prisms with the given volumes. Use trial and error if you wish.

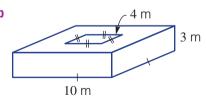


- **b** Can you explain a method that always works for finding the height of a rectangular prism?
- **c** Use V, l and w to write a rule for h.

Complex solids

13 These solids are made up of more than one rectangular prism. Use addition or subtraction to find the total volume of the solid.





13

11G Capacity

CONSOLIDATING

Learning intentions

- To understand that capacity is the volume of fluid or gas that an object can hold.
- To know that common metric units include millilitres, litres, kilolitres and megalitres.
- To be able to convert between common units for capacity.
- To be able to convert between the volume and capacity of a container.

Key vocabulary: capacity, volume, units

Capacity relates to the volume of fluid or gas that a container can hold. For example, the capacity of a water tank may be 5000 litres or a farmer's water allocation might be 300 megalitres (300 million litres).

The basic unit of capacity is the litre, which fills 1000 cm³ of space. Other common metric units include the millilitre, kilolitre and megalitre.

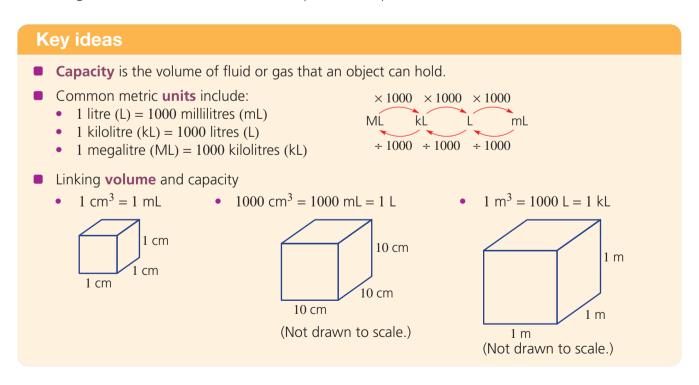


Lesson starter: Who has the most milk?

Megan, Rajesh and Toby each buy milk from their local store.

- Megan buys 1 litre.
- Rajesh buys 1000 cm³.
- Toby buys 1000 millilitres.

Who bought the most milk? How do these capacities compare?

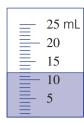


Exercise 11G

Understanding	1–3	3
 1 Complete these sentences. a The volume of fluid or gas that an object can hold is called its b 1 mL contains a volume of cm³. c 1 L contains mL. d 1 L contains cm³. e 1 kL contains L. f 1 ML contains kL. 	Hint: Refer back ideas for help	k to the Key
2 Copy and complete this flow chart.		
$\begin{array}{c} \times \underline{\qquad} \times 1000 \times \underline{\qquad} \\ \text{ML} kL \underline{\qquad} \text{mL} \\ \div 1000 \div \underline{\qquad} \div 1000 \end{array}$		
 Write the full name for these capacity units. a L b ML c mL d kL e cm³ f m³ 	centimetre,	e from: <i>cubic</i> , <i>cubic metre</i> , re, <i>megalitre</i> , <i>millilitre</i>
Fluency	4(1⁄2), 5, 6	4(1/2), 5, 6, 7(1/2)
Example 16 Converting units for capacity		
Convert to the units shown in brackets.a 500 mL (L)b 3 kL (L)SolutionExplanationa 500 mL = $(500 \div 1000)$ LWhen converting to There are 1000 mL in	U	livide.
= 0.5 L There are 1000 mL in $= 3000 L$ There are 1000 L in $= 3000 L$		y by 1000.
Now you tryConvert to the units shown in brackets.a 2.6 L (mL)b 500 kL (ML)		
 4 Convert to the units shown in brackets. a 400 mL (L) b 700 mL (L) c 2000 L (kL) d 36 000 L (kL) e 4000 kL (ML) f 500 kL (ML) g 2 L (mL) h 0.1 L (mL) i 6 ML (kL) j 3 ML (kL) k 24 kL (L) I 38 kL (L) m 2000 L (kL) n 3500 mL (L) o 70 000 mL (L) p 2500 kL (ML) q 0.257 L (mL) r 9320 mL (L) s 3.847 ML (kL) t 47 000 L (kL) u 5800 kL (ML) 	Hint: Divide by 1 mL to L, L to kL, Multiply by 1000 to kL, kL to L, L	, kL to ML.

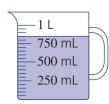
5 Read these scales to determine the amount of water in each of the containers.

b



а



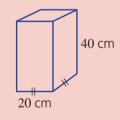


C

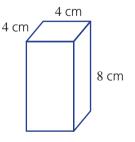
Example 17 Finding the capacity of rectangular prisms in litres Find the capacity of this container in: $a \text{ cm}^3$ b mL 10 cm c litres 20 cm **Explanation Solution** a $C = l \times w \times h$ C = lwh $= 20 \times 10 \times 10$ $= 2000 \text{ cm}^3$ $1 \text{ cm}^3 = 1 \text{ mL}$, so 2000 cm³ = 2000 mL. **b** C = 2000 mL $C = (2000 \div 1000) L$ There are 1000 mL in 1 litre, so divide by 1000. C = 2 LNow you try

Find the capacity of this container in:

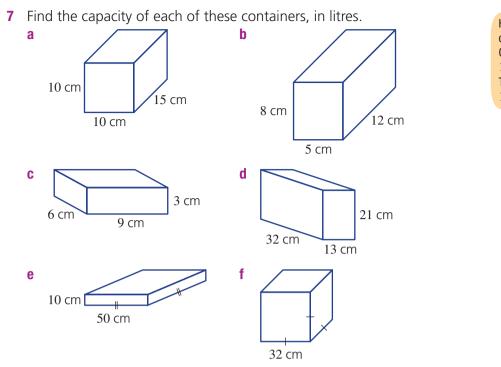
- a cm³
- b mL
- c litres



- 6 Find the capacity of this container in:
 - **a** cm³
 - b mL
 - c litres



11G



Hint: First find the volume in cm^3 . Convert to mL: $1 cm^3 = 1 mL$ Then convert to L: 1000 mL = 1 L

Problem-solving and reasoning

- 8 Write down which capacities are the same.
 - **a** 1 L, 10 kL, 1000 mL, 1 m³, 1000 cm³
 - **b** 1 m³, 100 L, 1000 L, 1000 ML, 1 kL

9 Choose the capacity (A to F) that best matches the container (a to f).

а	Teaspoon	Α	18 L
b	Cup	В	250 mL
C	Bottle	C	10 kL
d	Kitchen sink	D	20 mL
е	Water tank	Е	45 ML
f	Water in a lake	F	0.8 L



10-13

8-10

10 A cup of 200 mL of water is added to a jug already containing 1 L of water. Find the total capacity in:

a mL

С

h

- Convert to the units shown in brackets. 11
 - a 6 ML (L) 0.004 kL (mL)
- **b** 320 000 L (ML) **d** 992 700 mL (kL)
- 12 A farmer purchases 3.3 ML of water for her apple orchard. How many litres is this?



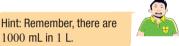
A dose of 12 mL of medicine is to be taken twice each day from a 0.36 L bottle. How many days will it 13 take to finish the medicine?

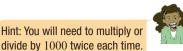




- 14 A swimming pool in the shape of a rectangular prism has length 50 m, width 25 m and depth 2 m. Find the swimming pool's:
 - **a** volume, in m^3 . **b** capacity, in L.
- **15** A dripping tap leaks about 10 mL every minute. Ħ
 - **a** If there are 50 drips per minute, find the volume of one drip.
 - Find the approximate volume of water, in litres, that has leaked from the tap after: b 100 minutes i. ii 1 hour iii 1 day iv 1 year







14-15

11H Mass and temperature CONSOLIDATING

Learning intentions

- To know that common metric units for mass are milligrams, grams, kilograms and tonnes.
- To know that temperatures are commonly measured in degrees Celsius °C, where 0° is the freezing point of water and 100°C is the boiling point of water.
- To be able to read a temperature scale (or thermometer).
- To be able to convert between units of mass.

Key vocabulary: mass, kilogram, tonne (t), temperature scale, Celsius

Mass relates to how heavy an object is. We use the metric units milligrams, grams, kilograms and tonnes to measure mass. The mass of a large elephant is about 4000 kg or 4 tonnes, while the mass of an ant is about 2 milligrams.

Temperature tells us how hot or cold something is. Anders Celsius (1701–1744), a Swedish scientist, worked to define a scale for temperature. After his death, temperature was officially defined by:

- 0°C (0 degrees Celsius) the freezing point of water.
- 100°C (100 degrees Celsius) the boiling point of water.

Lesson starter: Matching a mass or temperature

Work with a partner or group.

Name an object, place or situation to match each of these temperatures.

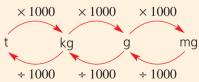
0°C
 20°C
 50°C
 100°C
 250°C
 −10°C

Name an object whose mass would be measured using:

tonnes
 • kilograms
 • grams
 • milligrams

Key ideas

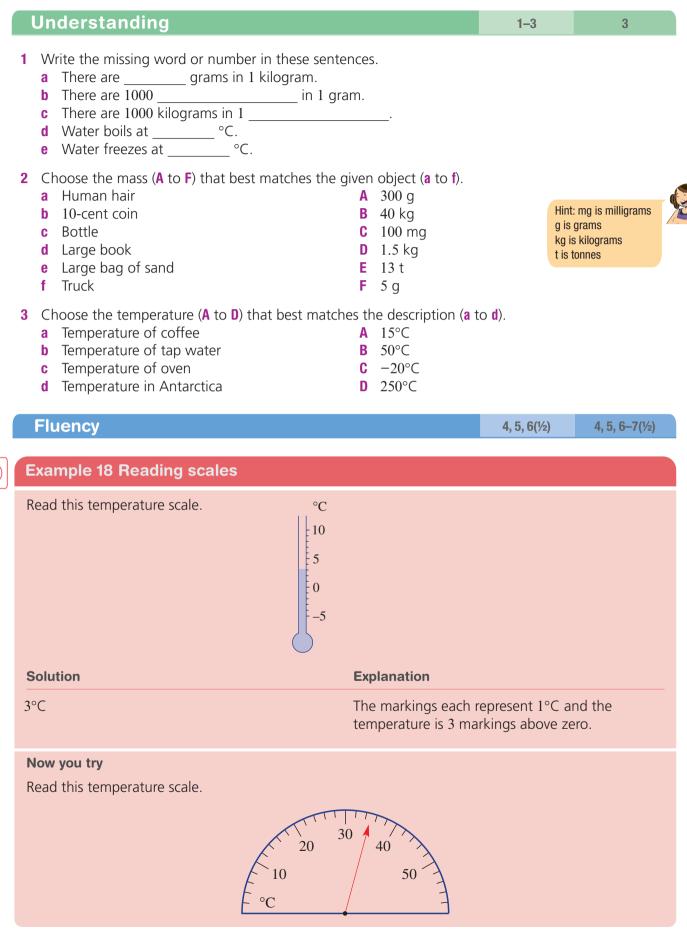
- The basic unit for mass is the kilogram (kg).
 - 1 litre of water has a mass that is very close to 1 kilogram.
- Metric units for mass include:
 - 1 gram (g) = 1000 milligrams (mg)
 - 1 kilogram (kg) = 1000 grams (g)
 - 1 **tonne** (t) = 1000 kilograms (kg)



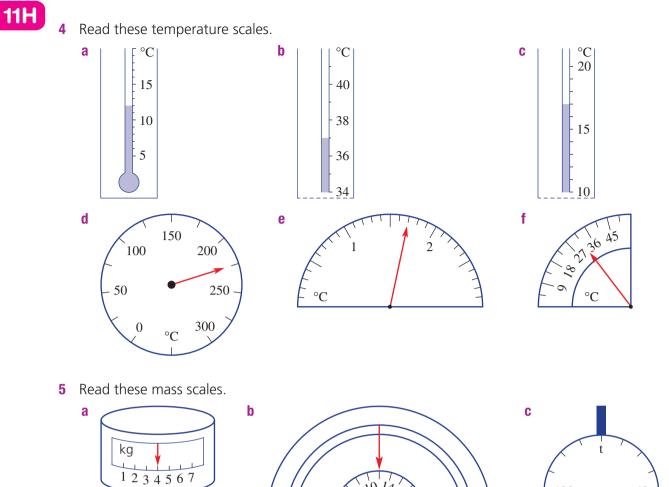
- The common unit for temperature is degrees Celsius (°C).
 - 0°C is the freezing point of water.
 - 100°C is the boiling point of water.



Exercise 11H



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Example 19 Converting units of mass	
Convert to the units shown in brackets.	
a 2.4 kg (g)	b 170 000 kg (t)
Solution	Explanation
a 2.4 kg = (2.4 × 1000) g = 2400 g	1 kg = 1000 g Multiply because you are changing to a smaller unit.
b 170 000 kg = (170 000 ÷ 1000) t = 170 t	1 t = 1000 kg Divide because you are changing to a larger unit.
Now you try	
Convert to the units shown in brackets. a 4.73 t (kg)	b 14000 mg (g)
	Convert to the units shown in brackets. a 2.4 kg (g) Solution a 2.4 kg = (2.4×1000) g = 2400 g b 170 000 kg = $(170\ 000 \div 1000)$ t = 170 t Now you try Convert to the units shown in brackets.

10 14

/6 g

5

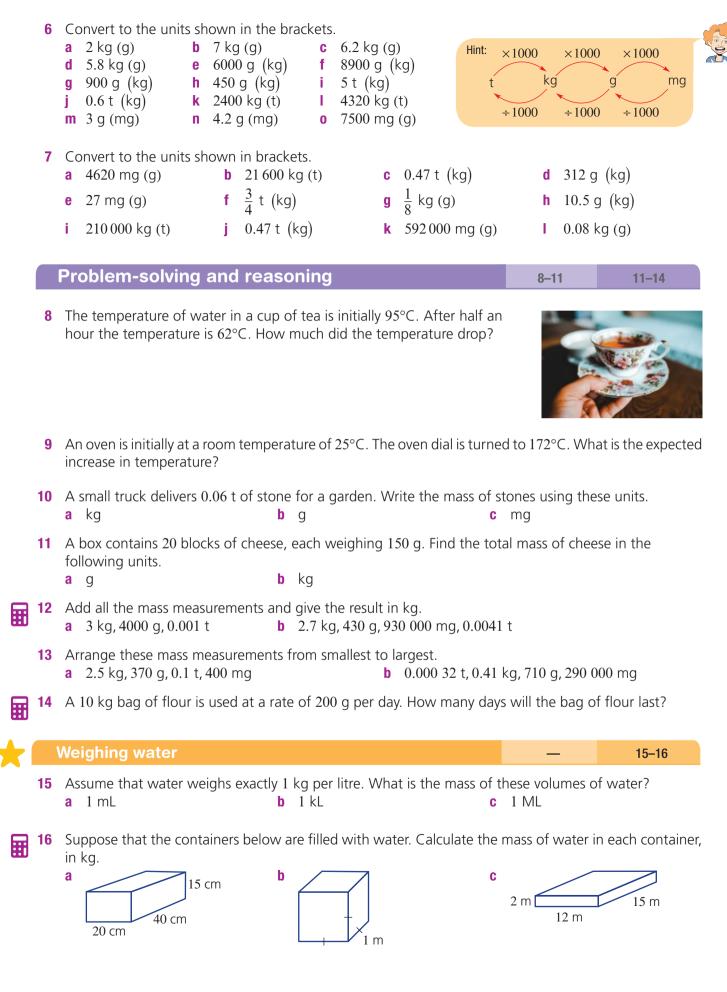
6

 $^{\circ}$

120

80

40



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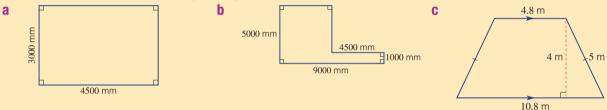
🔀 Maths@Work: Landscape gardener

Landscape gardening is a job suited to physically fit people who love the outdoors, plants and design. A friendly, cheerful manner and good communication skills are important when working with clients.

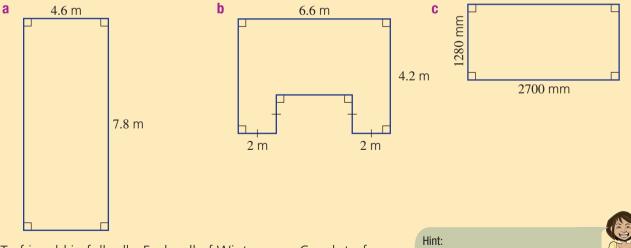
Landscape gardeners calculate perimeters, areas and volumes to work out costs and order materials. The geometry of angles and symmetry is applied when designing gardens.



- 1 For the following garden plots:
 - i calculate the perimeter (in metres) and area (in square metres) to 1 decimal place.
 - ii calculate the cost of a layer of garden mix soil at \$68.50 per 10 square metres.



- 2 Each of the areas below are to be covered with turf (i.e. lawn grass). For each lawn:
 - i calculate the area in square metres to 2 decimal places.
 - ii calculate the cost for Aussie Blue Couch turf at \$8.75 per square metre.



3 Turf is sold in full rolls. Each roll of Wintergreen Couch turf is a rectangle measuring 170 cm by 60 cm when rolled out. Determine the whole number of turf rolls needed to cover a rectangular lawn of length 6 m and width 3 m.

Work in the same units.

- Sketch a diagram.
- Calculate multiples of turf lengths and turf widths to cover the lawn.

4 Using these prices, calculate the cost of purchasing the materials needed, and the total cost for each landscape project (**a** and **b**), shown below. Round your answers to the nearest dollar.

Item	Selling unit	Price
Bedding sand to a depth of 80 mm	Volume	\$96.40/m ³
Pavers	Area	\$66.00/m ²
Sir Walter Buffalo turf	Area	\$10.24/m ²
Top soil over the lawn to a depth of 5 cm	Volume	\$135.70/m ³
Mulch to a depth of 100 mm	Volume	\$106.28/m ³
Edging – used around the mulch area	Length	\$19.96/m



a Backyard BBQ area

Bedding sand and pavers required.

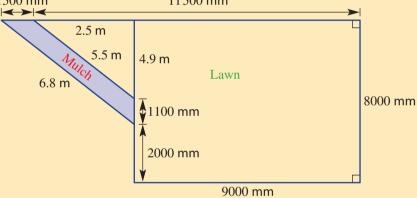


Hint: Bedding sand is laid under paving



b

Front yard Turf, top soil, mulch, and edging around the mulch area required. 1500 mm 11500 mm



Hint: The mulch area is the difference in area between two overlapping triangles.



Using technology

5 Using spreadsheets can help a landscape gardener with planning, ordering and cost calculations, and also to keep a record of projects. Set up the spreadsheet shown below and enter the required formulas. Follow the client's instructions (shown below right) to calculate relevant quantities. Format cost cells to currency/2 d.p.

1	A	В	с	D	E
1		Better La	ndscaping Comp	any	
2	Client: Jack and Jill Green				
3	Sections	Length in m	Width in m	Area in m ²	Perimeter in m
4	Front lawn	8	5.1		
5	Back garden	5.8	2.2		
6	PLANTS	Number	Price for one	Total cost	
7	Trees	2	\$36.00		
8	Shrubs	5	\$11.50		
9	Punnets of vegetables	6	\$4.55		
10	MATERIALS	Quantity	Cost per unit	Total cost	
11	Legend Couch turf in m ²		\$10.75		
12	Garden edge blocks in m		\$14.80		
13	Garden soil in m ³		\$65.00		
14			Overall cost		

CI	ient's instructions
•	Turf laid over the front lawn.
•	Edge blocks border the
	perimeter of the back

garden.

• Garden soil to the depth of 120 mm spread over the garden area.

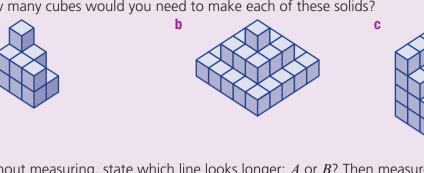
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How many cubes would you need to make each of these solids? 1

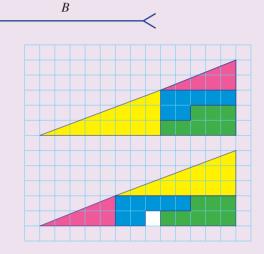




- Without measuring, state which line looks longer: A or B? Then measure to check your answer. 2
- Do these two shapes to the right have the same area? 3 Explain the 'hole' in the second shape.

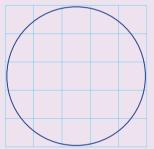
 \rightarrow

A



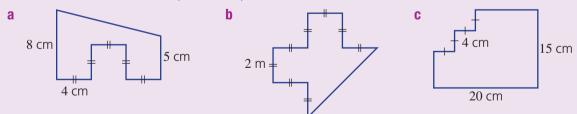
Count squares to estimate the area of these circles. 4





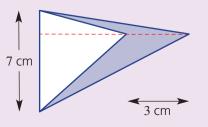
Find the areas of these composite shapes. 5

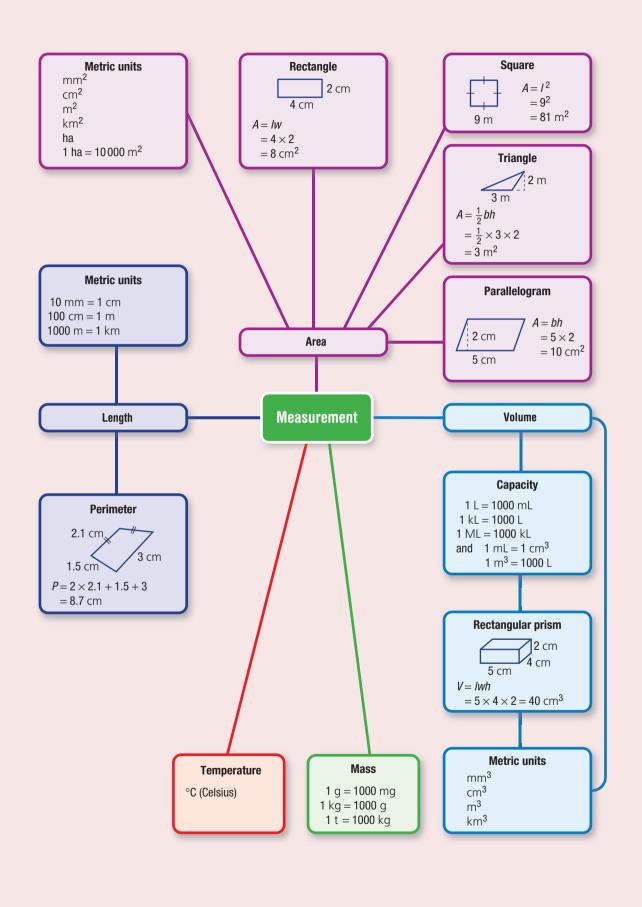
а



b

- 6 You have two sticks of length 3 m and 5 m. Neither stick is marked with a scale. How could you use the sticks to mark a length of 1 m?
- 7 Find the area of the shaded region.





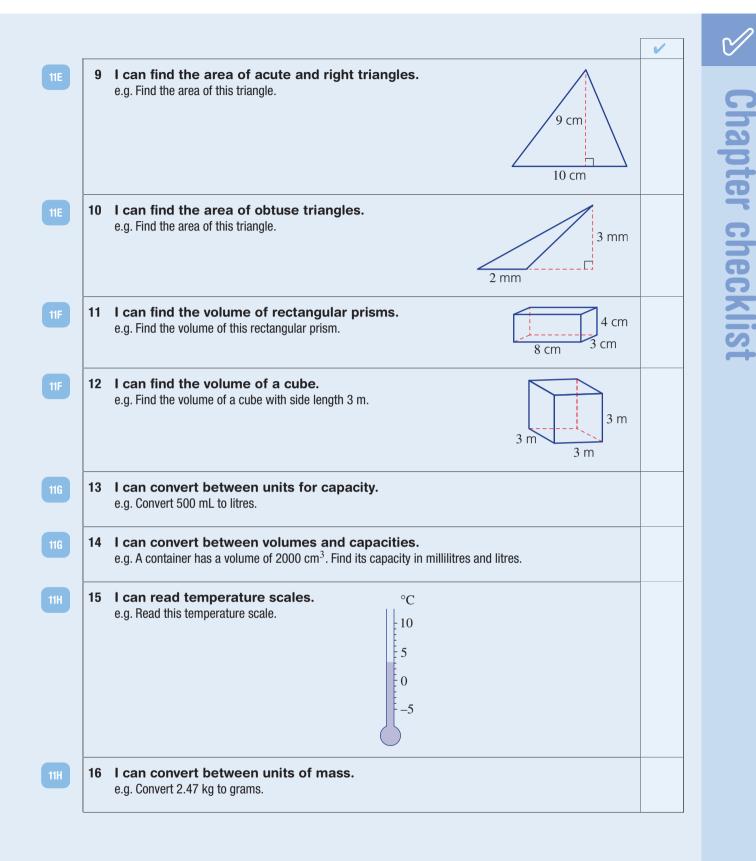
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Chapter checklist

A version of this checklist that you can print out and complete can be downloaded from your Interactive Textbook.

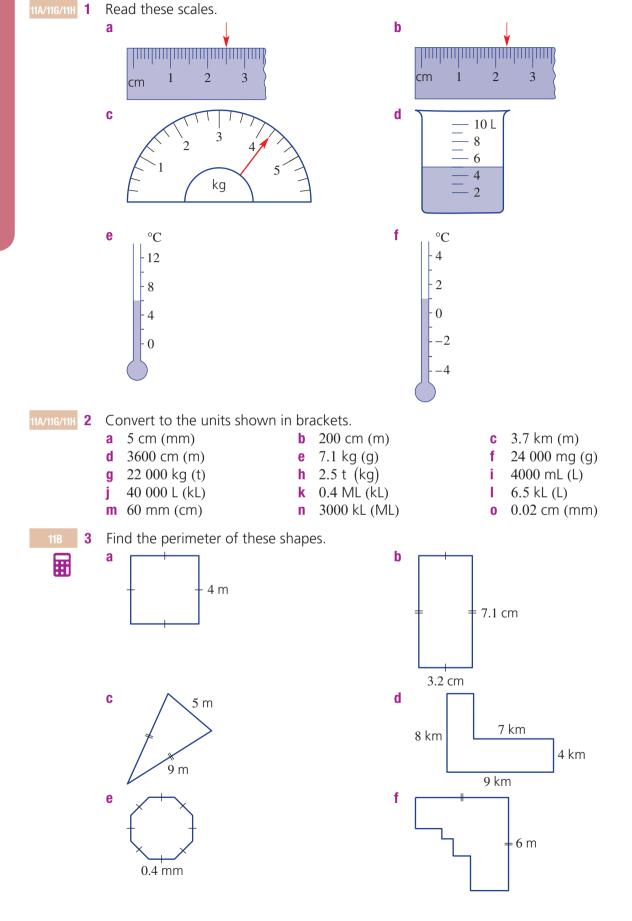
		~
11A	1 I can choose an appropriate metric unit for measuring a length. e.g. Which metric unit would be most appropriate for measuring the width of a large room?	
11A	2 I can read a length scale. e.g. Read the scale to measure the marked length.	
11A	3 I can convert metric units of length by multiplying or dividing. e.g. Convert 3 m to cm, and convert 39 mm to cm.	
118	4 I can find the perimeter of shapes. e.g. Find the perimeter of this shape.	
118	5 I can find the perimeter of L-shapes using a rectangle. 11 mm e.g. Use a rectangle to help find the perimeter of this L-shape. 7 mm	
110	6 I can find the area of a shape by considering squares on a grid. e.g. Count the number of squares to find the area of the shape drawn on this centimetre grid.	
110	7 I can find the area of squares and other rectangles. e.g. Find the area of this rectangle. 4 mm 10 mm	
110	8 I can find the area of parallelograms. e.g. Find the area of these parallelograms. 5 m 3 cm 12 m 2 cm	

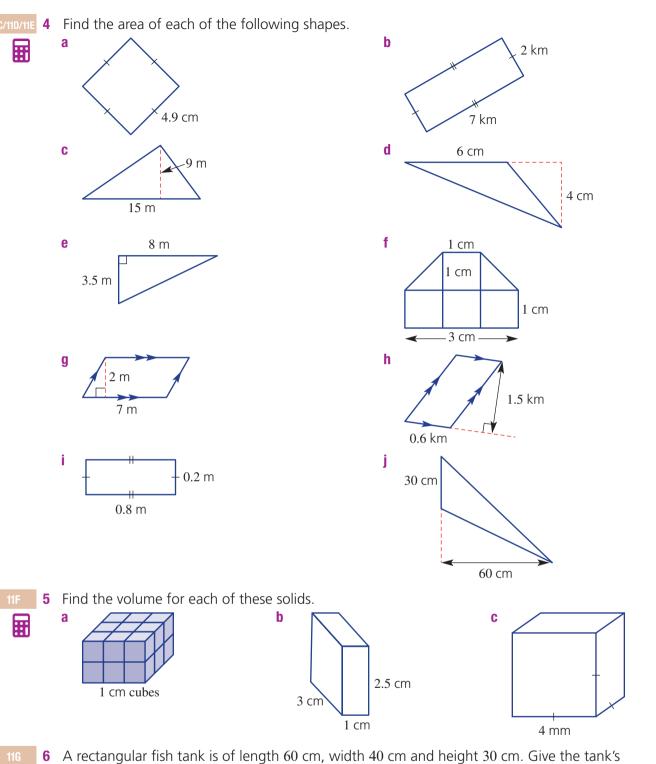
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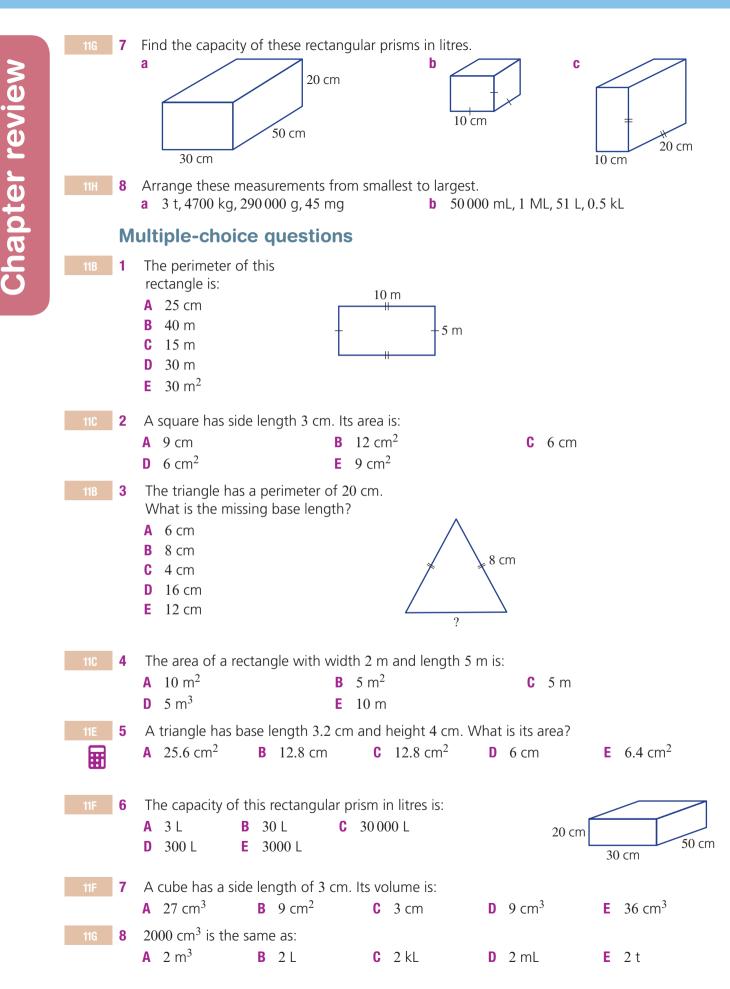
- 11G
- a cm³
 - b mL

capacity in:

C L



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9

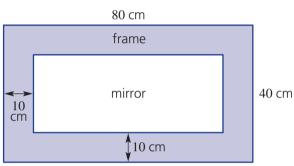
- **9** Gravel is being loaded onto a truck at a rate of 20 kg per second. How many minutes will it take to load all of the 9 tonnes of gravel?
- **A** 0.75 min **B** 45 min **C** 7.3 min **D** 450 min **E** 7.5 min



10The base length of a parallelogram is 10 cm and its height is 4 cm. The parallelogram's area is:A20 cm²B40 cm²C30 cm²D4 cm²E40 m²

Extended-response questions

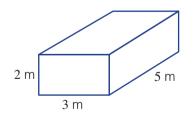
A mirror is surrounded by a 10-cm-wide frame so that the total dimensions are 80 cm by 40 cm as shown.



- **a** Find the outside perimeter of the frame.
- **b** Find the total area of the framed mirror.
- **c** Find the width and length of the mirror alone.
- **d** Find the perimeter of the mirror alone.
- e Find the area of the mirror alone.
- **f** Find the area of the frame.
- g Find the cost of the frame if it is \$5 per 50 cm².
- A simple rectangular swimming pool is 5 m long, 3 m wide and 2 m deep.
 - **a** Find the volume of the pool in m³.
 - **b** Find the perimeter of the rectangular top of the pool.
 - **c** By converting the given lengths to cm, find the volume of the pool in cm³.
 - **d** Give the capacity in litres and in kilolitres.
 - e Given that 1 L weighs 1 kg, how many tonnes of water fill the pool?



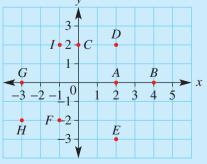




Semester review 2

	egative number													
	ort-answer question				,				(1		、			
1	For each of the f	ollo	wing, ins		-							_		
	a -3 3			b	-4	-5				C	-21			
2	Calculate: a 4 – 5 b	1	- 6	C	0 -	10	d	-4 -	2	е	-7 - 1	11	f -	-37 - 40
3	Calculate:													
	a $2 + (-1)$ d $-1 + (-4)$				11+	(-7) + (-2)					5 + (-31 +)	· · · · · · · · · · · · · · · · · · ·	`	
				C	10	+(2,)			1	51 +	(20)	
4	Calculate: a $3 - (-2)$			b	6 –	(-1)				С	11 - (-13)		
	d $-4 - (-3)$					- (-7)				-11 -)	
5	Copy and comple	ete:												
	a $+9 = -6$			b	4 -	= 7				C	-2+	_ = -	-10	
6	If $a = 6$ and $b = -$	-4. f	ind the v	/alu	e of:									
	a - <i>a</i> + <i>b</i>			b	a – 1						2(b -			
	d $2a-b$			е	<i>b</i> + (<i>ba</i>				f	4a - b	b + b		
М	ultiple-choice ques	tion	S											
1	Which of the foll											_		
	A $-2 > -4$	В	0 < 5		C	0 < ·	-10		D	-9 <	-8	E	-5 <	< 3
2	5-7 is equal to:		2		0	10				10			0	
	A −2	В	2		U	12			U	-12		E	0	
3	4 + (-2) is equal A -6	to: B	2		C	6			п	-2		F	-4	
		_	2		U	0			U	2		1	7	
4	9 – (–3) is equal A 13		-12		C	-6			D	6		Е	12	
5	The origin is the			con			umh	or pla			oordin	- atos:		
J	A (0, 1)	•	(1, 1)	Cen		(1, ((0, 0)		E	(10,	10)
E.	tondod roononoo r	1100	tions											
E) 1	tended-response q Look at this num													
	a Give the coord		-	ich	point	(A-I)								
	b Name any poi							Э.			J • 2		D	

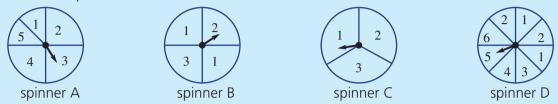
- Where does each point lie?
- **c** Find the number of units between points:
 - i A and B
 - i D and E
- **d** What shape is formed by joining the points *IDAG*?
- e If each square is one cm square, what is the area of *IDAG*?
- f Decode: (2, 2), (2, -3), (0, 2), (-1, 2) (2, 2), (2, -3) using the letters on the number plane.



Statistics and probability

Short-answer questions

- 1 Consider the set of numbers 1, 2, 5, 5, 8, 9, 10, 5, 3, 8.
 - a List the numbers in ascending order.
 - **b** How many numbers are in the set?
 - **c** Calculate the:
 - i mean ii mode iii median iv range
 - **d** If each number in the set is doubled, what is the new mean?
- 2 Consider the spinners A to D.



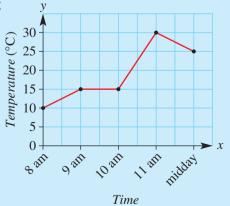
- **a** Which spinner has the lowest probability of landing on the number 1 in a single spin?
- **b** Which spinner has a 50% probability of landing on the number 1 in a single spin?
- **c** What is the probability that spinner C will land on the number 2?
- **3** A standard die is rolled.
 - a What is the sample space?
 - **b** What is the probability of rolling a 2?
 - **c** What is the probability of rolling an odd number?
- 4 This stem-and-leaf plot shows the ages of a group of people in a room.
 - a How many people are in the room?
 - **b** What are the ages of the youngest and oldest people?
 - **c** For the data presented in this plot, find the:
 - ii median iii mode i range

Stem	Le	af		
0	3	5		
1	1	7	9	
2	0	2	2	3
3	6	9		
4	3	7		
2	3 me	eans	23	years old

- 5 A line graph is drawn charting the room's temperature at different times of the day.
 - **a** What was the temperature at:

i 8 a.m.? **ii** 10 a.m.?

- 11 a.m.? **b** How much did the temperature increase between 10 a.m. and 11 a.m.?
- c What was the approximate temperature at 10:30 a.m.?



Multiple-choice questions

The following information is relevant for questions 1 and 2. A survey asked 60 participants their favourite colour. The results are shown below.

		blue	pink	green	purple	black	
		12	20	6	12	10	
1	The number of people we have a second		• •	as their fa 6		lour was: 60	E 10
2	Based on this survey, th favourite colour is black A 1 B	is:		robability t $\frac{1}{6}$		omly-seled	cted person's E $\frac{1}{3}$
3	For the set of numbers A 5.5 B			the media 7		5	E 1
4	For the set of numbers A 3 B			1, 2, the r 6	nean is: [22.375	E 3.125
5	Which of the following A Unlikely D Certain	could be	B Like		an event w		a probability of 0.9? Even chance

Extended-response questions

1 A pack of playing cards contains 13 cards for each suit: hearts, diamonds, clubs and spades. Each suit has an Ace, King, Queen, Jack, 2, 3, 4, 5, 6, 7, 8, 9 and 10. One card is drawn at random from the pack.

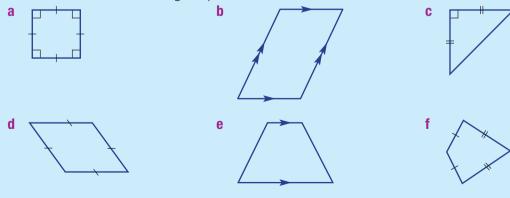
Find the following probabilities and write them as a fraction.

- **a** Pr(heart)
- **b** Pr(club)
 - e Pr(number less than 4)
- **d** Pr(Ace of hearts) **g** Pr(Ace or heart)
- **h** Pr(Queen or club)
- **c** Pr(diamond or spade)
- **f** Pr(King)

Shapes and transformations

Short-answer questions

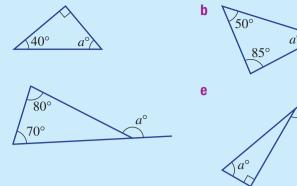
1 Name each of the following shapes.



2 Find the value of *a*.

а

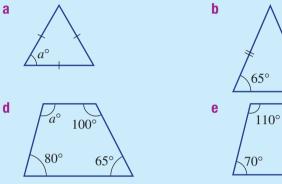
d



3 For each of the following, find the value of each pronumeral.

60°

 h°

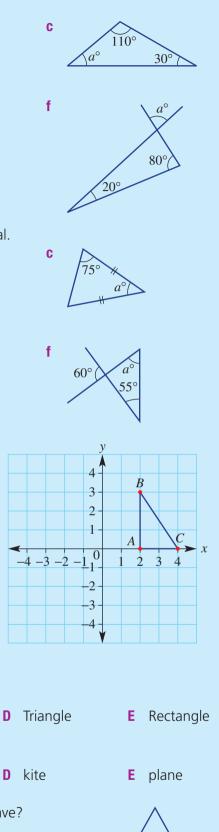


- 4 State the coordinates of the vertices of the image triangle (*A*', *B*' and *C*') if triangle *ABC* is transformed in the following ways:
 - a reflected in the x-axis
 - **b** reflected in the *y*-axis
 - **c** rotated about O(0,0) by 90° clockwise
 - **d** rotated about O(0, 0) by 90° anticlockwise
 - e rotated about O(0,0) by 180°
 - f translated 4 units to the left and 1 unit up
 - g translated 3 units to the left and 2 units down

Multiple-choice questions

- 1 Which of the following shapes has four 90° angles?
- A Trapezium B Rhombus C Pentagon
- 2 A quadrilateral with 4 equal sides is best described as a:
 - A rectangle B rhombus C trapezium
- 3 How many axes of symmetry does an equilateral triangle have?

A 0 **B** 1 **C** 2 **D** 3 **E** 4



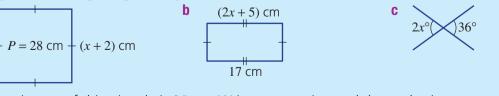
- 4 Which one of the following statements is true?
 - A All rectangles are squares.
 - **B** All isosceles triangles are equilateral triangles.
 - **C** A square is a rhombus with all angles equal.
 - **D** A trapezium is also a rectangle.
 - **E** An isosceles triangle has three equal angles.
- **5** The order of rotation of a parallelogram is:
 - **B** 4 **C** 3 **E** 1 **A** 2 **D** 0

Extended-response questions

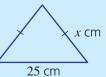
- **a** Draw any triangle and extend each side, as shown at the right.
 - **b** Measure the angles *a*, *b* and *c*. What should they add to?
 - **c** Find the values of x, y and z (i.e. the exterior angles of the triangle).
 - **d** What is the total of angles x + y + z?
 - e Repeat for any guadrilateral, as shown below. What is the value of w + x + y + z?

Equations

Short-answer questions 1 Classify the following equations as true or false. **a** 2+17=10+8 **b** 5=10-5**c** x + 2 = 10 if x = 8**d** a - 3 = 7 if a = 4e 12 = 20 - k if k = 6 f y - 3 = 3 if y = 62 Solve **b** $\frac{x}{9} = 12$ **c** x - 9 = 12 **d** 9x = 12**a** x + 9 = 12**3** Solve: **b** 2y-7=3 **c** $\frac{x}{2}+6=12$ **d** $\frac{m-1}{3}=2$ **a** 3x + 3 = 94 Consider the formula P = 4w. **a** Find the value of *P* if: w = 2w = 5w = 12**b** Solve the equation 24 = 4w. **c** Find the value of w if P = 24. **d** Find the value of w if P = 44. 5 Use your knowledge of geometry and shapes to find the value of x in each of the following.



6 The perimeter of this triangle is 85 cm. Write an equation and then solve it to find the value of *x*.



а

Multiple-choice questions

1 The solution to the equation x - 3 = 7 is:

B x = 10 **C** x = 9**D** x = 11 **E** x = 3**A** x = 4

- **2** The solution to the equation 2x + 6 = 12 is:
 - **C** x = 7**D** x = 6**E** x = 3**A** x = 4.5**B** x = 2
- 3 m = 4 is a solution to:
 - **B** $\frac{m}{4} = 16$ **C** 10 2m = 2 **D** m + 4 = 0 **E** 3m 6 = 2**A** 3m + 12 = 0
- 4 The solution to 2p 3 = 7 is: **A** p = 4**B** p = 5**C** p = 2 **D** p = 10**E** p = 3
- 5 Ying thinks of a number. If he multiplies the number by 5 and then subtracts 4, the result is 35. What equation represents this information?

A v + 9 = 35**B** 5y - 4 = 35**C** 5y + 4 = 35 **D** 5(y + 4) = 35 **E** y + 20 = 35

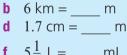
Extended-response questions

- 1 The cost of hiring a hall for an event is \$200 plus \$40 per hour.
 - a What is the cost of hiring the hall for 3 hours?
 - **b** What is the cost of hiring the hall for 5 hours?
 - **c** Write a formula for the cost \$*C* of hiring the hall for *n* hours.
 - d If the cost of hiring the hall totals \$460, for how many hours was it hired?

Measurement

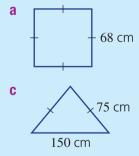
Short-answer questions

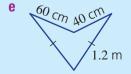
- 1 Complete these conversions.
 - **a** 5 m = cm
 - **c** 180 mm = cm
 - **e** 180 cm = ____ m

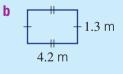


$$5\frac{1}{2}$$
 L = ____ ml

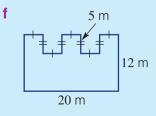
2 Find the perimeter of each of the following.



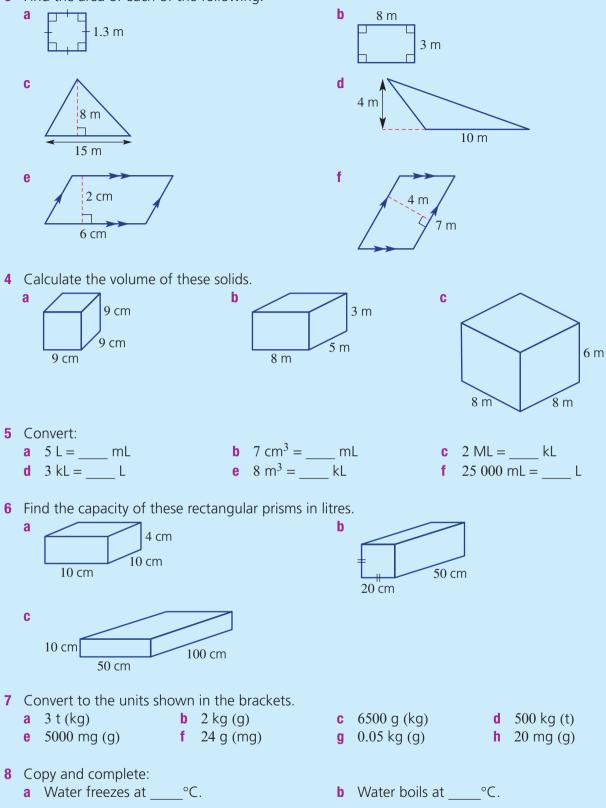


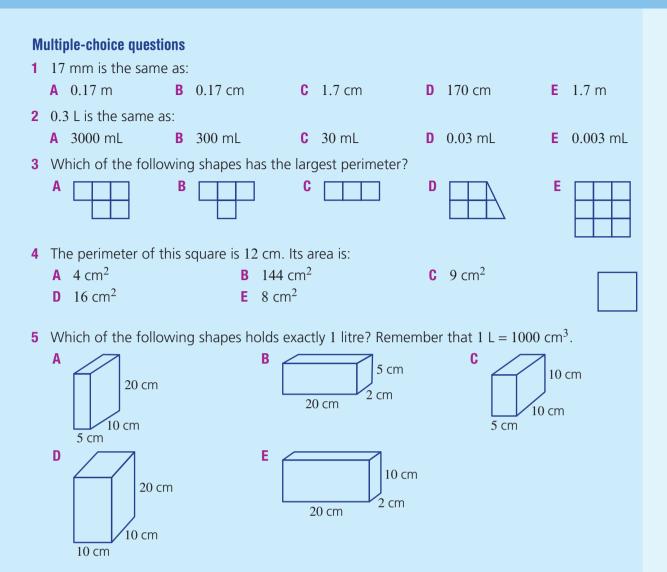






3 Find the area of each of the following.





Extended-response questions

- 1 Robert has been given 36 m of fencing with which to build the largest rectangular enclosure that he can, using whole number side lengths.
 - a Draw three possible enclosures and calculate the area of each one.
 - **b** What are the dimensions of the rectangle that gives the largest possible area?
 - **c** If Robert chooses the dimensions in part **b** and puts a post on each corner, and then posts every metre along the boundary, how many posts will he need?
 - d If each post costs \$25, what will be the total cost of the posts?



Chapter Algorithmic thinking

Autopilot algorithms

Modern aircraft are fitted with autopilot systems that allow the aircraft to fly safely without direct input from the pilot. Such systems rely on computer algorithms that have been designed to accept a range of inputs and deliver outputs resulting in actions that steer the aircraft safely.

Inputs for such algorithms might include the air speed, direction or tilt angle. The outputs might include engine thrust, flap angle or rudder direction. While looking at the wing on a passenger aircraft during flight you may have noticed the constant movement of a relatively small flap called an aileron. An autopilot algorithm causes this flap to change its angle, which adjusts the aircraft's tilt. A constant feed of information into the algorithm will allow the program to update the output and change the aileron's angle accordingly.

Autopilot systems have become a reliable and essential tool for the aeronautical industry. This would not have been possible without efficient algorithms designed using mathematics and computer code.

In this chapter

Activity 1: Algorithms for working with data _____

- 1.1 Finding an average
- 1.2 Generating data: simulation using a spreadsheet

Activity 2: Adding consecutive numbers

Activity 3: Turtle graphics 3.1 Basic shapes

3.2 Patterns

Victorian Curriculum

NUMBER AND ALGEBRA Patterns and algebra

Design and implement mathematical algorithms using a simple general purpose programming language (VCMNA254)

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Online resources

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Introduction

An **algorithm** is a procedure involving a number of steps. It should have clearly defined inputs and outputs.

Here are some examples that have been explored in earlier chapters.

- The addition algorithm for whole numbers: This algorithm has two inputs, for example, the inputs 37 and 82 would give the output 119. The steps involved include adding the digits in each place, and checking whether carrying is required. This algorithm is shown in Section 1D.
- The divisibility algorithm for determining if a number is divisible by 10: The input is a single number, such as 80 or 42, and the output is 'yes' or 'no'. This algorithm is shown in Section 3C.
- The averaging algorithm: The input for this algorithm is a list of numbers, such as 5, 2, 8. The algorithm adds the numbers (5+2+8=15) and divides by the number of terms in the input list (in this case, 3) to give an output $(15 \div 3 = 5)$. This algorithm is shown in Section 8B.

Activity 1: Algorithms for working with data

STATISTICS AND PROBABILITY

1.1 Finding an average

Let us look again at the algorithm for finding the average (or mean) of a set of numbers. The algorithm could be described as follows.

Step 1. Add all the numbers in the list.

Step 2. Count how many numbers are in the list.

Step 3. Divide the sum (from step 1) by the count (from step 2). This is the average.

- **a** Using the numbers 10, 1, 4 as the input list, calculate the results of steps 1, 2 and 3 of the averaging algorithm.
- **b** A spreadsheet can be used to implement this algorithm. Open a new spreadsheet and enter the following. Check that the values in cells B2, C2 and D2 match the values you found in **a**.

1	A	В	С	D
1	Values	Step 1	Step 2	Step 3
2	10	=SUM(A2:A4)	=COUNT(A2:A4)	=B2/C2
3	1			
4	4			

- **c** Change the values in column A until the average of the three values is 9. Write down the values you chose.
- **d** One advantage of using a spreadsheet is that it is easy to work with a longer list of values. Enter two more values into column A so that there are now five values. You will need to change the formula for step 1 to =SUM(A2:A6) and the formula for step 2 to =COUNT(A2:A6). Step 3 does not change. Check that your spreadsheet is giving the correct answer by calculating the average with a calculator.

- e Try to solve each of the following puzzles using your spreadsheet. You can use trial and error to find the missing values.
 - i The values are 1, 2, ?, 4, 5 and the average is 4. Find the missing number.
 - ii The values are 1, 10, 100, 1000, ? and the average is 500. Find the missing number.
 - iii The five values are all whole numbers but the average is 3.2. Find possible values that make this happen.
 - iv The average of five consecutive numbers is 100. What are the numbers?

1.2 Generating data: simulation using a spreadsheet

A spreadsheet can be used to generate data that simulates an experiment, such as rolling a fair die five times to see how many times the number 1 is rolled.

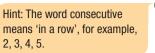
a Make a new spreadsheet with the following formulas. (If your spreadsheet does not have the function RANDBETWEEN, use = RANDINT(1, 6) or = RAND(1, 6) instead.)

À	A
1	Die
2	=RANDBETWEEN(1,6)
3	=RANDBETWEEN(1,6)
4	=RANDBETWEEN(1,6)
5	=RANDBETWEEN(1,6)
6	=RANDBETWEEN(1,6)
-	

Hint: Once you have entered the formula into A2, you can use Fill Down to copy it as many times as you wish.

- **b** To make your spreadsheet 'roll' the dice another five times, choose Calculate Now from the Formulas menu, or an equivalent function in different spreadsheets. Alternatively, if you just change the value in any cell, all other values will recalculate.
- **c** Count how many times the number 1 is rolled. You can easily do this by looking at the numbers, but it will be more useful to have the spreadsheet count for you. Enter the formula =COUNTIF(A2:A6,1) in B1 and check that the answer is correct.
- **d** Now change your spreadsheet to include 100 dice rolls by dragging the formula in A6 to row 101. Count how many times the number 1 was rolled, remembering to change the formula to =COUNTIF(A2:A101, 1).
- e In cell C1, enter the formula = SUM(A2:A101)/COUNT(A2:A101). This calculates the average of the 100 dice rolls.
 - i Write down the average of the 100 dice rolls.
 - ii Why does this average change every time you recalculate?

	А	В	С
1	Die	=COUNTIF(A2:A101,1)	=SUM(A2:A101)/COUNT(A2:A101)
2	=RANDBETWEEN(1,6)		
3	=RANDBETWEEN(1,6)		
4	=RANDBETWEEN(1,6)		
5	=RANDBETWEEN(1,6)		
6	=RANDBETWEEN(1,6)		
7	=RANDBETWEEN(1,6)		





Activity 2: Adding consecutive numbers

NUMBER AND ALGEBRA

One task that an algorithm can perform is adding the consecutive whole numbers 1, 2 and 3. Although it might seem unnecessary to use an algorithm for such a simple task, we can easily change the algorithm to add much longer sequences. The algorithm is written below in **pseudocode**. This is not an actual programming language, but uses some of the same concepts.

Line	Command	Explanation
1	total $\leftarrow 0$	total is the sum of the numbers so far.
2	current $\leftarrow 0$	current is the number we are up to as we loop.
3	loop:	Performs lines $4-6$ forever (until you hit break).
4	current \leftarrow current + 1	Adds 1 to the current number.
5	total \leftarrow total + current	Increases the total by the current number.
6	if current = 3: break	If we reach the number 3, we leave this loop.
7	display total	At the end we need to display the total.

A computer can run this program line by line. The execution is shown below and takes 13 steps.

Line	Command	Result
1	total $\leftarrow 0$	total is set to 0.
2	current $\leftarrow 0$	current is set to 0.
3	loop:	Get ready to repeat lines 4 to 6.
4	current \leftarrow current + 1	current is now 1 (because $0 + 1 = 1$).
5	total \leftarrow total + current	total is now 1 (because $0 + 1 = 1$).
6	if current = 3: break	No effect, because current is not 3.
4	current \leftarrow current + 1	current is now 2 (because $1 + 1 = 2$).
5	total \leftarrow total + current	total is now 3 (because $1 + 2 = 3$).
6	if current = 3: break	No effect, because current is not 3.
4	current \leftarrow current + 1	current is now 3 (because $2 + 1 = 3$).
5	total \leftarrow total + current	total is now 6 (because $3 + 3 = 6$).
6	if current = 3: break	Exit the loop, because current is 3.
7	display total	Displays the value of total, which is 6.

- **a** What is the sum of the consecutive numbers from 1 to 3?
- **b** What is the sum of the consecutive numbers from 1 to 5? Show a calculation that could be entered into a calculator or computer to get the result.
- **c** By changing a single line, the program above will add the consecutive numbers from 1 to 5.
 - i To describe this change, give the line number and write the exact command you think should go there.
 - ii Create a table like the one at the right to show the steps of this program. At first, the results will be the same as those in the table above, but this loop will exit at a different line.

Line	Result	
1	total is 0	
2	current is 0	
3	Begin loop	
4	current is 1	
5	total is 1	
6	No action	
4	current is 2	
5	total is 3	
6	No action	
	•••	

- **d i** When adding the numbers from 1 to 3, the total execution was 13 steps. How many steps does it take to add the numbers from 1 to 5?
 - ii Estimate how many steps it would take to add all the whole numbers from 1 to 100.
 - iii Describe how the program could be changed to add the whole numbers from 1 to 100.
- e Adding all the numbers from 1 to 100 is tedious to do by hand. You can perform this algorithm in any programming language, or in a spreadsheet. If you know how to use a programming language then try to complete this part in a programming language, but otherwise you can use the spreadsheet below.
 - i To set up the spreadsheet, just fill in the top three rows as shown. Then fill down row 3 to row 102.

1	A	В	
1	Current	Total	
2	0	0	
3	=A2+1	=A3+B2	
4	=A3+1	=A4+B3	
5	=A4+1	=A5+B4	
6	=A5+1	=A6+B5	
7	=A6+1	=A7+B6	
8	=A7+1	=A8+B7	
9	=A8+1	=A9+B8	
10	=A9+1	=A10+B9	
11	=A10+1	=A11+B10	
12	=A11+1	=A12+B11	
13	=A12+1	=A13+B12	

- ii What is the sum of all whole numbers from 1 to 100?
- iii The year 2016 was special because it is the sum of consecutive numbers starting at 1. How many consecutive numbers were added to get 2016?
- **f** Instead of adding consecutive numbers, we could write an algorithm to add numbers in a different sequence, such as 2, 4, 6, 8, 10.
 - i Using pseudocode, write an algorithm that uses a loop to add the numbers 2, 4, 6, 8 and 10.
 - ii Describe how to change your algorithm to add all the even numbers from 2 to 1000.
 - iii Find the sum of all the even numbers up to and including 1000. You could use a spreadsheet like the one above, but change A3 to "=A2 + 2," and then fill down to row 502.



Activity 3: Turtle graphics

MEASUREMENT AND GEOMETRY

'Turtle graphics' refers to a style of computer graphics made famous by the Logo programming language. It involves describing the path of a turtle that can draw as it moves along. The turtle faces a given direction (initially upwards) and at each step, it walks forward (or backward) a given distance, or turns by a given angle. A simple set of instructions to use is:

- FW x: Move the turtle forward x 'steps'.
- RT x: Turn the turtle right x degrees (clockwise).
- LT x: Turn the turtle left x degrees (anticlockwise).
- REP *n* [...]: Repeat the instructions in the brackets *n* times.

3.1 Basic shapes

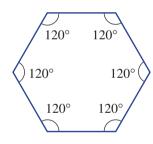


a Using a protractor and a ruler, draw an equilateral triangle by following the turtle graphics commands below. (The steps are in centimetres and you should start in the centre of the page, facing the top.)

FW 5, RT 120, FW 5, RT 120, FW 5, RT 120

The shape could also be formed using the loop REP 3 [FW 5, RT 120].

- **b** Explain what would happen if you turned 60° rather than 120°.
- **c i** Use your protractor and ruler to show the result of REP 3 [FW 5, LT 120].
 - ii How is this shape different from the one in a? How is it similar?
- **d** Write a set of commands that could be used to draw a square. Try to use the REP instruction.
- e A regular hexagon has six sides of the same length with internal angles of 120°.



i Jack predicts that the following program will draw a regular hexagon. Is he correct? Describe what happens when you follow the steps.

REP 6 [FW 5, RT 120]

- ii To draw a regular hexagon, what is the correct angle that the turtle needs to turn each time? Hint: Extend the line out from one side and measure the angle to turn.
- f Sarah wants the turtle to turn right each time. Rewrite the following program so that it draws the same shape but without using LT.

FW 10, LT 90, FW 10, LT 300, FW 5

3.2 Patterns

The following turtle graphics commands are useful for drawing patterns. They allow you to move the turtle without drawing a line.

- PU: Lift the pen up off the page.
- PD: Put the pen back down onto the page.

a A simple dashed line can be created by picking up the pen after drawing a section and then putting it down again. For instance, the following commands create a dashed line:

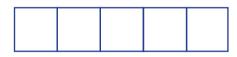
FW 2, PU, FW 1, PD, FW 2, PU, FW 1, PD

Write a simple program that makes a dashed line with 10 sections that are 2 cm long, with a 1 cm gap in between.

- **b** Another pattern can be formed with parallel lines.
 - i Draw the result of the following commands using a protractor and ruler.

FW 10, PU, RT 180, FW 10, LT 90, FW 5, LT 90, PD, FW 10

- ii Design a program that draws 10 parallel lines that are each 10 cm long. Hint: Use the REP command.
- **c** You can draw a 5-cm-wide square using REP 4 [FW 5, RT 90]. To draw a second square joined to the first, you could move the pen to the next starting point with the commands: PU, REP 3 [FW 5, RT 90], PD.
 - i The turtle is not facing upwards after these commands. Write a command that would turn it to face upwards again.
 - ii Write a program that draws 5 squares in a row.



d A similar technique can be used to draw regular hexagons in a row. After one hexagon has been drawn using REP 6 [FW 5, RT 60], the turtle is moved (with the pen up) from location A to location B, and turned to face upwards again using the commands PU, REP 4 [FW 5, RT 60], REP 2 [RT 60], PD



- i Follow the commands to check. Why is the command REP 2 [RT 60] used?
- ii How could this be simplified to a single command not involving repetition?
- iii Write a program that draws five hexagons in a row to form the pattern below.



• A honeycomb pattern of hexagons can continue indefinitely in each direction. The bottom two rows of a honeycomb pattern are shown below. Design a program that draws these two rows. Hint: Draw the bottom row first. With the pen up, move to the start of the top row.



Α

Acute angle An angle between 0 and 90 degrees

Acute triangle A triangle in which all the angles are acute (less than 90°)

Addition The process of calculating the total of two or more numbers

Adjacent Next to each other

Algorithm A procedure involving a number of steps to find the answer of a problem

Align To bring something into line with something else

Alternate angles Two angles that lie between two lines on either side of a transversal

Angle The amount of turn between two lines around their vertex

Angle sum The total measure of the interior angles in a 2D shape

Anti-clockwise In the opposite direction of hands moving on a clock

Approximation A value that is close to the real value

Arc Part of the circumference of a circle between two points

Area The amount of surface a shape covers

Ascending Going up, from smallest to largest

Associative law The result of adding or multiplying three or more numbers does not depend on how they are grouped

Axis A reference line drawn on a graph

В

Backtracking A method of solving equations systematically by applying opposite operations

Balance method The process of solving an equation by doing the same thing to both sides of the equation

Base (Measurement) One side of a shape, at right angles to the height

Base (Number) The number that is being raised to a power or index

Best buy The best value for money

Bisect To divide a line, angle, or shape into two equal parts

Boiling point The temperature at which a liquid boils and turns to vapour

Borrow Used in subtraction when taking one from a digit in a higher column in order to add 10 to the digit in the next lower column

Brackets A pair of symbols used to group things together

С

Capacity How much liquid or gas a container can hold

Carry Used in addition when transferring a digit from one column of digits to the next higher column

Cartesian plane A plane on which every point is related to a pair of numbers called coordinates (same as Number plane)

Categorical data Data that can be placed into categories or types of objects

Celsius Scale used for measuring temperature, where water freezes at 0° and boils at 100°

Census Collection of data from the whole population

Centre The middle

Centre point The middle point of a circle

Chance The likelihood of an event happening **Chord** A line interval joining two points on the

circumference of a circle

Clockwise In the same direction of hands moving on a clock

Coefficient A numeral placed before a pronumeral

Cointerior angles A pair of angles lying between two lines on the same side of a transversal

Collinear Lying on the same straight line

Column graph A graph where the height of each column represents a value

Commutative law When adding and multiplying, the order in which two numbers are combined does not matter

Compensating A mental strategy where you round a number and then add or subtract a smaller amount

Complementary Having a sum of 90°

Composite number A whole number greater than 1 that has at least three factors (i.e. it has a factor other than itself and 1.)

Concurrent Passing through the same point

Cone A solid with a circular base and a slanting curved surface that tapers to a point called the apex

Constant term The part of an expression without any pronumerals

Construction To draw a shape, line or angle accurately using a pair of compasses (compass) and ruler

Continuous numerical Data that can take any number value

Conversion The process of changing something (e.g. changing units)

Convert To change from one form to another **Convex** Curved outwards. A shape where there are no 'dents' in it. All vertices point outward

Coordinates Numbers or letters used to give a location or position, often an ordered pair written in the form (x, y)

Corresponding angles Pairs of angles in the same position, formed by two lines cut by a transversal

Critical digit The key digit to consider when rounding a number

Cube A solid (3D shape) with six square faces that are congruent (the same size and shape)

Cuboid A box-shaped solid object, also known as a rectangular prism

Cylinder A solid with two circular faces joined by a curved surface

D

Data Information (often numerical) gathered by observation, survey or measurement

Datum One score or piece of data

Decimal A number containing a decimal point

Decimal part The part of the number that occurs after the decimal point

Decimal places The number of digits after the decimal point

Decimal point Symbol that separates the whole part of a number from its fractional part

Decimal system A number system in which the basic units increase by powers of 10

Decreasing Becoming smaller or fewer

Denominator The bottom part of a fraction

Descending Going down, from largest to smallest

Diameter A line interval passing through the centre of a circle with its end points on the circumference, or the length of that interval

Digit A single symbol (such as a '3' or '7') that can be used alone, or in combinations (such as '37') to represent numbers

Discrete numerical Data that can only be collected in whole number values

Distance The length of the space between two points

Distributive law Adding numbers and then multiplying the total gives the same answer as multiplying each number first and then adding the products

Dividend The number being divided

Divisibility test A way to work out whether a whole number is divisible by another whole number, without actually doing the division **Divisible** When divided by a certain number gives a whole number answer

Division The process of separating a number into a specified number of parts

Divisor The number you are dividing by

Dot plot A graph in which each dot represents one score

Drag To shift or move a geometrical construction to a different position

Ε

Equally likely When two or more events have the same chance of occurring

Equation A mathematical statement that two expressions have the same value

Equilateral triangle A triangle with three equal sides and three equal (60°) angles

Equivalent Equal in value

Equivalent expressions Expressions that are always equal in value

Equivalent fractions Fractions that represent the same amount

Estimate An informed guess

Evaluate To find the numerical value of an expression

Even chance When two events have the same chance of occurring

Event Either a single outcome or a collection of outcomes

Expanded form A way of writing out in full a number written in index form

Expected number The number of occurrences you would expect to happen

Experiment A series of repeated probability trials that lead to outcomes

Experimental probability Probability based on recording the outcome of trials of an experiment

Expression A group of mathematical terms that does not contain an equals sign

Exterior angle The angle formed between the extended side of a shape and the adjacent side

F

Factor A whole number that will divide into another number exactly

Factor form The same as expanded form – a way of writing out in full a number written in index form

Factor tree A diagram showing the breakdown of a number into its prime factors

Formula An equation that shows the relationship between variables

Fraction Part of a whole

Fraction part The part of a mixed number that is not the whole number part

Freezing point The temperature at which a liquid turns into a solid when cooled

Frequency How many times something occurs

G

Geometrical shapes Figures or areas closed by a boundary which is created by points, lines and/or curves

Η

HCF Abbreviation of 'highest common factor' **Hectare (ha)** A unit of area equal to 10,000

square metres

Height The measurement of someone or something from head to foot or from base to top

Highest common factor (HCF) The largest number that is a factor of all the given numbers

Hindu-Arabic system A more formal way of naming our current decimal number system

Image The result of transforming a figure

Improper fraction A fraction where the numerator is greater than or equal to the denominator

Increasing Becoming bigger or larger

Index (plural: indices) The number of times a factor is repeated under multiplication

Index form A method of writing numbers that are multiplied by themselves

Input A number that is changed according to some rule

Inspection The process of solving an equation by inspecting or trying different values and seeing which one makes the equation true

Integers The set of positive and negative whole numbers and zero

Interior angle Any angle inside two adjacent sides of a shape

Isometric dot paper A grid of dots equally spaced apart

Isosceles triangle A triangle with at least two equal sides and two equal angles

Κ

Key An explanation for how numbers or symbols are used in a diagram or table

Kilogram Unit of metric measurement for mass **Kite** A quadrilateral with exactly two pairs of equal adjacent sides

L

LCD Abbreviation of 'lowest common denominator'

LCM Abbreviation of 'lowest common multiple'

Leaf The last digit of numbers represented on a stem-and-leaf plot

Left On or to the left side

Left-hand side (LHS) (Equations) The expression on the left side of the equals sign **LHS** See Left-hand side

Like terms Terms with the same pronumerals

Line A set of points forming a straight path that extends forever in opposite directions

Line graph A graph that shows the data as points joined with line segments

Line of symmetry The line (axis) along which a figure could be folded to produce identical halves

Lowest common denominator (LCD) The smallest common multiple of the denominators of two or more fractions

Lowest common multiple (LCM) The smallest number that two or more numbers divide into evenly

Μ

Mass A measure of how much matter is in an object

Mean An average value calculated by dividing the total of a set of numbers by the number of values

Measure To find a number that shows the amount or size of something

Median The middle score when all the numbers in a set are arranged in order

Mental strategy Carrying out mathematics operations in your head

Metre The standard metric unit for length, equal to 100 centimetres

Metric system A measurement system using the base-ten number system

Mirror line A line which can be drawn onto a shape to show that both sides are identical. Also known as a line of symmetry

Mixed number A number with a whole number part and a fraction part

ISBN 978-1-108-87846-3 © Greenwood et al. 2021 Cambridge University Press Photocopying is restricted under law and this material must not be transferred to another party. **Mode** The score that appears most often in a set of numbers

Model A mathematical representation of a system **Multiple** A multiple of a number is the product of that number and any other whole number

Multiplication The process of adding a number to itself a specified number of times

Ν

Negative integer A whole number that is less than zero

Negative number A number less than zero

Non-convex Curved inwards. A shape where one vertex (or more) points inward

Number line A line on which numbers are represented by points

Number plane A plane on which every point is related to a pair of numbers called coordinates (same as Cartesian plane)

Number sequence A list of numbers arranged in order according to a particular rule (also known as a Number pattern)

Numerator The top part of a fraction

Numerical data Data that can be counted or measured

Ο

Observation Survey and observation of data from those visible to us

Obtuse angle An angle between 90 and 180 degrees

Obtuse triangle A triangle with one obtuse angle (between 90° and 180°)

Of Another term for multiplication

Operation A mathematical process

Opposite (Angles) The angles on either side of a pair of intersecting lines

Opposite operation A mathematical process that undoes what was done by the previous operation

Order of rotational symmetry The number of times a figure matches its original position during rotation of 360°

Origin The point with coordinates (0, 0) on the number plane

Outcome One of the possible results of a chance experiment

Outlier A value that is much larger or much smaller than the rest of the data

Out of A way of referring to the whole group

Output The result from applying a rule to the input

Ρ

Pair of compasses A tool used to draw circles, also known as a compass

Parallel lines Lines in the same plane that are a fixed distance apart and never intersect

Parallelogram A quadrilateral with two pairs of opposite sides parallel

Partitioning A mental strategy where you break up a number into parts, e.g. 123 = 100 + 20 + 3

Pattern A list of numbers arranged in order according to a particular rule

Pattern rule An equation that describes the relationship present in a list of numbers

Per cent (%) Per hundred, out of a hundred

Percentage A way of writing a fraction with a denominator of 100

Perfect square A number with a square root that is a whole number

Perimeter The total distance (length) around the outside of a figure

Perpendicular At right angles

Place value The value of where a digit is within a particular number

Plane A flat surface that extends endlessly in all directions

Plot To draw on a graph

Point A position in space, marked with a dot and named with a capital letter

Positive integer A whole number that is greater than zero

Positive number A number greater than zero

Power (index) The number that a base is being raised to

Power of 10 Numbers which correspond to a base number of ten and an associated index number (e.g. $100 = 10^2$)

Primary source Information collected from the original source by the person needing the data

Prime factor A factor which is a prime number **Prime number** A whole number with only two factors, itself and 1

Prism A solid with two parallel congruent faces, joined by parallelograms (often rectangles)

Probability The likelihood that an event will occur, measured on a scale between 0 and 1

Product A number that is the result of multiplication

Pronumeral A letter or symbol used to represent a number

Proper fraction A fraction where the numerator is less than the denominator

Proportion One part considered in relation to the whole

Protractor A semicircular or circular tool for measuring or drawing angles

Pyramid A solid where the base has straight sides and the other faces are triangles meeting at a vertex (the apex)

Q

Quadrilateral A four-sided plane (2D) shape with straight sides

Quotient A number that is the result of division

R

Radius A line interval from the centre of a circle to its circumference (boundary), or the length of that interval

Raised (Indices) Placing the power or index number in a higher position to the right of the larger base number

Range The difference between the highest and lowest numbers in a set

Rate A comparison of two related quantities

Ratio A comparison of quantities usually written as a fraction or in the form a : b

Ray Part of a straight line, extending forever in one direction

Reciprocal A fraction in which the numerator and denominator have changed places

Rectangle A quadrilateral with both pairs of opposite sides equal and parallel, and with four right angles

Rectangular prism A box-shaped solid object, also known as a cuboid

Recurring decimal A decimal number with a digit (or group of digits) that repeats forever

Reflection Flipping a geometrical figure across a line

Reflex angle An angle between 180 and 270 degrees

Remainder Leftover amount after one number has been divided by another

Revolution A full turn or circle (360°)

Rhombus A quadrilateral with both pairs of opposite sides parallel and all sides equal

RHS See Right-hand side

Right angle An angle of 90 degrees

Right-hand side (RHS) (Equations) The expression on the right side of the equals sign

Right triangle A triangle in which one of the angles is a right angle (90°)

Rotation A turn around a centre point

Rotational symmetry When a figure rotated less than 360° matches its original position

Round down Approximating a number to a specified place value when the critical digit is less than five

Rounding Approximating a number to a specified number of places

Round up Approximating a number to a specified place value when the critical digit is five or more

Rule An equation that describes the relationship between two or more variables or amounts

S

Sample Collection of data from a smaller subset of the whole population

Sample space The list of all the possible outcomes of a trial

Scale (Measurement) A series of marks at regular intervals in a line

Scale (Ratio) The ratio of the length in a drawing (or a model) to the actual length in real-life

Scalene triangle A triangle with no equal sides or angles

Secondary source Information collected, published and summarised by someone else before we use it

Segment A section of a straight line (also called an interval)

Sequence A set of numbers ordered according to a rule

Shift Translating an object by moving it to the left, right, up or down

Sign The sign of a number refers to if the number is positive or negative

Simplify To make something as simple as possible

Simplifying Finding the simplest possible expression

Skew lines Lines that are not parallel

Solution The answer

Solving Finding the value of an unknown variable

Spatial pattern A sequence of geometrical shapes arranged in order according to a particular rule

Square A quadrilateral with all sides equal in length and four right angles

Square dot paper A grid of dots spaced apart as vertices of repeating squares

Square number The result of multiplying a number by itself

Square root (of a given number) The number that, when multiplied by itself, gives the number

ISBN 978-1-108-87846-3 © Greenwood et al. 2021 Cambridge University Press Photocopying is restricted under law and this material must not be transferred to another party. **Stem** The first digit or digits of numbers represented on a stem-and-leaf plot

Stem-and-leaf plot A table that lists numbers in order, grouped in rows

Straight angle An angle of 180 degrees

Substitute To replace pronumerals with numbers

Substitution Replacing pronumerals (letters) with values (numbers)

Subtraction The process of taking away the value of one number from another number

Sum A number that is the result of addition **Supplementary** Having a sum of 180°

T

Table of valuesA list of numbers shown forone or more variables to show the relationshipbetween the variables

Temperature scale A way to measure how hot or cold a substance or object is

Term One of the numbers in a sequence

Theoretical probability The expected probability of an event based on the number of favourable outcomes compared with the total possible outcomes

Tonne (t) A unit of mass equal to 1000 kilograms

Transformation Changing a figure's position, size or shape through a mathematical process

Translation Moving a shape a certain distance in a given direction

Transversal A line that cuts two or more lines

Trapezium A quadrilateral with exactly one pair of parallel sides

Travel graph A line graph that describes a traveller's position at different times

Trial One run of a chance experiment

Trial and error The process of solving a problem by trialling an answer, seeing the result and the error, then trialling another answer, and repeating this process until the correct answer is found

Triangle A plane (2D) shape with three straight sides and three angles

U

Unit A type of measurement (e.g. centimetres or litres)

Unknown A pronumeral with a value that is yet to be found to make the equation true

V

Variable Something that is measurable and observable, which is expected to change over time or between each observation

Vertex A point where two straight lines meet to make an angle

Vertically opposite Opposite each other across a common vertex

Vinculum The separating line in a fraction

Volume The amount of three-dimensional space in (or occupied by) an object

W

Whole numbers Numbers with no fractional or decimal part

Χ

*x***-axis** Horizontal axis of the number plane

Y

y-axis Vertical axis of the number plane

Answers

Chapter 1

W	arı	m-up quiz						
1	а	11	b	137	C	104	d	10 102
2	а	С	b	A	C	D	d	В
3	а	57	b	116	C	2044	d	11 002
4	а	13	b	37	C	99	d	8000
	e	26	f	28				
5	а	42, 49, 56, 63	3		b	54, 63, 72, 81	1	
	C	66, 77, 88, 99	9					
6	а	2	b	1	C	3	d	12
7	а	14	b	23	C	119	d	150
	e	210	f	1110	g	500	h	908
	i	9	j	32	k	79	L	79
	m	112	n	398	0	699	p	901
8	а	30	b	63	C	144	d	88
	e	56	f	130	g	1100	h	8000
	i	5	j	2	k	11	L	11
	m	10	n	9	0	3	p	9
9	а	37, 58, 59, 62	2,7	73, 159	b	31, 103, 130,	, 30	01,310
	C	13429,2431	19,	24 913, 24 93	81,	29 1 4 3		
10	а	0	b	1	C	1	d	2

1A _

Now you try

Example 1

a 60 **b** 600

Example 2

9, 37, 102, 117, 312, 324, 799, 8413, 9001

Exercise 1A

	_	0		-			•		7
1	а	0	b	5		C	2	d	7
2	а	46	b	263		C	7421	d	36 015
3	а	В	b	E		C	D	d	Α
	e	С	f	F					
4	а	7	b	70		C	70	d	700
	e	700	f	7000		g	700	h	70 000
5	а	3	b	30		C	30	d	300
	e	30	f	3000		g	3	h	30 000
6	а	20	b	2000		C	200	d	200 000
7	а	True	b	False		C	True	d	True
	e	False	f	True		g	False	h	True
	i	True	j	False		k	False	L	True
8	а	44, 45, 54, 5	5		b	29	, 92, 279, 729	, 92	27
	C	4, 23, 136, 9	51		d	34	5, 354, 435, 4	53,	, 534, 543
	e	12345,312	54,	34 512, 54	3	21			
	f	1001, 1010,	11(00, 10 001,	1(010	00		
9	а	872	b	13 469					
10	а	6	b	6		C	24		
11	а	i 7000				ii	46 000		
		iii 712000				iv	5 000 000		

v 44 000 000	vi 6 000 000 000
vii 437 000 000 000	viii 15 000 000 000 000
b 1 with 100 zeros	
1B	
Now you try	
Example 3	
•	c 75 d 106
Exercise 1B	
1 a Add, plus, sum	
b Minus, take away, subtract 2 a 7 b 10	c 69
d 4 e 12	f 20
3 a i 8 ii 27	iii 132
bi 6 ii 16	iii 8
4 a 18 b 19 d 140 e 21	c 32 f 9
5 a 34 b 46	c 59
d 64 e 97	f 579
g 748 h 948	i 5597
6 a 11 b 36 d 112 e 233	c 51 f 132
g 4 h 3111	i 10 001
7 a 24 b 75	c 95
d 133 e 167	f 297
8 a 24 b 26 d 222 e 317	c 108 f 5017
9 \$79	1 3017
10 38 hours	
11 107 runs	
12 a 12 b 27 d 133 e 14	c 107 f 90
d 133 e 14 g 1019 h 0	i 3
13 a 71 cards b 107 cards	
14 a True b True	c True
d False e True	f False
15 a 3 b 6 d <i>b</i> - <i>a</i> = <i>c</i>	c c-b=a
16 a 6 1 8	b 10 15 8
7 5 3	9 11 13
2 9 4	14 7 12
c 15 20 13	d 1 15 14 4
14 16 18	12 6 7 9
19 12 17	8 10 11 5
	13 3 2 16
10	
Now you try	
Example 4	
a 75 b 902	

Example 5

a 28 **b** 185

Exercise 1C

1	a	13		20	C		17		144
	e	1005	f	143	g		201	h	1105
2	а	7	b	5	C	;	8	d	67
	e	15	f	92	g	J	29	h	979
3	а	8	b	1	C	;	1	d	6
	e	2	f	1	g	1	8	h	3
4	a	87	b	99	Č		41	d	86
	e	81	f	51	g		92	h	81
5	a	222	b	322	5		521	d	920
J	e	226	f	745			2023	h	5080
c	-				g				
6	а	31	b	20	C		19	d	58
	e	58	f	29	g		26	h	39
7	а	149	b	273	C	;	656	d	888
	e	36	f	52	g	J	79	h	62
8	18	354 sheep							
9		6 kilometres							
10	а	77	b	192	C	;	418	d	4208
11		38			b	1	1 4		
		+ 5 3			+		7 7		
		9 1				1	91		
	C	6 2			d		265		
		-28			_	[1 8 4		
		3 4					8 1		
12	а	Answers may	y va	ary.					

12 a Answers may vary.

b Different combinations in the middle column can be used to create the sum.
13 a called a ca

c 80

62	67	60	b	101	115	114
61	63	65		112	106	107
66	59	64		108	110	111
				113	103	102

1D _____

Now you try

Example 6 a 205 b 133

Example 7

a 156 **b** 1144

Exercise 1D

1 2 3	a e a d a	False False 4 2 22	b f b e b	True True 2 4 27	g c f	True True 11 7 32	h	True False 56
3		28	ט f	60		32 44	u h	50 77
	i	108	j	72	3	21	I	54
	m	30	n	110	0	144	p	40
	q	49	r	63	S	132	t	72
	u	55	۷	22	W	24	X	96
	у	36						
4	а	105	b	124	C	93	d	132
	e	115	f	217	g	198	h	252
5	а	57	b	38	C	58	d	116
	e	90	f	126	g	117	h	196
6	а	70	b	90	C	110	d	180
	e	96	f	54	g	96	h	72

7 a 66 e 148 i 258 8 a 3		129 459 2849 0	g k	336 I 2630 I		
9 \$264 10 1680 r 11 116 ca						
12 a True e True i Fals	e f	True True			d Tri 1 Tri	
	9 7	b	25 ×5		C	79 ×3
2 <u>7</u> d 1]3 3 2	e	12 5 2 7		f	237 39
$\frac{\times}{10}$	8		\times 7 189			$\frac{\times 9}{35 1}$
	32 5	h	31 ×] 4 [7]	i	546 × 3
11]6 0		219	8		1638

14 Three ways: (0, 1), (1, 5), (2, 9). You cannot carry a number to the hundreds column.

1E _____

	•									
N	DW	you try								
E	ar	nple 8								
а	53	800	b	12	280	C	12	258		
E	ker	cise 1E								
1 2 3	a a C	10 True		b	100 False		C		d	10 True
4	e i	400 37 000 50 000		f j	290 1920 63 000		g k	1830 301 000 14 410	h I	4600 248 000 29 100 000
	e i	240 340 41 400		f j	540 1440 460 000		g k	520 6440 63 400	h I	
	e i			f	286 1368 2268		g	434 1232 1426	h	645 1254 4680
7 8 9		420 2176 1353		b	3036		C	1890	d	9416
	\$6	18 216 6020 6 400 secor	phr	f	40 768		g	18620	h	33 858
	а	39 984 2 3	lac		927 908		c b	4 752 188 1	d	146 420 482
		× 1 7 1 6 1						× 1 3 4 2 9		
		2 3 0						1 4 3 0		
	C	4	_				d	1 2 6 × 2 1		
		$\frac{\times 3}{3 4}$	_					× 2 1 1 2 6 2 5 2 0		
		181	_					2 5 2 0		

Answers

1F

_

Now you try				
Example 9 a 6	b 41	c 19	h	16
	W 11	0 10	ŭ	10
Example 10	- 1			1
a 22 and 1 ren	n. or 22 – 4	b 39 a	and 3 rem. o	r 39 <u>-</u> 2
Exercise 1F				
a 0	b 0	c (D	d 4
e 0 2 a 2	f 3 b 3	C 7	7	d 12
3 a 6	b 11	C 7		d 83
a 4	b 3	c 6		d 5
e 7	f 9	g 8		h 11
i 10	j 4	k i		I 12
m 8 5 a 13	n 12 b 21		11 21	p 12 d 21
e 21	f 11		32	h 16
a 29	b 19		24	d 9
e 39	f 14	g 2	29	h 9
a 22	b 31	C		d 7
3 a 26	b 1094	C (d 0
a 23 rem. 2	$=23{3}$	b	13 rem. 1 = 1	$\frac{13}{7}$
c 27 rem. 4	$= 27 \frac{4}{5}$	d 4	41 rem. 1 = 4	$41\frac{1}{6}$
e 43 rem. 2	$=43\frac{2}{5}$	f	126 rem. 2 =	$126\frac{1}{2}$
g 264 rem.	$2 = 264 \frac{2}{3}$	hS	90 rem. 4 = 9	$90\frac{4}{9}$
i 543 rem.	$1 = 543 \frac{1}{4}$	j 2	20 333 rem. :	$2 = 20333\frac{2}{3}$
k 818 rem.	$3 = 818\frac{3}{5}$	1 1	10 001 rem.	0 = 10 001
0 a 1	b 1	c 5	5	d 5
1 13 packs				
2 124 packs 3 67 posts				
4 15 taxis				
5 \$204				
6 a 33 rem. 8		rem. 8	c 31 re	
d 108 rem.	1 e 91	rem. 16	f 123 r	em. 26
	56			
40 28 2	3			
14 5 24	4			
12 8 7	10			
Progress quiz				
a 50	b 5000	0	50 000	
a 6	b 24			
a 478	b 223	c 6	66	d 42
i a True 5 a 95	b True b 5481	C	15	d 117
5 a 108	b 160	U	IJ	u II/
7 a 574	b 1602			
8 a 71000	b 7400	Cź	276	d 1357
9 \$315 10 a 21	b 99	c 8	8	d 15
	U 99 - 45 romaind		U	u IJ

11 a Quotient = 45, remainder = 2

b Quotient = 529, remainder = 5

1G							
Now you try							
Example 11							
a 90	b 59	900					
Example 12							
a 240	b 4	000	C	10)		
Exercise 1G							
1 a Up		Down		C	Up	d	Up
e Down 2 a Up		Down Up		C	Down	d	Down
e Down	f	Down		g	Up		Up
i Down	-	Up			Up		Down
3 a Down e Up		Down Down			Up Down		Up Up
i Up		Down			Up	Ï	
4 a 60		30			120		190
e 200 i 2000		900 1000			100 8000	n I	600 10 000
5 a 20	-	30			100	•	900
e 200		700		-	100		1000
i 6000 6 a 120		90 000 160			10 000 100	l h	10 12
e 10		3000			1200		3
i 40	j	2000			4000	Ι	100
7 \$1200 8 ≈ 2100 scoor	20						
$9 \approx 1200 \text{ scool}$ $9 \approx 1200 \text{ sheep}$							
$10 \approx 10$ people							
11 a Larger					Smaller		Larger 3 000 000
12 a 200 13 Compare you		100 000 wer with a	ı frie		800 's.	a	
12 a 200 13 Compare you 1H Now you try			ı frie			a	
12 a 200 13 Compare you 1H Now you try Example 13						a	e 12
12 a 200 13 Compare you 14 Now you try Example 13 a 3 b Example 14	r ans	wer with a			'S.	a	
12 a 200 13 Compare you 1H Now you try Example 13	r ans	wer with a			'S.	d	
12 a 200 13 Compare you 14	33	wer with a			d 16 b Brackets		e 12
12 a 200 13 Compare you 14	33	wer with a			d 16 b Brackets d Multiplic		e 12
12 a 200 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition	r ans	wer with a			d 16 b Brackets d Multiplic b Division	ation	e 12
12 a 200 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat e Division	r ans	wer with a			d 16 b Brackets d Multiplic	ation	e 12
12 a 200 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat e Division g Division	r ans	wer with a			 d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic 	ation ation	e 12
12 a 200 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat c Division g Division i Division	r ans	wer with a			 b Brackets d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract 	ation ation	e 12
12 a 200 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat e Division g Division	r ans	wer with a			 d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic 	ation ation	e 12
12 a 200 13 Compare you 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat e Division g Division i Division k Multiplicat 3 a 7 e 3	r ans	b 19 f 2			d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract I Division c 7 g 3	ation ation	e 12 d 20 h 24
12 a 200 13 Compare you 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat e Division g Division i Division k Multiplicat 3 a 7 e 3 i 1	r ans	b 19 f 2 j 23			d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract I Division c 7 g 3 k 21	ation ation	e 12 d 20 h 24 i 0
12 a 200 13 Compare you 13 Compare you 14 Now you try Example 13 a 3 b Example 14 2 Exercise 1H 1 a Multiplicat c Brackets 2 a Addition c Multiplicat e Division g Division i Division k Multiplicat 3 a 7 e 3	r ans	b 19 f 2			d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract I Division c 7 g 3	ation ation	e 12 d 20 h 24
12 a 200 13 Compare you 13 Compare you 14	r ans	b 19 f 2 j 23 n 32 r 38			 d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract l Division c 7 g 3 k 21 o 2 s 153 	ation ation	e 12 d 20 h 24 i 0 p 22 t 28
12 a 200 13 Compare you 13 Compare you 14	r ans	b 19 f 2 j 23 n 32 r 38 b 3			 b Brackets d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract l Division c 7 g 3 k 21 o 2 s 153 c 2 	ation ation	e 12 d 20 h 24 i 0 p 22 t 28 d 9
12 a 200 13 Compare you 13 Compare you 14	r ans	b 19 f 2 j 23 n 32 r 38 b 3 f 0			 d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract l Division c 7 g 3 k 21 o 2 s 153 c 2 g 22 	ation ation	e 12 d 20 h 24 i 0 p 22 t 28 d 9 h 2
12 a 200 13 Compare you 13 Compare you 14	r ans	b 19 f 2 j 23 n 32 r 38 b 3 f 0 j 18 n 20			 d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract l Division c 7 g 3 k 21 o 2 s 153 c 2 g 22 k 3 o 1 	ation ation ation	e 12 d 20 h 24 i 0 p 22 t 28 d 9 h 2 i 10 p 16
12 a 200 13 Compare you 13 Compare you 14	r ans	b 19 f 2 j 23 n 32 r 38 b 3 f 0 j 18			 b Brackets d 16 b Brackets d Multiplic b Division d Multiplic f Addition h Multiplic j Subtract l Division c 7 g 3 k 21 o 2 s 153 c 2 g 22 k 3 	ation ation ation	e 12 d 20 h 24 i 0 p 22 t 28 d 9 h 2 i 10

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Essential Mathematics for the Victorian Curriculum CORE Year 7

7 75 books 8 45 TV sets **b** $9 \div (12 - 9) = 3$ **9** a $(4+2) \times 3 = 18$ **c** $2 \times (3+4) - 5 = 9$ **d** $(3+2) \times (7-3) = 20$ **e** $(10-7) \div (21-18) = 1$ **f** $(4+10) \div (21 \div 3) = 2$ 10 a No b Yes c No d Yes f No e Yes **11 a** 48 **c** 13 **d** 28 **b** 18 e 22 **12 a** $[20 - (31 - 19)] \times 2 = 16$ **b** $50 \div (2 \times 5) - 4 = 1$ **c** $(25-19) \times (3+7) \div 12 + 1 = 6$

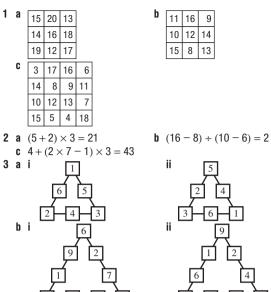
Maths@Work: Stock controller at sports events

- 1 See table at bottom of the page.
- **2** See second table at bottom of the page.

3	Event	AFL	Big Bash league	Japanese baseball	Major league baseball
	Average Attendance	37 968	20 552	34 655	28 199

- 4 Many correct answers including: the weather; the popularity of the team; a final or earlier in the season; and ticket price.
- 5 See third table at bottom of the page.

Puzzles and games





9

			Water bottles	Total wholesale cost	Earnings
Venue	Event	Attendance	required	@ \$0.80/bottle	@ \$3 a bottle
Suncorp Stadium, Brisbane	Brisbane Roar vs Perth Glory	35 200	52 800	\$42 240	\$158 400
MCG, Melbourne Cricket Ground	Hawthorn vs Freemantle	100 007	150 011	\$120 009	\$450 033
WACA, WA Cricket Association	T20 cricket India vs Australia	34 527	51 791	\$41 433	\$155 373
SCG, Sydney Cricket Ground	Sydney Swans vs Western Bulldogs	33 386	50 079	\$40 063	\$150 237
Adelaide Oval	Adelaide Crows vs West Coast Eagles	53 445	80 168	\$64 134	\$240 504
NIB Stadium, Perth	Wallabies vs Argentina	16 202	24 303	\$19 442	\$72 909
Darwin Football Stadium	Brumbies v Reds	4600	6900	\$5520	\$20 700
ANZ Stadium, Sydney	Broncos v Cowboys	82 758	124 137	\$99 310	\$372 411

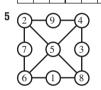
Event	Brisbane Roar vs Perth Glory			Sydney Swans vs Western Bulldogs	Adelaide Crows vs West Coast Eagles	Wallabies vs Argentina	Brumbies v Reds	Broncos v Cowboys
Attendance	35 000	100 000	35 000	33 000	53 000	16 000	5000	83 000

Stadium	Seating capacity	Fruit salad	Hot chips	Pies	Mini pizzas	Fresh wraps
WACA, Perth	24 500	4900	12 250	36 750	9800	9188
Adelaide Oval	53 500	10 700	26 750	80 250	21 400	20 063
The Gabba, Brisbane	42 000	8400	21 000	63 000	16 800	15 750
ANZ Stadium, Sydney	83 500	16 700	41 750	125 250	33 400	31 313
Rod Laver Arena, Melbourne	14 820	2964	7410	22 230	5928	5558
Blundstone Arena, Hobart	20 000	4000	10 000	30 000	8000	7500
Darwin Football Stadium	6000	1200	3000	9000	2400	2250

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						_	_	
5	4	6	1	3	2	9	8	7
2	8	3	7	5	9	6	1	4
7	9	1	6	8	4	3	2	5
8	2	4	5	1	3	7	6	9
1	3	7	9	2	6	4	5	8
9	6	5	4	7	8	1	3	2
3	7	9	2	6	5	8	4	1
6	1	2	8	4	7	5	9	3
4	5	8	3	9	1	2	7	6
1	7	5	4	6	9	3	8	2
2	9	4	1	3	8	6	5	7
8	6	3	7	5	2	9	1	4
3	4	1	2	7	6	8	9	5
9	2	8	5	4	3	7	6	1
7	5	6	8	9	1	2	4	3
4	3	9	6	2	5	1	7	8
6	1	7	3	8	4	5	2	9
5	8	2	9	1	7	4	3	6

4



6	Answers may v	/ary; e.g.		
	a 217		b	295
	× 7			× 3
	1519			885
7	a 2	b 5		

Short-answer questions

1 2 3 4 5	b a a a	137, 173, 3 199, 999, 7 50 459 128 95 33 14 678		00, 1	1 0 b b b b			C C C	50 000		d d	217 739 41 10 800
6		156 45			b f	840 101 rem	۱.		1413 46 ren	ı. 5	d	351
7	h a c	$7540 \text{ rem.} \\ 2 \boxed{2} 3 \\ +7 3 \boxed{8} \\ \hline 9 6 1 \\ \hline 4 1 \\ \times 7 \\ \hline 2 8 \boxed{7} \\ \hline \end{array}$	2			b		7 2 (3) = -4 7 (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	3 5			
8 9	a a	70 800				3300 400			1000 5000		d	10
10	a e i	24 14 13			b f	4 3		-	1 20		d h	92 0
М	Multiple-choice questions											
1 6	B A		2 7	C D			-	E C	4 9	A B		5 B 10 A

Extended-response questions

- 1 a 90 loads
 - **c** \$27 500

b 360 kilometres **d** \$4000

- 2 a 313 sweets
 - **b** 78
 - ${\boldsymbol{c}}~$ Jelly beans, 5

Chapter 2

Warm-up quiz

1				E	C	A	d	D
	e	В	T	F				
2	а	90°	b	180°	C	360°	d	270°
	e	45°	f	315°				
3	а	60°	b	140°	C	125°	d	80°
4	а	No	b	Yes	C	No		
5	a	80°	b	150°	C	150°		

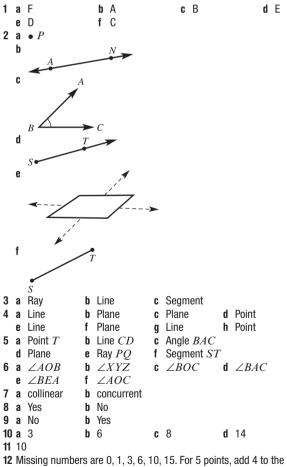
2	A	
 -	••	

Now you try

Example 1

a Line XY b Ray ST

Exercise 2A



previous total; for 6 points, add 5 to the previous total, and so on.13 All segments should intersect at the same point; i.e. are concurrent.

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Essential Mathematics for the Victorian Curriculum CORE Year 7

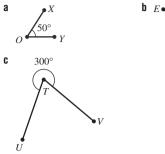
2B

Now you try



a 35° **b** 110°

Example 3

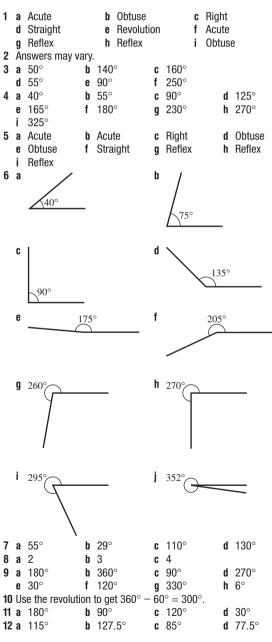


c 320°

145°

Ğ

Exercise 2B



Now you try Example 4 a ∠BOC b ∠YOS $C \ \angle PON$ Example 5 **a** 30 **b** 39 c 122 **d** 205 Exercise 2C 1 a, b angles should add to 90° c complementary 2 a, b angles should add to 180° **c** supplementary 3 a, b angles should add to 360° c vertically opposite angles 4 a $\angle ABD$ b ∠CBF C ∠CBT 5 a $\angle UOV$ c ∠BOA b ∠MON **6** a $\angle MFS$ or $\angle SFM$ **b** $\angle TFS$ or $\angle SFT$ **c** $\angle BFS$ or $\angle SFB$ **d** $\angle SFX$ or $\angle XFS$ **7** a 60 **c** 69 **d** 135 **b** 15 **g** 115 **e** 70 **f** 141 **h** 37 i 50 240 **k** 270 I 140 i 8 a N b N c S dΝ e C f C g C h S **9** a ∠BOC **b** $\angle AOD$ and $\angle BOC$ C ∠COD **10 a** 30 **b** 75 **c** 60 **d** 135 **e** 45 f 130 11 a No, should add to 90°. **b** Yes, they add to 180°. c Yes, they add to 360°. d Yes, they are equal. e No, they should be equal. f No, should add to 360°. **12** 24° 13 a 30 **b** 60 **c** 60 **d** 45 f 36 **e** 180 2D _ Now you try Example 6 a ∠HFB d ∠EFB b ∠EFB C ∠EFB Example 7 a 76 (alternate angles in parallel lines) **b** 123 (corresponding angles in parallel lines) c 65 (cointerior angles in parallel lines) Example 8 a Not parallel (corresponding angles are not equal) **b** Parallel (cointerior angles sum to 180°) **Exercise 2D 1** a 4 **b** No **2** a 2 b Yes 3 a equal **b** supplementary c equal d equal C ∠DEB d ∠CBG **4** a ∠*DEH* b ∠BEF **5** a ∠*FEG* b ∠DEB C ∠GEB d $\angle ABC$ 6 a 130, corresponding **b** 70, corresponding c 110, alternate d 120, alternate e 130, vertically opposite f 67, vertically opposite g 65, cointerior h 118, cointerior i 100, corresponding i 117, vertically opposite k 116, cointerior I 116, alternate m 110, cointerior n 48, cointerior

2C

Answers

o 117, corresponding

7	а	a = 70, b = 70, b	<i>c</i> =	= 110 b	<i>a</i> = 1	20, b = 120, c =	60			
	C	<i>a</i> = 98, <i>b</i> = 82,	<i>c</i> =	= 82, <i>d</i> = 82						
	d	a = 90, b =	<i>c</i> =	= 90 e	a = 9	5, b = 85, c = 95	5			
	f	a = 61, b = 119								
8	а	No, correspondir	na	angles should	d be ec	iual.				
		Yes, alternate an	~	0						
			les, cointerior angles are supplementary.							
		,	/es, corresponding angles are equal.							
			No, alternate angles should be equal.							
		No, cointerior angles should be supplementary.								
~		,	•			,		~~		
9	а	35		41	C	110	d	30		
	e	60	f	141						
10	а	65	b	100	C	62	d	67		
	e	42	f	57	g	100	h	130		
	i	59			-					
11	a	a = 120, b = 12	0	b	60					
		Opposite angles		e equal						
12		60	h	115	C	123	d	80		
	e	60	f	335	U	120	u	00		
	G	00		000						

Progress quiz

1	а	$\angle AOC$ or $\angle COA$	b $\angle YOZ$ or $\angle ZOY$	
2	а	Line = Z b Line segr	ment = Y c Ray =	X
3	а	Acute	b Reflex	
	C	Straight	d Acute	
	e	Obtuse	f Reflex	
	g	Right	h Obtuse	
4	Ā			
5	а	N b S	c S	d C
6	а	128 b 26	c 135	d 38
7	а	$\angle ABF$ or $\angle ABG$	b $\angle CFH$ or $\angle BFH$	
	C	$\angle EFB$ or $\angle EFC$	d $\angle ABG$ or $\angle ABF$	
8	а	115, alternate	b 88, corresponding	
9	а	<i>a</i> = 40, <i>b</i> = 140, <i>c</i> = 140)	
	b	a = 82, b = 82, c = 82, d	<i>l</i> = 82	

2E _____

Now you try

Example 9

The angle formed should be exactly 90°

Exercise 2E

1 Check each one using a ruler.

2 a Chordb Radiusc Centred Minor arce Diameter

3 a-e



- 4 $\angle AEC$ should be 90°.
- **5** $\angle BAD$ should be 60°.
- **6** $\angle AOE$ and $\angle BOE$ should be equal.
- 7 Your two circles should just touch.
- **8** $\angle BAC$ and $\angle ABC$ should be equal.
- 9 a Construct a 60° angle (see question 4) and then bisect this angle by constructing the angle bisector to form two 30° angles (see question 5).
 - **b** Construct an angle bisector of one of the 30° angles from part **a**.
- **10 a** First, construct a 90° angle by constructing a perpendicular line and then construct the angle bisector of the 90° angle.
 - **b** Construct the angle bisector of one of the 45° angles from part **a**.
- 11 a Circles should overlap and be the same size.
- **b** AE = BE
- **c** AB is at 90° to CD and CD cuts AB in half.

2F _

Now you try

Example 10

The angle should measure 60° exactly.

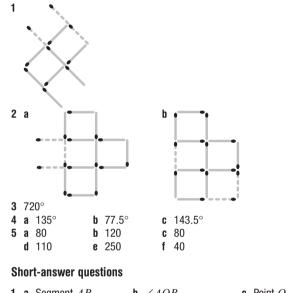
Exercise 2F

1–8 Answers may vary and can be checked by testing the properties of the constructions.

Maths@Work: Glass cutter and design artist for stained-glass windows

- 1 Answers will vary.
- 2 Answers will vary.
- 3 Answers will vary.

Puzzles and games



1	а	Segment AB	b	$\angle AOB$	C	Point O
	d	Plane	e	Ray AB	f	Line AB
2	а	Acute, 35°	b	Reflex, 210°		
	C	Obtuse, 115°	d	Reflex, 305°		
3	Cł	neck by measuring with	a	protractor. A right angle	is is	90°.

- **4 a** 20 **b** 230 **c** 35 **d** 41
- e
 15
 f
 38

 5
 a° and b° b
 a° and d°

 c
 a° and c° d
 b° and c°
- e c° and d° or b° and d°
- **6 a** 61 **b** 128 **c** 59
- 7 a Yes, corresponding angles are equal.b No, alternate angles should be equal.
 - c No, cointerior angles should be supplementary.
- **8 a** 100 **b** 95 **c** 30
- ${\bf 9} \ \ {\bf a} \ \ {\rm The \ angle \ should \ be \ divided \ in \ half.}$
 - **b** The angle should be 90°.

Multiple-choice questions

1 C	2 B	3 D	4 E	5 D
6 E	7 C	8 A	9 E	10 B

Extended-response questions

1	а	i 30°	ii 180°	iii 27 0°	
	b	i 30°	ii 210°	iii 15°	
	C	i 180°	ii 90°	iii 60°	
		iv 75°	v 105°	vi 127.5°	
2	а	12 pieces	b 30		
	C	i 15	ii 22.5	iii 20	iv 24

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Chapter 3

Warm-up quiz

	un	in up quiz					
1	а	100	b 1000	C	1 000 000		
2	а	4	b 10	C	20	d	1
	e	1, 2, 4, 5, 10,	. 20				
3		4 remainder					
-		3 remainder					
		2 remainder					
		3 remainder					
4		10	b 4	•	19	ч	24
4			f 5	U	19	u	24
-		18					
		2, 3, 4, 6, 8, 1					
		3 < 7					
		6, 8, 10					
8	а	6	b 8	-	6	d	9
	e	4	f 1	g	8	h	$4 \times 4 = 16$
9	а	$8 = 4 \times 2$		b	$15 = 3 \times 5$		
	C	$12 \times 4 = 48$		d	$4 \times 4 = 16 =$	= 8	× 2
	e	$12 \times 3 = 36$	$= 4 \times 9$				
10	а	7	b 3	C	7		
11	а	11	b Yes	C	10 remainde	r 2	
	d	No					
12	a	23	b 36	C	13	h	6
		B	b A	-	D		C
		$A = 16 \text{ cm}^2$	N C	U	0	u	0
14		A = 10 cm Side = 6 cm					
	n						

3A

Now you try

Example 1 a 1, 2, 3, 6, 9, 18

b 1, 2, 5, 10, 25, 50

Example 2

a 9, 18, 27, 36, 45, 54 **b** 21, 42, 63, 84, 105, 126

Example 3

34 is incorrect, 8, 16, 24, 32, 40, 48

Example 4 $72 = 8 \times 9$

Exercise 3A

1 a $12 \times 2 = 24$ or $2 \times 12 = 24$ **b** $24 \times 1 = 24$ or $1 \times 24 = 24$ $3\times8=24 \quad \text{or} \quad 8\times3=24$ $4 \times 6 = 24$ or $6 \times 4 = 24$ **2** a $1 \times 12 = 12, 2 \times 6 = 12, 3 \times 4 = 12,$ 1, 2, 3, 4, 6, 12 **b** $1 \times 5 = 5;$ 1, 5 **c** $1 \times 30 = 30, 2 \times 15 = 30, 3 \times 10 = 30, 5 \times 6 = 30$ 1, 2, 3, 5, 6, 10, 15, 30 3 a 10, 20, 30 **b** 20, 40, 50, 60 **c** 14, 21, 35 4 a factors **b** 2, 3, 4 c 12, 24, 30 d multiples **5 a** 1, 2, 5, 10 **b** 1, 2, 3, 4, 6, 8, 12, 24 c 1,17 **d** 1, 2, 3, 4, 6, 9, 12, 18, 36 **e** 1, 2, 3, 4, 5, 6, 10, 12, 15, 20, 30, 60 f 1, 2, 3, 6, 7, 14, 21, 42 **g** 1, 2, 4, 5, 8, 10, 16, 20, 40, 80

i 1, 2, 4, 7, 14, 28 **6 a** 5, 10, 15, 20, 25, 30 **b** 8, 16, 24, 32, 40, 48 c 12, 24, 36, 48, 60, 72 d 7, 14, 21, 28, 35, 42 e 20, 40, 60, 80, 100, 120 f 75, 150, 225, 300, 375, 450 **q** 15, 30, 45, 60, 75, 90 h 100, 200, 300, 400, 500, 600 i 37, 74, 111, 148, 185, 222 **7 a** 3,18 **b** 5 **c** 1, 4, 6, 9, 12, 24 **d** 3, 4, 5, 8, 12, 15, 24, 40, 120 **8** a 22; 3, 6, 9, 12, 15, 18, 21, 24, 27, 30 **b** 24; 5, 10, 15, 20, 25, 30 c 21; 11, 22, 33, 44, 55, 66, 77, 88, 99, 110 **d** 49; 12, 24, 36, 48, 60, 72, 84 **c** 7×6 **9** a 5×6 **b** 6×6 d 5×8 **e** 8×8 f $10 \times 10 \text{ or } 5 \times 20$ ii 5, 10, 15, 20, 25, 30 **10 a i** 4, 8, 12, 16, 20, 24 b Zane 5 laps. Matt 4 laps c 20 minutes **11 a** 13 **b** 2 **c** 11 **d** 1 **12 a** 12 pens (1 m \times 1 m), 6 pens (2 m \times 1 m), 4 pens (3 m \times 1 m) or 3 pens $(1 \text{ m} \times 4 \text{ m})$ **b** i 32 pens $(1 \text{ m} \times 1 \text{ m})$, 8 pens $(2 \text{ m} \times 2 \text{ m})$ or 2 pens $(4 \text{ m} \times 4 \text{ m})$ ii 54 pens $(1 \text{ m} \times 1 \text{ m})$ or 6 pens $(3 \text{ m} \times 3 \text{ m})$ c i 16 pens $(1 \text{ m} \times 2 \text{ m})$, 8 pens $(1 \text{ m} \times 4 \text{ m})$ or 4 pens $(2 \text{ m} \times 4 \text{ m})$ ii 27 pens $(1 \text{ m} \times 2 \text{ m})$, 18 pens $(1 \text{ m} \times 3 \text{ m})$ or 9 pens $(2 \text{ m} \times 3 \text{ m})$ **d** 25 pens (2 m \times 3 m), 15 pens (2 m \times 5 m), 10 pens $(3 \text{ m} \times 5 \text{ m}), 6$ pens $(5 \text{ m} \times 5 \text{ m}), 5$ pens $(5 \text{ m} \times 6 \text{ m or } 3 \text{ m} \times 10 \text{ m or } 2 \text{ m} \times 15 \text{ m}), 3 \text{ pens} (2 \text{ m} \times 25 \text{ m})$ or 5 m \times 10 m), or 2 pens (3 m \times 25 m or 5 m \times 15 m) 3B _ Now you try Example 5 8 Example 6 24 **Exercise 3B** 1 a highest common factor **b** factors c lowest common multiple **d** multiples **2** a 1, 2, 4 **b** 4 **3** a 24,48 **b** 24 **4 a** 1 **b** 1 **c** 2 **d** 3 e 4 **f** 15 **g** 10 **h** 3 **i** 1 5 a 20 **b** 21 **c** 30 **d** 40

h 1, 2, 3, 4, 6, 12

Answers

CH3

f 10

6 a 7 black ants. 11 red ants

7 a 3 teaspoons, 2 spoons

9 a 6 roses per bunch

11 b After 12 minutes

8 a 100 cm, 200 cm, 300 cm

c 6 red, 7 pink, 5 cream bunches

b 24, 32

c Lilli 8 laps, Aliyah 6 laps, Ciara 4 laps

d 15 mins more for Aliyah, 45 mins more for Ciara

e 12

i 42

10 a 8,16

h 60

c LCM

g 30

b 77 mm

b 42 cm

b 6 = HCF

 $\textbf{b} \ \text{LCM} = 100$

3C

Now you try
Example 7
a 126, 216, 13914 b 126, 216, 13914
c 126, 216, 13914 d 216
Example 8
a 570 b 570 c 2112 d None
Evenue 0
Example 9
a Yes b No
Exercise 3C
1 a divisible, remainder b 2 c 0, 2, 4, 6 or 8
d divisible, $4 + 3 + 2 = 9$, 9 e 6
2 a B b A c C
3 a 5,10 b 5 c 16,16,4 d 328,328,8
4 a 2+5+8+3=18 b divisible, 18, 3
c divisible, 18, 9 d odd
5 a 6, 14, 8, 54, 22, 34, 50, 18, 46
b 12, 18, 30, 27, 54, 36, 42, 24
c 12, 24, 60, 54, 252, 36, 66, 84
d 168, 7168, 40, 5032, 248, 6400, 9568
6 a 35, 125, 15, 100, 515, 730, 105
b 20, 800, 290, 610, 590, 90, 160
c 16, 32, 220, 12, 28, 432, 72, 316, 424, 1836
d 27, 432, 99, 387, 63, 720, 2799
7 a Yes b No c Yes d Yes e No
f Yes g No h Yes i No j Yes
k No I Yes nn Yes n No o No p Yes q No r No
8 See table at bottom of the page.
9 a Not even
b Digits do not sum to a multiple of 3
c 26 is not divisible by 4
d Last digit is not 0 or 5
e Not divisible by 3 (sum of digits is not divisible by 3)
f 125 is not divisible by 8 and it is not even
g Sum of digits is not divisible by 9
h Last digit is not 0
10 a 2 b 2 c 0 d 0
11 2, 4, 8, 11, 22, 44
12 36
13 a Yes
b Multiples of 3; adding a multiple of 3 does not change the result of
the divisibility test for 3.

c 18

3D ____

Now you try

Example 10 Prime: 7, 43, 73 Composite: 25, 39, 58

Example 11

2,3

Exercise 3D

1	a prime, 1,	itself	b composi	te
2	a No	b Yes		
3	a 2, 3, 5, 7,	11, 13, 17, 19, 23	3, 29	
	b 4, 6, 8, 9,	10, 12, 14, 15, 10	6,18	
4	a 11	b 12		
5	a C	b P	c C	dΡ
	eC	f C	g P	hΡ
	i C	j C	к С	ΙP
	mΡ	n P	o C	pР
6	a 2, 3, 7	b 3,13	c 2, 3, 5	d 5
	e 2,7	f 2,3		
7	a 32, 33, 34	1, 35, 36, 38, 39		
	b 51, 52, 54	, 55, 56, 57, 58		
	c 81, 82, 84	, 85, 86, 87, 88		
8	a 23, 29	b 41,4	3,47 c	71,73,79
9	a 3,5	b 3,7	c 5,7	
	d 5,11	e 11,13	f 7,19	
10	14			
11	5 and 7, 11	and 13, 17 and 1	9, as well as ot	her pairs
12	a No, 3, prii	ne		
	b Yes, 6×2	$2 ext{ or } 4 imes 3, 12, ext{ co}$	mposite	
	c Yes, 5×2	2, 10, composite		
	d No, 5, pri	ne		
	e No, 7, pri	ne		
	f Yes, 7×2	2, 14, composite		
	g No, 11, pr	ime		
	h Yes, 3×3	3, 9, composite		
31	E			

Now you try

Example 12 **a** 7⁵ $\textbf{b} \ 2^4 \times 5^3$

Example 13

a 81 **b** 392

Example 14

a 17	b 5	6

Exercise 3E

1	а	expanded	b	index
	C	power	d	base

e index, power

2 a $3^2 = 3 \times 3$ **c** $5^3 = 5 \times 5 \times 5$

3	Expanded form	Index form	Base	Index
	$7 \times 7 \times 7$	7 ³	7	3
	$5 \times 5 \times 5$	5 ³	5	3
	$2\times 2\times 2\times 2\times 2\times 2$	2 ⁶	2	6
	$6 \times 6 \times 6 \times 6$	6 ⁴	6	4

	Divisible							
Number	by 2	by 3	by 4	by 5	by 6	by 8	by 9	by 10
243 567	×	1	×	×	×	×	1	X
28 080	1	1	1	1	1	1	1	1
189 000	1	1	1	1	1	1	1	1
1 308 150	1	1	X	1	1	X	1	1
1 062 347	×	×	×	×	×	×	×	×

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4	Value	Base	Index (power)	Value
	2 ³	2	3	8
	5 ²	5	2	25
	10 ⁴	10	4	10 000
	2 ⁷	2	7	128
	1 ¹²	1	12	1
	12 ¹	12	1	12
	05	0	5	0
(j r 6 a 7 a	$\begin{array}{c} \mathbf{n} \ 5^3 \times 8^2 \\ \mathbf{p} \ 4^3 \times 7^1 \times 7^1 \\ \mathbf{a} \ 32 \\ \mathbf{p} \ 10\ 000 \\ \mathbf{a} \ 6, 3, 3, 9 \end{array}$	n 3 13 ¹ q 9 b 64 f 1000	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0^{3} 00^{2} $^{2} \times 12^{2}$ $^{4} \times 13^{2}$ $^{3} \times 3^{2} \times 5^{2}$ 172 121
8 8 1 0 0 1 1 1	 10, 5, 5, 25 2 × 2 × 2 × 17 × 17 9 × 9 × 9 3 × 3 × 3 × 3 × 3 × 3 × 4 × 4 × 4 × 7 × 7 × 5 × 4 × 4 × 4 × 	< 2 < 3 × 3 × 3 > < 3 × 3 × 2 > < 3 × 3 × 3 > < 5 × 5	< 2 × 2 < 3	
	1 4×4×4> 1 25	b 1		1 64
	i 128	f 8		1 900
i	-			
	a 4 e 3	b 2 f 2		16 14
11 2		b >		14 1<
	i >	f >		1 <
12 1				
	i 1110 pe	ople	ii 1111110 p	people
	• 40 min			
(: 50 min			
3F				

Now you try

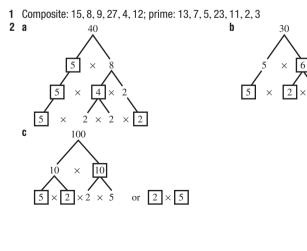
Example 15

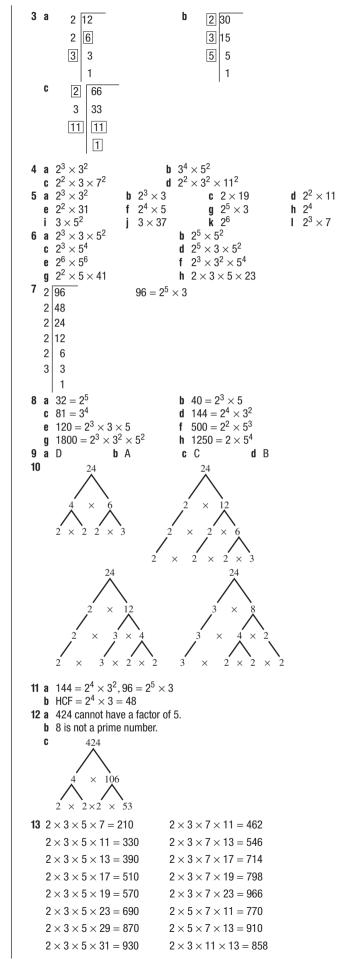
 $2^2\times 3\times 5^2$

Example 16

 $3^2\times5\times11$

Exercise 3F





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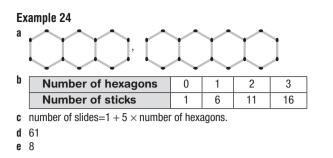
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3G				
Now you try				
Example 17				
•	121 c 81	d 64	e 10	f 2 m
Example 18				
a 6	b 70			
Example 19	h 0	. 10		
a 7	b 3	c 13		
Exercise 3G				
	b square root	c 36	d squ	ared
 See key ideas See key ideas 				
4 a 36	b 25	c 121		
d 100 5 a 5	e 49 b 4	f 144 c 10	d	7 cm
6 a 64	b 49	c 1	d	
e 9	f 225	g 25	h	-
i 121 7 a 5	j 10000 b 3	k 900 c 1	l d	
e 0	f 9	g 7		4
i2 mr50	j 12 n 80	k 20 o 90	l p	
8 a 7	b 5	c 12	•	30
e 64	f 65	g 36	h	
i 0 9 a A square is	j 81 s not possible.	k 4 b Draw₄	I 4 × 4 squa	13 re.
10 64, 81, 100				
11 121, 144, 169 12 a 9 + 16 = 2				
b No: 25 + 3				
	$64 = 100 = 10^2$			
	vers are possible $2^2 = 13^2, 9^2 + 1$			
13 a i ••••		ii 2 more dot	S	
7 iii Alwavs	9 one dot by itself			
b i ••••		ii 2 more dot	S	
8	10			
ni Samen ci	umber of dots in	ii 3, 5, 7, 9, 1	1 dots	
	••••			
••••	••••			
16 iii Dots for	25 rm a square, alter	rnate odd and even	numbers	
di 🖕	••	ii 2, 3, 4, 5, 6	6 dots	
•••	•••			
10	15			
	t at the top, triang	gle-shaped m of two triangular	numhers	
(4 = 1 + 3, 9)		or two trianyular		
Progress quiz				
• •	10.00		10 10 00	
1 a 1, 2, 4, 5, 1 2 a 12, 24, 36		b 1, 2, 3, 4, 6, 9 b 21, 42, 63, 84)
3 a 8	b 35	c 6	,	
4 a 24 5 a 14, 52, 88	b 77 1234	c 30 h 7	75,141	
c 52,88	d 75	u /	5, 171	
6 a Not possib		b Possible		
7 Prime – 23, 3 8 a 2, 3	1 composite – 1: b 2, 3	J, J9, J1, 80, 91		
9 a 4 ⁵	b $5^4 \times 6^3$			
10 a $3 \times 3 \times 3$ b $2 \times 2 \times 2$				
	$\times 2 \times 2 = 28$			

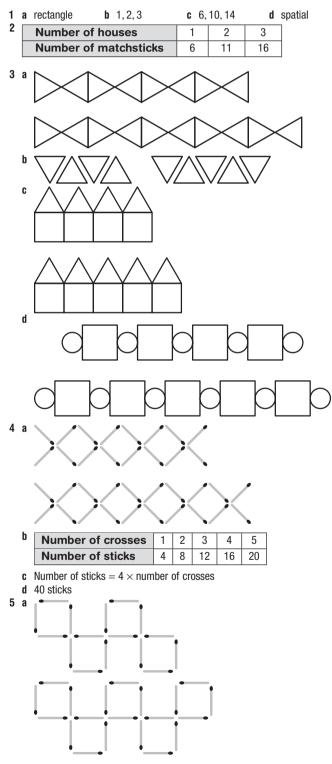
		169									•	
3H												-
		you try										
		nple 20										
		, 23, 27			b 8	32, 7	1,60					
		nple 21	00400									
		80, 5120,	20480		D S), 3, ⁻	1					
		nple 22										
		art with 3 art with 1 ⁻					4.					
		art with 62					/ 5.					
d	St	art with 12	23 and su	btract 9	fron	n ead	ch term					
Ex	er	cise 3H										
1	a	sequence	ł		t) tei	m	C	0	c	ł	
2		20, 24, 28			b	85,	80,75					
,		8, 4, 2	17 00				,80,16		0			
J		8, 11, 14, 52, 48, 44					, 31, 30 3, 130,		o 44, 151			
4		3, 6, 12, 2					20, 80,					
5		240, 120,		5			5,125,		1			
5		23, 28, 33 14, 11, 8)				, 54, 64 4, 116,					
	e	27, 18, 9				5,4		-				
c		505,606					45,39					
0		32, 64, 12 12, 6, 3	28				, 160, 3 , 15, 5	20				
		176, 352	704					000 000	,7000	000		
-	-	16, 8, 4					38, 19					
7		50, 32, 20 32, 64, 25					, 45, 55 15, 21					
		55, 44, 33			f		3, 111					
8		Start with						m.				
		Start with Start with					-					
	d	Start with	1 and m	ultiply e	ach 1	term	by 3.					
		Start with Start with										
9		17, 23, 30		16,2				10, 13	.11			
	d	45, 40, 50)									
		3, 1, 4, 2, × 3	5, 3, 6 b -2	5) 7 (; +1						
		Start with		-				n 4,				
	e	÷2										
		Start with List prime				reas	e or de		e by 10 -3			
12	•	49, 64, 8							5			
		21, 44, 65					2 - 2	.2.				
		216, 343, 19, 23, 29				i.e. 6	³⁹ , 7 ⁹ , 8	3°)				
		16, 18, 20										
4-		161,171				- F \						
13	1,	2, 3, 4, 5,	b,7,8,9,	i U (tota	al = 5	5)						
31												
No	w	you try										
		nple 23										
a) 	•	• • • •		- 1-	•	.—	· •	• •	• •	•	,
				,								
b		Numbe	er of		1	Τ	2	3	4	5		
		Numbe	or of stid	rks	2		4	6	8	10	-	

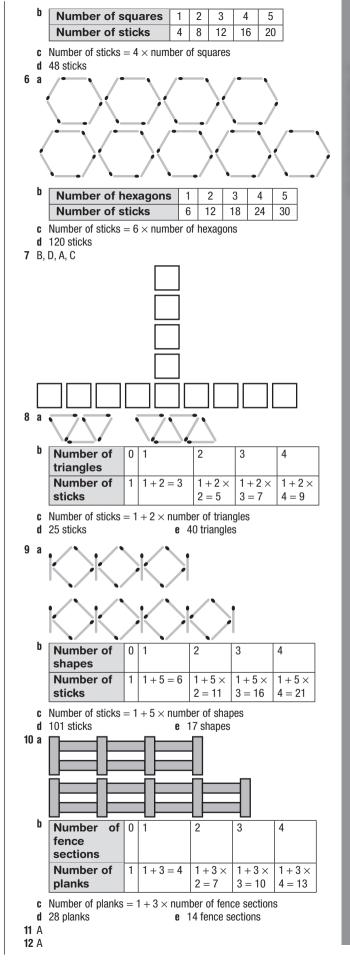
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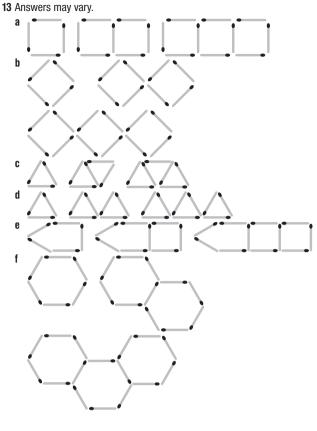
Exercise 3I





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3J _

Now you try

Example 25

1	input	0	1	5	10	12
	output	5	6	10	15	17
2	input	9	3	21	90	33
	output	4	2	8	31	12

Example 26

a output = input - 2

b $output = input \times 6$

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Exercise 3J

1 a flowers b Number of flowers (input) 2 1 3 4 5 Number of sticks (output) 4 8 12 16 20 2 a Ebony's age b José's age (input) 1 3 7 12 15 Ebony's age (output) 4 6 10 15 18 3 a input b Hours worked (input) 5 2 3 4 1 Amount earned (output) \$8 \$16 \$24 \$32 \$40 **4 a** 16 **b** 6 **d** 4 **c** 10 **5 a** *input* 4 5 6 7 10

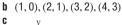
	mput	4	5	0	1	10
	output	7	8	9	10	13
b	input	5	1	3	21	0
	output	10	2	6	42	0
C	input	11	18	9	44	100
	output	3	10	1	36	92

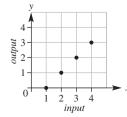
	d	input	5	-	15	55	Т	0	100		
		output	1		3	11	+	0	20		
6	a	input	1		2	3	Τ	4	5	I	
		output	7		17	27	+	37	47		
	b	input	6		8	10	T	12	14		
		output	7		8	9	+	10	11		
	C	input	5	-	12	2	T	9	0		
		output	16		37	7	+	28	1		
	d	input	3		10	11	T	7	50		
		output	2		16	18		. 10	96		
7	a	output = inp	<i>ut</i> + 1				b	out	put =	4 × inpl	ıt
	C	output = inp $tput = 3 \times in$		1			d	out	put =	input ÷	6
		A $a = 3 \times m$	b D				C	В		d C	;
10	a	Zac's ag			0			1	2	3	
		years (<i>in</i> Amount				-				-	
		account (<i>output</i>)	φ γ		\$1(00	\$1	50	\$200	\$250	
	b c	output = 50 \$1000	× inpl	ut-	+ 10	0					
11			arkov	d			Т	F	10		
	а	Hours wo (<i>input</i>)	JIKE		0	2		5	10		
	а		otal		0 64	2 80)	5 104	10		
	b	(input) Cindy's t saving (o output = 8 ×	otal <i>utput</i>)	64)				
	b c	(input) Cindy's t saving (d output = 8 × 17 hours	otal utput) !+	64 64)				
12	b c	(input) Cindy's t saving (a output = 8 × 17 hours output = 2 × output = 3 ×	otal utput input input) !+ !+	64 64 1 2	80		104			
12	b c a b	(input) Cindy's t saving (a output = 8 × 17 hours output = 2 × output = 3 × There are oth	otal utput input input input ner co) !+ !+	64 64 1 2 ct a	80		104	144	4 × inpu	<i>ıt</i> +1
12 13	b c a b a c	(input) Cindy's t saving (a output = 8 × 17 hours output = 2 × output = 3 × There are oth output = 2 × output = 5 ×	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2
12 13	b c a b a c e	(input) Cindy's t saving (a output = 8 × 17 hours output = 2 × output = 3 × There are otl output = 2 ×	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b	104 S. out	144 put = put =		6+2
12 13 3K	b c a b a c e	(input) Cindy's t saving (a output = 8 × 17 hours output = 2 × output = 3 × There are oth output = 2 × output = 5 ×	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2
12 13 3K No	b c a b a c e	(input) Cindy's t saving (d output = 8 × 17 hours output = 2 × output = 3 × There are oth output = 2 × output = 5 × output = 10	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2
12 13 3K No	b c a b a c e c w an	(input) Cindy's t saving (a output = 8 × 17 hours output = 2 × output = 3 × There are oth output = 2 × output = 5 × output = 10	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2
12 13 3K No Ex	b c a b a c e c w an	(input) Cindy's t saving (d output = 8 × 17 hours output = 2 × output = 3 × There are oth output = 2 × output = 5 × output = 10 you try ple 27	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2
12 13 3K No 5 4	b c a b a c e c w an	(input) Cindy's t saving (d output = 8 × 17 hours output = 2 × output = 3 × There are ottl output = 2 × output = 5 × output = 10 you try nple 27	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2
12 13 3K No Ex 5	b c a b a c e c w an	(input) Cindy's t saving (d output = 8 × 17 hours output = 2 × output = 3 × There are oth output = 2 × output = 5 × output = 10 you try ple 27	otal utput input input input ner co input input) t+ t- t- t-	64 64 1 2 ct ai 3 1	80	ers b d	104 S. out	144 put = put =	input ÷	6+2

 0^{\dagger} 2 3 4

Example 28

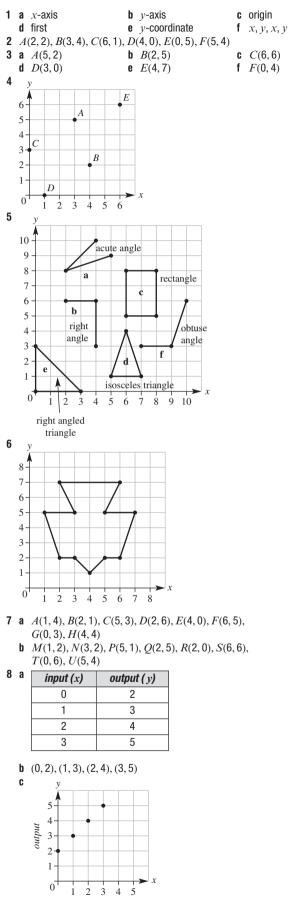
	•	
а	input (x)	output (y)
	1	0
	2	1
	3	2
	4	3

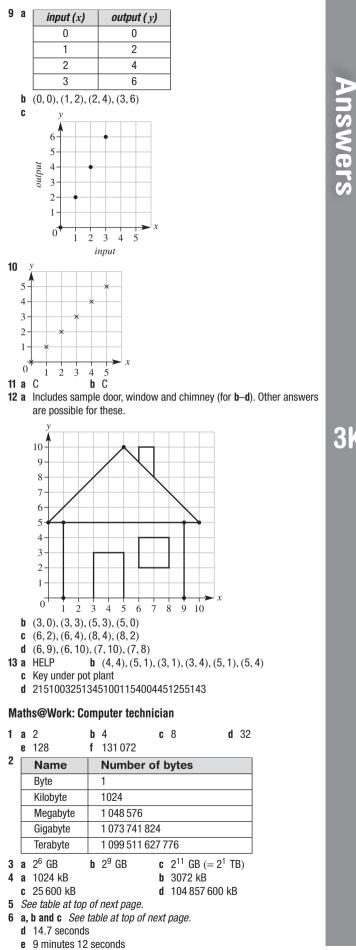




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Exercise 3K





input

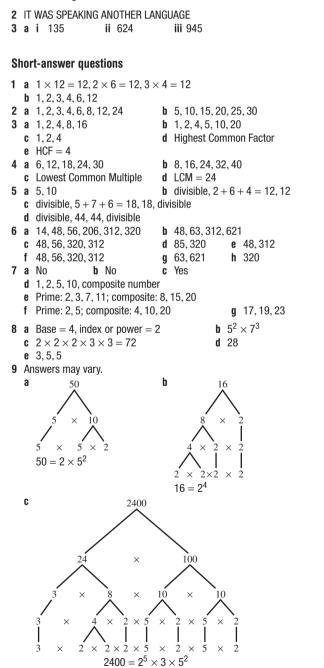
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b	7	155 648	22 235	6
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Media type	File size in MB MegaBytes	File size in Mb Megabits		Dow	nload tim	ies	
Арр	16	128	16.0	6.4	4.3	2.6	1.3
Music	24	192	24.0	9.6	6.4	3.8	1.9
Short Video	45	360	45.0	18.0	12.0	7.2	3.6
Gaming	120	960	120.0	48.0	32.0	19.2	9.6
Movie	600	4800	600.0	240.0	160.0	96.0	48.0

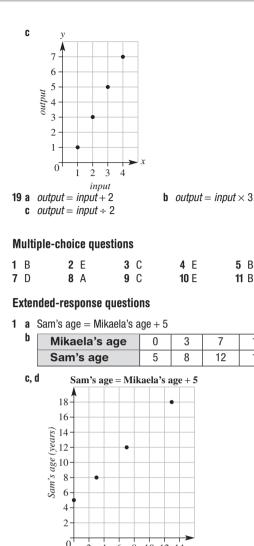
Puzzles and games



10	Index form	42	6	2	72	C	2	
_					,			
	Value	16	3	6	49	8	1	
	Square root form	√16	1	25	√10	ō	√1	44
	Value	4		5	10		1	2
11 a i 12 a c 13 a b	24, 48, 96, 192 16, 25, 36, 49	7 200 5 cm		1 32	cm , 32, 16, , 28, 24,	20	12	1
c d	No. of tria No. of stic Number of stick 36 sticks	ks	1 3 < numbe	2 6 er of	9 1	1 2 3	5 15	
14 a	No. of squa	res) 1		2	3		4
	No. of stick	s 1	1+3	= 4	$\frac{1+3}{2} \times \frac{1}{7}$		-	$1+3 \times$ 4=13
b C	Number of stick 31 sticks	(s = 1 +			r of squa squares		1	
15 a	input	3	5	7	7	12	2	20
	output	8	10	1	2	17	2	25
b	input	4	2		9	12		0
	output	15	11		25	31		7
16 a 17 a d	A(1,3), B(3,4) y-axis e		I) I) (0,	<i>tput = ii</i> , 0) axis	C	- 6 y-a C(
18 a	input (x)	outp	out (y)					
	1		1	_				
	2		3 5	_				
			0					
h	4 (1, 1), (2, 3), (3	5) (4	7					

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Essential Mathematics for the Victorian Curriculum CORE Year 7



6 B

12 D

13

18

0 2 4 6 8 10 12 14 Mikaela's age (years)

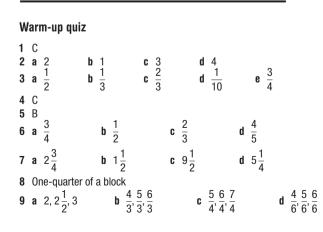
	0 (~ /			
Number of					
tables	1	2	3	4	5
Number of					
students	5	8	11	14	17
	Number of tables Number of	Number of tables1Number of	tables12Number of	Number of tables123Number of	Number of tables1234Number of </th

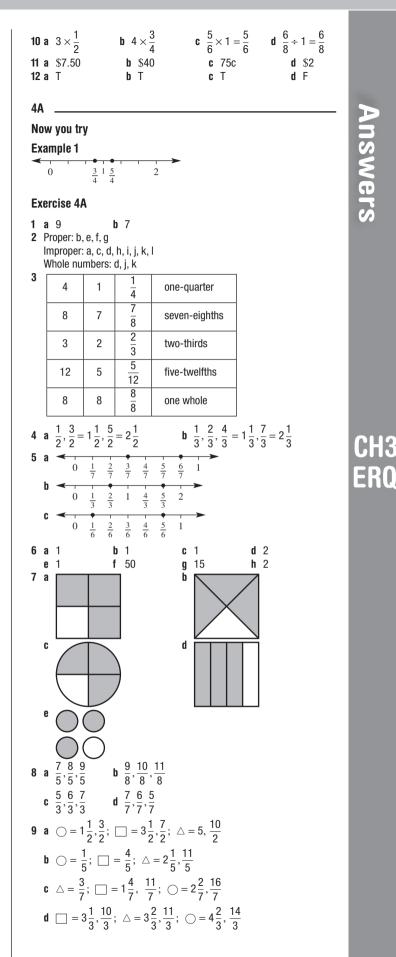
b Number of students = $3 \times$ number of tables + 2

c 23 students

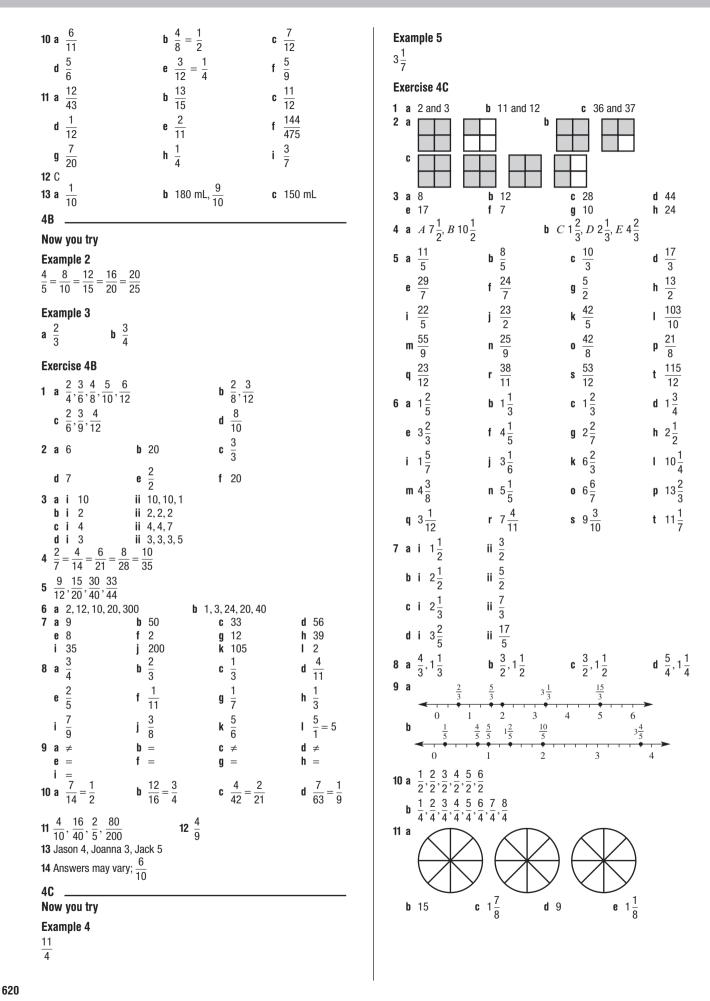
d 26 tables

Chapter 4





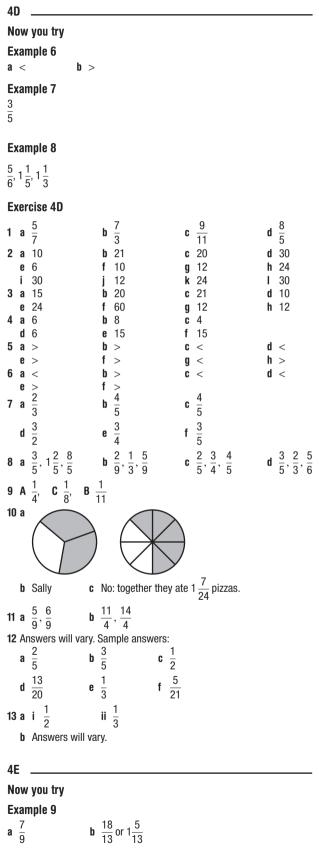
Essential Mathematics for the Victorian Curriculum CORE Year 7

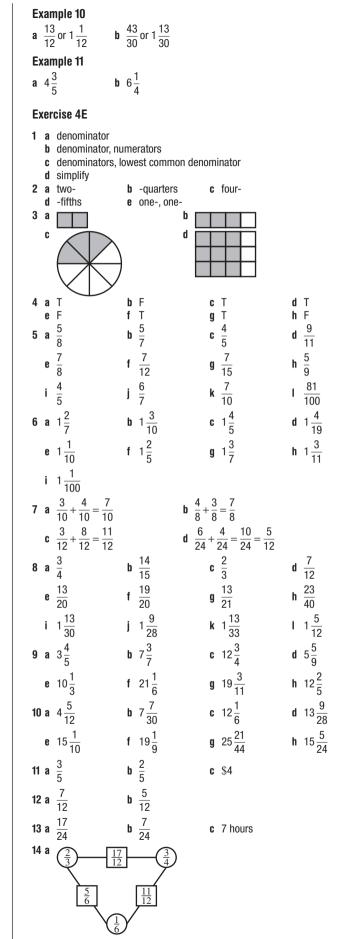


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$12 \frac{1}{2}, \frac{2}{1}, \frac{1}{3}, \frac{3}{1}, \frac{2}{3}, \frac{3}{2}, \frac{1}{23}, \frac{1}{32}, \frac{2}{32}, \frac{2}{13}, \frac{3}{12}, \frac{3}{12$





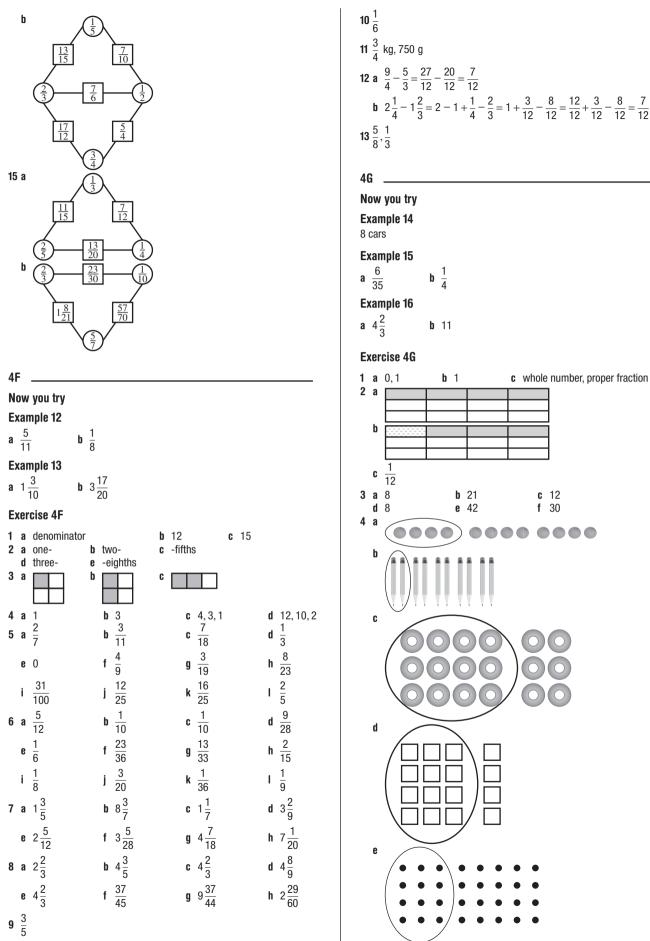
Answers

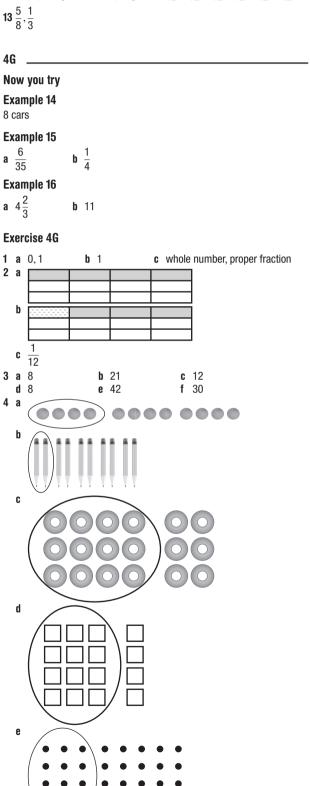
4D

621

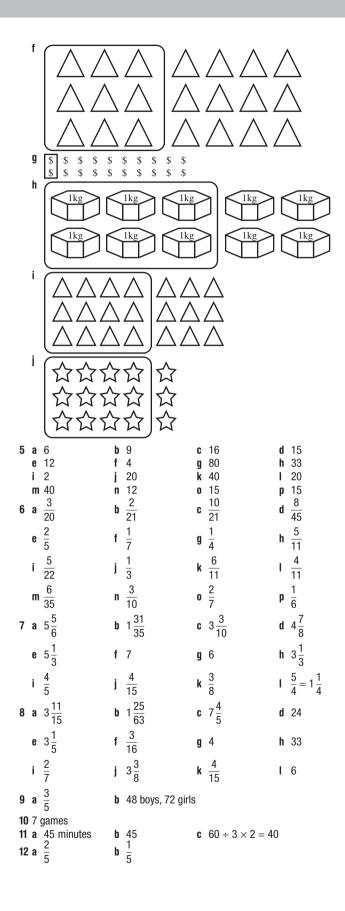
ISBN 978-1-108-87846-3

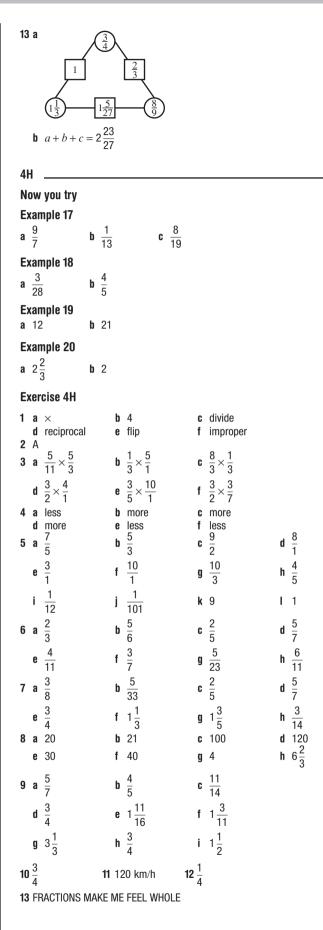
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Answers

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Progress quiz	!			
1 a P	b I	c W	d W	e P
10	b $\frac{4}{7}$	c $\frac{1}{4}$	d $\frac{3}{2}$	e $\frac{2}{3}$
3 D 4 a $\frac{23}{7}$	b $\frac{103}{9}$			
5 a $3\frac{3}{10}$	b $8\frac{1}{3}$			
6 a $\frac{5}{8}$	b $\frac{1}{3}$	C	$\frac{3}{5}$	d $\frac{13}{16}$
7 $\frac{8}{15}, \frac{3}{5}, \frac{2}{3}, \frac{5}{6}$	3		5	10
8 a $\frac{9}{13}$	b 16/21	C	$5\frac{13}{20}$	
9 a $\frac{4}{11}$	b $\frac{5}{24}$	C	$6\frac{1}{3}$	
10 a $\frac{9}{28}$	b 6	C	$4\frac{2}{3}$	
11 a $\frac{9}{2}$	b $\frac{1}{5}$	C	$\frac{4}{15}$	
12 a $\frac{2}{11}$	b 32		10 21	d $2\frac{1}{4}$
41				
Now you try				
Example 21	0		0	
a $\frac{29}{100}$	b $\frac{3}{5}$	c 1	$\frac{9}{10}$	
Example 22 a 37%	b 108%			
Example 23				
a $41\frac{2}{3}\%$	b 275%			
Exercise 41				
1 a 70,70 e 40,40	f 63,6	63	60, 60	d 20,20
2 a $\frac{1}{4} = 25\%$	$\frac{2}{4} = 50\%$	$\frac{3}{4} = 75\%$	$\frac{4}{4} = 100\%$	
b $\frac{1}{5} = 20\%$	$\frac{2}{5} = 40\%$	$\frac{3}{5} = 60\%$	$\frac{4}{5} = 80\%, \frac{5}{5}$	5 = 100%
c $\frac{1}{3} = 33\frac{1}{3}$	$\%, \frac{2}{2} = 66$	$\frac{2}{2}\%, \frac{3}{2} =$	100%	
3 a 86%	b 20%			
4 She scored	full marks: $\frac{2}{2}$	25 25		
5 a $\frac{11}{100}$	b $\frac{7}{1}$	71 00	c $\frac{43}{100}$	d $\frac{49}{100}$
$e \frac{1}{4}$	$f = \frac{3}{1}$	3	g $\frac{3}{20}$	h $\frac{22}{25}$
i $\frac{7}{100}$	j 1 1	0	$\frac{20}{k} \frac{21}{100}$	$I \frac{1}{2}$
$\frac{100}{m}$	$n \frac{9}{1}$		o $\frac{99}{100}$	p 11/20
6 a $1\frac{1}{5}$	b 1	1	c $2\frac{37}{100}$	d $4\frac{1}{100}$
e 1 $\frac{3}{4}$	f 1	1 10	g $3\frac{4}{25}$	h $8\frac{2}{5}$
i 2	j 2	$\frac{1}{20}$	k 3 $\frac{1}{10}$	$1 \ 3\frac{1}{2}$

7 8	e i m a	98% 8% 35% 112% $12\frac{1}{2}\%$ 115%	b 9% f 15% j 32% n 135% b $33\frac{1}{3}\%$ f 420%		g k o c	$79\% \\ 97\% \\ 86\% \\ 400\% \\ 26\frac{2}{3}\% \\ 290\%$	h I p d	$56\% \\ 50\% \\ 90\% \\ 160\% \\ 83\frac{1}{3}\% \\ 32\frac{1}{2}\%$
9	a	$\frac{3}{4}$	b 75%		C	$\frac{1}{4}$		25%
		$\frac{4}{2^{\frac{1}{2}}}$				4		
11		-						
)%,80% : 1	13					
13		40	ii $\frac{13}{400}$		1			
	b	i $\frac{33}{400}$	ii $\frac{1}{8}$		iii $\frac{1}{3}$			
4J	I							
No	w	you try						
Ex a		n ple 24 3 b 91						
ЕX 1		cise 4J	5	C	20 ÷	2 = 10		
2	а		35		16			
Ŭ	b	$\$900 \div 100 = \$$ $\$4 \text{ kg} \div 4 = 21$	S9					
	d	7 days \div 2 = 3	days, 12 hou	rs				
	f	84 kg \div 4 \times 3 = 35 minutes \div 5						
	a	hours 70	b 36		C	10		27
	e i	10 4	f 7 j 48		g k	150 44	h I	200 190
6		22 96	n 84 b 600		0 C	36 66	•	63 100
7		15 10% of \$200 =	f 72 \$20	b		73 \$500 = \$25		600
-	C	20% of \$120 = 10% of \$80 = \$	\$24	d	30% (of $310 = 93$ of $160 = 16$		
	g	50% of \$60 = \$	530	h	1% of	\$6000 = \$60		
8	а	20% of \$200 = \$42	\$40	b	24 mil	of \$88 = \$44 limetres		
		9 kilograms 8 minutes			90 ton 400 ce	nes entimetres		
	g i	1.5 grams 144 seconds		h	3 hect	ares		
9 10		5 marks 10 students						
11	12	2 students	420		660			
	a	They are the sar		U	000			
		$37\frac{1}{2}\%$						
	C	i \$140	ii \$1.50					
4	(
		you try nnle 25						

Example 25

$$\frac{3}{4} = 75\%$$

Essential Mathematics for the Victorian Curriculum CORE Year 7

Example 26

 $a \frac{1}{4}$ **b** 75%

Exercise 4K

Exercise 4K					
1 a 25%	b	20%	C	48%	d 99%
2 a 4	b	4	C	$\frac{1}{2}$	
d 50%	e	$\frac{1}{2}$	f	50%	
3 a 10	b	$\frac{1}{5}$	C	$\frac{4}{5}$	
d 2 <u>0</u> %	e	80%		4	
d 20% 4 a $\frac{7}{350}$	b	80% 1 50	C	$\frac{1}{50} \times 100\%$	= 2%
5 a $\frac{3}{10}$, 30%		0		0	
d $\frac{3}{4},75\%$	e	$\frac{1}{20}, 5\%$	f	$\frac{1}{2},50\%$	
g $\frac{1}{4}$, 25%	h	$\frac{3}{20}, 15\%$			
6 a $\frac{3}{5}$, 60%			b	$\frac{1}{2},50\%$	
c $\frac{1}{4}$, 25%			d	$\frac{2}{5}$, 40%	
e $\frac{3}{4}$,75%			f	$\frac{4}{5}$, 80%	
7 a 1/10	b	10%			
8 a $\frac{1}{5}$	b	20%	C	$\frac{4}{5}$	d 80%
9 a $\frac{80}{1600} = \frac{1}{20}$		b 5%		c 95%	
10 a 16 megalitr	es	b $\frac{16}{20} =$	4 5	c 80%	
11 a 1500 m ²		3		1	1
b i $\frac{1}{20}$, 5%		ii $\frac{5}{5}$, 60	%	iii $\frac{1}{8}$,	$12\frac{1}{2}\%$
c $\frac{29}{40}$					
d 27.5%				0	
12 a $\frac{1}{25}$, 4%			b	$\frac{2}{5}$, 40%	
c $\frac{1}{20}, 5\%$			d	$\frac{1}{20}, 5\%$	
e $\frac{1}{4}$, 25%			f	$\frac{3}{4},75\%$	
13 $\frac{45}{50} = 90\%$ $\frac{1}{10}$	72	= 72% Ros		-	
14 a 4	00				
b music	sp	ort	C	$\frac{1}{5}$	d 40%
$ \cap$	Ś			5	
	4)	6)			
\square	\leq				
4L					
Now you try					
Example 27 a 4:3 b	4:	1			
	, т.				

Example 28 a 15 km/h

a 7 blinks/min

Example 29

Sprout (\$4 per kg)

Exercise 41

E	kercise 4L			
1	D			
	A			
3	a 5 b	1 (: 1	d 4
			No No	d Yes
			3600	d 86 400
6	a 1:3 b	1:2	: 1:9	d 1:3
	e 3:1 f	4:1	j 10:1	h 5:1
	i 2:5 j	2:3	k 4:5	I 5:7
	m 9:7 n	12:5) 11:7	p 5:4
7	a 4:24, replace	with 4 : 16 or 6 :	24	
	b 10:600, replace	e with 10:60 o	r 100:600	
	c 8:24, replace			
	d 15:20, replace	e with 15 : 25 or	12:20	
8	a 12 km/h		ps/second	c \$7/kg
	d 7 m/s		als/game	
	f 2 km/min or 12			
9	a \$24	b 72 s		
	c 20 waves		airs of shoes	
10	a 5 kg of flour fo			
	b 5 kg of potatoe			
	c 500 g of ham f			
	d 20 L of cooking		(05/1)
11	10 kg for \$38.00	(\$3.80/kg), 2 kg	g tor \$7.90 (\$3)	.95/Kg),
40	5 kg for \$19.95 (.18/kg)
	a 22.5 kg) 2.5 kg	
13		51.2 minutes		
	c 145 600 words	i		
- 64	atha@Warks Duil	dina constaus	tion onnuontio	
M	aths@Work: Bui	ding construc	tion apprentic	e
M 1	aths@Work: Bui a 12.7 mm	b 6.4 ı		c 3.2 mm
1	a 12.7 mm d 0.8 mm	-	nm mm	
1	a 12.7 mm d 0.8 mm	b 6.4 i e 19.1	nm mm	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$	b 6.4 e 19.1 ii 6	nm	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$	b 6.4 e 19.1 ii 6	nm mm	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$	b 6.4 r e 19.1 ii 6 v 8 ³ / ₈	nm mm	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$	b 6.4 r e 19.1 ii 6 v 8 ³ / ₈	nm mm iii $6\frac{3}{4}$	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$	b 6.4 r e 19.1 ii 6 v 8 ³ / ₈	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$	
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$	b 6.4 n e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$	b 6.4 n e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}$, $10\frac{1}{2}$, $10\frac{1}{2}$,	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}^{"}$, $11^{"}$, $11\frac{1}{2}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}^{"}$, $11^{"}$, $11\frac{1}{2}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}$, $10\frac{1}{2}$, $\frac{1}{3}$ b 1', $11\frac{7}{8}$, $11\frac{3}{4}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ $10\frac{3}{4}^{"}, 11^{"}, 11\frac{1}{2}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}$, $10\frac{1}{2}$, $10\frac{1}{2}$,	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ $10\frac{3}{4}^{"}, 11^{"}, 11\frac{1}{2}$	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{4}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 ["] , 11 $\frac{1}{2}$ ", 11 $\frac{5}{8}$ ", 11 $\frac{1}{2}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}$, $10\frac{1}{2}$, $\frac{1}{3}$ b 1', $11\frac{7}{8}$, $11\frac{3}{4}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 ["] , 11 $\frac{1}{2}$ ", 11 $\frac{5}{8}$ ", 11 $\frac{1}{2}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1 3 4	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{4}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 ["] , 11 $\frac{1}{2}$ ", 11 $\frac{5}{8}$ ", 11 $\frac{1}{2}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1 3 4 5	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 10\frac{1}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 ["] , 11 $\frac{1}{2}$ ", 11 $\frac{5}{8}$ ", 11 $\frac{1}{2}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1 3 4	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 ["] , 11 $\frac{1}{2}$ ", 11 $\frac{5}{8}$ ", 11 $\frac{1}{2}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1 3 4 5 6 7	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 10\frac{1}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$	b 6.4 e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 ["] , 11 $\frac{1}{2}$ ", 11 $\frac{5}{8}$ ", 11 $\frac{1}{2}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{4}$, $11\frac{1}{2}$, $11\frac{3}{4}$	c 3.2 mm
1 3 4 5 6	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$	b 6.4 g 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ $10\frac{3}{4}^{"}, 11^{"}, 11\frac{1}{2}^{"}$ ", $11\frac{5}{8}^{"}, 11\frac{1}{2}^{"}$ " for 2' $7\frac{11}{16}$ "	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{11}, 11\frac{1}{2}, 11\frac{3}{4}$ $7, 11\frac{3}{8}, 11\frac{1}{4}$	c 3.2 mm
1 3 4 5 6 7	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 10\frac{1}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$ 203.2 mm $\frac{1}{5}$ 965.2 mm	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ ii $1\frac{5}{8}$, $11\frac{7}{2}$, $\frac{7}{11}$, $\frac{5}{8}$, $11\frac{1}{2}$, $\frac{7}{16}$ ii or 2' $7\frac{11}{16}$	mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ iii $\frac{7}{11}\frac{1}{2}$, $11\frac{3}{4}$ iii $\frac{1}{8}$, $11\frac{1}{4}$	c 3.2 mm
1 3 4 5 6 7	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$ 203.2 mm $\frac{1}{5}$ 965.2 mm Total A + E 99.9	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ ii $1\frac{5}{8}$, $11\frac{1}{2}$, $\frac{7}{11}$, $\frac{5}{8}$, $11\frac{1}{2}$, $\frac{7}{16}$, $\frac{7}{16}$ iii inches iii inches	nm mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{11}\frac{1}{2}, 11\frac{3}{4}$ $7, 11\frac{3}{8}, 11\frac{1}{4}$	c 3.2 mm ″, 1΄ 2.9
1 3 4 5 6 7	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$ 203.2 mm $\frac{1}{5}$ 965.2 mm Total A + E 99, 27	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 [°] , 11	mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ iii $1\frac{1}{2}$, $11\frac{3}{4}$ iii $1\frac{3}{8}$, $11\frac{1}{4}$	c 3.2 mm ", 1' B in mm 2.9 9.0
1 3 4 5 6 7	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1', 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$ 203.2 mm $\frac{1}{5}$ 965.2 mm Total A + E 99, 27, 5819	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 [°] , 11	mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{11}\frac{1}{2}, 11\frac{3}{4}$ $7, 11\frac{3}{8}, 11\frac{1}{4}$ Total A + 243 683 148	c 3.2 mm ", 1' B in mm 2.9 9.0 18.3
1 3 4 5 6 7	a 12.7 mm d 0.8 mm a i $4\frac{1}{4}$ iv $6\frac{7}{8}$ b i $1\frac{1}{4}$ iv $2\frac{9}{16}$ a $10\frac{1}{4}, 10\frac{1}{2}, 10\frac{1}{2}$ b $1, 11\frac{7}{8}, 11\frac{3}{4}$ c $\frac{5}{8}, 4\frac{5}{8}, 11\frac{5}{8}$ d $7\frac{11}{16}, 31\frac{11}{16}$ 203.2 mm $\frac{1}{5}$ 965.2 mm Total A + E 99, 27	b 6.4 r e 19.1 ii 6 v $8\frac{3}{8}$ ii $1\frac{5}{8}$ v $3\frac{3}{8}$ 10 $\frac{3}{4}$, 11 [°] , 11	mm iii $6\frac{3}{4}$ iii $2\frac{5}{16}$ vi $3\frac{3}{4}$ $\frac{7}{11}\frac{1}{2}, 11\frac{3}{4}$ $7, 11\frac{3}{8}, 11\frac{1}{4}$ Total A + 243 683 148	c 3.2 mm ", 1' B in mm 2.9 9.0

Puzzles and games

1 DELHI AGRA AND JAIPUR

4 a	$\frac{2}{5}$	$A = \frac{9}{10}$	4 5
	$B = \frac{11}{10}$	$C = \frac{7}{10}$	$D=\frac{3}{10}$
	$E = \frac{3}{5}$	$\frac{1}{2}$	1
b	$A = \frac{3}{4}$	$B=2\frac{5}{8}$	2 ¹ / ₄
	$C = 3\frac{3}{8}$	$1\frac{7}{8}$	$D = \frac{3}{8}$
	$E=1\frac{1}{2}$	$1\frac{1}{8}$	3

Short-answer questions

1 a $\frac{1}{6}$	b $\frac{1}{2}$	c $\frac{1}{4}$	d $\frac{1}{14}$
e $\frac{1}{10}$	$f \frac{1}{8}$	g $\frac{1}{5}$	h $\frac{1}{3}$
2 $\frac{2}{3}$			
3 a $\frac{3}{5}$	b $\frac{2}{7}$	c $\frac{5}{7}$	
4 a 1 $\frac{3}{4}$	b $1\frac{3}{7}$	c 1 $\frac{1}{3}$	d $1\frac{1}{2}$
5 a $\frac{2}{7} < \frac{4}{7}$	b $\frac{3}{8} \ge \frac{1}{8}$	c $\frac{2}{3} \ge \frac{3}{5}$	$d 3\frac{1}{9} \le \frac{29}{9}$
6 a $\frac{5}{7}$	b $\frac{5}{8}$		
7 a 10 8 a 10	b 21 b 21	c 24 c 24	
9 a $1\frac{1}{4}, \frac{4}{4}, \frac{3}{4}, \frac{1}{4}$		b $\frac{1}{3}, \frac{1}{5}, \frac{1}{8}, \frac{1}{10}$	
c $\frac{4}{3}, \frac{5}{6}, \frac{2}{3}, \frac{1}{12}$	-	_	20
10 a $\frac{1}{2}$	b $\frac{5}{6}$	c 1 $\frac{5}{24}$	d $5\frac{23}{30}$
e $\frac{1}{2}$	f $2\frac{1}{2}$	- 10	4.5
11 a 7 e 1/6	b 80 f 7 1 /2	c 12	d 5
12 a $\frac{4}{3}$	b $\frac{12}{7}$	c $\frac{4}{11}$	d $\frac{1}{8}$
13 a $\frac{1}{5}$	b 20	c 4	d 2
	%, C = 28%,	$D = \frac{1}{10}, E = \frac{3}{4}, F = 1\frac{3}{2}$	1
15 a \$20 d \$30	b \$210 e \$9	c 48 g	
16 a $\frac{3}{5}$, 60%		$\frac{1}{5}$, 20%	
c $\frac{1}{16}$, 6.25%	d	$\frac{3}{10}$, 30%	
17 a 3:4 d 30 km/h 18 5 kg bag is better	 b 10:3 e 2 L/m at 70c per kg 	c 25 : 1 f 13 words/r g compared to 80c per	
Multiple-choice qu	estions		
1 C 2 B 7 E 8 B	3 D 9 D	4 E 5 10 B 11	

Extended-response questions

1	а	300	b	75%	C	450
	d	45	е	1080		

Chapter 5

m-up quiz						
9		b 7		c 48		d 4
				c 4		d 5
						d 21 d 10
						d 10 d 20
						d 100
20						d 6
1		b 9		c 3		d 45
17		b 14		c 11		d 8
7 32 cm		f 18 b 24 cm			mm	h 17
you try						
n ple 1						
6						
nple 3						
⊦7 b	w	-6 c	x + y	,	d $\frac{m}{2}$	e 52
cise 5A						
expression		d co	efficier	nt		
2x, 7y		b 3 <i>a</i>	,2c,e			
5q, 3r, 2s				7		
3	b		c 4			
i 2		ii 1				
i 4		ii 12				
<i>x</i> + 3						
					- I-	07
						10k
<u>y</u> 8	f	$\frac{2}{2}$	g 3a	<i>i</i> + 4	h 2	2 <i>p</i> + 12
70	Ŀ	10				
			n 0/	~ · •		
False						
		False	f Tr			
True						
$\frac{\$A}{4}$						
$\frac{\$A}{4}$						
		ii \$30				
	9 13 11 13 11 8 17 20 20 1 17 7 32 cm you try mple 1 y, 3 mple 2 6 mple 3 +7 b cise 5A pronumerals expression 2x, 7y 5q, 3r, 2s 3 i 2 i 3 i 4 i 2 i 4 x + 3 g - 3 2u $\frac{y}{8}$	9 13 11 8 17 20 20 1 17 7 32 cm you try nple 1 y, 3 nple 2 6 nple 3 +7 b w cise 5A pronumerals expression 2x, 7y 5q, 3r, 2s 3 i 2 i 3 i 4 i 2 i 4 x + 3 b $g-3$ e $2u$ b $\frac{y}{8}$ f 70 b $8x$ 1000x b $8x$ 1000x b $8x$ 1000x b $8x$ 1000x b $3x$ b 1 b 1 b 1 b 1 b 2 c 1 c 1 c 1 c 1 c 1 c 1 c $2x, 7y$ c 1 c 1	9 b 7 13 b 21 11 b 5 8 b 36 17 b 8 20 b 44 20 b 6 1 b 9 17 b 14 7 f 18 32 cm b 24 you try nple 1 y, 3 nple 2 6 6 6 nple 3	9 b 7 13 b 21 11 b 5 8 b 36 17 b 8 20 b 44 20 b 6 1 b 9 17 b 14 7 f 18 32 cm b 24 cm you try nple 1 y, 3 nple 2 6 nple 2 6 pronumerals pronumerals b constant constant expression d 2x, 7y b 3 b 2x, 7y b 3 b 2x, 7y b 3 b 13 i 14 i 13 i 14 i 15 </td <td>9 b 7 c 48 13 b 21 c 4 11 b 5 c 5 8 b 36 c 40 17 b 8 c 5 20 b 44 c 22 20 b 6 c 2 1 b 9 c 3 17 b 14 c 11 7 f 18 g 35 32 cm b 24 cm c 48 you try nple 1 y, 3 nple 2 6 nple 3 +7 b $w-6$ c $x+y$ cise 5A pronumerals b constant expression d coefficient 2x, 7y b 3a, 2c, e 5q, 3r, 2s d 7d, 5f, 17 3 b 13 c 4 i 2 ii 17 i 3 ii 21 i 4 ii 2 i 2 ii 1 i 4 ii 2 y 3a+4 70 b 10n 8x b $x+3$ c $8(x+3)$ 1000x b 100x c 100 000x</td> <td>9 b 7 c 48 13 b 21 c 4 11 b 5 c 5 8 b 36 c 40 17 b 8 c 5 20 b 44 c 22 20 b 6 c 2 1 b 9 c 3 17 b 14 c 11 7 f 18 g 35 32 cm b 24 cm c 48 mm you try nple 1 y, 3 nple 2 6 nple 3 +7 b $w-6$ c $x+y$ d $\frac{m}{2}$ cise 5A pronumerals b constant expression d coefficient 2x, 7y b <math>3a, 2c, e 5q, 3r, 2s</math> d <math>7d, 5f, 17 3 b 13 c 4 i 2 ii 17 i 3 ii 21 i 4 ii 2 i 2 ii 1 i 4 ii 12 x+3</math> b $k+5$ c <math>b+2 g-3</math> e $H-4$ f <math>M-6 $2u$ b $4y$ c $3x$ d $1\frac{y}{8}$ f $\frac{z}{2}$ g $3a+4$ h 2 70 b $10n$ 8x</math> b $x+3$ c <math>8(x+3) 1000x b $100x$ c $100000x$</math></td>	9 b 7 c 48 13 b 21 c 4 11 b 5 c 5 8 b 36 c 40 17 b 8 c 5 20 b 44 c 22 20 b 6 c 2 1 b 9 c 3 17 b 14 c 11 7 f 18 g 35 32 cm b 24 cm c 48 you try nple 1 y, 3 nple 2 6 nple 3 +7 b $w-6$ c $x+y$ cise 5A pronumerals b constant expression d coefficient 2x, 7y b 3a, 2c, e 5q, 3r, 2s d 7d, 5f, 17 3 b 13 c 4 i 2 ii 17 i 3 ii 21 i 4 ii 2 i 2 ii 1 i 4 ii 2 y 3a+4 70 b 10n 8x b $x+3$ c $8(x+3)$ 1000x b 100x c 100 000x	9 b 7 c 48 13 b 21 c 4 11 b 5 c 5 8 b 36 c 40 17 b 8 c 5 20 b 44 c 22 20 b 6 c 2 1 b 9 c 3 17 b 14 c 11 7 f 18 g 35 32 cm b 24 cm c 48 mm you try nple 1 y, 3 nple 2 6 nple 3 +7 b $w-6$ c $x+y$ d $\frac{m}{2}$ cise 5A pronumerals b constant expression d coefficient 2x, 7y b $3a, 2c, e5q, 3r, 2s$ d $7d, 5f, 173 b 13 c 4i 2 ii 17i 3 ii 21i 4 ii 2i 2 ii 1i 4 ii 12x+3$ b $k+5$ c $b+2g-3$ e $H-4$ f $M-62u b 4y c 3x d 1\frac{y}{8} f \frac{z}{2} g 3a+4 h 270 b 10n8x$ b $x+3$ c $8(x+3)1000x b 100x c 100000x$

Essential Mathematics for the Victorian Curriculum CORE Year 7

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5B _____

Now you try

Example 4

a 3 **c** 30 **b** 1

Example 5

8

Exercise 5B

1	а	17		b	38	ł		C	15	5	h	21
2	a	6		b	28			C	1	,	d	2
								-				
3	а	10		b	15)		C	5		d	4
4	а	14		b	1			C	10)	d	8
5	a	7		b	17	,		C	12	20	d	5
6	а	8		b	42)		C	3		d	3
7	а	20		b	50)		C	35	5	d	100
8	а	17		b	20)		C	72	2	d	12
9	а	8		b	10)		C	9		d	14
	e	17		f	3			g	14	1	h	7
	i	18			-			3		-		-
10	a	14		b	21			C	23	3	d	12
	e	18		f	21			•			-	
11	-	8		b	4			C	5		d	9
	e	4		f	6				8		h	1
	i				0			g	0		"	
	•	15										
12												
		and 24,	2 and	12	2, 3	and 8	i, 4 a	nd	6			
14		x	5	g)	12	1	6	6	7		
		x + 6	11	1	5	18	7	1	2	13		
		4 <i>x</i>	20	3	6	48	4	2	4	28		

5C _____

Now you try

Example 6

	<i>x</i> = 1	<i>x</i> = 2	<i>x</i> = 3	<i>x</i> = 4
2(x - 1)	0	2	4	6
2 <i>x</i> - 1	1	3	5	7

Not equivalent

Exercise 5C

eq	uivalent	b	9	bers	C	Y	es	not n	natter.	
а			<i>a</i> =	0	<i>a</i> = ²	1	a	<i>i</i> = 2	<i>a</i> = 3	3
	2 <i>a</i> +	2	2		4			6	8	
	(a + 1)	× 2	2		4			6	8	
b	equivalen	t								
а		B	= 0	1	3 = 1	Ì	B =	2	<i>B</i> = 3	
	5 <i>B</i> + 3	;	3		8		13	;	18	
	6 <i>B</i> + 3	;	3		9		15	;	21	
b	No									
а		6 <i>x</i> ·	+ 5	4 ,	c + 5 +	- 2	x			
	<i>x</i> = 1	1	1		11					
	<i>x</i> = 2	1	7		17					
	<i>x</i> = 3	2	3		23					
	<i>x</i> = 4	2	9		29					
b	They are	equiva	alent b	beca	ause the	ey a	are	alwa	ys equal	
а	Ν	h	E		0	E			d M	
	a eq Tru a b a b	a 9 equivalent True. When a a 2a + (a + 1)b equivalent a 5B + 36B + 3 6B + 3 b No a x = 1 $x = 2$ $x = 3$ $x = 4$ b They are	a 9 b equivalent True. When adding a $2a + 2$ $(a + 1) \times 2$ b equivalent a $5B + 3$ 6B + 3 b No a $6x$ x = 1 1 x = 2 1 x = 3 2 x = 4 2 b They are equivalent	a 9 b 9 equivalent True. When adding num a $a = 2a + 2$ 2 $(a + 1) \times 2$ 2 b equivalent a $B = 0$ 5B + 3 3 6B + 3 3 b No a $6x + 5$ x = 1 11 x = 2 17 x = 3 23 x = 4 29 b They are equivalent b	a 9 b 9 equivalent True. When adding numbers a $a = 0$ 2a + 2 2 $(a + 1) \times 2$ 2 b equivalent a $B = 0$ <i>B</i> 5B + 3 3 6B + 3 3 b No a $6x + 5$ 4 <i>x</i> x = 1 11 x = 2 17 x = 3 23 x = 4 29 b They are equivalent beca	a 9 b 9 c equivalent True. When adding numbers, order a $a = 0$ $a = 1$ 2a + 2 2 4 $(a + 1) \times 2$ 2 4 b equivalent a $B = 0$ $B = 1$ 5B + 3 3 8 6B + 3 3 9 b No a $6x + 5$ $4x + 5 + 1$ x = 1 11 11 x = 2 17 17 x = 3 23 23 x = 4 29 29 b They are equivalent because the	a 9 b 9 c Ye equivalent True. When adding numbers, order do a $a = 1$ $2a + 2$ 2 4 a $a = 0$ $a = 1$ $2a + 2$ 2 4 $(a + 1) \times 2$ 2 4 b equivalent a $a = 0$ $B = 1$ a $a = 1$ a $B = 0$ $B = 1$ a a $a = 1$ a b equivalent a a $a = 1$ a a b $B = 0$ $B = 1$ a a a a a b $B = 0$ $B = 1$ a a a a a b $B = 0$ $B = 1$ a <th>a 9 b 9 c Yes equivalent True. When adding numbers, order does a $a = 0$ $a = 1$ a a $a = 0$ $a = 1$ a $a = 0$ $a = 1$ a a $a = 0$ $a = 1$ a $a = 0$ $a = 1$ a b equivalent a $a = 0$ $B = 1$ $B = 0$ $B = 1$ $B = 0$ b equivalent a a a a a a $b = 6b + 3$ 3 9 15 b b b b No a a a b a a</th> <th>a 9 b 9 c Yes equivalent True. When adding numbers, order does not n a<th>a 9 b 9 c Yes equivalent True. When adding numbers, order does not matter. a b a a a a a a b a <t< th=""></t<></th></th>	a 9 b 9 c Yes equivalent True. When adding numbers, order does a $a = 0$ $a = 1$ a a $a = 0$ $a = 1$ a $a = 0$ $a = 1$ a a $a = 0$ $a = 1$ a $a = 0$ $a = 1$ a b equivalent a $a = 0$ $B = 1$ $B = 0$ $B = 1$ $B = 0$ b equivalent a a a a a a $b = 6b + 3$ 3 9 15 b b b b No a a a b a	a 9 b 9 c Yes equivalent True. When adding numbers, order does not n a <th>a 9 b 9 c Yes equivalent True. When adding numbers, order does not matter. a b a a a a a a b a <t< th=""></t<></th>	a 9 b 9 c Yes equivalent True. When adding numbers, order does not matter. a b a a a a a a b a <t< th=""></t<>

9 y + y + y + y; other answers are possible.

10 2(w + l); other answers are possible.

11 6

12 If x = 8, all four expressions have different values.

13 A1 and C2, A2 and D3, A3 and C1, B1 and C3, B2 and D2, B3 and D1.

Now you	ı try										
Example	7										
a No	b	Ye	S	C	Ye	S	d	No	D	e	Yes
Example	8										
i 5 <i>m</i>	b	34	ab								
Example											
5x - 1	l D	4)	,	C	47	<i>n</i> + 1 or	1 + 4	m			
Exercise	5D										
a Tru	е		False			True			False		
2 a 14 3 a 50			21 20			35 30			35 30		
a xa	nd y		a, b ar	nd c	Ŭ	00		u	00		
C k			p and	-							
5 a like c terr			like ter terms	ms							
6 a N			L			L		d	Ν		
e N i L			L L		-	N L		h I	L N		
a 5x			L 6 <i>a</i>			L 16 <i>q</i>			3 <i>b</i>		
e 9 <i>ca</i>	l		6qr		g	9 <i>ab</i>			11 <i>cf</i>		
3 a 4x e 8ca	1	b f	3a 2qr			10 <i>q</i> 7 <i>ab</i>			6 <i>b</i> 3 <i>cf</i>		
a 3 <i>a</i>			7a + 9	b		x + 6y			7a + 2		
e 7+		f	6 <i>k</i> – 2	2							
0 a 5 <i>f</i> - c 6 <i>x</i>						4a + 6b 8a + 4b					
e 7g						14x + 3					
-	+9y + 10	0				8 <i>a</i> + 13					
i 12 <i>t</i> 1 a 30 <i>n</i>		b	35 <i>n</i>		j c	5 <i>d</i> + 3 65 <i>n</i>					
2 a 3a	+ 4	b	19								
3 a 📃			3 <i>x</i> + 2	2 <i>x</i>	1	5x					
	x = 1		5			5					
	x = 2 $x = 3$		10 15			10 15					
		.,								_	10
	example example										
4 a i 4	4 <i>x</i>		ii 7 <i>x</i>			iii 11 <i>x</i>		9	iv 3 <i>x</i>		
b Xav	ier has 4	8. (Camero	n has	84.						
Progress	s auiz										
a 11		b	13								
	7				C	3 <i>f</i>		d	$\frac{p}{2} + 4$		
3 D									2		
a 15			20					d	6		
5 a 13		b	66			16			16		
5 a 18 7 equiva		b	17		C	15		d	0		
3 a N		b	Е		C	E		d	E		
) a N			L		C	Ν		d	L		
eΝ		f		11 <i>kt</i> 14a +	- 4	k	C	16	x + 11y - 2g		
1 0 a 175							-		,		

5E _____

Now you try

Example 10 **b** 40*abc*

a 3*xy*

Example 11

a $\frac{6}{m}$ **b** $\frac{2x}{5}$

Exercise 5E

ENU							
1 a		b	True	C	False	d	True
e	False				0		0
2 a	$\frac{1}{2}$	b	$\frac{1}{3}$	C	$\frac{3}{5}$	d	$\frac{3}{4}$
	2						4
•	2		$\frac{2}{3}$	-	$\frac{2}{3}$		
3 a	$\frac{2}{3}$	b	3	C	3		
4 a	C		E		B	А	А
		b	E	C	D	u	А
_ e	D		_		_		
5 a		b	5 <i>p</i>	C	7 <i>r</i>	d	11 <i>s</i>
e	10 <i>ab</i>	f	5 <i>cd</i>				
6 a	10 <i>ab</i>	b	16 <i>xy</i>	C	10 <i>b</i>	d	28 <i>xz</i>
e	36 <i>abc</i>	f	48def	q	42 <i>ab</i>	h	42 <i>abc</i>
i		i	6xy	•			
	36 <i>a</i>	b	63 <i>d</i>	C	8 <i>e</i>	Ь	15 <i>a</i>
		f					
			63 <i>eg</i>		8abc		28 <i>adf</i>
i	12 <i>abc</i>	j	8 <i>abc</i>		60 <i>defg</i>	I	24abcd
8 a	$\frac{x}{5}$	b	<u>Z</u>	C	$\frac{a}{12}$	d	$\frac{b}{5}$
U u	5		2	v	12	u	5
	2		$\frac{z}{2}$ $\frac{5}{d}$		x		a
e	$\frac{2}{x}$	f	$\frac{d}{d}$	g	$\frac{x}{y}$	h	$\frac{a}{b}$
					y		
9 a	2 5	b	5 9	C	$\frac{9a}{4}$	d	$\frac{2b}{5}$
	5				4		5
	X		$\frac{3x}{4}$		$\frac{2}{3}$		3
e	$\frac{x}{2}$	f	4	y	3	h	$\frac{3}{4}$
	-						
i	2 <i>a</i>	j	3	k	2 <i>y</i>	L	$\frac{3}{y}$
			_				
10 a	3 <i>k</i>	b	6 <i>x</i>	C	12 <i>xy</i>	d	14 <i>ab</i>
11 a	\$20	h	$\frac{\$C}{5}$				
11 a	ΨΖΟ	n	5				
12 a	6 <i>p</i> b	3	imes 2 <i>p</i> also simplif	ies	to $6p$, so they ar	e e	quivalent.
13 a	2 <i>a</i>		b 12		·· · · · · · · · · · · · · · · · · · ·		4
10 4	20		1				
	6						
-	12 <i>a</i>		It has faire the second				
C	$\frac{3}{3a}$ simplifies to	4 ט	. It has four times	s th	e area.		
Ч	Area is multiplie						
u	Alca is multiplic	ul	Jy 5.				
5F							

Now you try

Example 12

54

Example 13

a $\frac{100}{n}$ **b** 80 + 100*t*

Exercise 5F

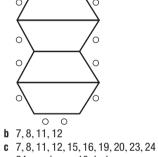
•	a	12 20		10 28		30 40	 27 100
4	а	3 <i>x</i>	b	36			
5	а	\$36	b	\$21	C	3 <i>n</i>	
6	а	6	b	11	C	<i>t</i> + 2	

7 a	a	10 <i>x</i>	b	15	x	C	kx			
8 2	<u>2</u> n	ı								
9 a	a	180 km	b	30	km	C	70 <i>n</i>			
		\$200	b	\$6	80	C	50 + 80	x		
11 a	a	Hours			1	2	3	4	5	
		Total cos	st (\$)	150	250	350	450	550]
I	b	100 <i>t</i> + 50				C	\$3050			
12 a	a	\$25	b	10	<i>x</i> + 5			C	\$75	
13 a	a	33	b	<i>g</i> =	= 8 and	<i>b</i> = 5				
(C	g = 3 and b	= 2	<u>2, g</u>	= 1 an	d b = 1	4, g = 0	D and b	= 20	
14 a	a	0.2 + 0.6t			b	0.8 + 0	.4 <i>t</i>		c Em	ma's
(d	3 min								

Maths@Work: Office designs

1		Design A	Design B	Design C
	i	7, 14, 21,	7, 12, 17, 22	6, 10, 14, 18
	ii	Number of people = $7 \times n$	Number of people = $2 + 5n$	Number of people = $2 + 4n$
	iii	70 people	52 people	42 people
	iv	\$33 249	\$27 039	\$23 589





```
24 people use 10 desks.
3 b
```

b		Cost of one row	
	Office	of furniture	Total cost
	I	\$9801	\$47 604
	11	\$15 604	\$162 576
		\$12 885	\$223 875
	IV	\$8558	\$247 392

Puzzles and games

- **1** A = 3, B = 7, C = 2, D = 1
- **2** 40 metres
- **3** a *a* = 4, *b* = 12, *c* = 16, *d* = 8, *e* = 36

```
b a = 6, b = 3, c = 5, d = 10, e = 15
```

4	x	2	2	3	0	5
	у	7	6	3	12	1
	3 x	6	6	9	0	15
	x + 2 y	16	14	9	24	7
	xy	14	12	9	0	5

5
$$a = 1, c = 4, d = 2, e = 1, f = 3, g = 4, h = 1, i = 3, i = 4, k = 2$$

Short-answer questions

6

1	а	5a, 3b, 7c, 1	2		b	12		
2	а	<i>u</i> + 7	b	3 <i>k</i>	C	<i>h</i> – 10		
3	а	6	b	104	C	16	d	21
4	а	13	b	24	C	2	d	17
5	а	15	b	24	C	2	d	4

628

Essential Mathematics for the Victorian Curriculum CORE Year 7

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6 a	15	b 8	C	4	d 27	
7 a		<i>x</i> = 0	<i>x</i> = 1	<i>x</i> = 2	<i>x</i> = 3	
	4 <i>x</i>	0	4	8	12	
	3 <i>x</i> + <i>x</i>	0	4	8	12	
b	equivalent					
8 a	E	b N	C	E	dN	
9 a	L	b N	C	L	dN	
e	L	f N				
10 a	7x + 3	b 11 <i>p</i>	C	7a + 14b -	⊦4	
d	3m + 17mm	n + 2n	е	1 + 7c + 4	h – 30	
f	4u + 3v + 2	luv				
11 a	12 <i>ab</i>	b 6 <i>xyz</i>	C	36fgh	d 64 <i>klm</i>	
12 a	$\frac{3}{2}$	b $\frac{3}{5}$	C	$\frac{a}{3}$	d $\frac{4x}{3z}$	
13 9 <i>t</i>	1	4 <i>g</i> + <i>b</i>	15 3 <i>x</i>			

Multiple-choice questions

1 B	2 D	3 A	4 B	5 D
6 D	7 D	8 C	9 A	10 A

Extended-response questions

1	а	\$60	b	\$60	C	\$90	d	30 <i>n</i>
	e	\$100						
2	а	i \$17		ii \$32		iii \$152		
	b	2 + 1.5 <i>k</i>						
	C	\$62						
	d	6 + 1.2 <i>k</i>						

Chapter 6

Warm-up quiz

1	e	0.1 0.001 0.5		0.3 4.7 0.25	-	1.7 0.75	d	0.01
3		\$0.70	~	\$0.85	-	\$1.00	d	\$0.05
	e	\$1.05	f	\$0.03				
4	а	50	b	25	C	75	d	250
5	а	\$0.90	b	\$10.50	C	\$22.50	d	\$0.81
6	10)c						
7	\$1	5.50						
8	а	\$85	b	\$0.10	C	\$2.70	d	\$0.70
	e	\$11.20	f	\$0.24				
9	а	\$7	b	\$2.90	C	\$3.95	d	\$29.75
	e	\$7.50						
10	а	\$87.50	b	\$92.60	C	\$20.90		
11	а	\$38.55						
12	а	523	b	839	C	312	d	1237

6A _____

Now you try

Example 1

a $\frac{3}{100}$ **b** $\frac{3}{1000}$

Example 2 a 0.2

b 0.006

b 5.47

Example 3

3.48, 3.84, 4.38, 4.83, 8.34, 8.43

Exercise 6A

	0.00 0								
1 a		D		В	_	d	С	e	Α
2 a	$\frac{2}{10}$	b	$\frac{3}{100}$	C	$\frac{7}{1000}$				
3 a	5	b	6	C	7		d	37	
4 a	6	b	_6	C	6		d	$\frac{6}{10}$	
	10	~	100	Ũ	1000		u	10	
е	6	f	6	g	6		h	6	
U	0	'	100	9	100			1000	
5 a	0.3	b	0.8	C	0.15		d	0.23	
e	0.9	f	0.12	g	0.121		h	0.174	1
i	0.1	j	0.11	k	0.111		- I	0.03	
6 a	6.4	b	5.7	C	212.3	3	d	1.16	
e	14.83	f	7.51	g	5.07		h	18.6	12
7 a	Т	b	F		Т		d	Т	
e	F	f	Т	g	Т		h	Т	
8 a	6.1	b	9.6	C	0.8		d	28.5	
e	0.171	f	0.203						
	3.05, 3.25, 3				3.06,				
	1.718, 1.871						2.96, 2	6.92,2	29.26, 29.62
	Waugh, Bord	er,	Gilchrist, Tay	lor, l	Hughe	S	b	First	
	Day 6		Day 4		Day 6	;			
12 a	$7 \times 1 + 1 \times$	1 10	$+\frac{3}{100}+5\times$	1 100	00		b	1.563	3
13 a	(0.1), (1.0) (2)	w	ays)						
b	0.12, 0.21,	1.0	02, 1.20, 2.01	, 2.7	10, 10.	2, 1	2.0, 2	20.1,2	21.0
	(10 ways)								
C	0.123, 0.13	2, 1	0.213, 0.231,	, 0.3	12, 0.3	321	, 1.023	3, 1.03	2,
	1.203, 1.230), 1	.302, 1.320,	2.01	13, 2.0	31,	2.103	, 2.130),
	2.301, 2.310), 3	.012, 3.021,	3.10)2, 3.1	20,	3.201	, 3.210),
			2.03, 12.30,						
	21.03, 21.30), 2	3.01, 23.10,	30.1	12,30.	21,	31.02	, 31.20),
			02.3, 103.2,						
			10.3, 213.0,			1.0,	301.2	, 302.1	,
	310.2, 312.0), 3	20.1, 321.0	(60	ways)				

6B _____

Now you try

Example 4		
a 2.17	b	(

2.17	7		b	36.39
		_		

b 1

Example 5 a 0.05

Exercise 6B

1 a 2	b	4	C	2	d	5
2 a 5	b	9	C	1	d	4
e 0	f	9	g	6	h	5
3 a 1	b	7	C	4	d	8
4 a 8	b	7	C	5		
5 a 14.8	b	7.4	C	15.6	d	0.9
e 6.9	f	9.9	g	55.6	h	8.0
i 0.7	j	0.7	k	0.7	T	0.9
6 a 3.78	b	11.86	C	5.92	d	0.93
e 123.46	f	300.05	g	3.13	h	9.85
i 56.29	j	7.12	k	29.99	T	0.90
7 a 15.9	b	7.89	C	236	d	1
e 231.9	f	9.4	g	9.40	h	34.713
8 a 24.0	b	14.90	C	7	d	30.000
9 a 28	b	9	C	12	d	124
e 22	f	118	g	3	h	11
10 a \$13	b	\$31	C	\$7	d	\$1567
e \$120	f	\$10	g	\$1	h	\$36
11 a 149.9 × 48						
b i 7195 cen	ts			ii \$72		
12 5, 6, 7, 8 or 9.						

13 0.35, 0.36, 0.37, 0.38, 0.39, 0.40, 0.41, 0.42, 0.43, 0.44

Answers

6C Now you try Example 6 a 24.47 **b** 61.763 Example 7 **a** 15.1 **b** 64.29 **Exercise 6C** 1 C **2** B 3 a 8.57 **b** 5.179 c 15.956 **d** 8.99 **4** a 6.8 **b** 14.96 **c** 3.87 f 25.94 **g** 247.4 **h** 58.31 e 27.97 **b** 5.8 **c** 0.9 **d** 0.99 **5 a** 2.6 **e** 8.47 f 15.507 **q** 16.06 h 21.33 i 0.013 **6 a** 0.79 **b** 0.516 **c** 0.4 **d** 1.73 **g** 6.33 e 12.1 f 114.13 **h** 70.79 **7** a 0.5 **b** 3.2 c 21.2 **d** 0.48 e 12.3 f 131.4 g 22.23 h 13.457 j 4947.341 i 43.27 8 16.189 9 a \$45.70 **b** \$54.30 10 49.4 mm 11 3.3°C 12 a b 0.6 0.7 0.2 1.6 0.5 0.9 0.4 0.1 0.5 0.9 0.3 1.0 0.6 1.5 0.8 0.3 0.4 0.2 1.1 0.7 1.4 1.3 0.8 1.2 0.1 Magic sum = 1.5 Magic sum = 3.46D _ Now you try Example 8 a 14.3 **b** 772.1 Example 9 **a** 6.2131 **b** 0.0394 Example 10 **a** 1400 **b** 0.0006 **Exercise 6D 1** a 1 **b** 2 **c** 4 **d** 2 **e** 1 **c** 00 **d** 00000 **2** a 00 **b** 000 **c** 0 **d** 00000 **3** a 000 **b** 00 4 a Right 2 places **b** Left 1 place d No change c Right 6 places f Right 3 places e Left 3 places g Right 1 place h Left 7 places **5 a** 48.7 **b** 352.83 c 4222.7 **d** 1430.4 e 5699.23 f 125.963 g 12700 h 154 230 **k** 86710000 i 3400 I 516000 j 2132 **b** 35.31 c 2.4422 **d** 56.893 6 a 4.27 f 9.32611 g 0.029 **h** 0.001 362 **e** 12.13518 i 0.000 54 **j** 0.367 **k** 0.000 002 I 0.0100004

11 12	a a d	ii iii iv v vi	200 4.714 1010 18 40 452.7 2184 7.4 (2.42	4, 4 (0)0 (7 (⁻ (7 148 (48	71 .05 (9.1 15. .28 3 ÷	5 × 2 × 09 3 × 10 ÷ 1	b b e 100 > 1000 > 100 > 0 ÷ 2) 00 ÷ × 10	10 × 2)) × 2 × 3 × 3) 2)	00 2))	ii 2,	2.4, 0.:	24	c 100	
					· · ·		98 ÷ ⁻			·				
6	Ε													
N	ow	you t	try											
	(ar 16	nple 1 5.2	1	b	0.6	538	}							
E	ker	cise 6	δE											
1	а	1			b					2			4	
2	e a	1 1				2 2				2 3			5 3	
3		5 19.2				2	92		g c	4 0.192	2		3 1.52	
	e	19.46		in-	f	0.0	0756		-			-		
		iestior 4.8	i; dec	im		olac 16			C	7.5		d	29	
	e	19.6				1.9			-	2.4		h I	0.24	
6	i a	0.56	3			0.2 5.4	427			0.74 3.556	6	'	0.81	
7		0.74 100.8	2			2.3	34 8.46			8.12 15.5	16	h	23.12	
'	e	12.42	2		f	5.4				311. ⁻			0.000 96	66
8		0.000 \$31.5 \$74.8	50, \$3	32						\$22.6 \$2.82	65, \$23 2, \$3	}		
0		\$2.10 100.8				h	483		f		79, \$12 25 40		Ь	9800
	e	1440	00			f	465 364 5	550			0.68	0		371
).47 m 56 kg	1											
		38.76	6			b	73.6			C	0.75			
13		42,0 \$13.				e	0.042	2						
				\$2,	\$1	CC	oins ai	nd a	10	c piece	e (Othe	r an	swers ar	e possible.)
61	F													
N	ow	you 1	try											
		nple 1 366		b	0.0	001	775							
		nple 1												
	12	•	0	b	0.6	59								
E)	cer	cise 6	õF											
1	В													
2		12 ÷ 5642								÷ 2 ÷ 1				152 ÷ 1 380 ÷ 1
3	а	32.4	56, 3					b	12	043.2			I	JUU - I
Δ		34.5, 4.2	1				h	d 6.1		34 12	0, 4		c 21.34	L
-		4.Z 0.70	55					0. 1.5					f 0.308	
	g	19.39						37		л			i 0.002	
	j m	117. ⁻ 0.39	CUI					0.6		4			0.0020.175	25625 5
		8.95						9.3					r 105.1	
		C) Gree	- - - -		nd e	etal 2	2021			Ċ	Cam	ibridae I li	niversity Pre

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b 31.67

c 0.49 e 63 489 000 f 0.001 003 2

c 22510

f 2134000

i 340 000

I 0.156

o 0.087

r 0.0034

b 43000

e 213 400

k 1.56

n 0.87

q 0.007

h 9900000

7 a 2291.3

d 0.222 **8** a 15600

d 16000

g 7000 j 15.6

m 8.7 **p** 0.016

630

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5	а	30.7	h	77.5	C	26.8
Ŭ		8.5	e	44.4	f	645.3
	u					
	g	0.08	h	0.050 425	İ.	980
	j	800.6	k	0.79	L	2161000
6	а	7.5	b	75	C	750
	d	7500	e	75 000	f	750 000
7	а	11.83 kg	b	\$30.46	C	304.33 m
	d	239.17 g	e	965.05 L	f	\$581.72
8	а	1.1807	b	8.267	C	0.0123748
	d	0.004 23	e	0.096 487	f	0.0007825
9	а	26.67, 26 can be filled		b 40		
10	\$1	.59 per L				
11	а	4	b	6	C	27
	d	39	e	76	f	5000
12	а	24.53	b	19.7	C	2453
	d	1.97	e	2.453	f	197

Progress quiz

1	a	$\frac{3}{10}$	b	3 1000				
2	а	F	b	Т	C	Т	d	F
3	а	5.35	b	9.7	C	0.8	d	0.271
4	а	13.48	b	8.04	C	72.68	d	45.40
5	а	\$9	b	\$16	C	\$104	d	\$1100
6	а	8.77	b	56.85	C	229.81	d	63.003
7	а	3.42	b	22.21	C	21.744	d	33.234
8	а	7351.6	b	49 200	C	56.789		
	d	0.005 609	e	27 800	f	0.00278		
9	а	3.24	b	3.138	C	177	d	28 400
10	а	17.614	b	0.0016	C	1704.9	d	0.1891
11	1(00						

6G __

Now you try

E	kample 14				
a	$\frac{31}{50}$	b	$1\frac{37}{1000}$		
E	kample 15				
a	0.6	b	2.75	C	0.2Ġ

Exercise 6G

E	ker	CISE OG						
	a			100		75,7		5,4
2	а	2		15,20	C	10, 4	a	16
3	а	0.3		$\frac{1}{2}$	C	0.8	d	1.5
	e	0.9	f	$\frac{1}{2}$				
4	a	$\frac{2}{5}$	b	$\frac{3}{5}$	C	$\frac{4}{5}$	d	$\frac{11}{50}$
	e	$1\frac{11}{50}$	f	$5\frac{1}{2}$	g	$\frac{3}{20}$	h	<u>99</u> 100
	i	$\frac{2}{25}$	j	$\frac{1}{100}$	k	$\frac{1}{1000}$	I	$\frac{101}{500}$
	m	$\frac{1}{2}$	n	$6\frac{2}{5}$	0	$10\frac{3}{20}$	p	$18\frac{3}{25}$
	q	$3\frac{1}{4}$	r	$\frac{1}{20}$	S	$9\frac{3}{40}$	t	$5\frac{24}{125}$
5	а	0.7	b	0.9	C	0.31	d	0.79
	e	1.21	f	3.29	q	0.123	h	0.03
	i	0.07			Ŭ			
6	a	$\frac{8}{10} = 0.8$			b	$\frac{5}{10} = 0.5$		
	C	$\frac{35}{100} = 0.35$			d	$\frac{46}{100} = 0.46$		

		05						25				
	~	-	= 5.95	5				$3\frac{25}{100} =$				
	$g \frac{2}{10}$	$\frac{5}{0} = 2$.5				h	$\frac{375}{1000} =$	0.37	5		
	$i \frac{2}{10}$	$\frac{8}{00} =$	0.28									
7	a 0.	.5 .3		b f	0.5 0.37	5	C	0.75 0.41 Ġ		d 0.4	28571	
	i 0.	. 2		'	0.57	5	-				20071	
	c 0,		5, 0.5					0, 0.3, 0, 0.2,			8, 1.0	
9	$\frac{1}{4}, 0.$	$4, \frac{1}{2}, \frac{1}{2}$	5, 0.7	5, ().99							
10	\$0	.01	\$ 0.0	5	10c	20c		c 50c		90c		9
	1($\frac{1}{20}$		$\frac{1}{10}$	$\frac{1}{5}$	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{9}{10}$	99 99 100	
						.1Ġ, O	.1428	357, 0.12	25, 0.	i,0.1		
			et sma <u>1</u> 2		r. $\frac{3}{5}, \frac{3}{5}, \frac{3}{5}$	3 4	9			b 4		c 2
		• •						_{oz} 7				• -
		J			100		3	67, <mark>7</mark> 10	6	1		
	b $\frac{3}{5}$	0.52	, 45%	, 0	.43, 2 5	= 0.4	4, 9 25	= 36%,	0 , 0.	$\dot{3} = \frac{1}{3}$		
	a No b 1.		1356	23.	, no	patte	ern					
	c No d In		al nur	nhi	ere eu	ch as	√2 ai	nd π car	not h	evnre	e hasse	\$ 2
								attern.	inor by	5 OAPIA	00000	lo u
EX	amp	le 16										
a Exa	0.67 amp	le 17		4.			c 0.	824	d	0.001	7	
a Exa a	0.67 amp 94.1	le 17 %	b		6 37%		c 0.	824	d	0.001	7	
a Exa Exa	0.67 amp 94.1 erci s	le 17 % se 6H	b	23	37%				d			
a Ex: a Ex: 1 2	0.67 amp 94.1 ercis a 95 C	le 17 %	b	23				824 75%	d	0.001 d 26 ⁴		
a Exa Exa 1 2 3 4	0.67 amp 94.1 ercis a 95 C A a 50	le 17 % se 6H 5%	b	23	37%				d			
a Exa Exa I 2 3 4	0.67 amp 94.1 ercis a 95 C A a 50 b 50	le 17 % se 6H 5% 0 0%	b	23	37% 60%			75%	d	d 26'	%	
a Ex: a Ex: 1 2 3 4	0.67 amp 94.1 ercis a 9! C a 5(b 5(b 5(c i d i	le 17 % se 6H 5% 0 0% 5 50%	b	23 b	37% 60% ii 1(ii 50	00	C	75% iii 20 iii 50%		d 26 iv iv	%	
a Ex: a Ex: 1 2 3 4 5	0.67 amp 94.1 ercis a 9! C a 5(b 5(b 5(c i d i	le 17 % se 6H 5% 0 0% 5 50% 00	b	23 b	37% 60% ii 10	00	C C C	75% iii 20 iii 50% out of 0.68		d 264 iv	% 1 50%	
a Ex: a Ex: 1 2 3 4 5 6	0.67 amp 94.1 ercis a 9! C a 9! C A 50 C a 50 c i a 10 a 0. e 0.	le 17 % se 6H 55% 00 55 50% 00 32 11	b	23 b b f	60% ii 1(ii 5(35 0.27 0.12	00 0%	C C C g	75% iii 20 iii 50% out of 0.68 0.18		d 26 ⁴ iv iv d 15 d 0.5 h 0.8	% 1 50% 54	
a Ex: 2 3 4 5 6	0.67 amp 94.1 ercis a 9! C A 9! C A 50 b 50 c i b 50 c i a 0. e 0. i 0. m 0.	le 17 % se 6H 55% 00 32 1 92 06	b	23 b b f j n	60% ii 10 ii 50 35 0.27 0.12 0.75 0.09	00 0%	C C g k o	75% iii 20 iii 50% out of 0.68 0.18 0.11 1		d 26 ⁴ iv iv d 15 d 0.5 h 0.8 I 0.6 p 0.0	% 50% 55 51	
a Ex: 2 3 4 5 6	0.67 amp 94.1 ercis a 9! C a 9! C A a 5(b 5(c i b 5(c i a 1(a 0. e 0. i 0.	le 17 % se 6H 55% 00% 5 50% 00 32 1 92 06 18	b	23 b b f j n r	 ii 10 ii 50 35 0.27 0.12 0.75 	00 0%	C C G k o S	75% iii 20 iii 50% out of 0.68 0.18 0.11	2	d 26 ⁴ iv d 15 d 0.5 h 0.8 I 0.6	% 1 50% 54 55 51 19	
a Exa Exa 1 2 3 4 5 6	0.67 amp 94.1 ercis a 95 C a 95 C b 5 c i a 10 a 10 c i a 10 c i a 0. c i i 0. c i 1. c c i 1. c c i 1. c c c c c c c c c c	le 17 % se 6H 55% 0 0 5 50% 00 32 1 92 06 18 225 11235	b 1	23 b b f j n r b f	60% ii 10 ii 50 35 0.27 0.12 0.75 0.09 1.42 0.17 1.88	00 9% 5 8	C C C G K O S C G	75% iii 20 iii 50% out of 0.68 0.18 0.11 1 0.75 0.3333 1.5	2	d 26 iv iv d 15 d 0.5 h 0.8 l 0.6 f 1.9 d 0.0 t 1.9 d 0.0 h 5.2	% 50% 55 11 99 825	
a Ex: a Ex: 1 2 3 4 5 6 7 8	0.67 amp 94.1 ercis a 99 C a 99 C a 99 C b 50 c i a 99 C c i b 50 c i c c i c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c c	le 17 % 55% 0 00% 5 50% 00 32 1 92 .06 18 .225 1235 0079 00%	b 1	23 b b f j n r b f j b	 ii 10 ii 50 0.27 0.12 0.75 0.09 1.42 0.17 1.88 0.00 30% 	00 9% 5 8 0 25	C C C C C C C C C C C C C C C C C C C	75% iii 20 iii 50% out of 0.68 0.11 1 0.75 0.3333 1.5 0.0104 45%	2	d 26 iv iv d 15 d 0.5. h 0.8 l 0.6 t 1.9 d 0.0 t 1.9 d 0.0 t 1.9 d 0.0 d 714	% 50% 54 55 99 9825 2095 %	
a Ex: a Ex: 1 2 3 4 5 6 7 8	0.67 amp 94.1 ercis a 99 C C a 99 C C a 99 C C a 99 C C a 99 C C a 99 C C a 99 C C b 50 c i i 0. c /b> i i 0. c i i i i i i i i	le 17 % 55% 0 00% 5 50% 00 32 1 92 006 18 225 1235 0079 00% 1.6%	b 1	23 b b f j n r b f j b	 ii 10 ii 50 0.27 0.12 0.75 0.09 1.42 0.17 1.88 0.00 30% 37.5 	00 9% 5 8 0 25 %	C C c g k 0 s c g k c g	75% iii 20 iii 50% out of 0.68 0.18 0.11 1 0.75 0.3333 1.5 0.0104 45% 250%	7	d 26 iv iv d 15 d 0.5 f 0.0 f 1.9 d 0.0 f 1.9 d 0.0 f 1.9 d 0.0 d 71 f h 23	% 50% 54 55 64 99 1825 2095 % 1.4%	
a Ex: a Ex: 1 2 3 4 5 6 7 8 9	0.67 amp 94.1 ercis a 9! c a 5(0 c i 0. b c i 0. m 0. q 2. a 0. i 0.	le 17 % 5% 5% 00% 5 50% 00 32 1 92 .06 18 .225 .1235 .0079 0% 1.6%	b 1	23 b b f j n r b f j b f	 ii 10 ii 50 35 0.27 0.12 0.75 0.09 1.42 0.17 1.88 0.00 30% 37.5 	00 9% 5 8 0 25 %	C C c g k 0 s c g k c g	75% iii 20 iii 50% out of 0.68 0.11 1 0.75 0.3333 1.5 0.0104 45%	7	d 26 iv iv d 15 d 0.5. h 0.8 l 0.6 t 1.9 d 0.0 t 1.9 d 0.0 t 1.9 d 0.0 d 714	% 50% 54 55 64 99 1825 2095 % 1.4%	
a Ex: a Ex: 1 2 3 4 5 6 7 8 9 10	0.67 amp 94.1 ercis a 9! c a 5(c i b 5(c i b 5(c i a 5(c i b 5(c i a 5(c i b 5(c i a 5(c i b 5(c i a 1(a 0.0, b 1(c) i a 0.0, i b 1(c) i a 0.0, i b 1(c) i a 0.0, i b 2(c) i b 1(c) i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c i c c i c c c c c c c c	le 17 % 5% 5% 00% 5 50% 00 32 1 92 .06 18 .225 .1235 .0079 0% 1.6% 5%	b 1	23 b b f j n r b f j b f	 ii 10 ii 50 0.27 0.12 0.75 0.09 1.42 0.17 1.88 0.00 30% 37.5 	00)% 5 8 0 25 % %	C C c g k 0 s c g k c g	75% iii 20 iii 50% out of 0.68 0.18 0.11 1 0.75 0.3333 1.5 0.0104 45% 250%	7	d 26 iv iv d 15 d 0.5 f 0.0 f 1.9 d 0.0 f 1.9 d 0.0 f 1.9 d 0.0 d 71 f h 23	% 50% 54 55 64 99 1825 2095 % 1.4%	
a Ex: a Ex: 1 2 3 4 5 6 7 8 9 10 11	0.67 amp 94.1 ercis a 9! c a 5(0 c i a 5(0 c i a 5(0 c i a 10 a 0. e 0. i 0. m 0. e 1. i 0. e 4. i 2. 35% 0.52	le 17 % 5% 5% 0 0% 5 50% 00 32 192 0.06 18 225 0079 0% 1.6% 5%	b 1 5 5	23 b b f j n r b f j b f	 ii 10 iii 50 35 0.12 0.75 0.09 1.42 0.17 1.88 0.00 30% 37.5 0.14 	00)% 5 8 0 25 % % 5 25	C C c g k 0 s c g k c g	75% iii 20 iii 50% out of 0.68 0.18 0.11 1 0.75 0.3333 1.5 0.0104 45% 250%	7	d 26 iv iv d 15 d 0.5 f 0.0 f 1.9 d 0.0 f 1.9 d 0.0 f 1.9 d 0.0 d 71 f h 23	% 50% 54 55 64 99 1825 2095 % 1.4%	

6G

ii 1

e i 100%

- 12 a 100% is all questions correct.
 - **b** 20 out of 40, half the answers correct.
 - **c** No questions correct.
- **13 a** F ÷ A × 100
 - **b** F: points scored for the team; A: points scored against the team **c** 100%

Maths@Work: Retail assistant

_	a \$38.50 a \$5.70	b \$138.80 b \$123.90		\$20.95 \$45.65	d \$3.0	0
3		Rounding a	amount	Total	Change	
	Customer	in cen	ts	due	due	
	Adam	-2		\$45.65	\$5.15	
	Blake	+2		\$123.05	\$6.95	
	Christy	+2		\$123.05	\$2.05	
	Dion	-2		\$56.90	\$0.10	
	Eden	-1		\$67.55	\$3.05	
4	a i \$5.20 b i \$14.63 v \$55.70	ii \$3.15 ii \$23.69 vi \$0.10	iii \$10 iii \$17		v \$0.35 v \$55.72	
5	a 2 cents	b 1 cent				
6	i \$1.28	ii 12	iii \$34.8	2 iv \$	\$15.20	
7	Total value	е				
	\$2050					
	\$4046					
	\$616					
	\$695					
	\$2280					

Puzzles	and	games
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\$576

\$10 263

1 a 7,8	3 b (6, 5, 1, 4 c	0, 1, 0, 2	
d 7,5 2 a 8,9 3 A MUS		9 c	5, 5, 1	d 7, 0, 7

4 Both the dollars and the cents match your age.

5 0.3 m, 0.42 m, 0.66 m, 0.78 m, 0.90 m, 1.02 m, 1.14 m, 1.38 m

Short-answer questions

1	a	0.44, 0.4, 0.0)4		b	0.98, 0.932,	0.8	95
2	а	8.1	b	0.81	C	8.01	d	0.801
3	a	3 hundredths	8 =	$\frac{3}{100}$	b	3 thousandth	IS =	$=\frac{3}{1000}$
	C	3 ones = 3						
4	а	False	b	False		True	d	True
	e		f	True	g	True	h	False
	i	True						
5	а	\$62.88		\$63	C	\$62.90		
6	а	12.7	b	8.4	C	9.4	d	7.5
	e	0.1	f	7.1				
7	а	12.81	b	423.46	C	15.89	d	7.25
	e	6.67	f	3.33				
8	а	1.6	b	1.56	C	19.594	d	9.6
	e	21.9	f	3.3	g	45.94	h	43.5
	i	\$7.76	j	\$7	k	\$24.80		
9	а	5		5	C	4		2
10		Т		F	C	Т	d	Т
	e		f	F	g	Т	h	Т
	i	Т	j	F	k	F	I	Т
11	а	19.2	b	63.99	C	19.32	d	0.95
	e	1.52	f	6	g	16	h	3
	i	34.2						

12	Decima		Fraction	Percentage		
	0.01		$\frac{1}{100}$	1%		
	0.1		$\frac{1}{10}$	10%		
	1 0.45 0.7 0.32		$\frac{100}{100}$	100%		
			$\frac{45}{100} = \frac{9}{20}$	45%		
			$\frac{70}{100} = \frac{7}{10}$	70%		
			$\frac{32}{100} = \frac{8}{25}$	32%		
	0.06		$\frac{6}{100} = \frac{3}{50}$	6%		
	0.79		$\frac{79}{100}$	79%		
	1.05		$\frac{105}{100} = \frac{21}{20}$	105%		
	0.35		$\frac{35}{100} = \frac{7}{20}$	35%		
	0.65		$\frac{65}{100} = \frac{13}{20}$	65%		
	0.125		$\frac{125}{1000} = \frac{1}{8}$	12.5%		
	a i 0.7 d i 40%	ii 1.2 ii 2%		iv 0.0021 iv 620%		
Multiple-choice questions						

Extended-response questions

2 B

7 D

1	а	Jessica \$12.57 per hour; Jaczinda \$13.31 per hour; hence, Jaczinda
		earns higher pay rate by 74c per hour.
	b	\$12.49, \$12.50 to the nearest 5 cents

3 C

8 B

4 E

9 D

5 A

10 C

N	Ψ	12.40, φ1		uio	noui	001	J	U
C	\$3	36.90						
d	i	\$1.40	ii	\$3	.20			

e	i	\$17.50	ii	\$3.50	iii	\$700

Semester review 1

1 D

6 D

Whole numbers Short-answer questions						
1 a 4	b 1	c 303				
2 a 7324	b 12092	- 147	d 7000			
3 a 4962 e 105	b 819 f 137	c 147	d 7600			
4 a False	b True	c True				
5 22						
6 a 10	b 5	c 17	d 30			
e 56	f 48	g 62	h 16			
i 42	h. T		4 T			
7 a False e True	b True f True	c False	d True			
8 a $(2+3) \times 4$		b (10 - 2) ÷	8 = 1			
c $4 \times (6 - 2)$			0			
9 a 10	b 40	c 140				
10 a 100	b 100	c 1500				
Multiple-choice questions						
1 E 2 B	3 D	4 C	5 A			

632

Geometry Short-answer questions 1 a Acute **b** Right c Obtuse d Straight e Reflex f Revolution **b** 80° **c** 150° **2** a 30° **3** 25° **4** 78° **5 a** *a* = 140 **b** *a* = 50 **c** *a* = 140 **d** *a* = 65 **e** a = 62 f *a* = 56 **6** a = 100, b = 80, c = 100, d = 80, e = 100, f = 80, g = 1007 Because the alternate angles are not equal. **8** a 115 **b** 71 **c** 100 **Multiple-choice questions** 1 A **2** B **3** B **4** B 5 D **Extended-response questions 1 a i** *x* = 56 **ii** *y* = 95 **iii** *z* = 29 **b** x + y + z = 180Number properties and patterns Short-answer questions **1** a 1, 3, 5, 15 **b** 1, 2, 3, 5, 6, 10, 15, 30 **c** 1, 2, 4, 5, 10, 20, 25, 50, 100 **b** 7, 14, 21, 28, 35 **2 a** 3, 6, 9, 12, 15 **c** 11, 22, 33, 44, 55 **3** 1, 2, 3 and 6 **4** 4 5 a 121 **b** 144 **c** 25 **6 a** 49 **b** 144 **c** 9 7 a 5² 3² 6² Index form Value 9 25 36 b Square root form $\sqrt{9}$ $\sqrt{25}$ $\sqrt{36}$ √64 Value 3 5 6 8 **8** a 1080, 536, 930, 316 **b** 1080, 135, 930 **c** 1080, 536, 316 d 1080, 135, 930 e 1080,930

Extended-response questions

b \$700

1 a 28 h

d 12 h

8²

64

c \$1000

U	1000, 300					
а	Number of squares	0	1	2	3	4
	Number of sticks	1	1+5=6	$\begin{array}{c} 1+5 \times \\ 2=11 \end{array}$	$\begin{array}{c} 1+5\times\\ 3=16\end{array}$	$\begin{array}{c} 1+5\times\\ 4=21 \end{array}$

- **b** Number of sticks = $1 + 5 \times$ number of squares **c** Number of sticks = $1 + 5 \times 9 = 46$ matchsticks
- d 16 squares

9

10	input	4	5	6	9	11	100	
	output	19	23	27	39	47	403	

11 *A*(1,0), *B*(4,1), *C*(3,2), *D*(1,3), *E*(3,4), *F*(0,2), *O*(0,0)

Multiple-choice questions

1	E	2 A	3 B	4 E	5	D

Extended response questions

Extended-	response	questi	ons				
- 144	-				_		
b 18	C	9th	d	\$61			
ractions a			;				
Short-ansv		uons					
$\frac{3}{10}, \frac{2}{5}, \frac{1}{2}$							
$2\frac{17}{3}$							
$\frac{3}{12}$ a $\frac{11}{12}$	h	2		_e 1			
		$2\frac{2}{3}$		$6\frac{1}{4}$			
d $\frac{1}{5}$	e	4	f	$\frac{1}{2}$			
$\frac{3}{20}$							
\$120							
58 a True	b	True	c	True	d False		
$\frac{2}{3}$ True	-	nuo	Ū	nuo			
3							
Aultiple-c	hoice qu	estions					
В	2 C	3	E	4 D	5 A		
Extended-	response	questi	ons				
a 6	h	8	c	9			
	nd dose or	0		0			
		· oundaj					
Algebra		.					
Short-ansv				0			
a 3 2 a x+3		7 12a		8x + 7y	d ^W		
e y - 2		120	U	2x + 3y	u <u>6</u>		
8 a L	b	Ν		L	d N		
a 13 e 3	b f	11 24	C	39	d 6		
i 36	h			10	d		
e 6 + 5a	a f	$4x \\ 4x + 2$		12 <i>a</i>	d m		
a 6+2 <i>:</i> a 6 <i>bc</i>		3 <i>x</i> 5 <i>b</i>	c	р			
a 10 <i>p</i>		25 <i>p</i>	Ū	P			
0 12 <i>x</i>							
Multiple-choice questions							
В	2 A	3	С	4 B	5 D		
. اد - ام مراب		A116-1					
Extended- a i \$10	-	ii 3 <i>x</i>		iii 2 ₂₂ 10	1		
a i \$10 b 3 <i>x</i> + 2 c 16		II 3 <i>X</i>		iii 3 <i>x</i> + 10	,		

SR1

Decimals

Short-answer questions

1	a	0.2	b	0.13	C	1.7		
2	a	6 ones	b	$\frac{4}{1000}$				
3	а	18	b	18.4	C	18.40		
4	а	4.07	b	269.33	C	19.01	d	0.24
	e	0.09	f	60				
5	а	0.833	b	2.4	C	0.042		
6	а	4.5387	b	45.387	C	0.045 387		
7	а	36 490	b	0.018	C	3886		
8	a	$\frac{4}{5}$	b	1.1	C	$\frac{2}{3}$		
9	а	True	b	False	C	False		
	d	True	e	False	f	True		

Multiple-choice questions

1 C 2 C 3 D 4 A 5 A

Extended-response questions

1 a \$5.83 b \$5.85 c :	\$4.15
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Chapter 7

Warm-up quiz

1	а	11	b	5	C	7	d	22
	e	0	f	6	g	1	h	12
	i	1	j	8	k	9	L	13
2	а	<	b	<	C	<	d	>
	e	<	f	<	g	>	h	>
3	а	5°C	b	2°C	C	7°C		
4	а	30	b	77	C	72	d	39
5	а	5	b	11	C	9	d	7
6	а	7	b	5	C	7	d	16
7	A	(1,1), B(3,2), C	(2,	, 3)				
8	Pe	erimeter = 14 uni	ts					

7A _____

Now you try

Example 1

 $-3 -2 -1 \ 0 \ 1 \ 2 \ 3$ Example 2 a 5 > -2 b -4 < -1

Exercise 7A

1	а	1	b 0	C	-4	
	d	-1	e -18	f	-36	
2	а	-2,2	b 0,2	C	-7, -5 d -	-5, -3, 0
3	а	greater	b less	C	greater	
	d	less	e greater	f	less	
4	a	-2 -1 0	1 2	b	-5 -4 -3 -2 -	1 0 1
	C	-10-9 -8	>	d	-16 -15 -14 -	-13 -12
5	а	right	b left	C	left	
	d	right	e left	f	right	
6	а	-2	b -6		c 3	d 7
	e	15	f −21		g -132	h 1071
7	а	<	b >		C >	d <
	e	>	f <		g <	h >
	i	<	j >		k <	I >
	m	<	n >		0 >	p <
8	а	4°C	b −1°C		c −7°C	d −25°C

9 a $-\frac{1}{2}$ b $-1\frac{1}{3}$ or $-\frac{4}{3}$ c $-2\frac{2}{5}$ or $-\frac{12}{5}$ d $-13\frac{3}{4}$ or $-\frac{55}{4}$ 10 a False b False c False d True e False f False g True h False 11 a -2, -1, 0, 1, 2, 3, 4 b -7, -6, -5, -4, -3, -2, -1, 0c -2, -1, 0, 1 d -4, 2, 2 f -4, -3, -2, -1, 0f -9, -8, -7, -6, -5, -4 **e** -3, -2, -1, 0, 1, 2, 3 **12 a** -10, -6, -3, -1, 0, 2, 4 **b** -304, -142, -2, 0, 1, 71, 126 **b** −2, 0, 2 **13 a** 0, -1, -2 $\begin{array}{c} \textbf{c} & -5, -10, -15 \\ \textbf{e} & -79, -75, -71 \\ \textbf{k} \textbf{a} \ 4^\circ \textbf{C} \\ \textbf{b} \ 0^\circ \textbf{C} \\ \textbf{c} & -1 \\ \textbf{c} & -1 \\ \textbf{c} & -1 \\ \textbf{d} & -7 \\ \end{array}$ **14 a** 4°C **15 a** −2 7B ____ Now you try Example 3 **a** 2 **b** -11 **c** −17 Example 4 **a** −7 b −4 **c** −33 Example 5 **b** -14 **a** -6 Exercise 7B **b** -2 **1** a 1 **c** -9 **e** -4 f −8 d -1 2 a Right **b** Right **c** Left d Left b A сB 3 a D d C **c** 2 **b** 3 **d** 1 **4 a** 1 **e** -5 i -1 **m** -4 **5 a** -2 **d** -19 **e** −3 **h** -13 i -4 **m** -41 **c** 6 6 a 2 **b** -9 **d** -31 **g** -93 **e** -300 **f** -100 **h** -634 **b** -9 **d** -13 **7 a** 5 **c** 1 f -8 **g** −7 **h** −13 **e** 1 **k** −32 **i** 1 j −22 I -4 с 5 g 3 **d** 2 **8 a** 5 **b** 9 **e** 5 **f** 7 **h** 10 I -5 i 5 **j** 16 **k** −4 **o** -30 **m** -6 n -13 **p** -113 **9 a** \$145 **b** \$55 **c** \$5250 **c** −46°C **10 a** 3°C **b** −3°C **11** 69°C **12 a** 59 m **b** 56 m 13 Other combinations may be possible. a -, + **b** +, -, -**C** +, +, −, + **d** -, +, +, +, -14 Answers may vary. **a** 2 + 3 = 5 **b** Not possible **c** -2+3=1**d** -4 + 2 = -2f 2-4=-2**e** 7-5=2**h** -3 - 4 = -7g Not possible

634

Essential Mathematics for the Victorian Curriculum CORE Year 7

70	
Now you try Example 6	11
a 4 u Example 7	-11
-	-25
Exercise 7C	
1 a 2 d 11 2 b 6, -3	b 6 c 4 e 37 f 142 c -3, 1 d -11, -7
e -10,1 3 a C	f -2, -4 g -6, -3 h -26, -37 b A c D d B
4 a 1 e -3	b 5 c 6 d 2 f -5 g -2 h -4
i —3 m —10	j −22 k −35 l −80 n −29 o −50 p −112
q −109 5 a 5	r -113 b 7 c -12
d −7 6 a 4 d −8	e -15 f -42 b 9 c 0 e -7 f -10
g −1 7 a −3	h -17 i -33 h -10 c -4 d 4
e -1 i -1	f 4 g 5 h 5 j -2 k -2 l -14
8 \$190 of debt 9 a i \$8000	ii —\$6000
b \$2000 10 a False	b False
11 a False 12 a -2 0 5	b True b -13 -11 -6
8 1 -6 -3 2 4	<u>-3</u> <u>-10</u> <u>-17</u> <u>-14</u> <u>-9</u> <u>-7</u>
7D Now you try	
Example 8	
a 7 b Example 9	-6
-	-18
Exercise 7D	
1 a 3 d 11 2 a 3,5	b 6 c 4 e 15 f 312 b 6,−2 c −3,7
2 a 3,5 d -11,-7 g -7,-11	b 6, -2 c -3, 7 e -4, -2 f -1, -6 h -12, 27
3 a D 4 a 5	b A c B d C b 11 c 50 d 90
e -4 i 2 m 28	f -3 g -5 h -34 j 1 k 0 l 8 n 34 n -12

13 a False 14 a +,+		c 8 g -6 k 17 c -, - f +, -	d 12 h -91 I 11
	- ,		
Progress quiz 1 a < 2 a -1, -3, -5 c -11, -16, - 3 a 2 4 a -3 5 a 8 6 a 9 7 a 3 8 a 8 9 a 8 10 a 0 11 \$25 of debt (or	 b -4 b -9 b -13 b 11 b -4 b -5 b 27 b -24 	$\begin{array}{l} {\bf c} &> \\ {\bf b} &-3,0,3 \\ {\bf d} &-44,-33,- \\ {\bf c} &-7 \\ {\bf c} &-77 \\ {\bf c} &-10 \\ {\bf c} &-41 \\ {\bf c} &-7 \\ {\bf c} &22 \\ {\bf c} &-18 \\ {\bf c} &3 \end{array}$	d < -22 d 25 d -61 d -9 d 65 d -62 d -10 d 23 d 16
Example 11	10 c 11	8	
Exercise 7E			
e 1 f 2 C 3 3 B -5 g 4 a 7 b f -5 g g b f -5 l p 7 q g 5 a 4 -13 e 19 7 a 20 L 8 a 4 -4 g -5 9 No, 20 10 a 5	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	h -7 3 d -11 8 i -6 9 n 5 6 c 28 g -6 k 40 c 20 g -14 c 110 L	e -1 j 6 o 8 d 3 h 1 I 5 d 3 h 11 c 3 f -1 i -6
7F Now you try			

A(4, 3), *B*(2, -2), *C*(-2, 0), *D*(-1, 4)

Answers

n 34

o -12

c 3

f −5

c −2

f -14

i 1

c -4

f −24

i 2

I -6

b 11

e −5

b 1

e -7

h −3

b -5

e 2

h -5

k −9

m 28

d 4

 $\boldsymbol{d} \ -6$

g 6

d 4

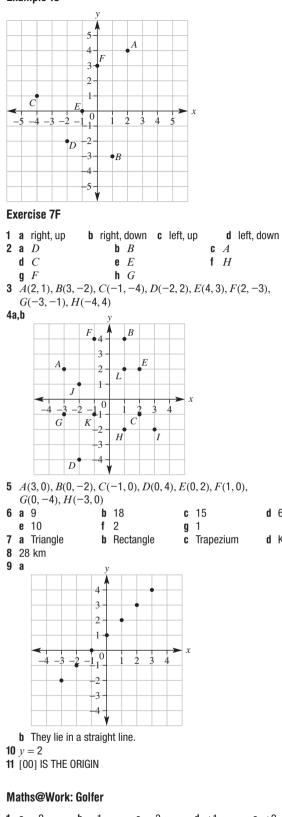
g -6

j -6

7 a -1

6 a −2

5 a 8



1	a -2	b -1	C —3	d +	⊦1	e +2	
2	a -7	b -20	c -5	d 0	e +3	f +	-2

	Final score	under/over par
Chelsea	78	+6
Mitchell	82	+10
Adam	70	-2
Bella	75	+3

la				under/		under/
			Rick's	over par	Brad's	over par
	hole	PAR	score	for Rick	score	for Brad
	1	4	4	0	5	1
	2	4	4	0	5	1
	3	4	4	0	5	1
	4	4	4	0	5	1
	5	4	6	2	4	0
	6	4	5	1	4	0
	7	3	5	2	4	1
	8	5	2	-3	6	1
	9	3	3	0	4	1
	10	4	3	-1	5	1
	11	5	4	-1	5	0
	12	4	3	-1	5	1
	13	4	3	-1	3	-1
	14	5	5	0	6	1
	15	3	3	0	4	1
	16	4	5	1	5	1
	17	5	4	-1	6	1
	18	3	3	0	4	1
	TOTALS	72	70	-2	85	13

b Rick 73 and Brad 78

c Rick won by 5 points

d Rick's average 3.89, Brad's average 4.72

e Rick 5 birdies, Brad 1 birdie

5

d 6

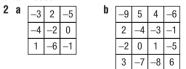
~

d Kite

X	У
-30	-40
-45	40
-40	45
0	40
5	35
50	20
45	15
-30	25
-30	20
0	0
10	0
45	-40
45	-45
-20	-25
	$\begin{array}{c} -30 \\ -45 \\ -40 \\ 0 \\ 5 \\ 50 \\ 45 \\ -30 \\ -30 \\ 0 \\ 10 \\ 45 \\ 45 \\ 45 \end{array}$

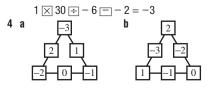
Puzzles and games

1 a House



3 a $-3 \times (4 + -2) = -6$ **b** $-2 \times 5 \times -1 + 11 = 21$ or $-2 \times 5 \div -1 + 11 = 21$

c $(1 = 30 \div - 6) \div - 2 = -3$ or



C	-14	0	-1	-11
	-3	-9	-8	-6
	-7	-5	-4	-10
	-2	-12	-13	1



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3

Essential Mathematics for the Victorian Curriculum CORE Year 7

	a -81, 243, c -10, -15 a 11 and -3	, –21	b 4, -2, 1 d -8, -13, b 21 and -1		
SI	hort-answer	questions			
1 2 3 4 5 6 7 8 9	a $-3, 0$ a $<$ a -5 e -1 i -11 a 1 e -2 i 7 a -6 e -6 a -1 e -21 a 4 e 30 a 4 e 10 i -15 A(3, 0), B(2, -1)	b 1, -2 b $<$ b -2 f 2 j -7 b 3 f -5 j -17 b 5 f -6 b -9 f -2 b -5 f 10 b -4 f 2 j 18 3), $C(-1, 2), D(-1)$	c $-6, -2$ c > c -15 g -7 k -47 c -3 g 12 k 3 c -11 g 5 c -1 g -87 c -3 g 1 c 6 g 0 k -5 (-4, -2), $E(0, -1)$	d $-1, -11$ d $<$ d 1 h -25 l -131 d -7 h -18 l 3 d 5 h -29 d 2 h 30 d 7 h 40 d -10 h 13 l 16 -3), $F(4, -4)$	
	ultiple-choic				
1 6	C 2 A 7		4 D 9 C	5 C 10 C	
1 2	a 16°C Rocket	onse questions b –31°C	c 8°C	d 19°C	e 27°C
w	'arm-up quiz				
1 2 3 4 5 6 7	a $15^{\circ}C$ a $\frac{1}{2}$ a 26 a C a 6 a 0.5 C, A, B, D a L	 b 24°C b 2/3 b 7 b 1 b 2 b 0.4 b H 	c 21°C c $\frac{3}{4}$ c 2,4,5,6,9 c C c 0.2 c M	dl	
8/	A				
Ex a Ex	kample 2	b Discrete r ta source			numerical
E	kercise 8A				
2		b C b sample iv c i	cC cprimary dv e	d N d secondar e vi f ii	

d Categorical

f Numerical

d Categorical

f Categorical

b Continuous numerical

- **q** Discrete numerical
- Continuous numerical i
- k Continuous numerical
- m Continuous numerical
- o Categorical
- **q** Discrete numerical
- a Primary
- **b** Primary

6

- c Secondary
- d Secondary
- 7 Answers will vary.
- 8 a Observation
 - **b** Sample of days using observation or secondary source records

h Discrete numerical

i

Continuous numerical

Discrete numerical

n Discrete numerical

p Discrete numerical

r Categorical

- within each day c Census of the class
- d Sample
- Sample e
- Sample using secondary source data f
- g Census (this question appears on the population census)
- h Census of the class
- i Sample
- Results from the population census
- Observation k
- I Observation
- m Sample
- n Sample

- 9 a Proximity to the Indian Ocean makes first hand collection of the data difficult.
 - **b** Too many people to ask and a sensitive topic means that using the census results as your source would be better.
 - c Extremely large population makes primary data difficult to collect. Sensitive topic might make students less keen to give d
 - honest and reliable answers.
 - e Cultural issues and the different cultural groups that exist in the community makes collection difficult.
- 10 The data is often collected by a market research company. It is not always possible to know how the data is collected, the areas it is collected from and whether there was a bias introduced in the surveys.
- **11 a** Population is the entire group of people but a sample is a selection from within it.
 - b If the population is small enough (e.g. a class) or there is enough time/money to survey the entire population (e.g. national census).
 - **c** When it is too expensive or difficult to survey the whole population, e.g. television viewing habits of all of NSW.
- 12 a The answers stand for different categories and are not treated as numbers. They could have been A–E rather than 1–5.
 - **b** i 1 = strongly disagree, 2 = somewhat disagree,
 - 3 = somewhat agree, 4 = strongly agree.
 - ii 1 = poor, 2 = satisfactory, 3 = strong, 4 = excellent.
 - iii 1 = never, 2 = rarely, 3 = sometimes, 4 = usually,
 - 5 = always.
 - iv 1 =strongly disagree, 2 =disagree, 3 =neutral,
 - 4 = agree, 5 = strongly agree.
- 13 a Too expensive and people might refuse to respond if it came too often.
 - b English as a second language can impact the collection of data (simple, unambiguous English is required). Some people from particular cultures may not be keen to share information about themselves.
 - c Some people cannot access digital technologies and they would be excluded from the results.
 - d Larger populations and a greater proportion of people in poverty can make census data harder to obtain.

8B Now you try Example 3 a 27 **b** 19 **c** 16 **d** 13

c Numerical

e Numerical

e Categorical

5 a Discrete numerical

c Continuous numerical

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8A

16

Exercise 8B

1	٦,	2, 3, 7, 8											
2	а	8	b	35									
3	а	median	b	mea	an		C	range		d	mode		
4	а	1, 2, 3, 5, 10	b	10			C	1	d	9			
5	а	30	b	5			C	6					
6	а	median	b	9									
7	а	mode	b	2									
8	а	9	b	12			C	9		d	7		
9	а	10	b	8	(c 3		d 7		e	15	f	56
10	а	12	b	9			C	7		d	6		
11	а	Mean $=$ 3, n	۱od	e = '	1		b	Mean	= 7	, moo	de = 2		
	C	Mean $= 12$,	mo	de =	11		d	Mean	= 2	6, ma	de = 25		
	e	Mean = 16,	mo	de =	10		f	Mean	= 3	4, mo	de = 55		
12	а	Brent	b	Bre	nt		C	Ali		d	Brent		
13	а	16.6	b	17.	5		C	12					
14	а	7	b	42									
15	а	2 b 12	C	24	d 2	e	0	saves	f	Ansv	vers will va	ry.	

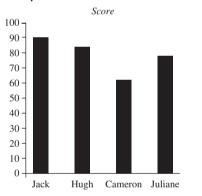


Now you try

Example 5

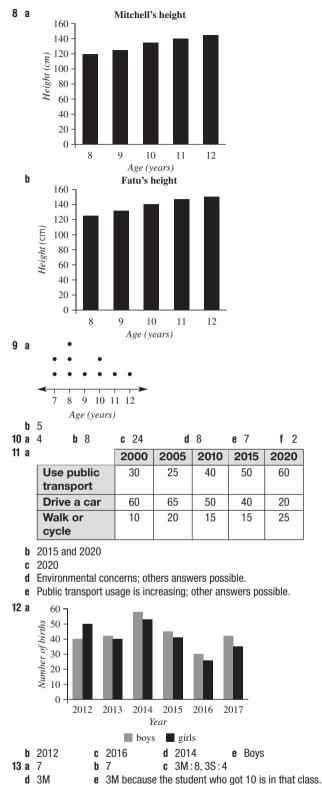
a 3 fish b 15 fish c 9 d 3 fish e 9 fish f 2 fish

Example 6



Exercise 8C

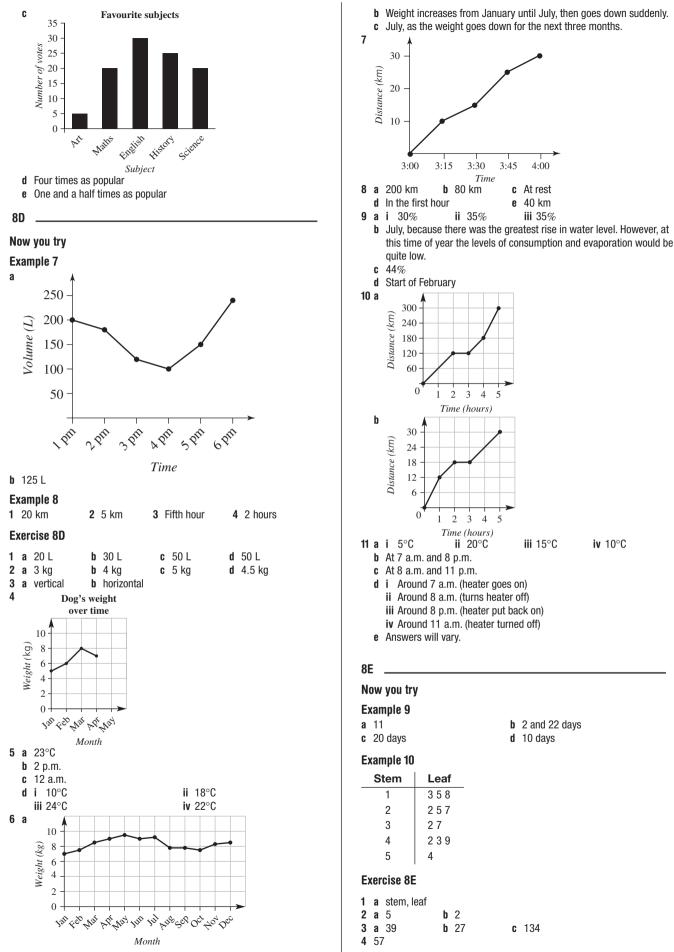
1 2 3	a	dot plot True	b	b col False		gr	aph c True	c outlier d True	e False
5		-	b	b 3 b 7 10 cm	1	C	c Sport c Red 35 cm d	d 20 d 27 11 years old	
		•		•	•		• • •		
		Sedans		agon s <i>in a c</i>	Ute: ar pa		SUVs		



14 a It is unequal.

b The axes have no labels and it does not have a title.

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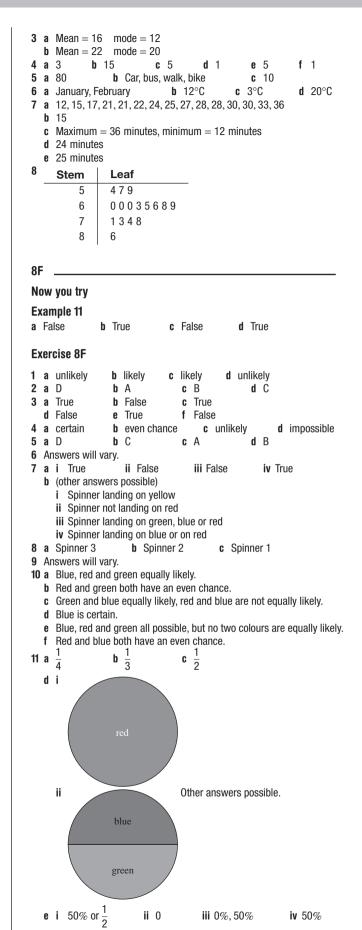
Answers

8D

5 a b	8, 9, 10, 11, 10	13, 15, 17, 18, 21	, 24		
C	i False	ii True	iii	True	iv False
6 a	Range $= 20$	median $= 17$			
		median $= 26$			
C	Range $= 19$	median $= 40.5$			
7	Stem	Leaf			
	2	579			
	3	029			
	4	125			
	5	1			
	3 2 r	means 32			
8 a	Stem	Leaf			
	1	1234457			
	2	0489			
	3	1235			
	2	4 means 24			
b	Stem	Leaf			
	1	124			
	2	79			
	3	2788			
	6	0 0			
	7	38			
	8	17			
	2 9 mean	s 29			
9 a	Stem	Leaf			
	8	0456	_		
	9	0 6			
	10	145			
	11	034459			
	10 4 mea	ns 104			
b	Stem	Leaf			
	39	156			
	40	1245668	9		
	41	1233567	8		
	42	0			
	41 3 mea	ns 413			
10 a	10	b 1	c 8		d 58
11 a	15	b 13			
C 12 o		o is 0, c is 8 or 9, a			
12 a b	i 49 years Radio statio	n 1	ii	36 years	
U C	i 33 to 53		ii	12 to 32 y	vears
5		,			
D					

Progress quiz

1	а	6	b	13	C	12	d	16
2	а	16	b	28				



Essential Mathematics for the Victorian Curriculum CORE Year 7

8G _

Now you try

Example 12 a $\{1, 2, 3, 4, 5, 6\}$ b $\{1, 3, 5\}$ c $Pr(odd) = \frac{1}{2}$ d $Pr(5) = \frac{1}{6}$

Exercise 8G

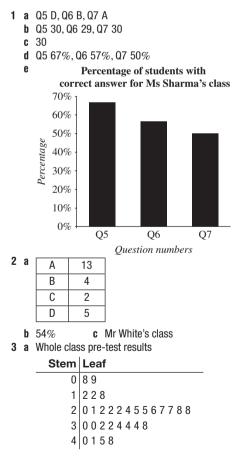
1 a sample space c certain **b** zero e impossible f less d more **b** 50% **2** a 0.5 **d** B **3** a C b A c D **b** $\frac{1}{3}$ $c \frac{1}{3}$ 4 a 3: red, green, blue d $\frac{2}{3}$ **e** 0 **b** $\frac{1}{7}$ **5** a {1, 2, 3, 4, 5, 6, 7} **c** 0 d $\frac{2}{7}$ $e \frac{3}{7}$ $f \frac{4}{7}$ g Number chosen is less than 8; other solutions possible. **6 a** {M, A, T, H, S} **b** 0.2 **7 a** $\frac{1}{11}$ **b** $\frac{2}{11}$ **c** $\frac{5}{11}$ **c** 0.2 **d** 0.8 d $\frac{9}{11}$ $e \frac{4}{11}$ 7 a ⁻/₁₁ f Choosing a letter in the word TRY; other solutions possible. 8 D 9 a 30% 10 a Yes, $\frac{19}{210}$ **b** 50% **c** 80% **b** 210 **c** 840 **11 a** $\{2, 3, 4, 5, 6, 7, 8, 9\}$ **b** 0.5 **c i** 0.375 **ii** 0.375 iii O d Possible spinner shown: 2 5 31 12 a 6 bi red green ii Cannot be done because adds to more than 1. iii Cannot be done because adds to less than 1. iv red green 8H _ Now you try Example 13 **b** $\frac{5}{8}$ $a \frac{1}{4}$

a 25 b Rolling a 4, 8 times Exercise 8H 1 C 2 a 4 b 6 c 10 2 a ¹ b ² a ³

Example 14

3 a $\frac{1}{10}$	b =		$\frac{3}{10}$		
10	5		10		
4 a $\frac{53}{100}$	b $\frac{4}{1}$	$\frac{47}{00}$	c No		
5 a $\frac{13}{20}$	b $\frac{1}{4}$		c <u>1</u> 10		
6 a 50					
b i $\frac{2}{5}$	i	$\frac{1}{10}$	iii $\frac{1}{2}$		
7 a 500					
b 1750	0				
ci 7		More			
8 a 100			is is verv unlike	ely) d From 2 rolls	
9 a i $\frac{1}{4}$	i	$\frac{3}{100}$	iii <u>31</u> 100		
b 60					
10 a 5	b 40	c 70	d $\frac{26}{35}$	$e \frac{1}{2}$ f 126	i
11 a 2 re	d, 3 green and	d 5 blue			
b i Ye	es ii	Yes	iii Yes		
iv Y					
12 a C	b C		с В	d A	
	rs will vary.				
	o win vary.				

Maths@Work: Teachers



d A

c Yes, but unlikely?

Answers

b	Girl's pre-test results
---	-------------------------

Stem	Leaf	Stem	Leaf
0	9	 1	8
1	2 2		2237
2	022258	3	244589
3	0244	4	2467
4	58		

Girl's post-test results

c The girls have improved their results. Many correct answers. E.g.

Girls: pre-test	Girls: post-test
3 under 20	1 under 20
4 in the 30s	6 in the 30s
2 in the 40s	4 in the 40s

- **d** i 8,18
- **ii** 7,5
- iii Pre-test: 40, 41; post-test: 43, 44, 45, 46 iv The boys have improved their results. Many correct answers. E.g.

Boys: pre-test	Boys: post-test
2 under 20	1 under 20
4 in the 30s	5 in the 30s
2 in the 40s	4 in the 40s

4 See table at bottom of page.

Puzzles and games

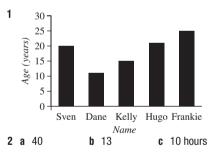
- 1 Andrew is 11, Brett is 15, Chris is 16
- 2 24 ways
- **3** 2, 2, 5, 7, 8, 12 4

No. of cars	0	1	2	3
No. of students	4	6	8	2

- 5 6 coins
- 6 19 more ways (21 in total)

7 12 blue, 8 green, 4 red

Short-answer questions



d 18 15 No. of students 12 9 6 3 0 9 10 12 8 11 TV watched (hours) **3 a** 4 students **b** 2 students d 6 students **c** 1 p.m. e The number of students must be a whole number. Joining the dots would include fractions for the number of students. **d** 26 g **4 a** 118 g **b** 105 g **c** 131 g 5 a 11 **b** 5 **c** 3.5 **d** 2 6 a 12 **b** 5 **c** 3.5 **d** 3 c $\frac{19}{20}$ d $\frac{3}{4}$ 1 **e** 0 **7 a** 1 b 8 **8** a {1, 2, 3, 4, 5, 6} **b** {heads, tails} $\boldsymbol{c} \hspace{0.2cm} \{D, E, S, I, G, N\}$ d {blue, yellow, green} **9** a 9 5 ii $\frac{1}{3}$ iv $\frac{4}{9}$ b i iii O <u>9</u> **b** 50% **10 a** 42% 1 $\frac{1}{4}$ 11 a b **c** 25 **d** 250 $\overline{2}$ **Multiple-choice questions** 1 D **2** D **3** B **4** B 5 A 6 A 7 C 8 D **9** C **10** B **Extended-response questions** 1 -

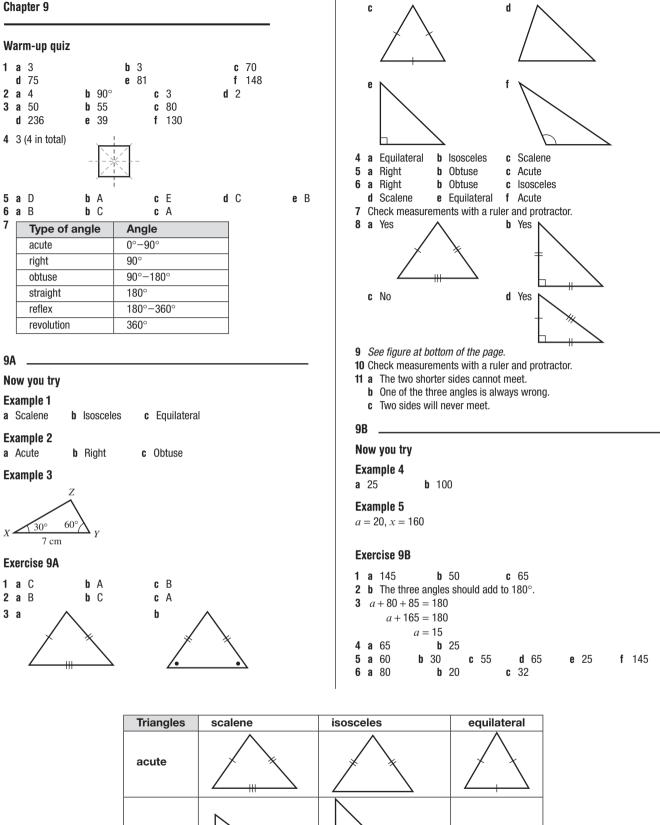
1	а	12			
		12- 3-10			
		(ip 10		*	
		ainy 8	*		
		No. of rainy days	$ \land $		
		°, ⁴] ↓	'\ /		
		2			
		0+			
		Jan Foo Mar	APINAS JUN JULA	36 50 00 40 Dec	
			Month		
	h	66 c	$\frac{6}{92} = \frac{3}{46}$		
			92 46		
2	а	40			
	b	Cheesecake			
	C	$\frac{7}{40}$			
			:: No		tu Ma
	d	i Yes	ii No	iii Yes	iv No
	e	80			

Mrs Best's year 7 maths class											
Test	Term 1 Ter		rm 2 Mental Arithmetic			Term 3		Term 4		Averages	
Total marks	22	%	19	%	10	%	34	%	26	%	
Oscar	20	91%	18	95%	10	100%	32	94%	23	88%	94%
Molly	17	77%	16	84%	9	90%	29	85%	22	85%	84%
Blake	14	64%	12	63%	5	50%	16	47%	16	62 %	57%
Angus	19	86%	19	100%	8	80%	33	97%	23	88%	90%
Bhavin	17	77%	14	74%	7	70%	26	76%	18	69 %	73%
Scarlett	14	64%	11	58%	6	60%	24	71%	19	73%	65%
Vedika	18	82 %	16	84%	8	80%	31	91%	24	92%	86 %
Class averages	17.0	77%	15.1	80%	7.6	76%	27.3	80%	20.7	80%	79 %

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Essential Mathematics for the Victorian Curriculum CORE Year 7

Chapter 9



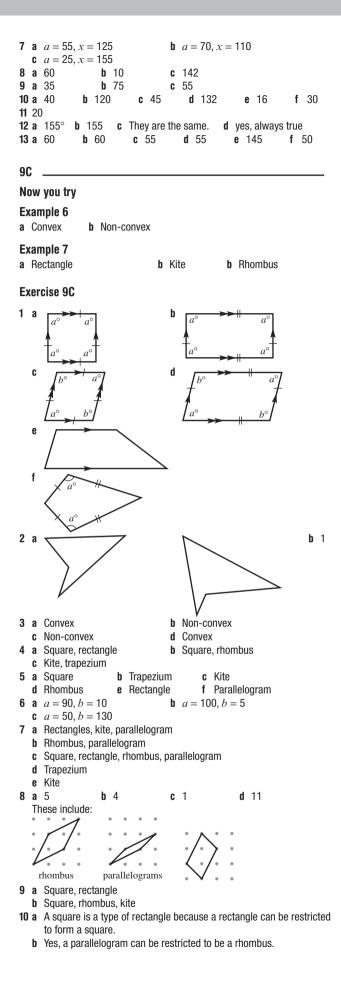
9A

Answers

Essential Mathematics for the Victorian Curriculum CORE Year 7

right

obtuse



C	Yes, a parallelogram is a trapezium where the second pair of sides
	are parallel.

d No, there needs to be a pair of parallel sides.

11 Forming a square is possible.

9D _

Now you try

Example 8

a 110 **b** 35

Example 9

x = 95, *a* = 85

Example 10

a = 240 *b* = 45, *c* = 135

Exercise 9D

	Ar	-	ry,			ngles should be very close to 360°.
3					of ai	ngles should be very close to 360°.
4	а	145	b	265	C	170
5	а	130	b	90	C	230
	d	215	e	120	f	22
6	а	<i>x</i> = 80, <i>a</i> =	100)	b	<i>x</i> = 70, <i>a</i> = 110
	C	<i>x</i> = 60, <i>a</i> =	120	C		
7	а	<i>a</i> = 80, <i>b</i> =	90		b	<i>a</i> = 20, <i>b</i> = 10
	C	<i>a</i> = 120, <i>b</i> =	= 15	55	d	<i>a</i> = 90, <i>b</i> = 35
	e	<i>a</i> = 265, <i>b</i> =	= 4()	f	<i>a</i> = 270, <i>b</i> = 35
8	а	Possible	b	Impossible	C	Impossible
	d	Possible	e	Impossible		
9	а	<i>a</i> = 90	b	<i>a</i> = 50, <i>b</i> =	130) c <i>a</i> = 131
10	а	100	b	70	C	77.5
11	а	130	b	110	C	150
	d	60	e	115	f	108

Progress quiz

1	а	Isosceles	b	Acute
2	а	Equilateral	b	Obtuse
3	а	80	b	56
4	а	160	b	48
5	а	Kite	b	Rhombus
6	а	168	b	120
7	а	75	b	106
8	а	= 230, <i>b</i> = 1	2	

9E ____

Now you try

Example 11

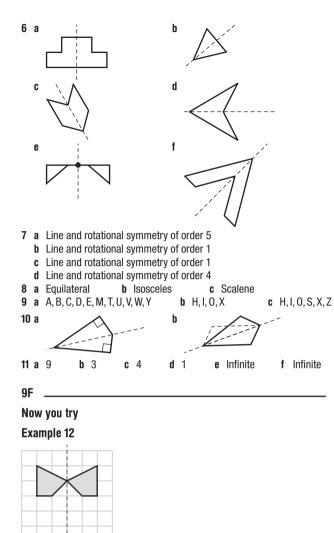
a 0 and 1 (no rotational symmetry)

Exercise 9E

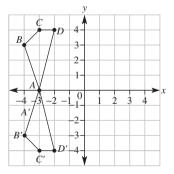
1	а	Yes	b	Yes	C	No
	d	No	e	No	f	Yes
2	а	4 ways	b	2 ways	C	3 ways
	d	1 way	e	2 ways	f	0 ways
3	а	4	b	2	C	3
	d	1	е	2	f	2
4	а	4 and 4	b	2 and 2	C	2 and 2
	d	1 and 1	e	1 and 1	f	0 and 2
	g	0 and 2	h	4 and 4	i	1 and 1
5	a	i Kite			ii	Rectangle, rhombus
		iii None			i۱	/ Square
	b	i Trapeziur	n, k	ite	ii	Rectangle, rhombus, parallelogram
		iii None	-		i۱	/ Square
						•

b 0 and 2

9F

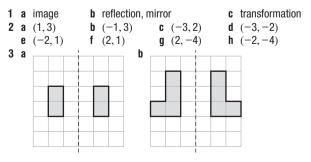


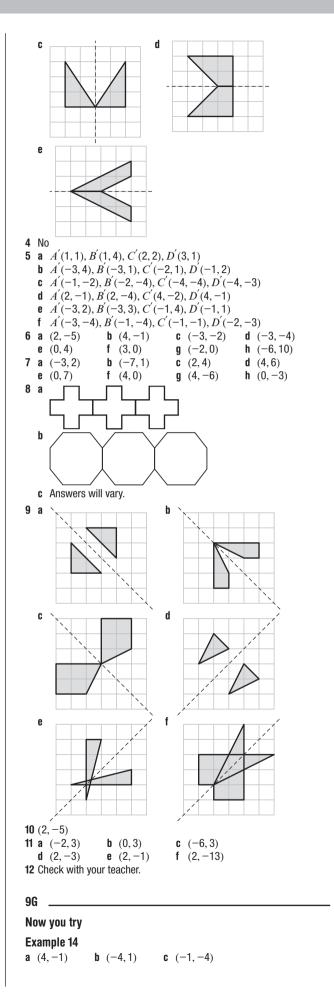
Example 13

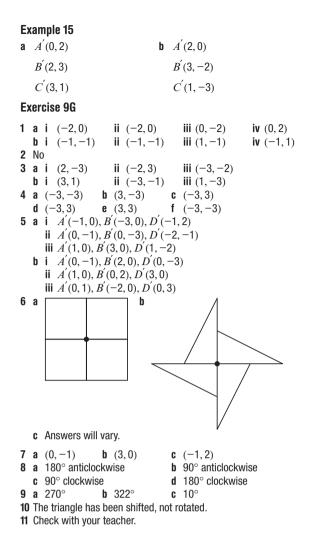




Exercise 9F









Now you try

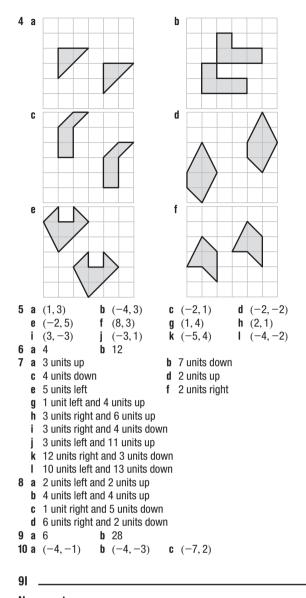
	•				
		А			F
		В			
A'			С		
		\mathbf{F}'	D	Е	
\mathbf{B}'	\mathbf{C}'				
	\mathbf{D}'	\mathbf{E}'			

Example 17

Translation 5 right and 5 down.

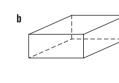
Exercise 9H

1	a	7 units						
	b	3 units						
	C	i 7 units		ii 3 units				
2	а	up	b	left	C	down	d	up
	e	left	f	left	g	right	h	right
3	а	(4, 2)	b	(1, 2)	C	(3, 5)	d	(3, 1)
	e	(2, 4)	f	(0,1)	g	(5,1)	h	(3,0)



Now you try

Example 18 а



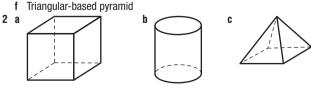
Example 19





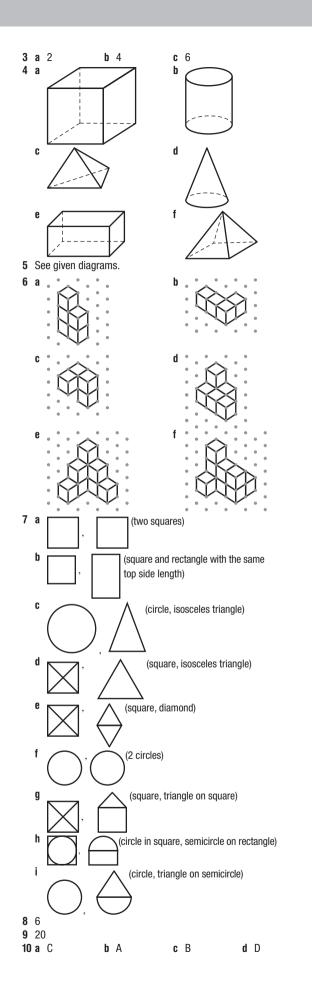
Exercise 9I

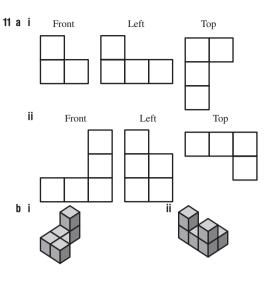
- 1 a Cube **b** Rectangular prism c Cylinder d Cone e Square-based pyramid
 - Triangular-based pyramid



Essential Mathematics for the Victorian Curriculum CORE Year 7

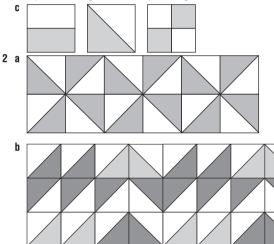






Maths@Work: Quilting

1 a Two equal sides; angles are 90° , 45° , 45° ; has one axis of symmetry **b** Square; rectangle; rhombus; parallelogram; kite

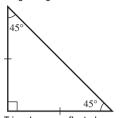


CH9

- **3 a i** Reflection over a line of symmetry or 180° rotation around the centre of the star
 - ii Rotation around the centre of the star or reflection over connecting sides
 - iii Rotation around the centre or reflection over a connecting side **b** i Translation ii Rotation
 - iii Reflection then translation (or the reverse order)
- ii Rotational symmetry of order 4 4 a i 4 lines of symmetry
 - iii Reflection over lines of symmetry, translation and rotation around the centre
 - **b** i 8 lines of symmetry ii Rotational symmetry of order 8 iii Reflected over lines of symmetry, reflection over connecting sides and rotation around the centre

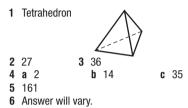
5 a Hexagon interior angles =
$$120^{\circ}$$
, $\frac{360}{120}$ = 3, a whole number
Pentagon interior angles = 108° , $\frac{360}{108}$ = 3.3, not a whole number.

b i A right-angled isosceles triangle

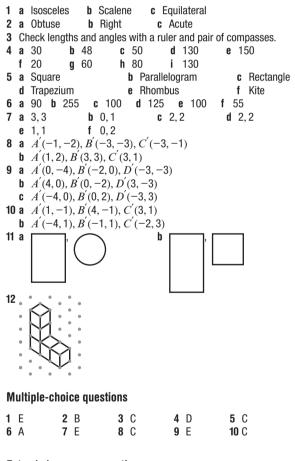


- ii Triangles are reflected over their connecting sides and rotated about the centre.
- 6 Answers will vary

Puzzles and games

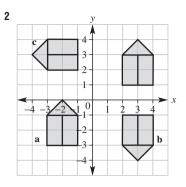


Short-answer questions



Extended-response questions

1 a 150 **b** 120



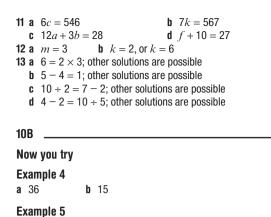
Chapter 10

Warm-up quiz

2 a 3 a 4 a 5 a 6 a	12 7 False 7 3 C	b 2 b 7 b 2 b 2	15 20 True 5 27 A		C C C C C	16 16 Tru 15 2 B	е		d	False	
7 a	n		1	2		3		4		5	
	$5 \times n$		5	10		15		20)	25	
b	n	2		4	6		8		10)	
	<i>n</i> – 2	0)	2	4		6		8		
C		1	2		5		8		9		
	2 <i>n</i>	2	4		10		16		18		
	D		В			С			d		
	27 17		40 14		C	18			d	26	
-	Mia is 17 an	-		20.	g b	6 \$28	8				
10A											
Now	you try										
Exam False											
Exam a Fal	-	Tru	е								
Exam a 3y	ple 3 = 36	b	4 <i>d</i> =	3.2			C	x –	- 7 =	34	
Exerc	ise 10A										
1 a 2 a 3 a 4 9	True True 9	b I b	True False 15			Fal Fal 2			d d		
6 a d 9 7 a 8 a 9 a	True True False True False 19 True 3 + x = 10	b e l h l b	False True False False True 19 True	b 5/	f i c c	Fal Fal Tru Fal Tru Fal 100	se e se e se			True True c <i>a</i> +	<i>b</i> = 1
	2 <i>d</i> = 78				x =						= 21

22

Essential Mathematics for the Victorian Curriculum CORE Year 7

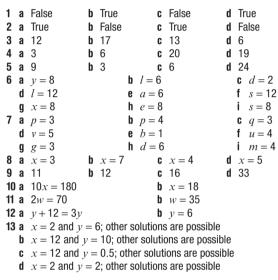


c 8

a 31

b 12

Exercise 10B



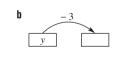
100 _

Now you try

Example 6

4y

a v



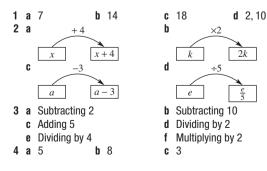
c = 32

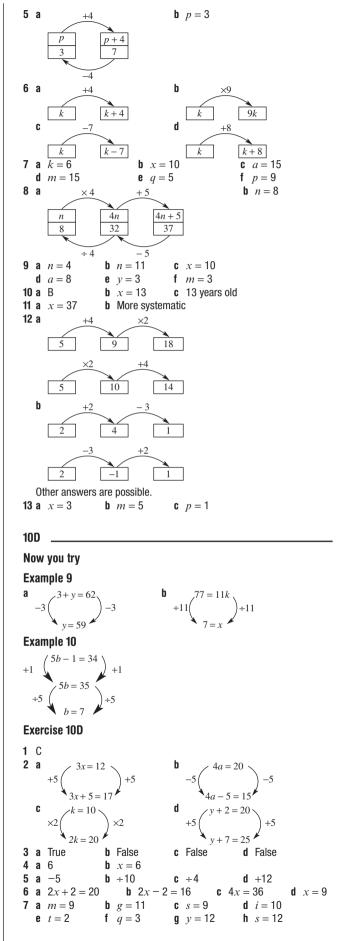
Example 8

Example 7

x = 9

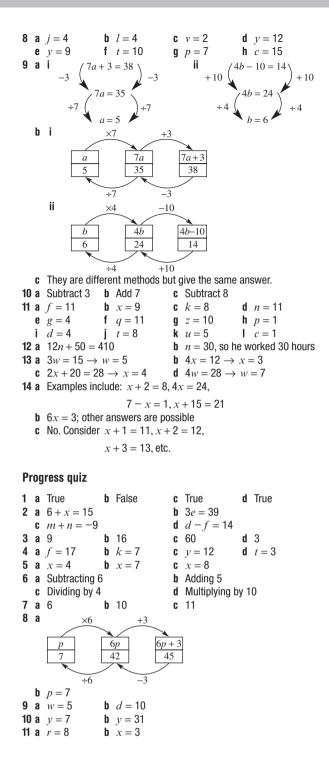
Exercise 10C





Answers

10C



10E ____

Now you try

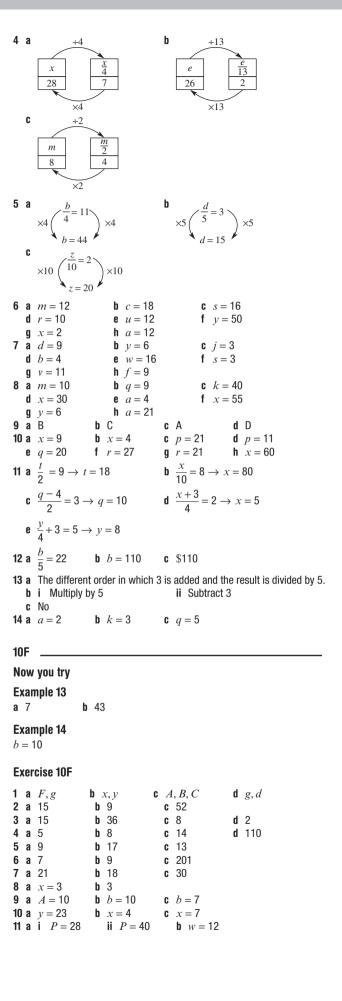
Example 11 x = 90

Example 12

a a = 10 **b** b = 12

Exercise 10E

1	а	True	b	False	C	;	True	d	False
2	а	True	b	False	C	;	False	d	True
3	а	Dividing by 4			b)	Adding 2		
	C	Multiplying b	у 7	,	Ċ	I	Subtracting 1	11	



650

Essential Mathematics for the Victorian Curriculum CORE Year 7

Essential Mathematics for the Victorian Curriculum CORE Year 7

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a 15 mm or 1.5 cm **a** 1.7 cm or 17 mm

12 a $A = 35$ b $20 = w \times 4 \rightarrow w = 5$ c i $25 = 5h \rightarrow h = 5$ 13 a $F = 68$ b $C = 10$	ii Square c 73°F d 36°C	e 15°C
10G		
Now you try		
Example 15		
a Let $n =$ number of hours worke	d.	

Exercise 10G 1 a D b A c E d B e C 2 a x = 6 b a = 2 c k = 9 3 D 4 a 7k = 42 b k = 6 5 a Let p = cost of one pen b 12p = 18 c p = 1.5 d \$1.50 6 a Let t = cost of a car tyre b k = 0 5 240 b k = 0 5210 k = 0

- 6 a Let $t = \cot of$ a car tyre c t = 3107 a Let $h = \operatorname{number}$ of hours worked c h = 34c h = 34d hours 8 a 24w = 720b w = 30c m d m g $2x + 3 = 31 \rightarrow x = 14$ 10 a x = 4b 17h + 65 = 643c m d m hours b 17h + 65 = 643c m hours c m hours c m hours c m hours c c c c c c c m hours c
- 14 years old **12 a** Both equal 18.

b 30n + 100 = 730**c** n = 21

d 21 hours

- **b** Examples: l = 4 and w = 4, l = 12 and w = 2.4
- **c** Yes, if the width equals 4.

Maths@Work: Uber fares

1	b 34.14 km c 48 minute	es	23.90 iii \$	50.90	
	f Formula f a \$77.32	b 1.81 nutes CT fare = 4 are = \$8.70 b \$35.3	km c $\$265$ + $0.55t + 1.8n$ but the UberSE 84 c 9.61	LECT minimum km	fare is \$10.
5	d UberBLAC Answers ma <i>See table at</i> uzzles and g	y vary. bottom of p	+ 0.68 <i>t</i> + 2.04 <i>i</i> age.	1	
2 3 4 5 6	a 26 7 and 13 Divide by 2 30 A CORNY JO 26 sheep, 15	5 ducks	c 368	d 31 $\frac{1}{3}$	e 36
- 7	a $M = 2n$	+1	b 201		

8 8 and 13

Short-answer questions

1 a False	b True c	True	
d Faise 2 a 2 + <i>u</i> = 22	e True f b $5k = 41$	False c $3z = 36$	3
d <i>a</i> + 12 = 15			
3 a x = 3 d y = 9	b $x = 6$ c e $a = 2$ f	y = 1 a = 10	
4 a <i>x</i> = 5	b $q = 6$ c	<i>a</i> = 21 d	
e k = 10 5 a x = 3	b $r = 45$ c	$b = 5 \qquad \mathbf{II}$ $x = 9$	<i>r</i> = 2
d $r=4$	e $q = 2$ f	<i>u</i> = 8	
6 a $u = 24$ d $y = 40$			
7 a No 8 a <i>A</i> = 450	b LHS = 16, RHS =	= 16 : solution	
b <i>l</i> = 8			
c w = 5, l = 8; 9 a 36	other solutions are	e possible 3	
10 a 5	b 25 c	20 d	5
Multiple-choice q			
1 D 2 C 6 E 7 C	3 A 8 B	4 D 5 9 A 10	A
Extended-respon	se questions		
1 a \$120	b B	10	c \$60
d 7 hours2 a 75 cents	e 252 b \$1.	2 = 12 <i>n</i> 35	c t = 12
d 12 seconds		seconds	f \$1.50
Chapter 11			
Warm-up quiz			
1 a E	b C c	B d	A and D
1 a E 2 a 7.5 cm	b 13 cm c	2 cm	A and D
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10	b 13 cm c b C, A, B, D c b 100 c	2 cm	
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60	b 13 cm c b C, A, B, D c b 100 c f 1000 c	2 cm C, E, A, D, B 1000 d	60
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180	b 13 cm c b C, A, B, D c b 100 c f 1000 c b 2 c f 7200 g	2 cm C, E, A, D, B 1000 d 56 d 1.4 h	
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180 6 a 55 m	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 7000 g b 27 cm c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm	60 2500
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 7000 g b 27 cm c b 77 cm c b 7 c b 6 c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 8	60 2500 0.027
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 7000 g b 27 cm c b 77 c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 8	60 2500 0.027
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 7000 g b 27 cm c b 77 cm c b 7 c b 6 c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 8	60 2500 0.027
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16 9 a B	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 7000 g b 27 cm c b 77 cm c b 7 c b 6 c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 8	60 2500 0.027
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16 9 a B	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 7000 g b 27 cm c b 77 cm c b 7 c b 6 c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 8	60 2500 0.027
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16 9 a B 11A	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 2000 g b 27 cm c b 7 c b 6 c b C c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 8	60 2500 0.027
1 a E 2 a 7.5 cm 3 a D, A, C, B 4 a 10 e 60 5 5 a 2000 e 180 6 a 55 m 7 a 32 8 a 16 9 a B 11A	b 13 cm c b C, A, B, D c b 100 c f 1000 c f 2000 g b 27 cm c b 7 c b 6 c b C c	2 cm C, E, A, D, B 1000 d 56 d 1.4 h 28 cm 8 D d	60 2500 0.027

Uber level	Pickup place	Destination	Fare
UberX	Burke and Wills Hotel, Toowoomba, Qld	Byron Bay, NSW	\$333.00
UberX	Melbourne Airport, Vic	Mornington Peninsula, Vic	\$139.80
UberXL	Brisbane Airport, Qld	Surfers Paradise, Gold Coast, Qld	\$177.30
UberXL	Perth Airport, WA	Margaret River, WA	\$562.80
UberBLACK	Napier Street, Adelaide SA	Adelaide Airport, SA	\$34.10
UberASSIST	Canberra Airport, ACT	Goulburn, NSW	\$158.50

Answers

a 60 mm **a** 410 cm

Example 4

a 0.46 m **a** 4.321 km

Exercise 11A

1	м	illimetre, cent	ime	otro	motro ki	lom	otro				
2		100		100			divide	Ь	multiply	,	
3		Right		Left	-	U	uiviuc	u	munipiy	/	
4	a a				imetres	•	Motros				
4	a d	Metres			timetres	-		~~~~			
5	-	2 cm					1.5 cm		3.2 cm		
J	a e		f	3 ci		q			2.8 cm		
6	e a		'		200 cm	y		3500 r			
0	a d	2610 cm			200 cm		-	53 mm			
	-	620 cm			200 mm			684 cn	-		
	g i	20 m			200 mm			670 cn			
7		20 m 4 cm			5 m	1	•	4.2 km			
'		4 cm 47.2 cm			3.6 m		-	4.2 KII 3.2 cm			
		50 km		-	27 km			36.2 Cli			
	•	0.04 cm			926.1 ci	~		4.23 k			
0	j	Metres			Millimet			4.23 K Kilome			
0		Kilometres			Centime		-				
9		2.5 cm	h	82 I			2.5 m		730 cm		
9	a e	6200 m	ม f		732 km	U	2.5 11	u	750 01	I	
10		8.5 km	•	310		•	19 cm				
		2.7 m		0.4	••••	U	19 011				
		38 cm, 0.5 n				h	160 cm	2100 r	nm 0.03) kr	n 25 m
12		142 mm, 20						,21001	1111, 0.02	- 1	II, 23 III
		10 mm, 0.1 i									
13		25 cm	п,	0.00	1 KIII, 10	00	GIII				
		\$8200	h	\$6	56	ſ	\$4.10				
) 000 years	n	ψ0.,	50	U	ψτ.10				
		3000 mm		h	600 000	cn	n c	2400 r	nm		
10		4000 cm			0.47 km		f				
	q	0.216 km			0.0005		•	2 m			
17	•		h !	5 mn			cm '	d 5 a	m	e	8 cm
		9 cm		10 (25 cm	u 00		Ŭ	0.011
	-	0.011	~			Ŭ	_0 0.11				

11B _____

Now you try

Example 5

a 71 mm **b** 2 m

Example 6

76 m

Example 7

28 cm

Exercise 11B

4	~	parimator	h	oqual				
	a	perimeter	n	equal				
2	а	10 cm	b	12 cm	C	12 cm	d	12 cm
3	а	15 cm	b	12 cm	C	20 cm	d	12.8 cm
4	а	15 cm	b	37 m	C	36 cm	d	11 m
	e	30 km	f	2.4 m	g	26 cm	h	10 cm
5	а	42 cm	b	34 m	C	20.8 m	d	90 km
6	а	8.4 cm	b	14 m	C	46.5 mm		
7	а	34 m	b	52 km	C	8.8 mm		
	d	56 m	e	36 km	f	40 mm		
8	\$2	21 400						
9	а	40.7 cm	b	130.2 cm	C	294 cm	d	568 cm

10 a 5 cm **b** 5 m c 7 km **11 a** 516 ft **b** 157.38 m 110 ____ Now you try Example 8 6 cm² Example 9 **a** 15 m² **b** 121 mm² Exercise 11C **1** 1 km^2 , 1 ha, 1 m², 1 cm², 1 mm² **2 a** 9 **b** 3 cm and 3 cm **c** 9 cm² **c** 9 cm-**c** 8 cm² **3 a** 8 **b** 4 cm and 2 cm **4 a** 4 square units **b** 6 square units **c** 4 square units **d** 6 square units e 8 square units f 96 square units **5 a** 3 cm² **b** 4 cm² **c** 6 cm² **d** 3 cm² **e** 2 cm² f 5 cm² **g** 4.5 cm² **h** 9 cm² **6 a** 8 cm² **b** 9 cm² **c** 100 m² **d** 200 cm² e 22 mm² **f** 7 cm² **h** 1.44 mm² **g** 25 m² **i** 6.25 mm² **j** 1.36 m² **k** 0.81 cm² l 179.52 km² 7 \mathbf{a} cm² \mathbf{b} m² \mathbf{c} ha \mathbf{d} km² \mathbf{e} ha \mathbf{f} mm² 8 5000 m² **9** 2500 cm² 10 a 2 cm **b** 5 m c 12 km **11 a** 25 cm² **b** 12 cm c 4 units **12 a i** 10 cm **ii** 9 mm **b** Divide the area by the given length. 13 Half of a rectangle with area 4 cm² **14** 20 000 cm² = 2 m^2 **15** \$2100 **16** 5 L

11D ____

Now you try

Example 10

```
a 36 m<sup>2</sup> b 84 cm<sup>2</sup>
```

Example 11 a 78 cm² **b** 1.2 m²

Exercise 11D

1 C **2 a** A = bh**b** A = bh **c** A = bh= 20 × 3 = 60 $= 5 \times 7$ $= 8 \times 2.5$ = 35 = 20 **3 a** b = 6 cm, h = 2 cm **b** b = 10 m, h = 4 m **c** b = 3 mm, h = 5 mm **d** b = 5 m. h = 7 m **e** b = 5.8 cm, h = 6.1 cm **f** b = 5 cm, h = 1.5 cm **g** b = 1.8 m, h = 0.9 m **h** b = 5 m, h = 12 mb 28 m² e 42 m² h 48 m² b 16 m² **4 a** 40 m² **b** 28 m² **c** 17.5 m² **d** 14 cm² f 176 mm² **g** 50 m² **5 a** 36 km² **c** 48 mm² **d** 6.3 cm² **f** 1.8 cm² **6** 54 m² **b** 4 cm^2 **7 a** 6 cm² **c** 15 cm² **d** 8 cm² **8 a** 1800 cm² **b** 4200 cm² **b** 7 cm **9 a** 2 m **10 a** 10 cm **b** 5 m

	11	\$1200	
--	----	--------	--

•••	01200	
12	Half; area (parallelogram) $= bh$ and area (triangle) $=$	$\frac{1}{2}bh$

b 36 m²

13 a	6500 m ²	b	6300 m ²
C	25 600 m ²	d	\$4 608 000

11E _____

Now you try

Example 12

a 7.5 mm²

Example 13

a 24 cm² **b** 7 m²

Exercise 11E

1		6 m		11mm	C	1.9 m	d	3.2 mm
		4 m	•	28 mm				
2	а	20 cm	b	7 m	C	2 m	d	6.3 cm
	е	6 cm	f	5 m				
3	а	10	b	56	C	12.5	d	5.25
4	а	3 m ²	b	40 cm ²	C	12 mm ²		
	d	16 m ²	e	30 cm ²	f	160 m ²		
	a	1.2 m ²	h	15 m ²	i	63 mm ²		
5		10 cm ²	h	3 mm^2	C	24.5 km^2		
•		1.3 cm^2	ē	20 m ²	f	4.25 m ²		
6	-	2 cm^2		6 cm^2	•	3 cm ²	h	3 cm ²
		300 m ²	~	0 0111	Č	0 0111	ŭ	0 0111
		30 m ²						
-								
9 160 m ²								
10 \$6300								
11	11 No, the base and height are always the same.							
12	а	7 cm ²	b	8 cm ²	C	11 cm ²	d	11 cm ²

Progress quiz

1	а	500	b	4200	C	62 100	d	147
2	а	7.2	b	0.051	C	4.132	d	35
3	а	38	b	6.82	C	5708		
4	а	29 cm	b	15.6 m				
5	а	68 cm	b	260 mm				
6	\$1	2960						
7	а	34.85 cm ²	b	169 mm ²				
8	а	100 cm ²	b	20 cm				
9	а	40 m ²	b	12.3 cm ²				
10	а	120 cm ²		6 m ²				
11	а	24 cm ²	b	2.86 m ²				

11F _____

Now you try

Example 14

30 m³

Example 15

64 m³

Exercise 11F

•	B D							
3	а	6	b	24		c 24		d 144
4	a	V = lwh		b	V =	= lwh	C	$V = l^3$
		= 4 × 2	× 3		=	$1 \times 3 \times 6$		$= 2 \times 2 \times 2$
		= 24 cn	1 ³		=	= 18 cm ³		$= 8 \text{ km}^3$
5		84 m ³		10 cm		c 98 cm ³		d 240 m ³
		720 km ³			cm ³			
6	а	8 cm ³	b	27cm ³		c 1000 km ³		d 2.744 mm ³

7 a 360 m^3 b 28 cm^3 c 100 m^3 d 11.25 km^3 8 96 m^3 9 24000 cm^3 10 27000000 km^3 11 600 12 a i 2 m ii 5 cm b Use: Volume \div area of base c $h = V \div (l \times w)$ 13 a 28 cm^3 b 252 m^3
11G
Now you try
Example 16 a 2600 mL b 0.5 mL
Example 17 a 16 000 cm ³ b 16 000 mL c 16 L
Exercise 11G
1 a capacity b 1 c 1000 d 1000 e 1000 f 1000 2 ×1000 ×1000 ×1000 ML kL L mL
$\begin{array}{c} \begin{array}{c} \begin{array}{c} +1000 \\ +1000 \\ +1000 \end{array} \\ +1000 \end{array} \\ \begin{array}{c} \begin{array}{c} \ & +1000 \end{array} \\ \hline \\ \ & +1000 \end{array} \\ \begin{array}{c} \ & -100 \end{array} \\ \begin{array}{c} \ & -100 \end{array} \\ \begin{array}{c} \ & -100 \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} $ \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \begin{array}{c} \ & -1000 \end{array} \\ \end{array} \\ \end{array}
11H
Now you try
Example 18 35°C
Example 19 a 4730 kg b 14 g
Exercise 11H
1 a 1000b milligramsc tonned 100°Ce 0°C2 a Cb Fc Ad De Bf E

1	а	1000		b n	nilligrams	(tonr	1e		d	100°	С	e	0°C
2	а	С	b	F	c A	d	D	e	В		f E	-		
3	а	В		b	Α	C	D			d	С			
4	а	12°C		b	37°C	C	17°C			d	225	°C		
	e	1.7°C		f	31.5°C									
5	а	4 kg		b	12 g	C	65 t							

Essential Mathematics for the Victorian Curriculum CORE Year 7

6	а	2000 g	b	7000 g	C	6200 g	d	5800 g
	e	6 kg	f	8.9 kg	g	0.9 kg	h	0.45 kg
	i	5000 kg	j	600 kg	k	2.4 t	L	4.32 t
	m	3000 mg	n	4200 mg	0	7.5 g		
7	a	4.620 g	b	21.6 t	C	470 kg	d	0.312 kg
	e	0.027 g	f	750 kg	g	125 g	h	0.0105 kg
	i	210 t	j	470 kg	k	592 g	L	80 g
8	33	°C						
9	14	7°C						
10	a	60 kg	b	60 000 g		c 60 000 000	m	g
11	a	3000 g	b	3 kg				
12	a	8 kg	b	8.16 kg				
13	a	400 mg, 370	g,	2.5 kg, 0.1 t				
	b	290 000 mg,	0.0	000 32 t, 0.41	kç	j, 710 g		
14	50	days						
15	а	1 g	b	1 t	C	1000 t		
16	a	12 kg	b	1000 kg	C	360 000 kg		

Maths@Work: Landscape gardener

1			15 m, 13.5 m ²	ii	\$92.48
	b	i	28 m, 27 m ²	ii	\$184.95
			25.6 m, 31.2 m ²	ii	\$213.72
2	а	i	35.88 m ²	ii	\$313.95
	b	i	22.52 m ²	ii	\$197.05
	C	i	3.46 m ²	ii	\$30.24
3	18	3 ro	IIs of turf		

4 a Bedding sand \$181; pavers \$1551; total \$1732

b Turf \$800; top soil \$530; mulch \$62; edging \$297; total \$1689
5 See table at bottom of page.

Puzzles and games

- **1 a** 12 **b** 35 **c** 50
- **2** B
- **3** No. Although both shapes look like triangles, this is an optical illusion. The 'hypotenuse' (longest side) on each shape is not quite straight.
- **4 a** 3 cm² **b** 20 cm²
- **5 a** 62 cm^2 **b** 16 m^2 **c** 252 cm^2
- $\begin{array}{l} \textbf{6} \quad \text{Mark a length of 5 m, then use the 3 m stick to reduce this to 2 m.} \\ \text{Place the 3 m stick on the 2 m length to show a remainder of 1 m.} \\ \textbf{7} \quad 10.5 \ \text{cm}^2 \end{array}$

Short-answer questions

1	а	2.5 cm	b	2.3 cm	C	4.25 kg		
	d	5 L	e	6°C	f	1°C		
2	а	50 mm	b	2 m	C	3700 m		
	d	36 m	e	7100 g	f	24 g	g	22 t
	h	2500 kg	i	4 L	j	40 kL	k	400 kL
	L	6500 L	m	6 cm	n	3 ML	0	0.2 mm

3		16 m		20.6 cm	C	23 m	d	34 km
		3.2 mm	•	24 m				
4	а	24.01 cm ²	b	14 km ²	C	67.5 m ²	d	12 cm ²
	e	14 m ²	f	5 cm ²	g	14 m ²	h	0.9 km ²
	-	0.16 m ²		900 cm ²				
5	а	18 cm ³	b	7.5 cm ³	C	64 mm ³		
6	а	72 000 cm ³	b	72 000 mL	C	72 L		
7	а	30 L	b	1 L	C	4 L		
8	а	45 mg, 290 000 g, 3 t, 4700 kg						
	b	50 000 mL, 5	51	L, 0.5 kL, 1 N	ΛĽ			

Multiple-choice questions

1	D	2 E	3 C	4 A	5 E
6	В	7 A	8 B	9 E	10 B

Extended-response questions

а	240 cm		b	3200 cm ²
			d	160 cm
e	1200 cm ²		f	2000 cm ²
а	30 m ³	b 16 m	C	30 000 000 cm ³
d	30 000 L,	30 kL	е	30 t
	c e g a	e 1200 cm ² g \$200 a 30 m ³	c 20 cm, 60 cm e 1200 cm ² g \$200	c 20 cm, 60 cm d e 1200 cm ² f g \$200 a 30 m ³ b 16 m c

Semester review 2

Negative numbers

Short-answer questions

1	а	<	b	>	C	<
2	а	-1	b	-5	C	-10
	d	-6	e	-18	f	-77
3	а	1	b	4	C	-2
	d	-5	e	-12	f	-57
4	а	5	b	7	C	24
	d	-1	e	-6	f	2
5	а	-15	b	-3	C	-8
6	а	-10	b	10	C	-20
	d	16	e	32	f	24

Multiple-choice questions

1 C	2 A	3 B	4 E	5 D
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Extended-response questions

1 a A(2,0), B(4,0), C(0,2), D(2,2), E(2,-3), F(-1,-2), G(-3,0), H(-3,-2), I(-1,2)

Better Landscaping Company										
	Client: Jack and	Jill Green								
Sections	Length in m	Width in m	Area in m ²	Perimeter in m						
Front lawn	8	5.1	40.8	26.2						
Back garden	5.8	2.2	12.76	16						
PLANTS	Number	Price for one	Total cost							
Trees	2	\$36.00	\$72.00							
Shrubs	5	\$11.50	\$57.50							
Punnets of vegetables	6	\$4.55	\$27.30							
MATERIALS	Quantity	Cost per unit	Total cost							
Legend couch turf in m ²	40.8	\$10.75	\$438.60							
Garden edge blocks in m	16	\$14.80	\$236.80							
Garden soil in m ³	1.5312	\$65.00	\$99.53							
		Overall cost	\$ 931.73							

Essential Mathematics for the Victorian Curriculum CORE Year 7

b A, B	, <i>O</i>	and	G;	all	lie	on	the	x-axis.
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- ii 5 units c i 2 units
- d Trapezium
- e 8 square units
- f DECIDE

Statistics and probability

Short-answer questions

а	1, 2, 3, 5, 5, 5,	8,	, 8,	9,10				
b	10							
C	i 5.6		ii	5		iii 5		iv 9
d	11.2							
а	A I	b	В		C	$\frac{1}{3}$		
а	{1, 2, 3, 4, 5, 6	5}			b	$\frac{1}{6}$	C	$\frac{1}{2}$
а	13							
b	3,47							
C	i 44		ii	22		iii 22		
a	i 10°C		ii	15°C		iii 30°C		
b	15°C							
C	22.5°C							
	b d a b c a b	 b 10 c i 5.6 d 11.2 a A a {1,2,3,4,5,6 a 13 b 3,47 c i 44 a i 10°C 	b 10 c i 5.6 d 11.2 a A b a {1,2,3,4,5,6} a 13 b 3,47 c i 44 a i 10°C b 15°C	b 10 c i 5.6 ii d 11.2 a A b B a {1,2,3,4,5,6} a 13 b 3,47 c i 44 ii a i 10°C ii b 15°C	c i 5.6 ii 5 d 11.2 a A b B a {1,2,3,4,5,6} a 13 b 3,47 c i 44 ii 22 a i 10°C ii 15°C b 15°C	b 10 c i 5.6 ii 5 d 11.2 a A b B c a {1,2,3,4,5,6} b a 13 b 3,47 c i 44 ii 22 a i 10°C ii 15°C b 15°C	b 10 c i 5.6 ii 5 iii 5 d 11.2 a A b B c $\frac{1}{3}$ a $\{1, 2, 3, 4, 5, 6\}$ b $\frac{1}{6}$ a 13 b 3, 47 c i 44 ii 22 iii 22 a i 10°C ii 15°C iii 30°C	b 10 c i 5.6 ii 5 iii 5 d 11.2 a A b B c $\frac{1}{3}$ a $\{1, 2, 3, 4, 5, 6\}$ b $\frac{1}{6}$ c a 13 b 3, 47 c i 44 ii 22 iii 22 a i 10°C ii 15°C iii 30°C b 15°C

Multiple-choice questions

1 A **2** C **3** B **4** A

Extended-response questions

1	a $\frac{1}{4}$	b $\frac{1}{4}$	c 1/2	d $\frac{1}{52}$ h $\frac{4}{13}$
	e 2/13	f $\frac{1}{13}$	g $\frac{4}{13}$	h $\frac{4}{13}$

5 B

Shapes and transformations

Short-answer questions

1	b c d	Square Parallelogram Isosceles rigi Rhombus Trapezium Kite			
2	а	50	b 45	c 40	
		150		f 80	
3	а	<i>a</i> = 60	b <i>a</i> = 65		d <i>a</i> = 115
		<i>a</i> = 90, <i>b</i> = 9		f <i>a</i> = 65	
4	а	A'(2,0), B'((2, -3), C'(4, 0)		
	b	A'(-2,0), B	C'(-2,3), C'(-4)	, 0)	
	C	A'(0, -2), B	′(3, -2), <i>C</i> ′(0, -	-4)	
	d	<i>A</i> ′(0, 2), <i>B</i> ′(-3, 2), C'(0, 4)		
		· · · · ·	r'(-2, -3), <i>C</i> '(-	· /	
			C'(-2, 4), C'(0, 1)	/	
	g	A'(-1, -2),	B'(-1,1), C'(1,1)	, -2)	

Multiple-choice questions

1	E	2 B	3 D	4 C	5 A

Extended-response questions

1 a Student's own construction **b** a+b+c = 180**d** x + y + z = 360**c** Student's own measurements **e** 360

Equations

Short-answer questions

1		False False	b True e False		True True		4
2	a	<i>x</i> = 3	b x = 108	C	<i>x</i> = 21	d	$x = \frac{4}{3}$
	a b c	x = 2 i 8 w = 6 w = 6 w = 11	b $y = 5$ ii 20		<i>x</i> = 12 iii 48	d	<i>m</i> = 7
		x = 5 x + 25 = 85		C	<i>x</i> = 18		

Multiple-choice questions

1	В	2 E	3 C	4 B	5 B
•	D		• •	4 0	00

Extended-response questions

1	a	\$320	b	\$400	C	C = 200 + 40n	d	$6\frac{1}{2}$ hours
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Measurement

Short-answer questions

		500				0000			10	
1	а	500			D	6000		0	18	
	d	0.017			e	1.8		f	5500	
2	а	272 cm			b	11 m		C	300 cm	
	d	220 cm			e	3.4 m		f	84 m	
3	а	1.69 m ²			b	24 m ²			60 m ²	
	d	20 m ²			e	12 cm ²		f	28 m ²	
4	а	729 cm ³			b	120 m ³		C	: 384 m ³	
5	а	5000	b	7	C	2000	d	3000	e 8	f 25
6	а	0.4 L			b	20 L	(: 50 L		
7	а	3000 kg			b	2000 g		C	6.5 kg	d 0.5 t
	e	5 g			f	24 000	mg	g	50 g	h 0.02 g
8	а	0		b	100					

Multiple-choice questions

1	С	2 B	3 E	4 C	5	А

Extended-response questions

- 1 a Many answers are possible; e.g. 8 m \times 10 m, 4 m \times 14 m, $15 \text{ m} \times 3 \text{ m}$
 - **b** $9 \text{ m} \times 9 \text{ m} (\text{area} = 81 \text{ m}^2)$
 - c 36 posts
 - **d** \$900

Answers